

Q → Given a character array/string,
count the pairs (i, j) s.t. $i < j$, $A[i] = 'a'$ &
 $A[j] = 'g'$.

$A = [a^0 \ b^1 \ e^2 \ g^3 \ a^4 \ g^5]$

Pairs → $(0, 3)$

$(0, 5)$

$(4, 5)$

Ans = 3

$A = [a^0 \ c^1 \ g^2 \ d^3 \ g^4 \ a^5 \ g^6]$

Pairs → $(0, 2)$ $(0, 6)$

$(0, 4)$ $(5, 6)$

Ans = 4

$A = [b^0 \ c^1 \ a^2 \ g^3 \ g^4 \ a^5 \ a^6 \ g^7]$

Pairs → $(2, 3)$ $(5, 7)$

$(2, 4)$ $(6, 7)$

$(2, 7)$

Ans = 5

Brute force → $i < j$, $A[i] = 'a'$ & $A[j] = 'g'$.

cnt = 0

for $i \rightarrow 0$ to $(N-1)$ {

for $j \rightarrow 0$ to $(N-1)$ {

if $(i < j \ \&\& \ A[i] == 'a' \ \&\& \ A[j] == 'g')$

cnt++

}

} return cnt

TC = $O(N^2)$

SC = $O(1)$

cnt = 0

for i → 0 to (N-1) {

if (A[i] == 'a') {

for j → (i+1) to (N-1) {

if (A[j] == 'g')

cnt++

}

}

} return cnt

→ count # 'g' from
(i+1) to (N-1)

→

A → [a a a ...]

TC = $O(N^2)$ SC = $O(1)$

A = [⁰b ¹c ²a ³g ⁴c ⁵g ⁶a ⁷x ⁸a ⁹g ¹⁰t]

'g' → 3 3 3 3 2 2 1 1 1 1 0

cnt_g

if (A[i] != 'g') cnt_g[i] = cnt_g[i+1]
else cnt_g[i] = cnt_g[i+1] + 1

if (A[N-1] == 'g') cnt_g[N-1] = 1

else cnt_g[N-1] = 0

for i → (N-2) to 0 {

if (A[i] != 'g') cnt_g[i] = cnt_g[i+1]

else cnt_g[i] = cnt_g[i+1] + 1

}

→ TC = $O(N)$

→ calculating
& storing

ans = 0

for i → 0 to (N-1) {

if (A[i] == 'a') {

ans += ~~cnt_g[i+1]~~ → cnt_g[i] ✓

}

→ using

→ TC = $O(N)$

```
} return ans
```

Overall $TC = O(N+N) = O(N)$

$SC = O(N) \rightarrow \text{cnt_g}[1]$

```
ans = 0
if (A[N-1] == 'g') cnt_g = 1
else cnt_g = 0
for i → (N-2) to 0 {
    if (A[i] == 'g') cnt_g = cnt_g + 1 // calculating
    if (A[i] == 'a') ans += cnt_g // using carry forward
}
```

return ans

$TC = O(N)$ $SC = O(1)$

i
 $A = [b, c, a, g, c, g, a, x, a, g, t]$
 $ans = 0 + x + 2 + \underline{5} \checkmark$
 $cnt_g = 0 + x + 3$

Sol 2 → Travel $L \rightarrow R$ & count 'a'

Subarrays → continuous part of the array.

$A = [b, c, a, g, c, g, a, x, a, g, t]$
subarray

single element ✓

full array ✓

$A = [2, 4, 1, 6, -3, 7, 8, 4]$
 L R
subarray
(5, 7)

$A = [4 \quad 2 \quad 10 \quad 3 \quad 12 \quad -2 \quad 5]$

subarrays starting from index 0 $\rightarrow L=0$ Ans = 7

$R = [0 \quad 6] \rightarrow 7$

subarray starting from index 1 $\rightarrow L=1$ Ans = 6

$R = [1 \quad 6] \rightarrow 6$

$A = [4 \quad 2 \quad 10 \quad 3 \quad 12 \quad -2 \quad 5]$

Total # subarrays = $1 + 2 + 3 + \dots + N$ $1 + 2 + \dots + 7 = \underline{28}$

$$= \frac{N * (N+1)}{2}$$

Q \rightarrow Given an integer array & print subarray from index L to R.

$A = [4 \quad 2 \quad 10 \quad 3 \quad 12 \quad -2 \quad 5]$

L
 R

3
5

for $i \rightarrow L$ to R {

print ($A[i]$)

}

TC = $O(N)$

SC = $O(1)$

Q \rightarrow Print all possible subarrays.

$A = [1 \quad 2 \quad 3]$

1

1 2

1 2 3

2

2 3

3

```

for L → 0 to (N-1) {
  for R → L to (N-1) { R ≥ L    L — R
    for i → L to R {
      print (A[i])
    }
  }
}

```

$TC = \underline{O(N^3)}$ $SC = \underline{O(1)}$

Q → Given an integer array, find the length of smallest subarray which contains both min & max element of the array.

0 1 2 3 4 5 6 7 8
 A = [5 8 1 3 8 10 6 1 2]

min = 1

max = 10

Ans = 3

0 1 2 3 4 5 6 7 8 9 10
 A = [2 2 6 4 5 1 5 2 6 4 1]

min = 1

max = 6

Ans = 3

```

minA = A[0]      maxA = A[0]
for i → 1 to (N-1) {
  minA = min(minA, A[i])
  maxA = max(maxA, A[i])
}

```

}



ans = N // complete array

for $L \rightarrow 0$ to $(N-1)$ {

for $R \rightarrow L$ to $(N-1)$ { $L \text{ --- } R$

 resMin = false resMax = false

 for $i \rightarrow L$ to R {

 if ($A[i] == \text{minA}$) resMin = true

 if ($A[i] == \text{maxA}$) resMax = true

 }

 if (resMin && resMax)

 ans = min(ans, $R - L + 1$)

 }

} return ans

TC = $O(N^3)$

SC = $O(1)$

$$A = \overset{L}{\underset{0}{2}} \quad \overset{1}{2} \quad \overset{2}{\textcircled{6}} \quad \overset{3}{4} \quad \overset{4}{5} \quad \overset{R}{\underset{5}{\textcircled{1}}} \quad \overset{6}{5} \quad \overset{7}{2} \quad \overset{8}{6} \quad \overset{9}{4} \quad \overset{10}{1}]$$

..... } large length

ans = N

for $L \rightarrow 0$ to $(N-1)$ {

 resMin = false resMax = false

 for $R \rightarrow L$ to $(N-1)$ {

 if ($A[R] == \text{minA}$) resMin = true

 if ($A[R] == \text{maxA}$) resMax = true

 if (resMin && resMax) {

 ans = min(ans, $R - L + 1$)

 break

 }

}

TC = $O(N^2)$

SC = $O(1)$

} return ans

L . . .

0 1 2 3 4 5 6 7 8 9 10

A = [2 2 6 4 5 1 5 2 6 4 1]

R . . .

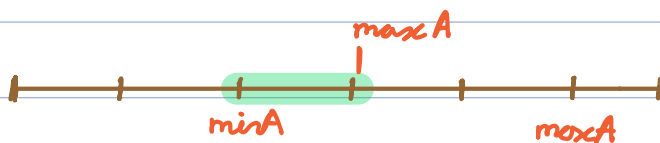
minA = 1 nextMin = ~~false~~ true

maxA = 6 nextMax = ~~false~~ true

ans = 11 6 5 4

3

Observations → min length
minA & maxA



ans subarray → start at min & end at max OR
start at max & end at min

(A[i] == minA) → find next closest maxA index
on right side } ✓

(A[i] == maxA) → find next closest minA index

// minA maxA ✓

minInd = -1 maxInd = -1 ans = N

for i → (N-1) to 0 {

if (A[i] == minA) {

minInd = i // calculate

if (maxInd != -1) // minInd — maxInd

ans = min (ans, maxInd - minInd + 1) // use

```
} if (A[i] == maxA) {
```

```
    maxInd = i // calculate
```

```
    if (minInd != -1) // maxInd - minInd
```

```
        ans = min(ans, maxInd - minInd + 1) // use
```

```
}
```

```
} return ans
```

TC = $O(N)$

SC = $O(1)$

$A = [5, 8, 1, 3, 8, 10, 6, 1, 2]$

Indices: 0 1 2 3 4 5 6 7 8

... i

minA = 1

minInd = ~~7~~

ans = ~~At~~ 3

maxA = 10

maxInd = ~~5~~
