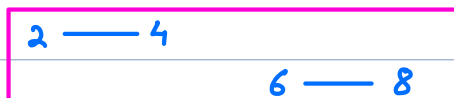
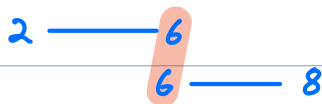
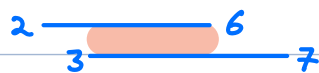


start — end (start ≤ end)

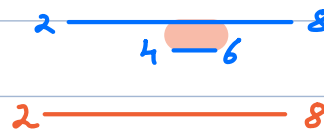
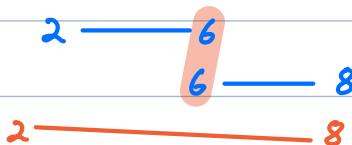
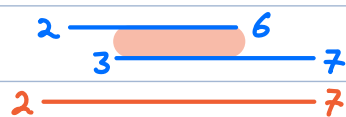


non-overlap

Non-Overlapping (s₁, e₁) (s₂, e₂)

→ ((s₂ > e₁) || (s₁ > e₂))

Merge 2 overlapping intervals

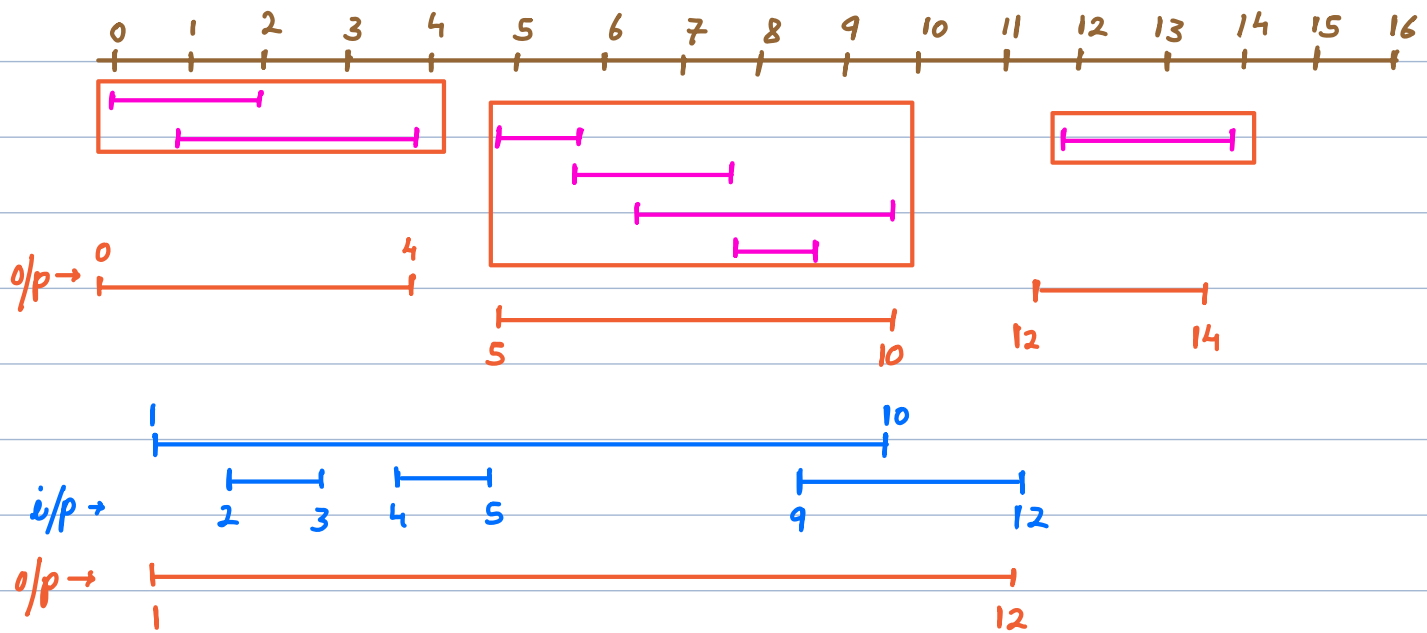


start = min(s₁, s₂)

end = max(e₁, e₂)

Q → Given a list of intervals (start ≤ end),
sorted wrt start time. Merge all overlapping
intervals & return the result of non-overlapping
intervals in sorted order wrt start time.

i/p → S = [0⁰ 1¹ 5² 6³ 7⁴ 8⁵ 12⁶]
E = [2 4 6 8 10 9 14]



start = s[0] end = E[0] // current interval

for i → 1 to (N-1) {

 if (s[i] ≤ end) { // check if ith interval overlaps

 end = max(end, E[i])

 } else {

 print (start + " " + end)

 start = s[i] end = E[i]

 }

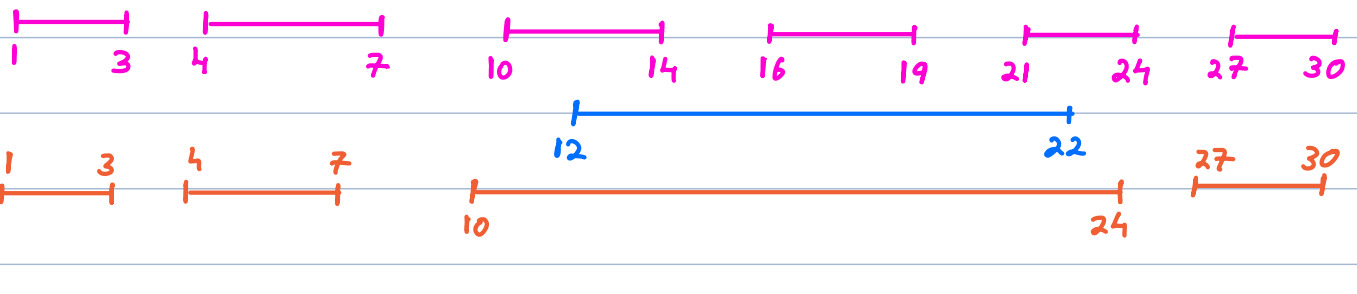
} print (start + " " + end)

TC = O(N)

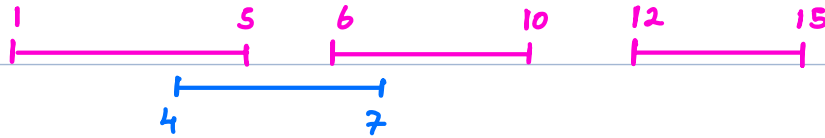
SC = O(1)

Q → Given a set of non-overlapping intervals, sorted wrt start time. Insert the given new interval s.t. final list is sorted & non-overlapping.

s = [1 4 10 16 21 27] L=12 R=22
E = [3 7 14 19 24 30]



o/p →



o/p →

$S = []$ $E = []$ $L = 2$ $R = 4$

```

if (N == 0) {
    print (L + " " + R)
    return
}

if (R < S[0]) {           // L — R   S[0] — E[0] — ...
    print (L + " " + R)
    for i → 0 to (N-1) {
        print (S[i] + " " + E[i])
    }
    return
}

if (L > E[N-1]) {        // ... S[N-1] — E[N-1]   L — R
    for i → 0 to (N-1) {
        print (S[i] + " " + E[i])
    }
    print (L + " " + R)
}

```

$i = 0$

while ($i \leq N-1$) { // intervals on left of $L-R$

if ($E[i] < L$) {

print($S[i] + " " + E[i]$)

} else { break }

$i++$

} // 0 — (i-1) ✓

start = L end = R

while ($i \leq (N-1)$) { // overlapping $L-R$

if ($!(S[i] > end \parallel start > E[i])$) {

start = min(start, $S[i]$) end = max(end, $E[i]$)

} else { break }

$i++$

} // i — (i-1) → merged

print(start + " " + end)

while ($i \leq (N-1)$) { // after $L-R$

print($S[i] + " " + E[i]$)

$i++$

}

	0	1	2	3	4	5	
S = [1	4	7	16	21	27]	L = 8
E = [3	6	14	19	24	30]	R = 22
					i		

1 — 3

st = 8 7

4 — 6

end = ~~22~~ 24

7 — 24

27 — 30

TC = $O(N)$ SC = $O(1)$

Q → Given an integer array, find the first missing positive integer.

$$A = [3 \quad -2 \quad 1 \quad 2 \quad 7] \quad \text{Ans} = \underline{4}$$

$$A = [-2 \quad -8 \quad 0 \quad 4] \quad \text{Ans} = \underline{1}$$

$$A = [5 \quad 3 \quad 1 \quad -1 \quad -2 \quad -4 \quad 7 \quad 2] \quad \text{Ans} = \underline{4}$$

Brute force → check every number from 1 to (N+1).

$$TC = \underline{O(N^2)} \quad SC = \underline{O(1)}$$

$$A = [1 \quad 2 \quad 3] \quad \text{Ans} = \underline{4}$$

Sort →

$$A = [-8 \quad -2 \quad 1 \quad 2 \quad 4 \quad 8]$$

→

	0	1	2	3	4	5
	-8	-2	1	2	4	8
			↑	↑	↑ _x	
			1	2	3	
					✓	

$$TC = \underline{O(N \log(N))} \quad SC = \underline{O(1)}$$

$$A = [5 \quad 3 \quad 1 \quad -1 \quad -2 \quad -4 \quad 7 \quad 2] \quad SC = \underline{O(1)}$$

Keep track of numbers from 1 to N

for any number 1 to N swap it to

index 0 to (N-1)

ind

$$\begin{aligned} 1 &\rightarrow 0 \\ 2 &\rightarrow 1 \\ 3 &\rightarrow 2 \\ &\vdots \end{aligned}$$

$A = [\overset{0}{5} \overset{1}{3} \overset{2}{1} \overset{3}{-1} \overset{4}{-2} \overset{5}{5} \overset{6}{7} \overset{7}{-2} \overset{8}{6}]$

$N = 8$

$i = 0$
 $\text{while } (i < N) \{$

$\begin{matrix} -2 & + & 3 & & 5 & 6 & & -2 & 5 \\ & 1 & -2 & & & & & & \end{matrix}$

$\text{while } (A[i] \text{ is } [1 \ N] \ \&\& \ A[i] \neq i+1 \ \&\& \ A[i] \neq A[A[i]-1]) \{$
 $\text{swap } (i, A[i]-1)$
 $\}$

$i++$
 $\}$
 $A = [1 \ 2 \ 3 \ -1 \ 5 \ 6 \ 7 \ -2 \ 5]$
 $\checkmark \quad \checkmark \quad \checkmark$

4 (Ans)

$TC = O(N)$

$\text{if } (A[i] \neq i+1) = \text{Ans} = \underline{i+1}$

$SC = O(1)$
