

Q → Given an integer array, find the index of nearest smaller element on left i.e.

$\forall i$, find index j s.t. $A[j] < A[i]$, $j < i$ & j is maximum.

$A = [8 \ 2 \ 4 \ 9 \ 7 \ 5 \ 3 \ 10]$

$[-1 \ -1 \ 1 \ 2 \ 2 \ 2 \ 1 \ 6]$ (Ans)

$A = [4 \ 6 \ 10 \ 11 \ 7 \ 8 \ 3 \ 5]$

$[-1 \ 0 \ 1 \ 2 \ 1 \ 4 \ -1 \ 6]$ (Ans)

$A = [4 \ 5 \ 2 \ 10 \ 8 \ 2]$

index → $[-1 \ 0 \ -1 \ 2 \ 2 \ -1]$

values → $[-1 \ 4 \ -1 \ 2 \ 2 \ -1]$

Brute force → $\forall i$, iterate j from $(i-1)$ to 0 ,
first $A[j] < A[i] \Rightarrow j$ is ans.

$\forall i, \text{ans}[i] = -1$

for $i \rightarrow 1$ to $(N-1)$ {

for $j \rightarrow (i-1)$ to 0 {

if $(A[j] < A[i])$ { ans[i] = j

break }

}

} return ans

TC = $O(N^2)$

SC = $O(1)$

$A = [\overset{0}{8} \quad \overset{1}{_} \quad \overset{2}{_} \quad \overset{3}{_} \quad \overset{4}{_} \quad \overset{5}{5} \quad \overset{6}{_} \quad \overset{7}{_} \dots]$

For any index > 5 , can 8 (index 0) be the ans?

$i > 5$, if $A[0] < A[i]$
& $A[5] < A[0] \Rightarrow A[5] < A[i]$

$\therefore i > 5 \Rightarrow$ index 5 will be closer w.r.t index 0
 $\Rightarrow A[5]$ is always a better answer.

$A = [\overset{0}{8} \quad \overset{1}{2} \quad \overset{2}{4} \quad \overset{3}{9} \quad \overset{4}{7} \quad \overset{5}{5} \quad \overset{6}{3} \quad \overset{7}{10}]$
-1 -1 1 2 2 2 1 6

check latest element first \rightarrow use stack

$A = [\overset{\cancel{i}}{0}{4} \quad \overset{\cancel{i}}{1}{6} \quad \overset{\cancel{i}}{2}{10} \quad \overset{\cancel{i}}{3}{11} \quad \overset{\cancel{i}}{4}{7} \quad \overset{\cancel{i}}{5}{8} \quad \overset{\cancel{i}}{6}{3} \quad \overset{\cancel{i}}{7}{5}]$
ans \rightarrow -1 0 1 2 1 4 -1 6

7
6

stack

for $i \rightarrow 0$ to $(N-1)$ {

while $(!st.isEmpty() \&\& A[st.peek()] \geq A[i])$ {

st.pop()

}

if (st.isEmpty()) ans[i] = -1

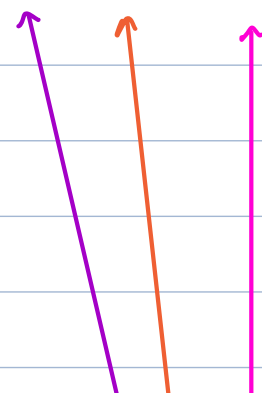
else ans[i] = st.peek()

st.push(i)

} return ans

TC = $O(N)$ SC = $O(N)$

> <= <



Q2 → Find nearest smaller or equal on left.


Q3 → Find nearest greater element on left.

Q4 → Find nearest greater or equal on left.

Q5 → Find nearest smaller element on right.

```
for i → N-1 to 0 {  
    while (!st.isEmpty() && A[st.peek()] >= A[i]) {  
        st.pop()  
    }  
    if (st.isEmpty()) ans[i] = -1  
    else ans[i] = st.peek()  
    st.push(i)  
}
```

TC = O(N) SC = O(N)

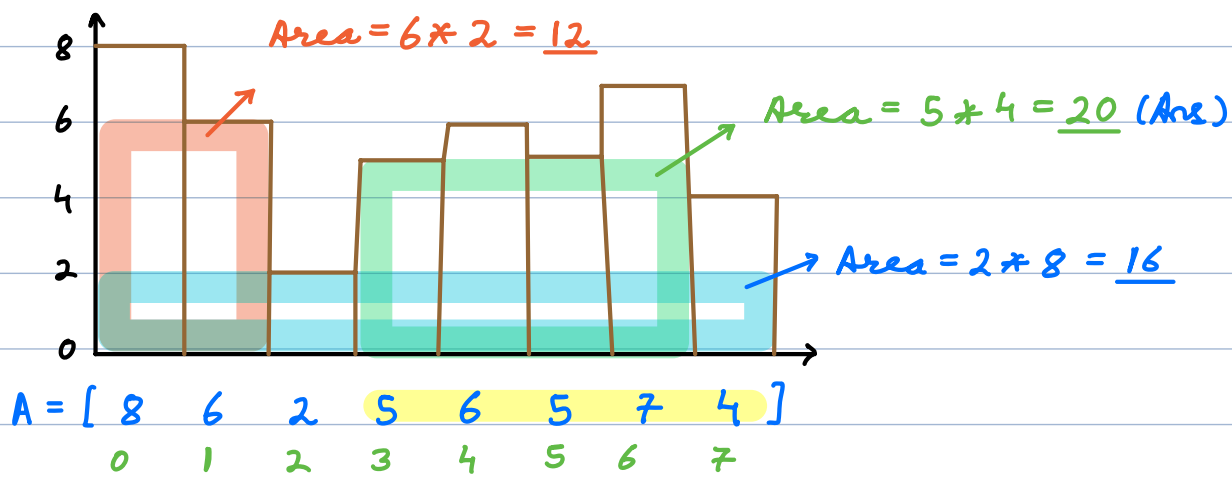


Q6 → Find nearest smaller or equal on right.

Q7 → Find nearest greater element on right.

Q8 → Find nearest greater or equal on right.

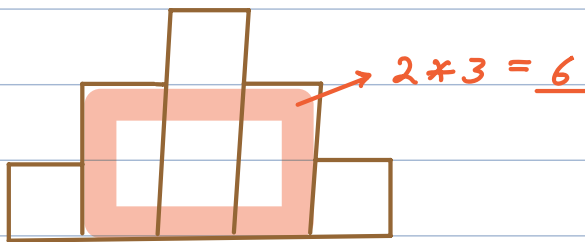
Q9 → Given an integer array A[],
A[i] = height of ith bar in histogram.
Width of each bar is 1.
Find the area of largest rectangle
formed by continuous bars.



$$\text{Area of bars } (l - r) = \forall \min(A[i]) * (r - l + 1) \quad i \rightarrow l \text{ to } r$$

$$A = [1, 2, 3, 2, 1]$$

0 1 3 3 4



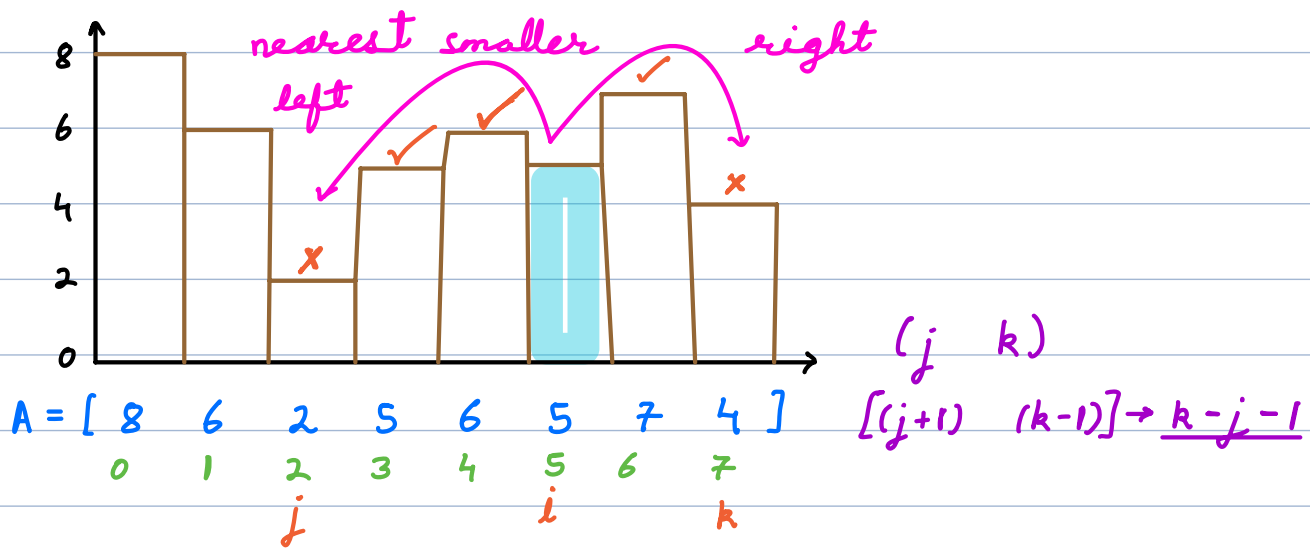
Brute force \rightarrow \forall subarray of bars calculate area & take maximum.

$$TC = O(N^2 * N) \rightarrow O(N^3)$$

$$SC = O(1)$$

\forall subarrays \rightarrow find height
base \rightarrow height

Sol $\rightarrow \forall A[i]$ as height, find max base.



$$\text{Area} = A[i] * (k-j-1)$$

```

ans = 0
for i → 0 to (N-1) {
    j = nearestSmallerLeft[i] // if not present → -1
    k = nearestSmallerRight[i] // if not present → N
    ans = max(ans, A[i] * (k-j-1))
}
return ans

```

$$TC = O(N + N + N) \rightarrow O(N) \quad SC = O(N + N + N) \rightarrow O(N)$$

Q → Given an integer array with distinct values, for all subarrays find (max - min) & return its sum as the answer.

			(max - min)
A = [2	5	3]	2 - 2 = 0
	2	5	5 - 2 = 3
	2	5	5 - 2 = 3
	5		5 - 5 = 0

Brute force \rightarrow

\forall subarray,

find max & min.

calculate (max - min) &

take its sum as answer.

$$TC = O(N^3) \rightarrow \underline{O(N^2)}$$

$$SC = \underline{O(1)}$$

$$5 \quad 3$$

$$5 - 3 = 2$$

$$3$$

$$3 - 3 = \underline{0}$$

$$\underline{8} \text{ (Ans)}$$

(max - min)

$$A = [1 \quad 2 \quad 3]$$

$$1$$

$$1 - 1 = 0$$

$$1 \quad 2$$

$$2 - 1 = 1$$

$$1 \quad 2 \quad 3$$

$$3 - 1 = 2$$

$$1 * (1 - 3) = -2$$

$$2$$

$$2 - 2 = 0$$

$$2 * (2 - 2) = 0$$

$$2 \quad 3$$

$$3 - 2 = 1$$

$$3 * (3 - 1) = \underline{6}$$

$$3$$

$$3 - 3 = \underline{0}$$

$$\underline{4}$$

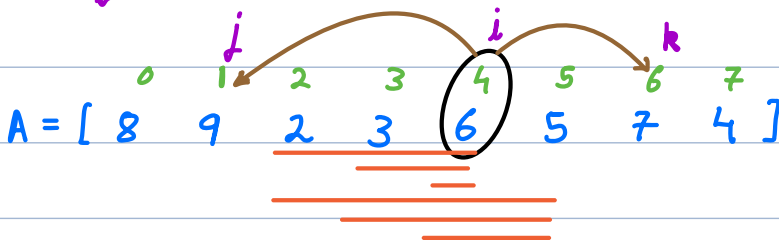
$$\underline{4} \text{ (Ans)}$$

Contribution Technique

$$\text{Ans} = \sum_{\forall i} \boxed{\text{contribution of } A[i]}$$



$$A[i] * \left(\underbrace{\# \text{ of subarrays where } A[i] \text{ is max}}_{\text{left}} - \underbrace{\# \text{ subarrays where } A[i] \text{ is min}}_{\text{right}} \right)$$



Find # subarrays where $A[4]$ is max $\rightarrow \underline{6}$

j = nearest greater on left

k = nearest greater on right

$$\text{start} \rightarrow [j+1 \quad i] \rightarrow i - (j+1) + 1 = \underline{i-j}$$

$$\text{end} \rightarrow [i \quad k-1] \rightarrow k - 1 - i + 1 = \underline{k-i}$$

$$\boxed{\# \text{ subarrays} = (i-j) * (k-i)}$$

Find # subarrays where $A[i]$ is min.

j = nearest smaller on left

k = nearest smaller on right

start $\rightarrow [(j+1) \quad i] \rightarrow i - (j+1) + 1 = \underline{i-j}$

end $\rightarrow [i \quad (k-1)] \rightarrow k - 1 - i + 1 = \underline{k-i}$

$$\# \text{ subarrays} = (i-j) * (k-i)$$

// pre-compute

ans = 0

for $i \rightarrow 0$ to $(N-1)$ {

gl = nearest GreaterLeft $[i]$

gr = nearest GreaterRight $[i]$

sl = nearest SmallerLeft $[i]$

sr = nearest SmallerRight $[i]$

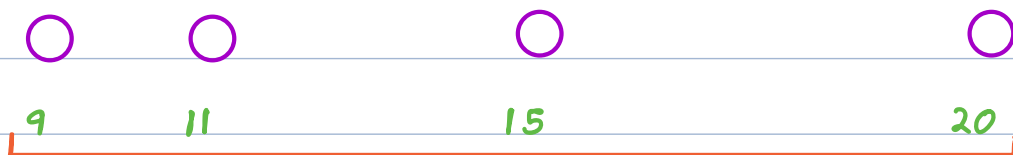
ans += $A[i] * ((i-gl) * (gr-i) -$
 $(i-sl) * (sr-i))$

}

return ans

TC = $O(5N) \rightarrow \underline{O(N)}$

SC = $O(5N) \rightarrow \underline{O(N)}$

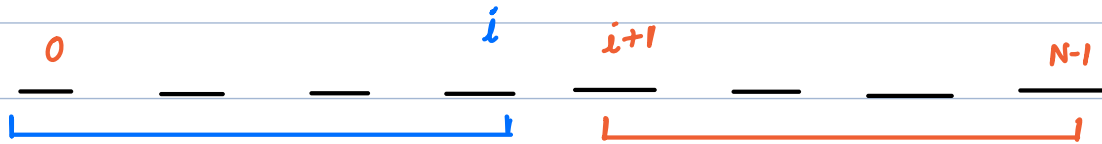
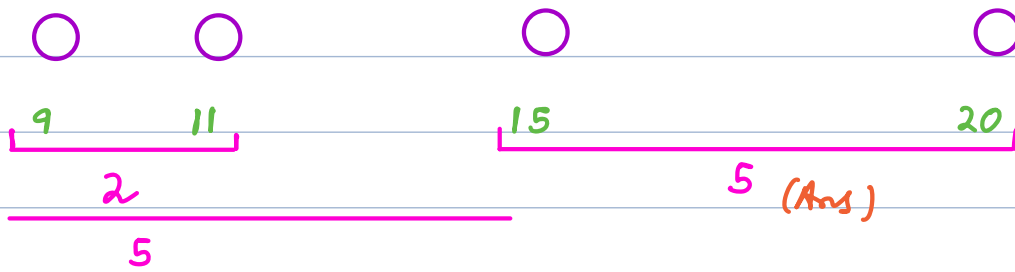


$A[k] \rightarrow$ position of k^{th} hole

1 board ($\max A - \min A$)

$$9 + L = 20$$

$$\Rightarrow L = 20 - 9 = \underline{11}$$



$$A[i] - A[0]$$

$$A[N-1] - A[i+1]$$

// sort A

ans = Int_Max

for i → 0 to (N-2) {

$$L = A[i] - A[0]$$

$$R = A[N-1] - A[i+1]$$

$$ler = \max(L, R)$$

$$ans = \min(ans, ler)$$

}

$$TC = \underline{O(N \log(N))}$$