Space Complexity → Rate of growth of space wrt input size.

int → 4B

long → 8B

1)
```
{
    int x = 2;      // 4 B
    int y = 8;      // 4 B
    long z = x+y;   // 8 B
}
```
Total space = 16 B

SC = O(1)

2)
```
func(int N) {       // 4B
    int arr[10];    // 40 B
    int x;          // 4B
    int y;          // 4B
    long z;         // 8 B
    int a = new int[N];  // 4*N B
}
```
Total space = (56 + 4N) B

SC = O(N)

SC is only wrt space apart from input & output.

3)
```
func (int N) {
    int x = N;          // 4B
    int y = x * x;      // 4B
    long z = x + y;     // 8B
    int arr[] = new int[N];      // 4N B
    long a[][] = new long[N][N]; // 8 * N^2 B
}
```

Total = $(16 + 4N + 8N^2)$ B

SC = $O(N^2)$

4)
```
int maxArray (int a[], int N) {
    int m = A[0]
    for (i → 1 to (N-1)) {
        m = max(m, A[i])
    }
    return m // Output Space
}
```

Input space

4B

Algo Space SC = O(1)

```
for (int i = 1; i < (N-1); i++) {
    :
}
```

4B

Array → linear collection of same data type.

A = [	5	8	3	4	1]
index →	0	1	2	3	4

A[3] = 4

0 to (N-1)

first last

Q → print all array elements.

```
for i → 0 to (N-1) {
    print (A[i])
}
```

Access i^{th} element → A[i] TC = O(1)

Array → continuous memory allocation

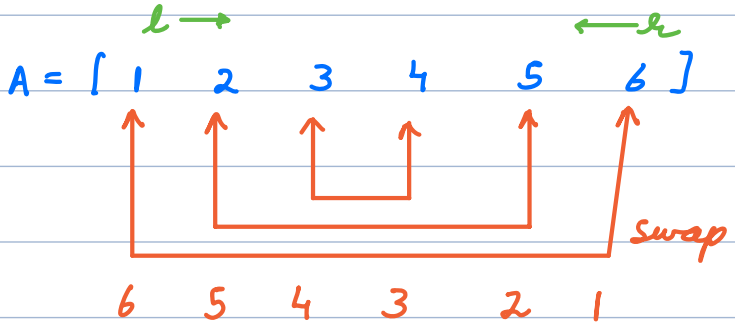
A[2] → 2000 + 2 * 4 = 2008

Q → Given an integer array of size N.

Reverse the array.

A = [1 2 3 4 5]

↳ 5 4 3 2 1




```
swap (A[], i, j) {
    temp = A[i]
    A[i] = A[j]
    A[j] = temp
}
```

```
swap (x, y) {  // without 3rd variable   (x = 2, y = 5)
    x = x + y   // 2+5 = 7
    y = x - y   // 7-5 = 2
    x = x - y   // 7-2 = 5
}
```

```
}
```

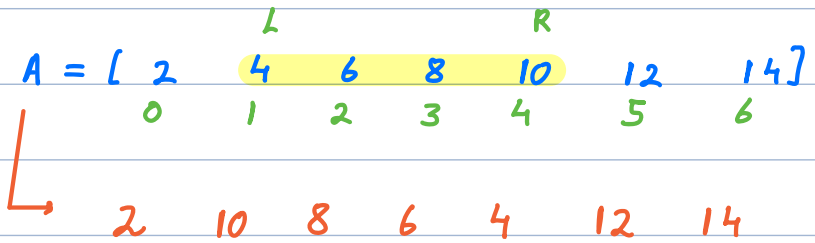
```
l = 0          r = (N-1)
while ( l < r ) {
    swap ( A, l, r )
    l++
    r--
}
```

$O(N/2) \rightarrow \underline{O(N)}$

TC = $\underline{O(N)}$

SC = $\underline{O(1)}$

Q → Given an integer array & 2 integers L & R. Reverse the array from index L to R.

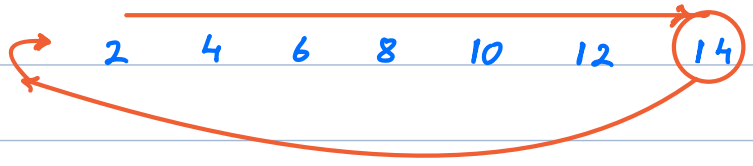



```
l = L          r = R
while ( l < r ) {
    swap ( A, l, r )
    l++
    r--
}
```

TC = $\underline{O(N)}$

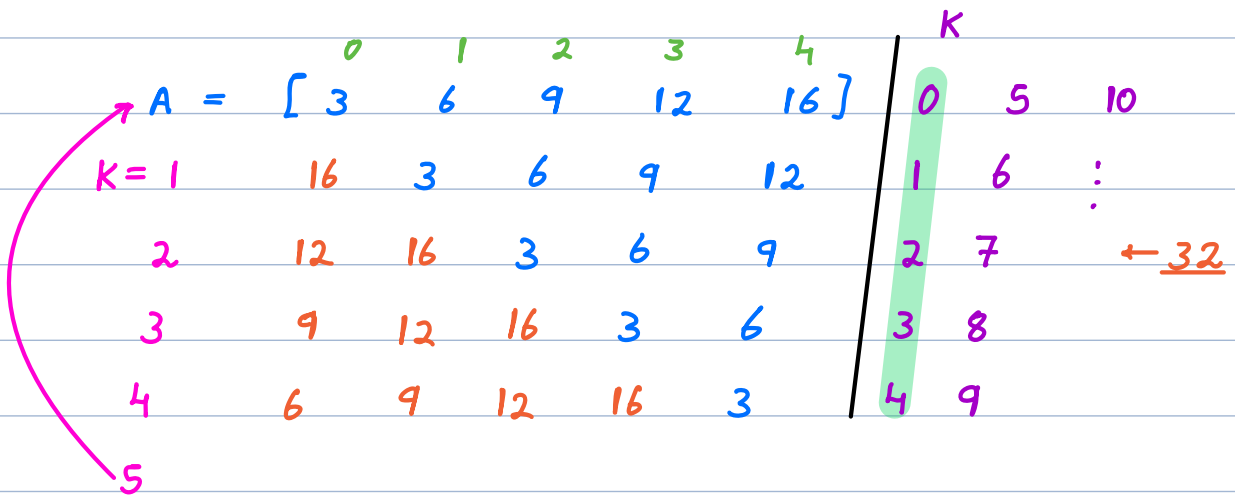
SC = $\underline{O(1)}$

Rotate array left to right (clockwise) ↻



14 2 4 6 8 10 12

Q → Given an integer array, rotate the array left to right K times.



K = 32 → 32 % 5 = 2

K = K % N

Bruteforce →

```
K = K % N
for i → 1 to K {
    t = A[N-1]
    for j → (N-1) to 1 {
        A[j] = A[j-1]
    }
    A[0] = t
}
```

TC = O(N * K) SC = O(1)

Sol. A = [3 6 9 12 16]

K = 2 12 16 3 6 9

Reverse A → [16 12] [9 6 3]

K = 2 → [12 16] [3 6 9]

first K elements — (N-K) elements

Sol → 1) Reverse (A, 0, (N-1)) → O(N)
2) Reverse (A, 0, (K-1)) → O(K)
3) Reverse (A, K, (N-1)) → O(N-K)

} O(2N)

TC = O(N) SC = O(1)

K = 3

	0	1	2	3	4	5	6	7	8
	1→		(K-1)	K					(N-1)
A =	3	6	9	12	16	18	20	15	17
✓	17	15	20	18	16	12	9	6	3
✓	20	15	17	3	6	9	12	16	18

Dynamic Arrays

Limitation in array → fixed size

→ Resizing of the array is possible

→ continuous memory allocation → Access A[i] → TC = O(1)

	0	1	2	3	
DA =	1	2	3	4	← 4 ← 5

↓ double the size ✓

[1 2 3 4 5 _ _ _] new memory add.

Eg → Java → Arraylist

C++ → Vector

Python → List

:

Next class ✓

Recap ✓

Doubts ✓

$3^1 + 3^2 + 3^3 \ldots + 3^N$

$= \frac{3(3^N - 1)}{3 - 1} = 1.5 * (3^N - 1)$ $\quad TC = O(3^N)$

```
for (int a=1; a<10; a++) {

}
```