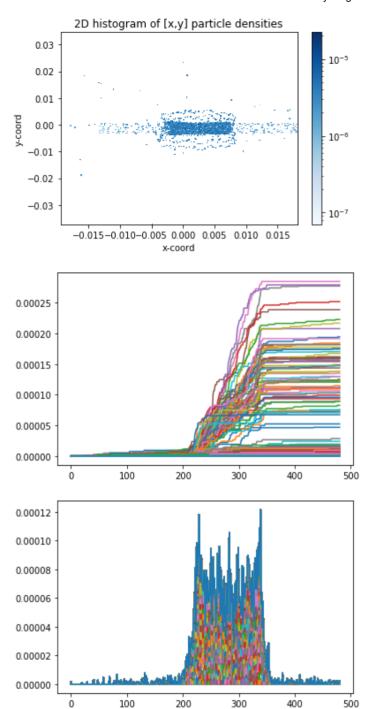
```
In [2]: import math

def round_up(n, decimals=0):
    multiplier = 10 ** decimals
    return math.ceil(n * multiplier) / multiplier
```

```
In [3]: import csv
        import pandas as pd
        x in = []
        # x-position of each particle.
        y in = []
        # y-position of each particle.
        pI = []
        # particle current in [Amperes].
        p_KP = []
        # particle power in [Watts].
        with open('quick input.out') as file:
            reader = pd.read csv(file,delimiter='\t',header=2,skipfooter=1,engine='python')
            columns = reader.columns.values
            listCol = list(columns)
            print(listCol)
            # Obtain the column headers.
            x_in = reader['x[in]']
            y_in = reader['y[in]']
            p I = reader['pI[A]']
            p KP = reader['pKP[W]']
            # Take column headers and save separate lists for needed values.
        x \min = \min(x in)
        x max = max(x in)
        y min = min(y in)
        y max = max(y in)
        # Built-in calculation for max and min of x,y components.
        x_range = x_max - x_min
        y range = y max - y min
        # Obtain the total length of both sides of our parameter space.
        # x_range = round_up(x_range, 10)
        # y range = round up(y range, 10)
        # Approximate the x,y ranges to a larger, nicer decimal value.
        print(x range,y range)
        ratio = (y range / x range)
        # Attempting to find subdivision interval unique to having dx == dy??
```

```
['pID', 'eTag', 'x[in]', 'y[in]', 'z[in]', 'vx/c', 'vy/c', 'vz/c', 'pI[A]', 'pKP[W]']
0.0375251999999999 0.0719152
```

```
In [4]: import matplotlib.pyplot as plt
        import numpy as np
        from matplotlib import colors
        from mpl toolkits.mplot3d import Axes3D
        from matplotlib.ticker import NullFormatter
        dl = 0.000078*1
        # [inches], two microns * constant
        (a, b, c, d) = plt.hist2d(x_in,y_in,bins=[np.arange(x_min,x_max,dl),
                                    np.arange(y min,y max,dl)],
                                    weights=p I,cmap='Blues',
                                    norm=colors.LogNorm())
        density = plt.colorbar()
        plt.xlabel('x-coord')
        plt.ylabel('y-coord')
        plt.title('2D histogram of [x,y] particle densities')
        plt.show()
        \# Projected histograms in x and y directions.
        chx, chy = a.cumsum(axis=0), a.cumsum(axis=1)
        hx, hy = a.sum(axis=0), a.sum(axis=1)
        plt.plot(chx)
        # plt.axis([x_min,x_max,y_min,y_max])
        plt.show()
        # print(hx)
        plt.plot(chy)
        # plt.axis([x_min,x_max,y_min,y_max])
        plt.show()
        # print(hy)
```



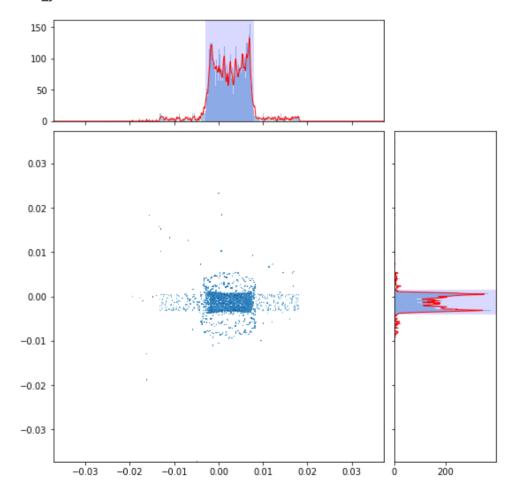
```
In [613]: def bandwidth(x_in):
    particles = len(x_in)
    constant = (3000 / 0.1)
    bandwidth = (particles / constant)

    return bandwidth
```

```
In [614]: | from statsmodels.stats.weightstats import DescrStatsW
          import scipy.stats as stats
          nullfmt = NullFormatter()
                                           # no LabeLs
          # definitions for the axes
          left, width = 0.1, 0.65
          bottom, height = 0.1, 0.65
          bottom_h = left_h = left + width + 0.02
          rect scatter = [left, bottom, width, height]
          rect histx = [left, bottom_h, width, 0.2]
          rect_histy = [left_h, bottom, 0.2, height]
          # start with a rectangular Figure
          plt.figure(1, figsize=(8, 8))
          axScatter = plt.axes(rect scatter)
          axHistx = plt.axes(rect histx)
          axHisty = plt.axes(rect histy)
          # no LabeLs
          axHistx.xaxis.set major formatter(nullfmt)
          axHisty.yaxis.set major formatter(nullfmt)
          # the 2D histogram plot:
          axScatter.hist2d(x in,y in,bins=[np.arange(x min,x max,dl),
                                      np.arange(y_min,y_max,dl)],
                                      weights=p_I,cmap='Blues',
                                      norm=colors.LogNorm())
          # now determine nice limits by hand:
          binwidth = dl
          xymax = np.max([np.max(np.fabs(x_in)), np.max(np.fabs(y_in))])
          lim = (int(xymax/binwidth) + 1) * binwidth
          axScatter.set_xlim((-lim, lim))
          axScatter.set_ylim((-lim, lim))
          bins = np.arange(-lim, lim + binwidth, binwidth)
          (n,x,_) = axHistx.hist(x_in, bins=bins, density=True,alpha=0.4)
          for width factor in [bandwidth(x in)]:
              kde = stats.gaussian kde(x in)
              f = kde.covariance factor()
              bw = f * x in.std() * width factor
              x curve = axHistx.plot(bins, kde sklearn(x in, bins, bw), ('red'), linewidth=1, alp
          ha=1)
              xx out = x curve[0].get xdata()
              xy out = x curve[0].get ydata()
              weighted x stats = DescrStatsW(xx out, weights=xy out)
              std = weighted x stats.std
              fit mu = weighted x stats.mean
              FWHM = 2*np.sqrt(2*np.log(2))*std
              print ("FWHM x:", FWHM)
              axHistx.axvspan(fit mu-FWHM/2, fit mu+FWHM/2, facecolor='b', alpha=0.15)
          (n,y,_) = axHisty.hist(y_in, bins=bins, orientation='horizontal', density=True,alpha=0.
```

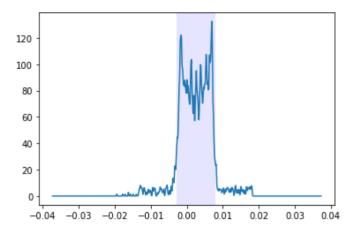
```
for width factor in [bandwidth(x in)]:
    kde = stats.gaussian kde(y in)
    f = kde.covariance factor()
    bw = f * y in.std() * width factor
    y curve = axHisty.plot(kde sklearn(y in, bins, bw), bins, ('red'), linewidth=1, alp
ha=1)
   yx_out = y_curve[0].get_xdata()
   yy_out = y_curve[0].get_ydata()
    weighted y stats = DescrStatsW(yy out, weights=yx out)
    std = weighted y stats.std
    fit_mu = weighted_y_stats.mean
    FWHM = 2*np.sqrt(2*np.log(2))*std
    print ("FWHM_y:", FWHM)
    axHisty.axhspan(fit mu-FWHM/2, fit mu+FWHM/2, facecolor='b', alpha=0.15)
axHistx.set_xlim(axScatter.get_xlim())
axHisty.set_ylim(axScatter.get_ylim())
plt.show()
# Need to fit the FWHM to the gaussian and not just the input data!!!
```

FWHM_x: 0.010781772126063368 FWHM_y: 0.005725382172496123

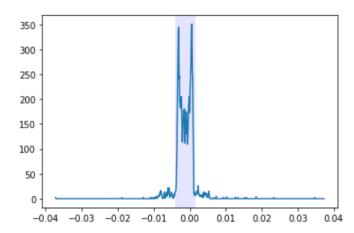


```
In [599]: # Testing for FWHM implementation!!!
          weighted x stats = DescrStatsW(xx out, weights=xy out)
          # Currently using saved x_out from .get_xydata() of axHist plots.
          plt.plot(xx_out,xy_out)
          std = weighted x stats.std
          print('std:', std)
          fit_mu = weighted_x_stats.mean
          print('mean:', fit_mu)
          FWHM = 2*np.sqrt(2*np.log(2))*std
          print ("FWHM x:", FWHM)
          plt.axvspan(fit mu-FWHM/2, fit mu+FWHM/2, facecolor='b', alpha=0.1)
          plt.show()
          weighted y stats = DescrStatsW(yy out, weights=yx out)
          plt.plot(yy out,yx out)
          std = weighted y stats.std
          print('std:', std)
          fit_mu = weighted_y_stats.mean
          print('mean:', fit_mu)
          FWHM = 2*np.sqrt(2*np.log(2))*std
          print ("FWHM_y:", FWHM)
          plt.axvspan(fit mu-FWHM/2, fit mu+FWHM/2, facecolor='b', alpha=0.1)
          plt.show()
          plt.hist(x_in, bins=bins, density=True)
          std = np.std(x_in)
          fit_mu = np.mean(x_in)
          print(fit_mu)
          FWHM = 2*np.sqrt(2*np.log(2))*std
          print ("FWHM_x:", FWHM)
          plt.axvspan(fit_mu-FWHM/2, fit_mu+FWHM/2, facecolor='b', alpha=0.25)
          plt.show()
          plt.hist(y in, bins=bins, density=True)
          std = np.std(y in)
          fit mu = np.mean(y in)
          print(fit mu)
          FWHM = 2*np.sqrt(2*np.log(2))*std
          print ("FWHM_y:", FWHM)
          plt.axvspan(fit mu-FWHM/2, fit mu+FWHM/2, facecolor='b', alpha=0.25)
          plt.show()
```

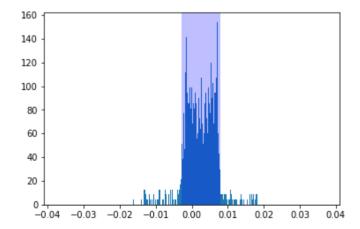
std: 0.004578597056201662 mean: 0.0025026347692282866 FWHM_x: 0.010781772126063368



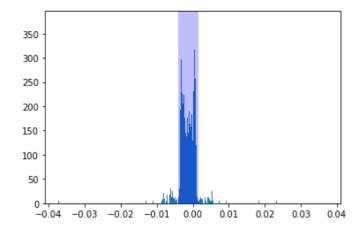
std: 0.0024313459470406682 mean: -0.001286683014460906 FWHM_y: 0.005725382172496123



0.002502634769228329 FWHM_x: 0.0107795918822097



-0.0012872854114746512 FWHM_y: 0.005735293939890718



In []: