

# Sorting

- Bubble sort:
  - Compares consecutive items : swaps them if they are in incorrect order; repeat until no more swaps are necessary
- Insertion sort:
  - Insert one item at a time in the right position in a partial sorted array.
- Selection sort:
  - Find the smallest item and move it in the first position; find the second smallest, move it in the second position and so on until the end of the array.

# Bubble-sort example

0	1	2	3	4
3	1	5	4	2

1<sup>st</sup> pass swaps: (3,1), (5,4), (5,2) # swaps = 3

3 1 5 4 2 → 1 3 5 4 2 → 1 3 4 5 2 → 1 3 4 2 5

2<sup>nd</sup> pass swaps: (4,2) # swaps = 1

1 3 4 2 5 → 1 3 2 4 5

3<sup>rd</sup> pass: swaps (3,2), # swaps = 1

1 3 2 4 5 → 1 2 3 4 5

4<sup>th</sup> pass: no swaps # swaps = 0

1 2 3 4 5 STOP !!!

# Bubble-sort pseudo-code

Inputs: array *a*, array size: *size*

```
Data:  nrPasses = 0;
       nrSwaps = 1;
       WHILE (nrSwaps > 0 && nrPasses < size);
           nrSwaps = 0
           FOR i = 0 TO size-nrPasses-1
               IF (a[i] > a[i+1])
                   nrSwaps++
                   swap a[i] with a[i+1]
               ENDIF
               i++
           ENDFOR
           nrPasses++
       ENDWHILE
```

# Insertion sort example

0	1	2	3	4
3	1	5	4	2

1<sup>st</sup> pass: key = 1

3 1 5 4 2 → 1 3 5 4 2

Blue box =  
Sorted array

2<sup>nd</sup> pass : key = 5

1 3 5 4 2 → 1 3 5 4 2

3<sup>rd</sup> pass: key = 4

1 3 5 4 2 → 1 3 4 5 2

4<sup>th</sup> pass: key = 2

1 3 4 5 2 → 1 2 3 4 5

# Insertion sort pseudo-code

Inputs: array A, array size: size

```
1.      FOR ind_key = 1 to size-1
           Add A[ind_key] to the sorted sequence
           A[1, .. ind_key-1]
2.      key = A[ind_key]
3.      ind_sorted = ind_key - 1
4.      WHILE ind_sorted >= 0 and A[ind_sorted]>key
5.          A[ind_sorted +1] = A[ind_sorted]
6.          ind_sorted = ind_sorted -1
7.      ENDWHILE
8.      A [ind_sorted +1] = key
9.  ENDFOR
```

# Selection sort example

A	0	1	2	3	4
	3	1	5	4	2

1<sup>st</sup> pass:  $\min(0, \text{size}-1) = 1$ , swap min to A[0]

1 3 5 4 2

2<sup>nd</sup> pass:  $\min(1, \text{size}-1) = 2$  swap min to A[1]

1 2 5 4 3

3<sup>rd</sup> pass:  $\min(2, \text{size}-1) = 3$  swap min to A[2]

1 2 3 4 5

4<sup>th</sup> pass:  $\min(3, \text{size}-1) = 4$  swap min to A[3]

1 2 3 4 5

# Selection sort pseudo-code

Inputs: array A, array size: size

```
FOR k = 0 TO k = size -1
    ind_min = k;
    FOR ind_not_sorted = k+1 TO size-1
        IF (A[ind_not_sorted] < A[ind_min])
            ind_min = ind_not_sorted
        ENDIF
    ENDFOR
    swap A[ind_min] with A[k]
ENDFOR
```

# Questions

- What happens after the first pass of the bubble-sort? What about after the second pass?
- Do you need to check the whole array in each pass of the bubble sort?
- What is the minimum number of passes for an array of size  $N$  in case of:
  - Bubble-sort
  - Insertion-sort
  - Selection-sort



# Questions

- Which sorting algorithm you think is better among the three discussed here?
- Why?