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(Note: Authors of books and articles listed in Sections 17.7 (p. 396), 18.5 (p. 408), 25.9 (pp. 581–584), 26.4 (p. 588) and in the main Bibliography (pp. 593–603) are not individually referenced in this index unless their names appear otherwise in the text.)

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