

# Signals and Systems

## Lab Experience Session 2

### Exercise 1

Write a code (Matlab or Python) that computes the convolution between two signals  $x[n]$  and  $y[n]$ :

- Applying the definition formula:  $z[n] = x[n] * y[n]$
- Using the matrix computation:  $\mathbf{z} = \mathbf{M}_y \mathbf{x}$
- Verify the obtained results for the convolution using the built-in function: Matlab's `conv` function or Python's `numpy.convolve`.

The two signals are defined as follows:

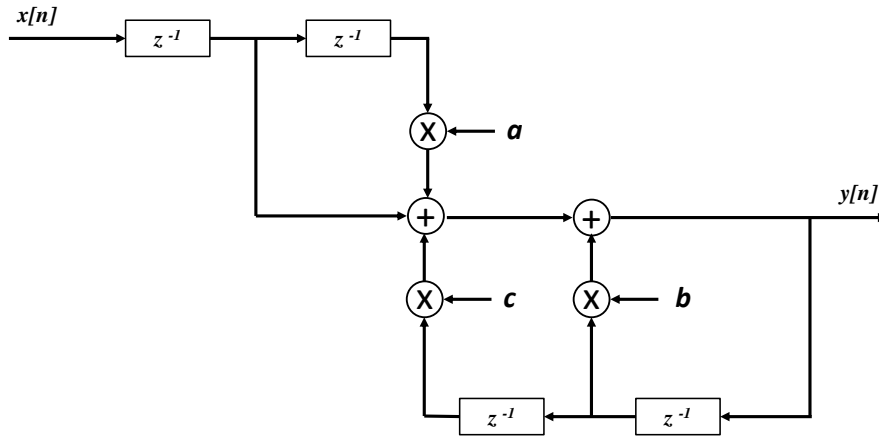
- $x[n] = Aa^n u[n]$ , where  $n \in ]-\infty, \infty[$ ,  $A = 4$  and  $a = -3/4$
- $y[n] = B \cdot r_{10}[n - 5]$ , where  $B = 2$

*Required outputs:*

- Plot the signals and the result of the convolution;
- Compare the results obtained with the different convolution implementations;
- What is the extension of the convolution?

## Exercise 2

Consider the block diagram of the following LTI system:



*Required outputs*

- Find the transfer function in the Z domain;
- Write the difference equation;
- Given  $a = 2$ ,  $b = 3/5$  and  $c = 1/9$ , determine the zeros, the poles and the region of convergence (ROC) of the LTI system;
- Determine the impulse response analytically and verify if it is correct through a script;
- Considering the input signal  $x[n] = (1/a)^n u[n]$ , compute the output  $y[n]$  both analytically using the inverse Z transform and using a script. For  $a$  you can assume the same value defined above. Plot  $x[n]$ ,  $y[n]$  and the impulse response  $h[n]$ .

## Exercise 3

Consider the following difference equation  $y[n] = k_1 x[n] + k_2 x[n-1] + k_3 x[n-2]$ , with  $k_1 = 1/4$ ,  $k_2 = 3/4$  and  $k_3 = -3/4$ .

*Required outputs*

- Draw the block diagram and determine the transfer function in the Z domain;
- Determine the zeros and the poles;
- Determine the impulse response both analytically and using a script;
- Compute the output  $y[n]$  assuming at the input the signal  $x[n] = r_5[n-3]$  and verify the result using a script. Then plot  $x[n]$ ,  $y[n]$  and the impulse response  $h[n]$ .