

HW0

Shane Drafahl

23 August, 2017

This is an inline equation $x + y = 3$

This is a displayed equation:

$$x + \frac{y}{z - \sqrt{3}} = 2$$

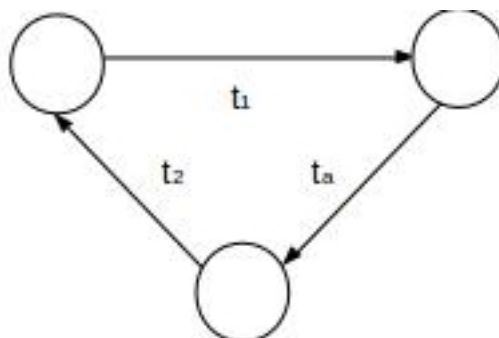
This is how you define a piece-wise linear function:

$$f(x) = \begin{cases} 3x + 2 & \text{if } x < 0 \\ 7x + 2 & \text{if } x \geq 0 \text{ and } x < 10 \\ 5x + 22 & \text{otherwise.} \end{cases}$$

This is a matrix:

9	9	9	9
6	6	6	
3		3	3

This is a figure incorporated in a LaTeX file



2. Show that \mathbb{N} (natural numbers) and \mathbb{Z} (integer numbers) are equinumerous.

To show that the set of natural numbers and integer numbers are equinumerous we have to show the cardinality of \mathbb{N} and \mathbb{Z} are the same. If there is a function $f: \mathbb{N} \rightarrow \mathbb{Z}$ that is bijective then the cardinalities of sets \mathbb{N} and \mathbb{Z} would be the same.

Suppose we have a function where $x \in \mathbb{N}$ and $f(x) \in \mathbb{Z}$

$$f(x) = \begin{cases} 0 & \text{if } x \text{ equals } 0 \\ \frac{x}{2} * -1 & \text{if } x \bmod 2 = 0 \\ \frac{(x-1)}{2} + 1 & \text{otherwise.} \end{cases}$$

If f is onto then $\forall_y \in \mathbb{Z} \exists_x \in \mathbb{N}$ where $f(x) = y$. Using existential instantiation and universal instantiation either $\frac{x}{2} * -1 = y$ or $\frac{(x-1)}{2} + 1 = y$.