

HW4

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1. Define a context-free grammar for the language $L = \{ 0^n 1^m 0^m 1^n \}$
Where S is the start production $G = \{ (S, A), (0, 1), S, P \}$
 $P = \{$
 $S \rightarrow 0S1 | 1A0 | \epsilon ,$
 $A \rightarrow 1A0 | \epsilon , \}$

2. Define a context-free grammar for the language $L = \{ a^n b^m : n \leq 3m \}$
Where S is the start production $G = \{ (S, B, C), (a, b), S, P \}$
 $P = \{$
 $S \rightarrow aB | Sb | b | \epsilon ,$
 $B \rightarrow aC | Bb | b ,$
 $C \rightarrow aSb | Db | b$
 $\}$

3. The truth value of a logical expression is defined recursively as: Where
S is the start production $G = \{ (S, A, B), (t, f, \wedge, \vee, \neg, (,), =), S, P \}$
 $P = \{$
 $S \rightarrow A = t | B = f ,$
 $A \rightarrow t | (A \wedge A) | (A \vee B) | (A \vee A) | (F \vee A) | \neg(B) ,$
 $B \rightarrow f | (B \wedge A) | (A \wedge B) | (B \vee B) | (B \wedge B) | \neg(A) \}$