Training in ade4 in R - Module I: Basic methods

Introduction

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2023-12-06

Material

The content of the course is available at

https://github.com/sdray/LausanneBasic/

In R, you can download the course by

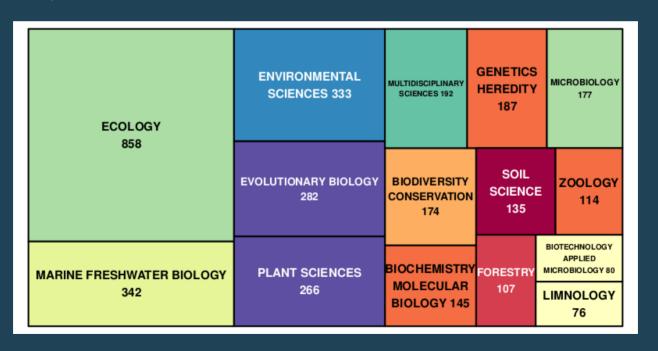
```
usethis::use_course("sdray/LausanneBasic", destdir = "~/Bureau/")
```

Required packages

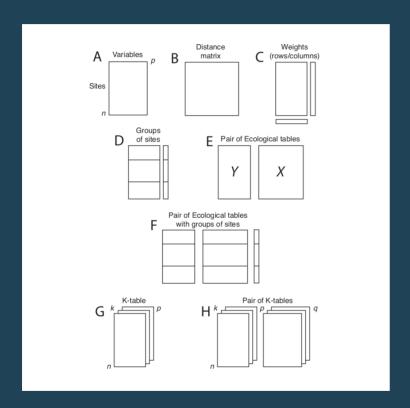
- ade4 to run the analyses
- adegraphics to represent results
- rgl to understand multivariate methods in interactive 3D

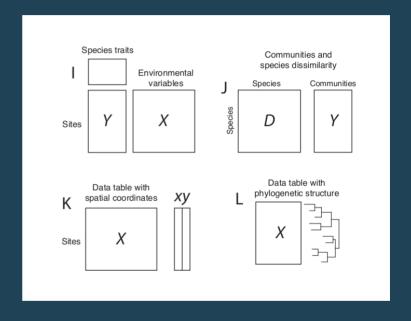
ade4

- R package since 2002
- Exploratory analysis of ecological data
 - Multivariate methods
 - Graphical functions

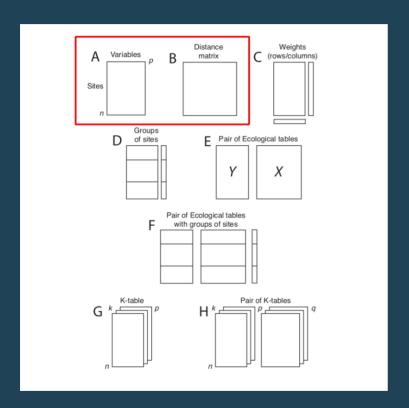


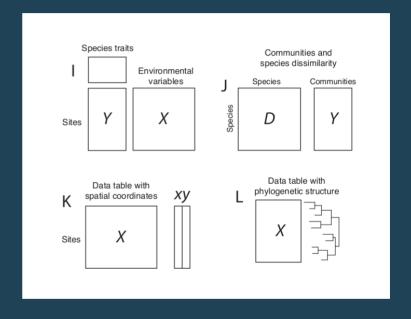
Data structure





Data structure





Module 1: course outline

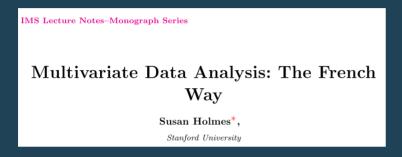
We will explore the geometric properties, outputs and interpretation of multivariate analysis focusing on one-table methods. Last afternoon for case studies.

variables



- Environmental variables
 - Quantitative variables → Principal Component Analysis (dudi.pca)
 - Categorical variables → Multiple Correspondence Analysis (dudi.acm)
 - Mix of both → Hill-Smith Analysis (dudi.hillsmith)
- Species table
 - Contingency table → Correspondence Analysis (dudi.coa)
 - Distance matrix → Principal Coordinates Analysis (dudi.pco)

ade4: the French way

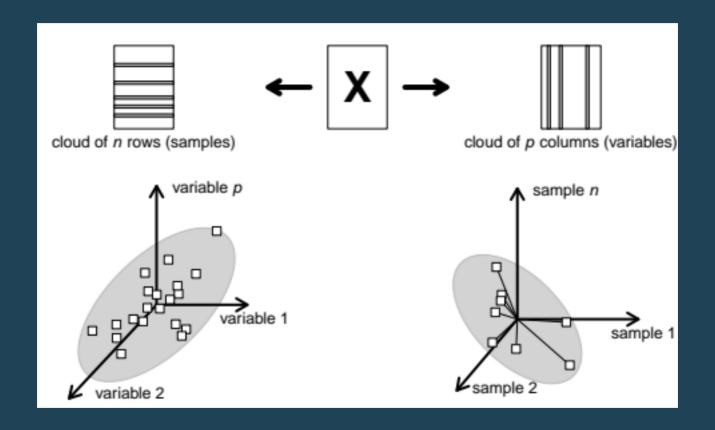




Implementation of functions in ade4 follows the duality diagram theory

More details are provided in the paper published in Journal of Statistical Software available here

Two geometric views



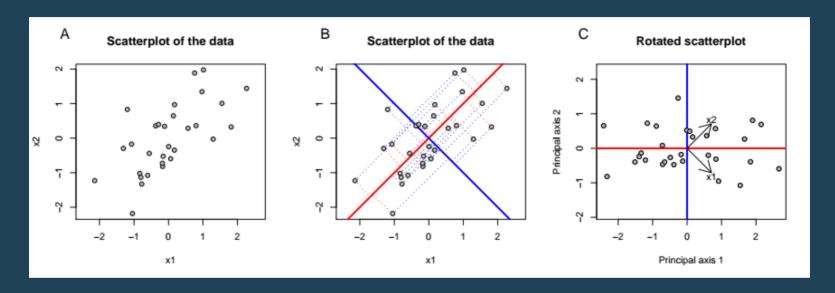
what are the main similarities and differences between the individuals?

what are the main relationships between the variables?

Explore the space of individuals

Go to practical 1

Geometric view for individuals



- Multivariate methods only perform geometric operations (rotations) to obtain the best viewpoint on the data
- When many variables are considered, dimension reduction is also applied to simplify the interpretation

Statistical triplet

Multivariate methods aim to answer these two questions and seek for small dimension hyperspaces (few axes) where the representations of individuals and variables are as close as possible to the original ones.

To answer the two previous questions, we define

- ${f Q}$, a p imes p positive symmetric matrix, used as an inner product in ${\Bbb R}^p$ and thus allows to measure distances between the n individuals
- \mathbf{D} , a $n \times n$ positive symmetric matrix, used as an inner product in \mathbb{R}^n and thus allows to measure relationships between the p variables.

 $(\mathbf{X},\mathbf{Q},\mathbf{D})$

Duality diagram theory

$$\mathbf{X}\mathbf{Q}\mathbf{X}^{\mathsf{T}}\mathbf{D}\mathbf{B} = \mathbf{B}\mathbf{\Lambda}$$

 $\mathbf{X}^{\mathsf{T}}\mathbf{D}\mathbf{X}\mathbf{Q}\mathbf{A} = \mathbf{A}\mathbf{\Lambda}$

- ullet ${f B}$ contains the principal components (${f B}^{ op}{f D}{f B}={f I}_r$).
- ullet ${f A}$ contains the principal axis (${f A}^{ op}{f Q}{f A}={f I}_r$).
- $\mathbf{L} = \mathbf{XQA}$ contains the row scores (projection of the rows of \mathbf{X} onto the principal axes)
- ullet ${f C}={f X}^{ op}{f D}{f B}$ contains the column scores (projection of the columns of ${f X}$ onto the principal components)

Maximization of:

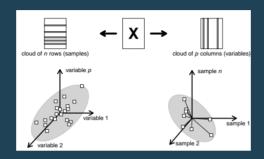
$$Q(\mathbf{a}) = \mathbf{a}^{ op} \mathbf{Q}^{ op} \mathbf{X}^{ op} \mathbf{D} \mathbf{X} \mathbf{Q} \mathbf{a} = \lambda ext{ and } S(\mathbf{b}) = \mathbf{b}^{ op} \mathbf{D}^{ op} \mathbf{X} \mathbf{Q} \mathbf{X}^{ op} \mathbf{D} \mathbf{b} = \lambda$$
 $\langle \mathbf{X} \mathbf{Q} \mathbf{a} | \mathbf{k}
angle_{\mathbf{D}} = \left\langle \mathbf{X}^t \mathbf{D} \mathbf{b} | \mathbf{a}
ight
angle_{\mathbf{Q}} = \sqrt{\lambda}$

Implementation in ade4

Computations are performed by the function as.dudi. This functions takes 3 arguments defining the statistical triplet and returns an object of class dudi that contains:

tion
data table
for rows
for columns
oonents
5

From the theory



• The principal axes

$$\mathbf{X}^{\mathsf{T}}\mathbf{D}\mathbf{X}\mathbf{Q}\mathbf{A} = \mathbf{A}\mathbf{\Lambda}$$

• The row scores

$$L = XQA$$

Maximization of

$$egin{aligned} Q(\mathbf{a}) &= \mathbf{a}^ op \mathbf{Q}^ op \mathbf{X}^ op \mathbf{D} \mathbf{X} \mathbf{Q} \mathbf{a} = \lambda \ Q(\mathbf{a}) &= \| \mathbf{X} \mathbf{Q} \mathbf{a} \|_{\mathbf{D}}^2 = \lambda \end{aligned}$$

• The principal components

$$\mathbf{X}\mathbf{Q}\mathbf{X}^{\mathsf{T}}\mathbf{D}\mathbf{K} = \mathbf{B}\mathbf{\Lambda}$$

• The column scores

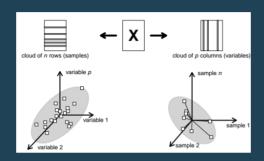
$$\mathbf{C} = \mathbf{X}^{\mathsf{T}} \mathbf{D} \mathbf{B}$$

Maximization of

$$S(\mathbf{b}) = \mathbf{b}^ op \mathbf{D}^ op \mathbf{X} \mathbf{Q} \mathbf{X}^ op \mathbf{D} \mathbf{b} = \lambda$$

$$S(\mathbf{b}) = \|\mathbf{X}^{ op}\mathbf{D}\mathbf{b}\|_{\mathbf{Q}}^2 = \lambda$$

To the practice in ade4



• The principal axes

\$c1

• The row scores

\$li

Maximization of

\$eig

• The principal components

\$11

• The column scores

\$co

Maximization of

\$eig

Compute a PCA by hand

Go to practical 1

Methods for dudi objects

- print
- summary
- screeplot
- scatter/biplot
- score
- is
- t
- inertia
- suprow/supcol
- reconst
- dist.dudi

User-level functions

- The as. dudi function is an internal function
- It is called by user-friendly functions corresponding to different analyses
- It can be used by experimented users to define their own analysis

Available methods

Different definitions of a statistical triplet correspond to different methods

Function name	Analysis name
dudi.pca	Principal component analysis
dudi.pco	Principal coordinate analysis
dudi.coa	Correspondence analysis
dudi.acm	Multiple correspondence analysis
dudi.dec	Decentered correspondence analysis
dudi.fca	Fuzzy correspondence analysis
dudi.fpca	Fuzzy PCA
dudi.mix	Mixed nalysis
dudi.hillsmith	Hill-Smith analysis
dudi.nsc	Non-symmetric correspondence analysis

Graphical functions

- Outputs of multivariate methods are usually provided as plots
- ade4 contains several graphical functions
- they have been re-implemented in a much more flexible way in the package adegraphics

A comprehensive overview of the package is available in its vignette available online or in R by:

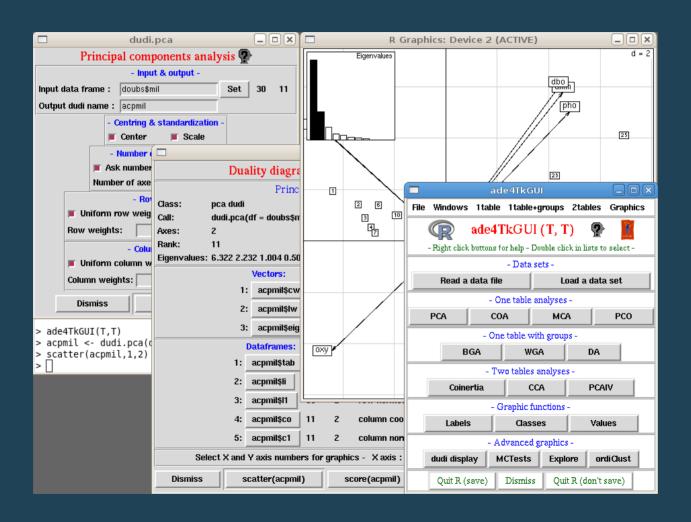
vignette("adegraphics")

See also the paper published in the R Journal here

The ade packages

- adegraphics: S4-lattice based multivariate graphics
- adespatial: spatial multiscale multivariate analysis
- adiv: analysis of diversity
- adehabitat: analysis of habitat selection by animals
- adegenet: classes and methods for the multivariate analysis of genetic markers
- adephylo: exploratory analyses for the phylogenetic comparative method
- ade4TkGUI: graphical interface

ade4TkGUI



Resources



• Mailing list:

http://listes.univlyon1.fr/wws/info/adelist

• Development:

https://github.com/sdray/ade4

• Courses (in French):

http://pbil.univlyon1.fr/R/enseignement.html

https://www.springer.com/fr/book/9781493988488