# Training in ade4 in R - Module I: Basic methods

Principal component analysis

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#### Data structure

#### variables



- One table with *p* variables measured on *n* individuals
- All variables are quantitative
- For instance
  - o sites environmental variables
  - o species traits
  - o individuals alleles
  - o populations alleles

## Objectives

- Identify what is the main information contained in the table
  - o Identify which variables are the most linked
  - o Identify the principal differences/similarities between individuals

#### Data

We consider the meaudret data set

```
library(ade4)
data(meaudret)
names(meaudret)

## [1] "env"    "design"    "spe"    "spe.names"

dim(meaudret$env)

## [1] 20 9

names(meaudret$env)

## [1] "Temp" "Flow" "pH"    "Cond" "Bdo5" "Oxyd" "Ammo" "Nitr" "Phos"
```

The data set contains an environmental table with 20 measurements of 9 environmental variables. The measurements have been made in 6 sites at each season along a small French stream (see ?meaudret)

#### head(meaudret\$design)

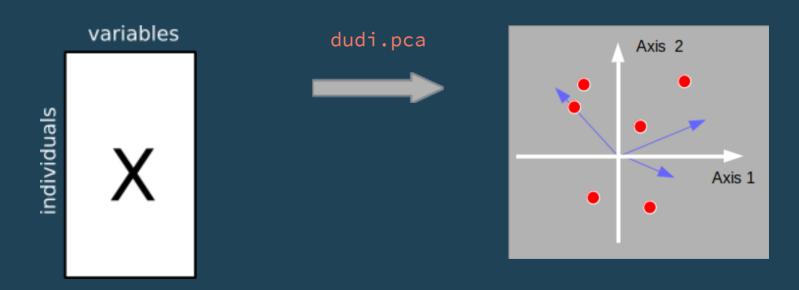
```
## season site
## sp_1 spring    S1
## sp_2 spring    S2
## sp_3 spring    S3
## sp_4 spring    S4
## sp_5 spring    S5
## su_1 summer    S1
```

#### We want to know

- what are the main environmental gradients, i.e., which variables co-vary (if any)
- which samples have similar/different environmental conditions

# Principal component analysis

- contains centred or scaled variables
- is the identity matrix (diagonal matrix with 1s)
- — is the diagonal matrix with —



## Maximized criteria

For individuals

For variables

o Centred data (

∘ Scaled data (

## The dudi.pca function

### Arguments

```
args(dudi.pca)
```

```
## function (df, row.w = rep(1, nrow(df))/nrow(df), col.w = rep(1,
## ncol(df)), center = TRUE, scale = TRUE, scannf = TRUE, nf = 2)
## NULL
```

- df is a data, frame with the data
- row.w and col.w are optional vectors of weights
- center and scale define the standardization of the data
- scannf and nf allow to set the number of dimensions to interpret

```
pca.meau <- dudi.pca(meaudret$env, scannf = FALSE)</pre>
```

#### Returned values

```
names(pca.meau)
    [1] "tab" "cw" "lw" "eig" "rank" "nf" "c1" "li"
                                                                   "CO"
##
It returns an object of class dudi containing:
 • $eig: eigenvalues ( )
 • $cw: column weights (
 • $\text{lw: row weights (} - )
 • $tab: transformed data table ( )
 • $c1: principal axes or variable loadings ( )
 • $li: row scores (
 • $11: principal components ( )
 • $co: column scores ( —
```

# Graphical representation and interpretation

As we have *two* analyses (individuals and variables spaces), two representations can be defined:

- **distance biplot** where and (\$c1, \$li) are superimposed.
- **correlation biplot** where and (\$11, \$co) are superimposed.

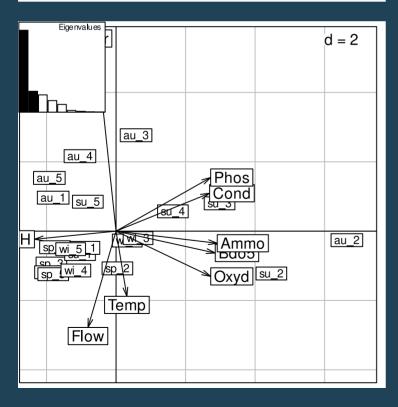
In the first interpretation, PCA finds coefficients for variables (\$c1) to compute a linear combination (\$li) that provides an ordination of individuals with the greatest dispersion (maximum variance).

In the second interpretation, PCA provides a linear combination (\$11) that maximise the correlations (\$co) with all variables (or covariances for centred PCA). Hence, it is the best summary of the variables.

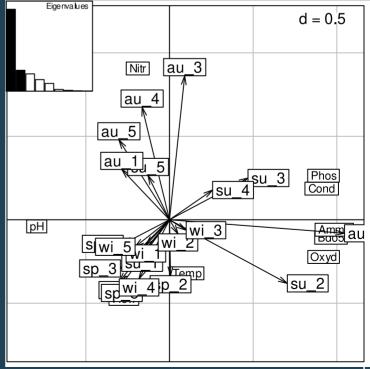
## The biplot function

library(adegraphics)

biplot(pca.meau)

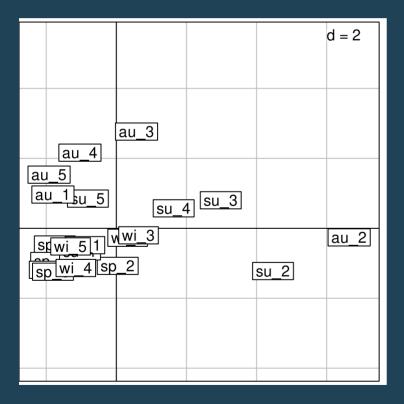


biplot(pca.meau, permute = TRUE)

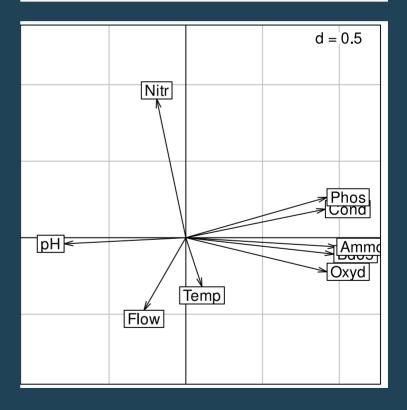


### Separate representations

s.label(pca.meau\$li)

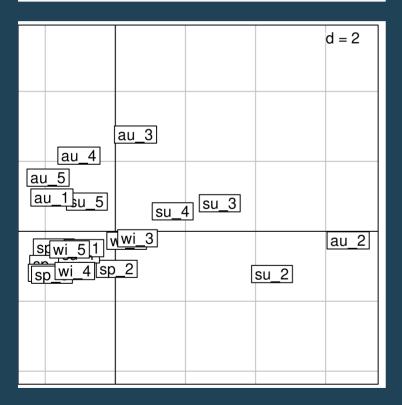


s.arrow(pca.meau\$co)

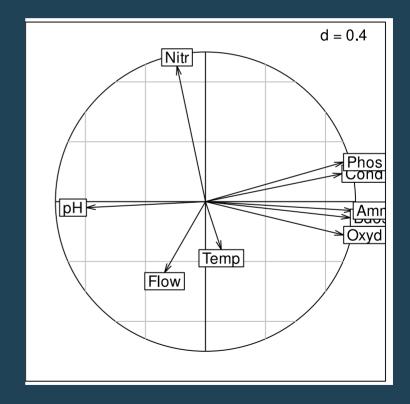


### Separate representations

s.label(pca.meau\$li)

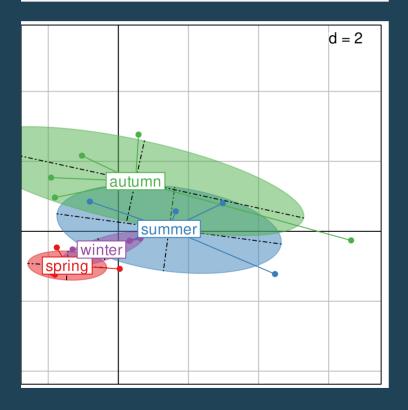


s.corcircle(pca.meau\$co)

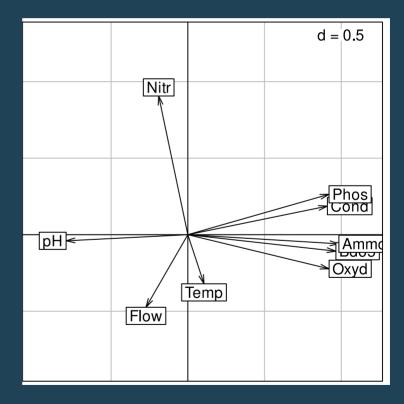


## Separate representations

s.class(pca.meau\$li, meaudret\$des

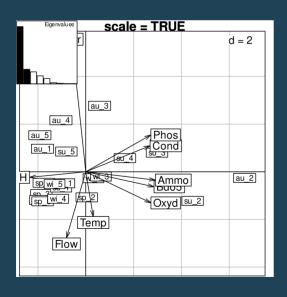


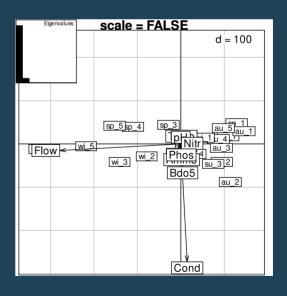
s.arrow(pca.meau\$co)



#### To scale or not to scale

Scaling should be performed when we do not want that differences in variances affect the results





In our case, we must scale the data as differences in variances are mainly due to differences in units

#### **Inertia statistics**

#### summary(pca.meau)

```
## Class: pca dudi
  Call: dudi.pca(df = meaudret$env, scannf = FALSE)
##
  Total inertia: 9
##
##
  Eigenvalues:
      Ax1
##
             Ax2 Ax3
                           Ax4
                                 Ax5
## 5.1747 1.3204 1.0934 0.7321
                                0.4902
##
  Projected inertia (%):
##
      Ax1
             Ax2
                    Ax3
                        Ax4 Ax5
##
  57.497 14.671 12.149 8.135 5.447
##
  Cumulative projected inertia (%):
      Ax1 Ax1:2 Ax1:3 Ax1:4 Ax1:5
##
##
  57.50 72.17 84.32 92.45 97.90
##
## (Only 5 dimensions (out of 9) are shown)
```

# **PCA** in practice

Go to practical 2