

cblearn: Comparison-based Machine Learning in Python

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Summary

The cblearn package implements comparison-based machine learning algorithms and routines to process comparison-based data in Python. Comparison-based learning algorithms are used when only comparisons of similarity between data points are available, but no explicit similarity scores or features. For example, humans struggle to assign *numeric* similarities to apples, pears, and bananas. Still, they can easily *compare* the similarity of pears and apples with the similarity of apples and bananas—pears and apples usually appear more similar. There exist comparison-based algorithms for most machine learning tasks, like clustering, regression, or classification (e.g., [Balcan et al., 2016](#); [Heikinheimo & Ukkonen, 2013](#); [Perrot et al., 2020](#)); The most frequently applied algorithms, however, are the so-called ordinal embedding algorithms (e.g., [Agarwal et al., 2007](#); [Amid & Ukkonen, 2015](#); [Anderton & Aslam, 2019](#); [Ghosh et al., 2019](#); [Maaten & Weinberger, 2012](#); [Tamuz et al., 2011](#); [Terada & Luxburg, 2014](#)). Ordinal embedding algorithms estimate a metric representation, such that the distances between embedded objects reflect the similarity comparisons. These embedding algorithms have recently come into fashion in psychology and cognitive science to objectively quantify the perceived similarity of various stimuli (e.g., [Haghiri et al., 2020](#); [Roads & Mozer, 2019](#); [Wills et al., 2009](#)).

Statement of need

This work presents cblearn, an open-source Python package for comparison-based learning. In contrast to related packages, cblearn provides not just a specific algorithm but an ecosystem for comparison-based data with access to multiple real-world datasets and a collection of algorithm implementations. cblearn is fast and user-friendly for applications but flexible for research on new algorithms and methods. The package integrates well into the scientific Python ecosystem; for example, third-party functions for cross-validation or hyperparameter tuning of scikit-learn estimators can typically be used with cblearn estimators. Although our package is relatively new, it has already been used for algorithm development ([Mandal et al., 2023](#)) and data analysis in several studies ([Assen & Pont, 2022](#); [Huber et al., 2024](#); [Künstle et al., 2022](#); [Sauer et al., 2023](#); [Schönmann et al., 2022](#); [Zhao et al., 2023](#)).

We designed cblearn as a modular package with functions for processing and converting the comparison data in all its varieties (cblearn.preprocessing, cblearn.utils, cblearn.metrics), routines to generate artificial or load real-world datasets (cblearn.datasets), and algorithms for ordinal embedding and clustering (cblearn.embedding, cblearn.cluster).

Various data formats supported

The atomic datum in comparison-based learning is the quadruplet, a comparison of the similarity δ between two pairs (i, j) and (k, l) , for example, asserting that $\delta(i, j) < \delta(k, l)$. Alternative comparisons like the triplet, where $i == l$, can be reduced to one or more

41 quadruplets. Comparison-based learning algorithms estimate classes, clusters, or metrics to
42 fulfill as many quadruplets as possible. In ordinal embedding, for example, the problem is to
43 find $x_i, x_j, x_k, x_l \in \mathbb{R}^d$ s.t. $\|x_i - x_j\|_2 < \|x_k - x_l\|_2 \Leftrightarrow \delta(i, j) < \delta(k, l)$.

44 Besides triplets and quadruplets, there are many ways to ask for comparisons. Some tasks
45 ask for the “odd-one-out”, the “most-central” object, or the two most similar objects to a
46 reference. `cblearn` can load these different queries and convert them to triplets, ready for
47 subsequent embedding or clustering tasks.

48 Different data types can store triplets, and `cblearn` converts them internally. A 2D array with
49 three columns for the object indices (i, j, k) stores a triplet per row. In some applications,
50 it is comfortable to separate the comparison “question” and “response”, which leads to an
51 additional list of labels 1, if $\delta(i, j) \leq \delta(i, k)$, and -1 , if $\delta(i, j) > \delta(i, k)$. An alternative format
52 stores triplets as a 3-dimensional sparse array. These sparse arrays convert fast back and forth
53 to dense 2D arrays while providing an intuitive comparison representation via multidimensional
54 indexing. For example, the identical triplet can be represented as `[[i, j, k]]`, `[[[i, k,`
55 `j]], [-1]]` or `sparse_arr[i, j, k] == 1`.

56 Interfaces to diverse datasets

57 There is no Iris, CIFAR, or ImageNet in comparison-based learning—the community lacks
58 accessible real-world datasets to evaluate new algorithms. `cblearn` provides access to various
59 real-world datasets, summarized in Figure 1, with functions to download and load the com-
60 parisons. These datasets—typically comparisons between images or words—consist of human
61 responses. Additionally, our package provides preprocessing functions to convert different
62 comparisons to triplets or quadruplets, which many algorithms expect.

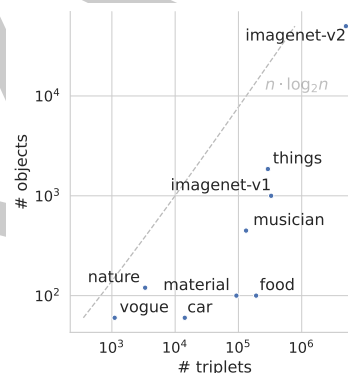


Figure 1: Real-world datasets that can be accessed with `cblearn` cover many object and triplet numbers. Please find a detailed description and references to the dataset authors in our package documentation.

63 Algorithms implemented for CPU and GPU

64 In the current version 0.1.2, `cblearn` implements an extensive palette of ordinal embedding
65 algorithms and a clustering algorithm (Table 1); additional algorithms can be contributed
66 easily within the modular design. Most algorithm implementations use `scipy` to be fast and
67 lightweight. Inspired by the work of Vankadara et al. (2021), we added GPU implementations
68 using `pytorch`, which use the stochastic optimization routines known from deep-learning
69 algorithms. These GPU implementations can be used with large datasets and rapidly adapted
70 thanks to automated differentiation.

Table 1: Algorithm implementations in cblearn. Most of these come in multiple variants: Different backends for small datasets on CPU or large datasets on GPU, or varied objective functions.

Algorithm	Reference
Crowd Kernel Learning	Tamuz et al. (2011)
Fast Ordinal Triplet Embedding	Jain et al. (2016)
Generalized Non-metric MDS	Agarwal et al. (2007)
Maximum-likelihood Difference Scaling	Maloney & Yang (2003)
Soft Ordinal Embedding	Terada & Luxburg (2014)
Ordinal Embedding Neural Network	Vankadara et al. (2021)
Stochastic Triplet Embedding	Maaten & Weinberger (2012)
ComparisonHC (clustering)	Perrot et al. (2020)

User-friendly and compatible API

One of Python's greatest strengths is the scientific ecosystem, into which cblearn integrates. Our package does not only make use of this ecosystem internally but adopts their API conventions—every user of scikit-learn (Buitinck et al., 2013; Pedregosa et al., 2011) is already familiar with the API of cblearn: Estimator objects use the well-known scikit-learn methods `.fit(X, y)`, `.transform(X)`, and `.predict(X)`. This convention allows the use of many routines from the scikit-learn ecosystem with cblearn's estimators while representing comparisons as numpy arrays (Harris et al., 2020). Interested readers can find a code example in the [Supplementary Material](#), which shows in just four lines how to fetch a real-world dataset, preprocess the data, estimate an embedding, and cross-validate the fit. More examples are available in the package's documentation.

Related work and empirical comparison

Most comparison-based learning algorithms were implemented independently as part of a research paper (e.g., Ghoshdastidar et al., 2019; Hebart et al., 2020; Maaten & Weinberger, 2012; Roads & Mozer, 2019); Just a few of these implementations, for example loe (Terada & Luxburg, 2014) or psiz (Roads & Mozer, 2019), come in the form of software packages.

Related packages with collections of comparison-based learning algorithms have a focus on metric learning (metric-learn with a high compatibility to scikit-learn, de Vazelhes et al., 2020) and crowd-sourced data collection, using active ordinal embedding algorithms Sievert et al. (2023). Our package cblearn, on the other hand, focuses on providing comparison data and interoperable estimator implementations of the remaining areas of comparison-based learning.

A small empirical comparison to third-party packages reveals that cblearn's algorithm implementations typically are accurate and fast. Details are described in [Supplementary Material](#). A more comprehensive evaluation of various ordinal embedding algorithms per se, focusing on large data sets, can be found in Vankadara et al. (2021).

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