```
In [1]: # Initialize autograder
    # If you see an error message, you'll need to do
    # pip3 install otter-grader
    import otter
    grader = otter.Notebook()
```

Project 3: Predicting Taxi Ride Duration

Due Date: Wednesday 3/4/20, 11:59PM

Collaboration Policy

Data science is a collaborative activity. While you may talk with others about the project, we ask that you **write your solutions individually**. If you do discuss the assignments with others please **include their names** at the top of your notebook.

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Score Breakdown

Question	Points		
1b	2		
1c	3		
1d	2		
2a	1		
2b	2		
3a	2		
3b	1		
3с	2		
3d	2		
4a	2		
4b	2		
4c	2		
4d	2		
4e	2		
4f	2		
4g	4		
5b	7		
5c	3		
Total	43		

This Assignment

In this project, you will use what you've learned in class to create a regression model that predicts the travel time of a taxi ride in New York. Some questions in this project are more substantial than those of past projects.

After this project, you should feel comfortable with the following:

- The data science lifecycle: data selection and cleaning, EDA, feature engineering, and model selection.
- Using sklearn to process data and fit linear regression models.
- Embedding linear regression as a component in a more complex model.

First, let's import:

```
In [2]: import numpy as np
import pandas as pd

import matplotlib.pyplot as plt
%matplotlib inline

import seaborn as sns
```

The Data

Attributes of all <u>yellow taxi (https://en.wikipedia.org/wiki/Taxicabs of New York City)</u> trips in January 2016 are published by the <u>NYC Taxi and Limosine Commission (https://www1.nyc.gov/site/tlc/about/tlc-trip-record-data.page)</u>.

The full data set takes a long time to download directly, so we've placed a simple random sample of the data into taxi.db, a SQLite database. You can view the code used to generate this sample in the taxi_sample.ipynb file included with this project (not required).

Columns of the taxi table in taxi.db include:

- pickup_datetime: date and time when the meter was engaged
- dropoff datetime: date and time when the meter was disengaged
- pickup lon: the longitude where the meter was engaged
- pickup lat: the latitude where the meter was engaged
- dropoff lon: the longitude where the meter was disengaged
- dropoff lat: the latitude where the meter was disengaged
- passengers: the number of passengers in the vehicle (driver entered value)
- distance: trip distance
- duration: duration of the trip in seconds

Your goal will be to predict duration from the pick-up time, pick-up and drop-off locations, and distance.

Part 1: Data Selection and Cleaning

In this part, you will limit the data to trips that began and ended on Manhattan Island (<u>map</u> (<a href="https://www.google.com/maps/place/Manhattan,+New+York,+NY/@40.7590402,-74.0394431,12z/data=!3m1!4b² 73.9712488)).

The below cell uses a SQL query to load the taxi table from taxi.db into a Pandas DataFrame called all_taxi.

It only includes trips that have both pick-up and drop-off locations within the boundaries of New York City:

- Longitude is between -74.03 and -73.75 (inclusive of both boundaries)
- Latitude is between 40.6 and 40.88 (inclusive of both boundaries)

You don't have to change anything, just run this cell.

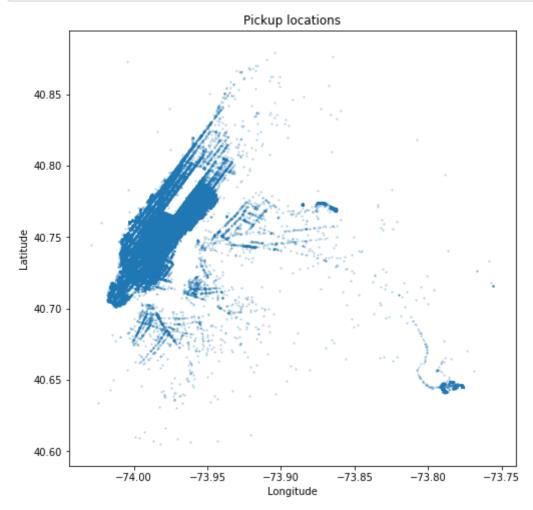
```
In [3]: import sqlite3
        conn = sqlite3.connect('taxi.db')
        lon bounds = [-74.03, -73.75]
        lat bounds = [40.6, 40.88]
        c = conn.cursor()
        my string = 'SELECT * FROM taxi WHERE'
        for word in ['pickup_lat', 'AND dropoff_lat']:
            my string += ' {} BETWEEN {} AND {}'.format(word, lat bounds[0], lat
        bounds[1])
        for word in ['AND pickup lon', 'AND dropoff lon']:
            my string += ' {} BETWEEN {} AND {}'.format(word, lon bounds[0], lon
        bounds[1])
        c.execute(my string)
        results = c.fetchall()
        row res = conn.execute('select * from taxi')
        names = list(map(lambda x: x[0], row res.description))
        all taxi = pd.DataFrame(results)
        all taxi.columns = names
        all taxi.head()
```

Out[3]:

	pickup_datetime	dropoff_datetime	pickup_lon	pickup_lat	dropoff_lon	dropoff_lat	passengers
0	2016-01-30 22:47:32	2016-01-30 23:03:53	-73.988251	40.743542	-74.015251	40.709808	1
1	2016-01-04 04:30:48	2016-01-04 04:36:08	-73.995888	40.760010	-73.975388	40.782200	1
2	2016-01-07 21:52:24	2016-01-07 21:57:23	-73.990440	40.730469	-73.985542	40.738510	1
3	2016-01-01 04:13:41	2016-01-01 04:19:24	-73.944725	40.714539	-73.955421	40.719173	1
4	2016-01-08 18:46:10	2016-01-08 18:54:00	-74.004494	40.706989	-74.010155	40.716751	5

A scatter plot of pickup locations shows that most of them are on the island of Manhattan. The empty white rectangle is Central Park; cars are not allowed there.

```
In [4]: def pickup_scatter(t):
    plt.scatter(t['pickup_lon'], t['pickup_lat'], s=2, alpha=0.2)
    plt.xlabel('Longitude')
    plt.ylabel('Latitude')
    plt.title('Pickup locations')
plt.figure(figsize=(8, 8))
    pickup_scatter(all_taxi)
```



The two small blobs outside of Manhattan with very high concentrations of taxi pick-ups are airports.

Question 1b

Create a DataFrame called clean taxi that only includes trips with a positive passenger count, a positive distance, a duration of at least 1 minute and at most 1 hour, and an average speed of at most 100 miles per hour. Inequalities should not be strict (e.g., <= instead of <) unless comparing to 0.

The provided tests check that you have constructed clean taxi correctly.

```
In [5]: clean taxi = all taxi.copy()
        clean taxi = clean taxi[(clean taxi["passengers"] > 0) & (clean taxi["dis
        tance"] > 0) \
                                 & (60 <= clean taxi["duration"]) & (clean taxi["d
        uration"] <= 3600)]</pre>
        clean_taxi["avg_speed"] = clean taxi["distance"]/(clean taxi["duration"]/
        3600)
        clean taxi = clean taxi[clean taxi["avg speed"] <= 100]</pre>
        clean taxi = clean taxi.drop("avg speed", axis=1)
In [6]: grader.check("q1b")
```

Out [6]: All tests passed!

Question 1c (challenging)

Create a DataFrame called manhattan taxi that only includes trips from clean taxi that start and end within a polygon that defines the boundaries of Manhattan Island (https://www.google.com/maps/place/Manhattan,+New+York,+NY/@40.7590402,-74.0394431,12z/data=!3m1!4b <u>73.9712488</u>).

The vertices of this polygon are defined in manhattan.csv as (latitude, longitude) pairs, which are published here (https://gist.github.com/baygross/5430626).

An efficient way to test if a point is contained within a polygon is described on this page (http://alienryderflex.com/polygon/). There are even implementations on that page (though not in Python). Even with an efficient approach, the process of checking each point can take several minutes. It's best to test your work on a small sample of clean taxi before processing the whole thing. (To check if your code is working, draw a scatter diagram of the (lon, lat) pairs of the result; the scatter diagram should have the shape of Manhattan.)

The provided tests check that you have constructed manhattan taxi correctly. It's not required that you implement the in manhattan helper function, but that's recommended. If you cannot solve this problem, you can still continue with the project; see the instructions below the answer cell.

```
def in manhattan(x, y):
            """Whether a longitude-latitude (x, y) pair is in the Manhattan polyg
        on."""
            polyX = polygon["lon"].tolist()
            polyY = polygon["lat"].tolist()
            polyCorners = len(polyX)
            j = polyCorners - 1
            oddNodes = False
            for i in range(polyCorners):
                if (((polyY[i] < y) & (polyY[j] >= y)) | ((polyY[j] < y) & (polyY
        [i] >= y))):
                     if (polyX[i] + (y - polyY[i]) / (polyY[j] - polyY[i]) * (poly
        X[j] - polyX[i]) < x):
                        oddNodes = not oddNodes
                j = i
            return oddNodes
        clean taxi first 100 = clean taxi[:100]
        # Recommended: Then, apply this function to every trip to filter clean ta
        хi.
        # 1) Make numpy arrays of pickup lons and pickup lats
        pickup lon arr = clean taxi["pickup lon"].to numpy()
        pickup lat arr = clean taxi["pickup lat"].to numpy()
        dropoff lon arr = clean taxi["dropoff lon"].to numpy()
        dropoff lat arr = clean taxi["dropoff lat"].to numpy()
        # 2) Iterate over the arrays, checking if the points are valid (hint: loo
        k at zip() in python)
        manhattan mask = np.zeros((len(clean taxi), 1), dtype=bool)
        lat lon list = list(zip(pickup lon arr, pickup lat arr, dropoff lon arr,
        dropoff lat arr))
        for i in range(len(lat lon list)):
            if in manhattan(lat lon list[i][0], lat lon list[i][1]) \
                     and in manhattan(lat lon list[i][2], lat lon list[i][3]):
                manhattan mask[i] = True
        # 3) Construct a boolean mask from the results, and use it to select rows
         from your dataframe
        manhattan taxi = clean_taxi[manhattan_mask].copy()
In [8]: | grader.check("q1c")
Out [8]: All tests passed!
```

Recommended: First develop and test a function that takes a position and returns whether it's in Manhattan.

In [7]: | polygon = pd.read csv('manhattan.csv')

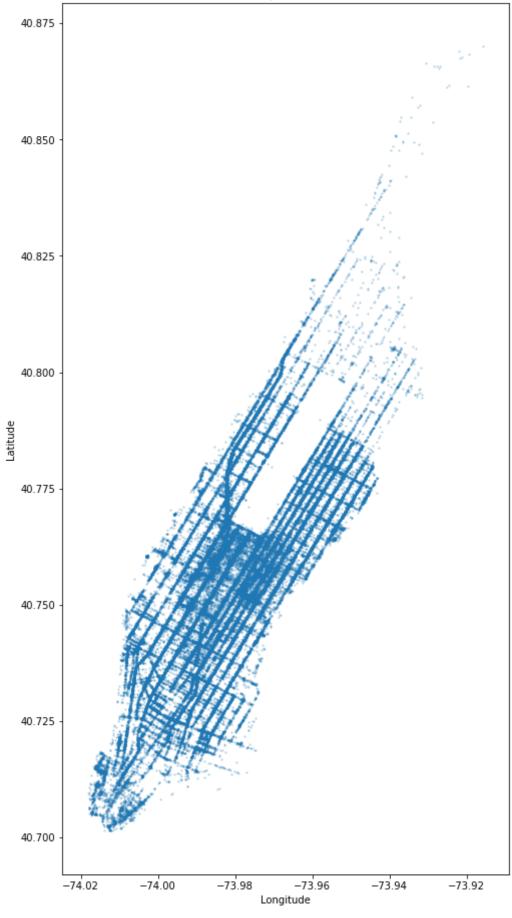
If you are unable to solve the problem above, have trouble with the tests, or want to work on the rest of the project before solving it, run the following cell to load the cleaned Manhattan data directly. (Note that you may not solve the previous problem just by loading this data file; you have to actually write the code.)

```
In [9]: # manhattan_taxi = pd.read_csv('manhattan_taxi.csv')
```

A scatter diagram of only Manhattan taxi rides has the familiar shape of Manhattan Island.

In [10]: plt.figure(figsize=(8, 16))
 pickup_scatter(manhattan_taxi)





Question 1d

Print a summary of the data selection and cleaning you performed. Your Python code should not include any number literals, but instead should refer to the shape of all_taxi, clean_taxi, and manhattan taxi.

E.g., you should print something like: "Of the original 1000 trips, 21 anomalous trips (2.1%) were removed through data cleaning, and then the 600 trips within Manhattan were selected for further analysis."

(Note that the numbers in the example above are not accurate.)

One way to do this is with Python's f-strings. For instance,

```
name = "Joshua"
print(f"Hi {name}, how are you?")
prints out Hi Joshua, how are you?.
```

Please ensure that your Python code does not contain any very long lines, or we can't grade it.

Your response will be scored based on whether you generate an accurate description and do not include any number literals in your Python expression, but instead refer to the dataframes you have created.

Of the original 97692 trips, 1247 anomalous trips (1.28%) were removed through data cleaning based on negative passenger count, negative distance, duration less than 1 minute or greater than 1 hour, or average speed greater than 100 miles per hour. Then the 82800 trips with both pick up and dropoff within Manhattan were selected for further analysis. At rip was determined to be within Manhattan based on the latitude and longitude of pickup and dropoff being calculated to be within a polygon that defines the boundaries of Manhattan Island.

Part 2: Exploratory Data Analysis

In this part, you'll choose which days to include as training data in your regression model.

Your goal is to develop a general model that could potentially be used for future taxi rides. There is no guarantee that future distributions will resemble observed distributions, but some effort to limit training data to typical examples can help ensure that the training data are representative of future observations.

January 2016 had some atypical days. New Year's Day (January 1) fell on a Friday. MLK Day was on Monday, January 18. A historic blizzard (https://en.wikipedia.org/wiki/January 2016 United States blizzard) passed through New York that month. Using this dataset to train a general regression model for taxi trip times must account for these unusual phenomena, and one way to account for them is to remove atypical days from the training data.

Question 2a

Add a column labeled date to manhattan_taxi that contains the date (but not the time) of pickup, formatted as a datetime.date value (docs (https://docs.python.org/3/library/datetime.html#date-objects)).

The provided tests check that you have extended manhattan taxi correctly.

Question 2b

Create a data visualization that allows you to identify which dates were affected by the historic blizzard of January 2016. Make sure that the visualization type is appropriate for the visualized data.

As a hint, consider how taxi usage might change on a day with a blizzard. How could you visualize/plot this?

Finally, we have generated a list of dates that should have a fairly typical distribution of taxi rides, which excludes holidays and blizzards. The cell below assigns final_taxi to the subset of manhattan_taxi that is on these days. (No changes are needed; just run this cell.)

```
In []: import calendar
import re

from datetime import date

atypical = [1, 2, 3, 18, 23, 24, 25, 26]
typical_dates = [date(2016, 1, n) for n in range(1, 32) if n not in atypical]
typical_dates

print('Typical dates:\n')
pat = ' [1-3]|18 | 23| 24|25 |26 '
print(re.sub(pat, ' ', calendar.month(2016, 1)))

final_taxi = manhattan_taxi[manhattan_taxi['date'].isin(typical_dates)]
```

You are welcome to perform more exploratory data analysis, but your work will not be scored. Here's a blank cell to use if you wish. In practice, further exploration would be warranted at this point, but the project is already pretty long.

```
In [ ]: # Optional: More EDA here
```

Part 3: Feature Engineering

In this part, you'll create a design matrix (i.e., feature matrix) for your linear regression model. This is analagous to the pipelines you've built already in class: you'll be adding features, removing labels, and scaling among other things.

You decide to predict trip duration from the following inputs: start location, end location, trip distance, time of day, and day of the week (*Monday, Tuesday, etc.*).

You will ensure that the process of transforming observations into a design matrix is expressed as a Python function called <code>design_matrix</code>, so that it's easy to make predictions for different samples in later parts of the project.

Because you are going to look at the data in detail in order to define features, it's best to split the data into training and test sets now, then only inspect the training set.

```
In []: import sklearn.model_selection

train, test = sklearn.model_selection.train_test_split(
    final_taxi, train_size=0.8, test_size=0.2, random_state=42)
    print('Train:', train.shape, 'Test:', test.shape)
```

Question 3a

Create a box plot that compares the distributions of taxi trip durations for each day **using train only**. Individual dates should appear on the horizontal axis, and duration values should appear on the vertical axis. Your plot should look like the one below.

You can generate this type of plot using sns.boxplot

Question 3b

In one or two sentences, describe the assocation between the day of the week and the duration of a taxi trip. Your answer should be supported by your boxplot above.

Note: The end of Part 2 showed a calendar for these dates and their corresponding days of the week.

The duration of a taxi trip increases for the days later in the week. This is supported by the boxplot "Duration by Day of Week" by larger outliers, larger third quartile, and larger medians later in the week. We can also observe there is a greater variability in the interquartile range later in the week.

Below, the provided augment function adds various columns to a taxi ride dataframe.

- hour: The integer hour of the pickup time. E.g., a 3:45pm taxi ride would have 15 as the hour. A 12:20am ride would have 0.
- day: The day of the week with Monday=0, Sunday=6.
- weekend: 1 if and only if the day is Saturday or Sunday.
- period: 1 for early morning (12am-6am), 2 for daytime (6am-6pm), and 3 for night (6pm-12pm).
- speed : Average speed in miles per hour.

No changes are required; just run this cell.

```
In [ ]: | def speed(t):
            """Return a column of speeds in miles per hour."""
            return t['distance'] / t['duration'] * 60 * 60
        def augment(t):
            """Augment a dataframe t with additional columns."""
            u = t.copy()
            pickup time = pd.to datetime(t['pickup datetime'])
            u.loc[:, 'hour'] = pickup time.dt.hour
            u.loc[:, 'day'] = pickup_time.dt.weekday
            u.loc[:, 'weekend'] = (pickup time.dt.weekday >= 5).astype(int)
            u.loc[:, 'period'] = np.digitize(pickup time.dt.hour, [0, 6, 18])
            u.loc[:, 'speed'] = speed(t)
            return u
        train = augment(train)
        test = augment(test)
        train.iloc[0,:] # An example row
```

Question 3c

Use sns.distplot to create an overlaid histogram comparing the distribution of average speeds for taxi rides that start in the early morning (12am-6am), day (6am-6pm; 12 hours), and night (6pm-12am; 6 hours). Your plot should look like this:

```
In []: ax = sns.distplot(train[train["period"] == 1]["speed"], color="red", labe
l="Early Morning")
ax = sns.distplot(train[train["period"] == 2]["speed"], color="blue", lab
el="Day")
ax = sns.distplot(train[train["period"] == 3]["speed"], color="green", la
bel="Night")
ax = ax.legend()
```

It looks like the time of day is associated with the average speed of a taxi ride.

Question 3d

Manhattan can roughly be divided into Lower, Midtown, and Upper regions. Instead of studying a map, let's approximate by finding the first principal component of the pick-up location (latitude and longitude).

<u>Principal component analysis (https://en.wikipedia.org/wiki/Principal component analysis)</u> (PCA) is a technique that finds new axes as linear combinations of your current axes. These axes are found such that the first returned axis (the first principal component) explains the most variation in values, the 2nd the second most, etc.

Add a region column to train that categorizes each pick-up location as 0, 1, or 2 based on the value of each point's first principal component, such that an equal number of points fall into each region.

Read the documentation of pd.qcut_ (<a href="https://pandas.pydata.org/pandas-pydata.org/p

You don't need to add any lines to this solution. Just fill in the assignment statements to complete the implementation.

Before implementing PCA, it is important to scale and shift your values. The line with np.linalg.svd will return your transformation matrix, among other things. You can then use this matrix to convert points in (lat, lon) space into (PC1, PC2) space.

Hint: If you are failing the tests, try visualizing your processed data to understand what your code might be doing wrong.

The provided tests ensure that you have answered the question correctly.

```
In [ ]: # Find the first principle component
        D = train[["pickup lon", "pickup lat"]]
        pca n = len(train)
        pca means = D.mean()
        X = (D - pca means) / np.sqrt(pca n)
        u, s, vt = np.linalg.svd(X, full matrices=False)
        def add region(t):
            """Add a region column to t based on vt above."""
            D = t[["pickup lon", "pickup lat"]]
            assert D.shape[0] == t.shape[0], 'You set D using the incorrect tabl
        e '
            # Always use the same data transformation used to compute vt
            X = (D - pca means) / np.sqrt(pca n)
            first pc = X.dot(vt)[0]
            t.loc[:,'region'] = pd.qcut(first pc, 3, labels=[0, 1, 2])
        add region(train)
        add region(test)
```

```
In [ ]: grader.check("q3d")
```

Let's see how PCA divided the trips into three groups. These regions do roughly correspond to Lower Manhattan (below 14th street), Midtown Manhattan (between 14th and the park), and Upper Manhattan (bordering Central Park). No prior knowledge of New York geography was required!

```
In [ ]: plt.figure(figsize=(8, 16))
    for i in [0, 1, 2]:
        pickup_scatter(train[train['region'] == i])
```

Question 3e (ungraded)

Use sns.distplot to create an overlaid histogram comparing the distribution of speeds for nighttime taxi rides (6pm-12am) in the three different regions defined above. Does it appear that there is an association between region and average speed during the night?

```
In [ ]: ...
```

Finally, we create a design matrix that includes many of these features. Quantitative features are converted to standard units, while categorical features are converted to dummy variables using one-hot encoding. The period is not included because it is a linear combination of the hour. The weekend variable is not included because it is a linear combination of the day. The speed is not included because it was computed from the duration; it's impossible to know the speed without knowing the duration, given that you know the distance.

```
In []: from sklearn.preprocessing import StandardScaler
        num_vars = ['pickup_lon', 'pickup lat', 'dropoff lon', 'dropoff lat', 'di
        cat vars = ['hour', 'day', 'region']
        scaler = StandardScaler()
        scaler.fit(train[num vars])
        def design matrix(t):
            """Create a design matrix from taxi ride dataframe t."""
            scaled = t[num vars].copy()
            scaled.iloc[:,:] = scaler.transform(scaled) # Convert to standard uni
        ts
            categoricals = [pd.get dummies(t[s], prefix=s, drop first=True) for s
            return pd.concat([scaled] + categoricals, axis=1)
        # This processes the full train set, then gives us the first item
        # Use this function to get a processed copy of the dataframe passed in
        # for training / evaluation
        design matrix(train).iloc[0,:]
```

Part 4: Model Selection

In this part, you will select a regression model to predict the duration of a taxi ride.

Important: Tests in this part do not confirm that you have answered correctly. Instead, they check that you're somewhat close in order to detect major errors. It is up to you to calculate the results correctly based on the question descriptions.

Question 4a

Assign constant_rmse to the root mean squared error on the **test** set for a constant model that always predicts the mean duration of all **training set** taxi rides.

```
In []: def rmse(errors):
    """Return the root mean squared error."""
    return np.sqrt(np.mean(errors ** 2))

    constant_rmse = rmse(np.mean(train["duration"])-test["duration"])
    constant_rmse
In []: grader.check("q4a")
```

Question 4b

Assign simple_rmse to the root mean squared error on the test set for a simple linear regression model that uses only the distance of the taxi ride as a feature (and includes an intercept).

Terminology Note: Simple linear regression means that there is only one covariate. Multiple linear regression means that there is more than one. In either case, you can use the LinearRegression model from sklearn to fit the parameters to data.

```
In []: from sklearn.linear_model import LinearRegression

model = LinearRegression()
    y_train = train["duration"].values.reshape(-1, 1)
    X_train = train["distance"].values.reshape(-1, 1)
    y_test = test["duration"].values.reshape(-1, 1)
    X_test = test["distance"].values.reshape(-1, 1)
    model.fit(X_train, y_train)
    preds = model.predict(X_test)
    simple_rmse = rmse(preds-y_test)
    simple_rmse
In []: grader.check("q4b")
```

Question 4c

Assign linear_rmse to the root mean squared error on the test set for a linear regression model fitted to the training set without regularization, using the design matrix defined by the design_matrix function from Part 3.

The provided tests check that you have answered the question correctly and that your <code>design_matrix</code> function is working as intended.

```
In []: model = LinearRegression()
    y_train = train["duration"].values.reshape(-1, 1)
    X_train = design_matrix(train)
    y_test = test["duration"].values.reshape(-1, 1)
    X_test = design_matrix(test)
    model.fit(X_train, y_train)
    preds = model.predict(X_test)
    linear_rmse = rmse(preds-y_test)
    linear_rmse
In []: grader.check("q4c")
```

Question 4d

For each possible value of <code>period</code>, fit an unregularized linear regression model to the subset of the training set in that <code>period</code>. Assign <code>period_rmse</code> to the root mean squared error on the test set for a model that first chooses linear regression parameters based on the observed period of the taxi ride, then predicts the duration using those parameters. Again, fit to the training set and use the <code>design_matrix</code> function for features.

```
In []: model = LinearRegression()
    errors = []

for v in np.unique(train['period']):
        model.fit(design_matrix(train[train["period"] == v]), train[train["period"] == v].loc[:, "duration"])
        preds = model.predict(design_matrix(test[test["period"] == v]))
        errors.extend(preds-(test[test["period"] == v].loc[:, "duration"]).to
        list())
        period_rmse = rmse(np.array(errors))
        period_rmse
In []: grader.check("q4d")
```

This approach is a simple form of decision tree regression, where a different regression function is estimated for each possible choice among a collection of choices. In this case, the depth of the tree is only 1.

Question 4e

In one or two sentences, explain how the period regression model above could possibly outperform linear regression when the design matrix for linear regression already includes one feature for each possible hour, which can be combined linearly to determine the period value.

This is possible because in a given dataset there may be instances periodically where the data correlates differently. For the taxi trip dataset, this could be periods corresponding to peak driving hours such as pre-work and post-work rush hours. This means that the data is nonlinear, but by separating out the features by period the model can more accurately represent the data.

Question 4f

Instead of predicting duration directly, an alternative is to predict the average *speed* of the taxi ride using linear regression, then compute an estimate of the duration from the predicted speed and observed distance for each ride.

Assign <code>speed_rmse</code> to the root mean squared error in the **duration** predicted by a model that first predicts speed as a linear combination of features from the <code>design_matrix</code> function, fitted on the training set, then predicts duration from the predicted speed and observed distance.

Hint: Speed is in miles per hour, but duration is measured in seconds. You'll need the fact that there are 60 * 60 = 3,600 seconds in an hour.

```
In []: model = LinearRegression()

y_train = train["speed"].values.reshape(-1, 1)
X_train = design_matrix(train)
y_test = test["speed"].values.reshape(-1, 1)
X_test = design_matrix(test)
model.fit(X_train, y_train)
pred_speeds = model.predict(X_test)
pred_durations = (test["distance"].values.reshape(-1, 1)*60*60)/pred_spee
ds

speed_rmse = rmse(pred_durations-test["duration"].values.reshape(-1, 1))
speed_rmse
In []: grader.check("q4f")
```

Optional: Explain why predicting speed leads to a more accurate regression model than predicting duration directly. You don't need to write this down.

Question 4g

Finally, complete the function tree_regression_errors (and helper function speed_error) that combines the ideas from the two previous models and generalizes to multiple categorical variables.

The tree regression errors should:

- Find a different linear regression model for each possible combination of the variables in choices;
- Fit to the specified outcome (on train) and predict that outcome (on test) for each combination (outcome will be 'duration' or 'speed');
- Use the specified <code>error_fn</code> (either <code>duration_error</code> or <code>speed_error</code>) to compute the error in predicted duration using the predicted outcome;
- Aggregate those errors over the whole test set and return them.

You should find that including each of period, region, and weekend improves prediction accuracy, and that predicting speed rather than duration leads to more accurate duration predictions.

If you're stuck, try putting print statements in the skeleton code to see what it's doing.

```
choices = ['period', 'region', 'weekend']
        # def duration error(predictions, observations):
              """Error between duration predictions (array) and observations (dat
        a frame)"""
              return predictions - observations['duration']
        # def speed error(predictions, observations):
              """Duration error between speed predictions and duration observatio
        ns"""
              pred durations = (observations["distance"].values.reshape(-1, 1)*60
        *60)/predictions
             return pred durations - observations["duration"].values.reshape(-1,
         1)
        # def tree regression errors(outcome='duration', error fn=duration erro
              """Return errors for all examples in test using a tree regression {\tt m}
        odel."""
              errors = []
        #
              for vs in train.groupby(choices).size().index:
                  v train, v test = train, test
                  for v, c in zip(vs, choices):
                      v train = ...
                      v test = \dots
        #
              return errors
        # errors = tree regression errors()
        # errors via speed = tree regression errors('speed', speed error)
        # tree rmse = rmse(np.array(errors))
        # tree speed rmse = rmse(np.array(errors via speed))
        # print('Duration:', tree rmse, '\nSpeed:', tree speed rmse)
        # TODO
In [ ]: | grader.check("g4g")
```

Here's a summary of your results:

In []: | model = LinearRegression()

```
In [ ]: models = ['constant', 'simple', 'linear', 'period', 'speed', 'tree', 'tre
e_speed']
pd.DataFrame.from_dict({
    'Model': models,
    'Test RMSE': [eval(m + '_rmse') for m in models]
}).set_index('Model').plot(kind='barh');
```

Part 5: Building on your own

In this part you'll build a regression model of your own design, with the goal of achieving even higher performance than you've seen already. You will be graded on your performance relative to others in the class, with higher performance (lower RMSE) receiving more points.

Question 5a

In the below cell (feel free to add your own additional cells), train a regression model of your choice on the same train dataset split used above. The model can incorporate anything you've learned from the class so far.

The model you train will be used for questions 5b and 5c

```
In [ ]: | # from future import absolute import, division, print function, unico
        de literals
        # # Use seaborn for pairplot
        # !pip install -q seaborn
        # # Use some functions from tensorflow docs
        # !pip install -q git+https://github.com/tensorflow/docs
        # import pathlib
        # import matplotlib.pyplot as plt
        # import numpy as np
        # import pandas as pd
        # import seaborn as sns
        # import tensorflow as tf
        # from tensorflow import keras
        # from tensorflow.keras import layers
        # print(tf. version )
        # import tensorflow docs as tfdocs
        # import tensorflow docs.plots
        # import tensorflow docs.modeling
In []: | # y train = train["duration"].values.reshape(-1, 1)
```

```
In []: # y_train = train["duration"].values.reshape(-1, 1)
# X_train = design_matrix(train)
# y_test = test["duration"].values.reshape(-1, 1)
# X_test = design_matrix(test)
```

```
In [ ]: | # def build model():
        # model = keras.Sequential([
              layers.Dense(64, activation='relu', input shape=[len(X train.keys
        ())]),
              layers.Dense(64, activation='relu'),
        #
        #
              layers.Dense(1)
        #
          ])
            optimizer = tf.keras.optimizers.RMSprop(0.001)
            model.compile(loss='mse',
        #
                          optimizer=optimizer,
        #
                          metrics=['mae', 'mse'])
            return model
        # model = build model()
In [ ]: | # model.summary()
In [ ]: | # example batch = X train[:10]
        # example result = model.predict(example batch)
        # example result
In [ ]: # EPOCHS = 1000
        # history = model.fit(
        # X train, y train,
        # epochs=EPOCHS, validation split = 0.2, verbose=0,
            callbacks=[tfdocs.modeling.EpochDots()])
In [ ]: | # hist = pd.DataFrame(history.history)
        # hist['epoch'] = history.epoch
        # hist.tail()
```

Question 5b

Print a summary of your model's performance. You **must** include the RMSE on the train and test sets. Do not hardcode any values or you won't receive credit.

Don't include any long lines or we won't be able to grade your response.

```
In [ ]: ...
```

Question 5c

Describe why you selected the model you did and what you did to try and improve performance over the models in section 4.

Responses should be at most a few sentences

Write your response here

Congratulations! You've carried out the entire data science lifecycle for a challenging regression problem.

In Part 1 on data selection, you solved a domain-specific programming problem relevant to the analysis when choosing only those taxi rides that started and ended in Manhattan.

In Part 2 on EDA, you used the data to assess the impact of a historical event---the 2016 blizzard---and filtered the data accordingly.

In Part 3 on feature engineering, you used PCA to divide up the map of Manhattan into regions that roughly corresponded to the standard geographic description of the island.

In Part 4 on model selection, you found that using linear regression in practice can involve more than just choosing a design matrix. Tree regression made better use of categorical variables than linear regression. The domain knowledge that duration is a simple function of distance and speed allowed you to predict duration more accurately by first predicting speed.

In Part 5, you made your own model using techniques you've learned throughout the course.

Hopefully, it is apparent that all of these steps are required to reach a reliable conclusion about what inputs and model structure are helpful in predicting the duration of a taxi ride in Manhattan.

Future Work

Here are some questions to ponder:

- The regression model would have been more accurate if we had used the date itself as a feature instead of just the day of the week. Why didn't we do that?
- Does collecting this information about every taxi ride introduce a privacy risk? The original data also
 included the total fare; how could someone use this information combined with an individual's credit card
 records to determine their location?
- Why did we treat hour as a categorical variable instead of a quantitative variable? Would a similar treatment be beneficial for latitude and longitude?
- Why are Google Maps estimates of ride time much more accurate than our estimates?

Here are some possible extensions to the project:

- An alternative to throwing out atypical days is to condition on a feature that makes them atypical, such as the weather or holiday calendar. How would you do that?
- Training a different linear regression model for every possible combination of categorical variables can overfit. How would you select which variables to include in a decision tree instead of just using them all?
- Your models use the observed distance as an input, but the distance is only observed after the ride is over. How could you estimate the distance from the pick-up and drop-off locations?
- · How would you incorporate traffic data into the model?

```
In []: # Save your notebook first, then run this cell to generate a PDF.
# Note, the download link will likely not work.
# Find the pdf in the same directory as your proj3.ipynb
grader.export("proj3.ipynb", filtering=False)
```