

# Internal mesh optimization Semantic linking and siloing Big data

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## Plan

1. Heuristic
2. Metaheuristics
3. Shrinking our universe with siloing and semantic similarity
4. Same problem with an e-commerce flavor
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## 1. Heuristic

### Some notations

Let  $N \in \mathbb{N}$  be the number of nodes in our mesh.

Let  $(X_i)_{i \in \{1, \dots, N\}}$  be the vertices (URLs) of our oriented graph.

Let  $(G_{ij}) \in \{0, 1\}^{N \times N}$  be the adjacency matrix of our oriented graph.

Let here define  $f$ , a given data per URL, which gives a potentiality metrics for our vertices.

$$\begin{aligned} f & : (X_i)_{i \in \{1, \dots, N\}} & \rightarrow & \mathbb{R}^+ \\ & x & \mapsto & f(x) \end{aligned} \tag{1}$$

## In-rank

We restrain the universe to our site where we compute the standard page-rank.

Initialization :

$$\forall u \ PR(u) = \frac{1}{N} \quad (2)$$

Iterative computation :

$$PR(u) = \frac{(1 - c)}{N} + c \times \sum_{v \rightarrow u} \frac{PR(v)}{\text{card}(\{v \rightarrow u\})} \quad (3)$$

## Our heuristic

We want here to optimize the adequacy of our mesh ( $X_i$ ) to our potentiality vector  $f$ . We here postulate the following heuristic to assess the relevance of a mesh :

$$\max_{(G_{ij}) \in \{0,1\}^{N \times N}} \left\{ \sum_{i=1}^N \text{traffic}(X_i) \times \text{pageRank}(X_i) \right\} \quad (4)$$

## 2. Metaheuristics

### Exhaustive brute force doesn't work

For a  $N = 10^6$  millions URLs web site, we have  $2^{N^2}$  with a 2048 bits mantissa, 256 bits exponent

$2^{10^{6^2}} =$

9.5762442314927432848050594956989483747127095675192905698213128517073583274396016675898

714705184143146468453752442806484690561169975498415015777492655947375270159476651418975

300707658547568802353384879419803574730952480197774380552040662758127609571333683703207

910070247048194459504686986124786492353387550318495241621572271925127288273993787778380

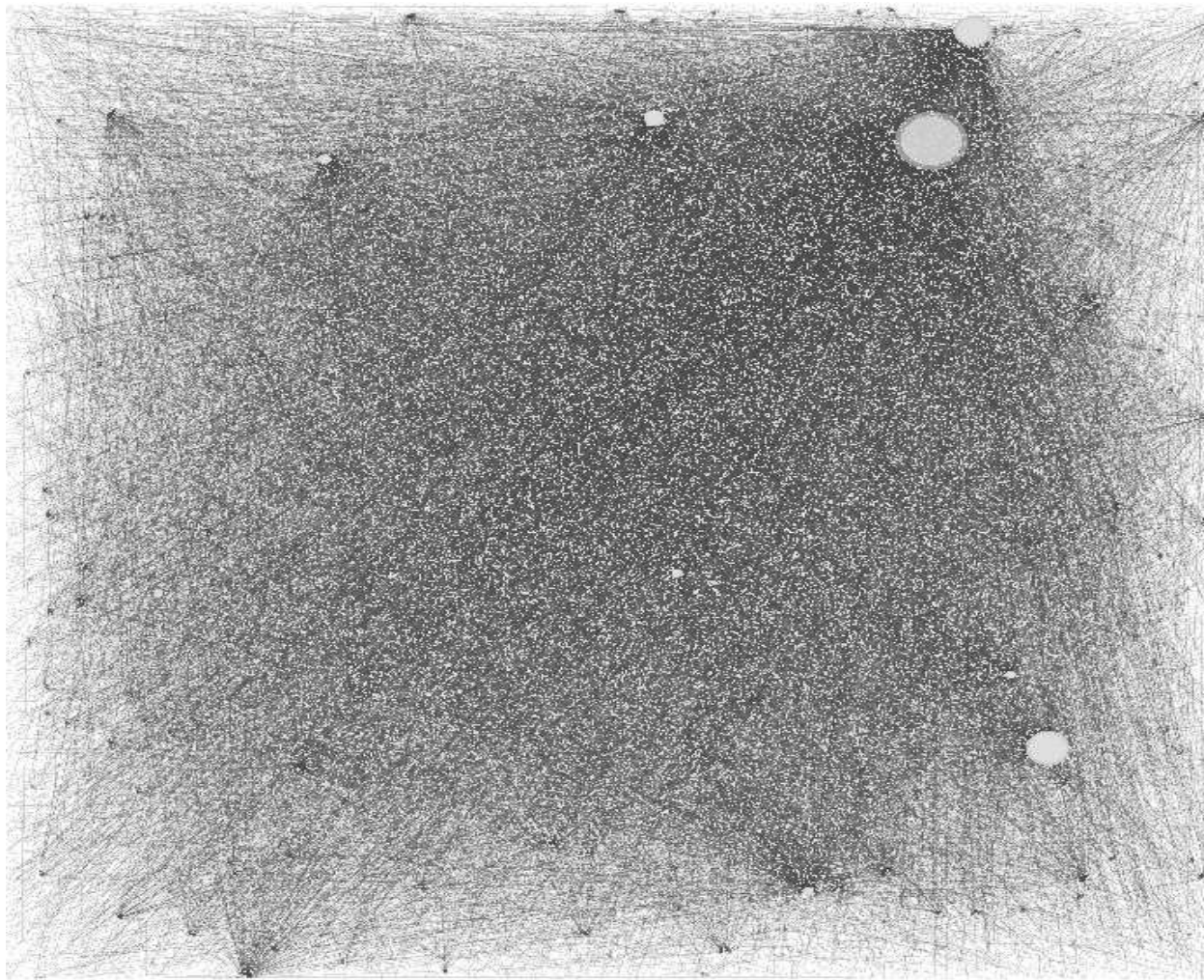
450774809611395810191417363401889038757182279484019203870177413318113073911418463615759

647977538478560166958988721048687854280187283661925937530017243461145905573802314471888

491758757162677684017424597014433418179115289463552630751896559312213624470617453325056

5836008e+301029995663

## Picturing our smallest store : jewelery



## Metaheuristics

We here have to maximize over all possible graphs. We have to find a clever global optimization methodology : metaheuristics such as global search, multistart, particle swarm, simulated annealing or genetic algorithm are all good candidates.

### **What is a genetic algorithm**

- Genetic algorithm mimics evolutionary biology to find approximate solutions to optimization problems
- Start with an initial generation of candidate solutions that are tested against the objective function (fitness of the individual)
- Subsequent generations evolve from the first through selection, crossover and mutation
- The individual that best minimizes the given objective is returned as the ideal solution

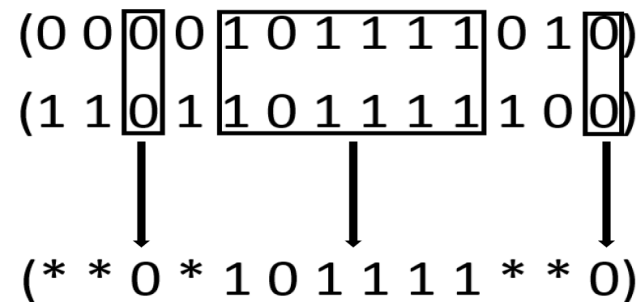
### **Why a genetic algorithm**

- Lots of local minima to avoid
- Non continuous universe, constraints and objective
- Problem with noise and non-smooth data



## Cleverly evolving through our universe

### Child spawning from 2 parents crossover

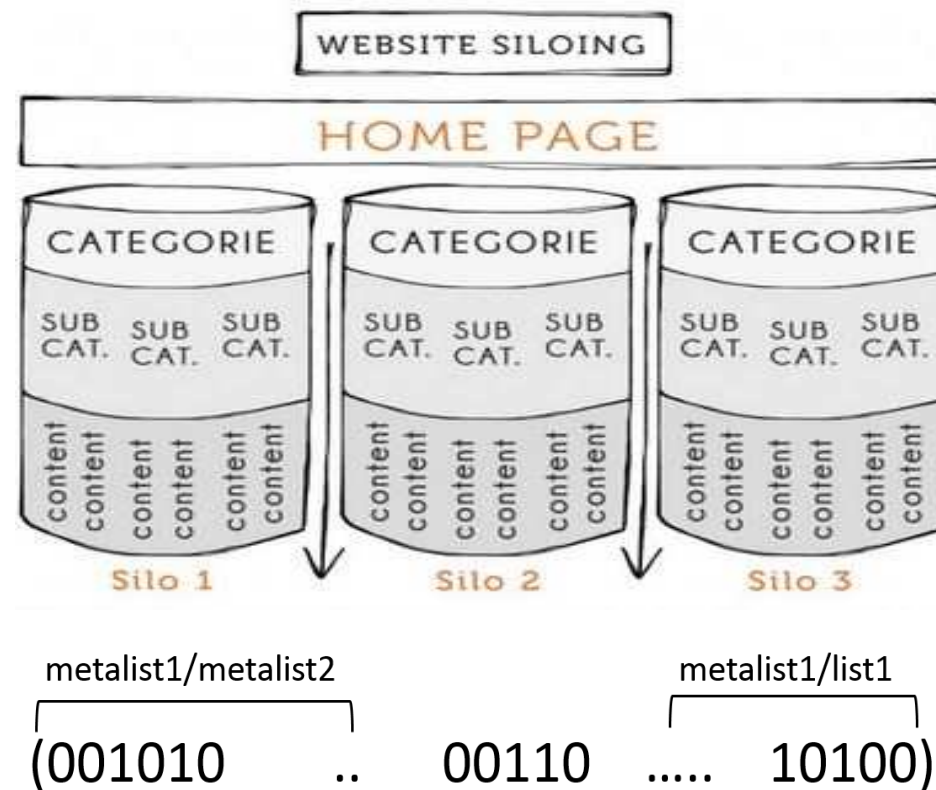


### Mutation of an individual

(1 1 0 \* 1 0 1 1 \* 1 1 0 0)

### 3. Shrinking our universe with siloing and semantic similarity

## Siloing and links categorizing



## Semantic similarity

We slack our universe by allowing links only between semantically similar URLs :

$$\max_{(G_{ij}) \in \{0,1\}^{N \times N}} \left\{ \sum_{i=1}^N f(X_i) \times PR(X_i) \right\} \quad \text{if } CS(ij) \leq t \quad (5)$$

where  $CS(ij)$  is a semantic distance between the two linked pages  $i$  and  $j$ .  $CS(ij)$  can be defined very easily as the scalar product of the tf/idf vectors of the product descriptions whose weight are defined by the well known formula :

$$w_{ik} = \frac{tf_{ik} \log \left( \frac{N}{n_k} \right)}{\sqrt{\sum_{k=1}^t (tf_{ik})^2 \log \left( \frac{N}{n_k} \right)^2}} \quad (6)$$

#### 4. Same problem with an e-commerce flavor

$$\sum_{i \in \text{Keywords}} SV(i) \times CTR(\text{position}(i)) \times CR(i) \times P(i) \quad (7)$$

where  $\text{position}(i)$  is the estimated position in search engine results coming from the modification of our new mesh,

$SV(i)$  is the search volume for the keywords  $i$  estimated by the search engine.

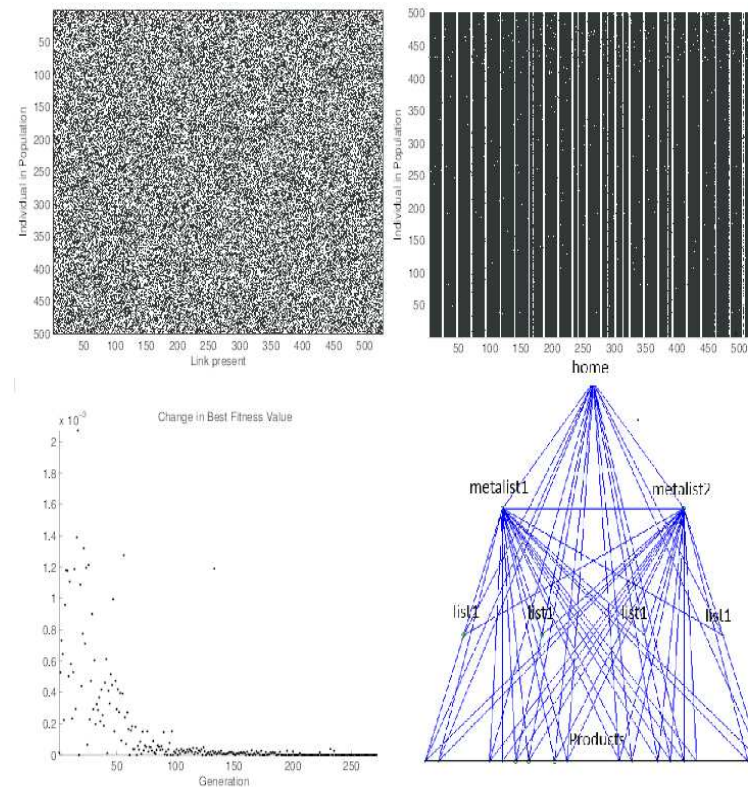
and  $CTR(i)$  is the click through rate for an URL at the position place in the search engine results.

## 5. Prototyping example

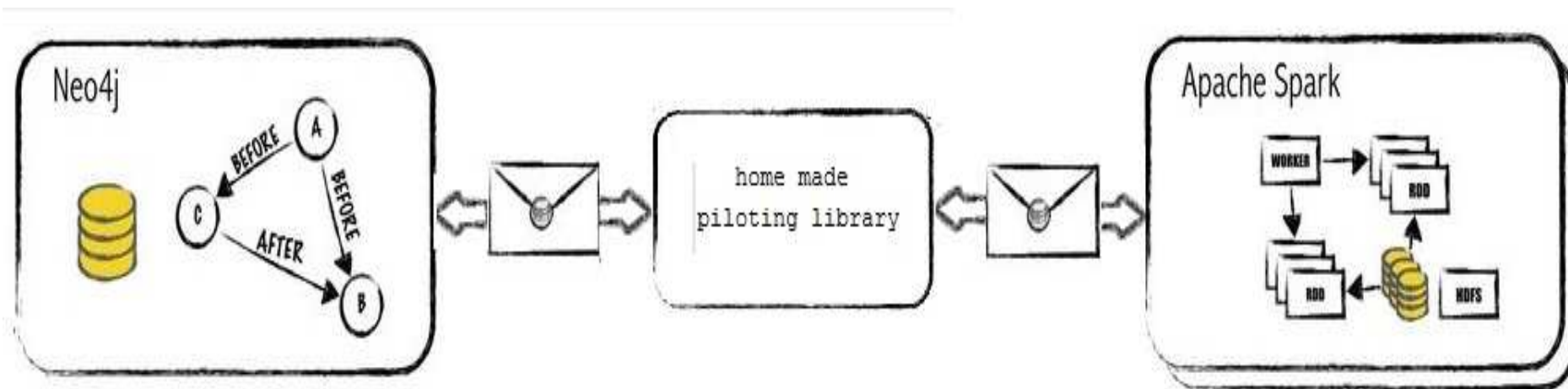
$(X_i) = \text{'home', 'metalist1', 'metalist2', 'list1', 'list2', 'list3', 'list4', 'product1', 'product2', ..., 'product32'}$  ;

$f(X_i) = [100, 80, 55, 40, 35, 25, 20, 4, 5, ..., 3]$  ;

## Results



## 6. Big data implementation : Neo4j and Spark GraphX



### 7. Video and paper link

[http://sduprey.github.io/page\\_rank\\_optimization\\_video.html](http://sduprey.github.io/page_rank_optimization_video.html)

[http://sduprey.github.io/article\\_sduprey\\_iswag\\_02\\_06\\_2015.pdf](http://sduprey.github.io/article_sduprey_iswag_02_06_2015.pdf)

[http://sduprey.github.io/PRESENTATION\\_ISWAG.pdf](http://sduprey.github.io/PRESENTATION_ISWAG.pdf)