

seL4 Summit

Splitting the seL4 Specification



Thomas Sewell

4 September 2025

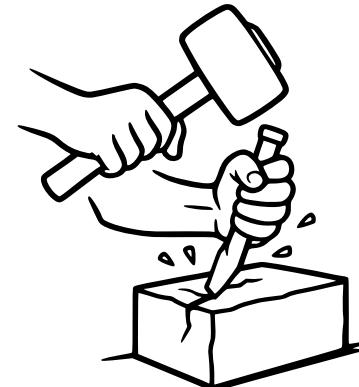


Splitting transitions in the seL4 Specification

Existing work:

- The seL4 μ -kernel.
- **Verified** functionally correct!

This talk: spec splitting.



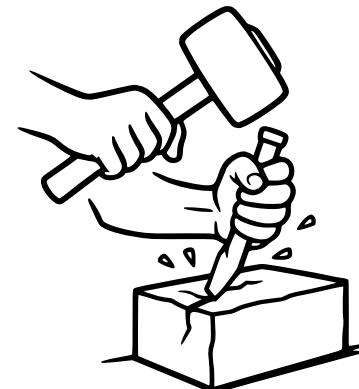
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- What does that mean?
- Why might we do that?
- How?
- When will it be finished?



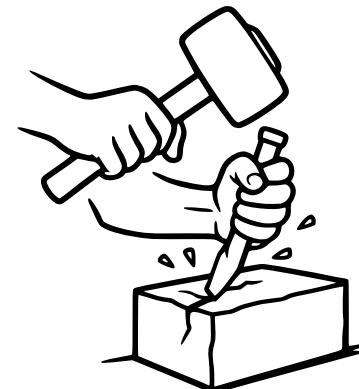
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- What does that mean?
- Why might we do that?
- How?
- When will it be finished?
 - Yeah, dunno.



This talk is also splitting a time slot.

See:

“Verifying Kernel–Userland Integration for LionsOS”

- Dr Rob Sison, UNSW.

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Both talks are about using the seL4 abstract spec to justify a user verification environment.

An Example

In thread *X*:

```
int do_send(void) {
    seL4_MessageInfo_t i;
    ...
    i = mk_send_info();
    i = seL4_Send(cptr, i);
    ...
}
```

In thread *Y*:

```
int do_recv(void) {
    seL4_MessageInfo_t i;
    ...
    ...
    i = seL4_Recv(cptr, NULL);
    ...
}
```

What does this do?

- Under the right conditions, *X* sends a message to *Y*.

An Example

In thread *X*:

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int do_send(void) {
    seL4_MessageInfo_t i;
    ...
    i = mk_send_info();
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```

In thread *Y*:

```
int do_recv(void) {
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    ...
    ...
    i = seL4_Recv(cptr, NULL);
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```

What does this do?

- Under the right conditions, *X* sends a message to *Y*.

Can we verify that?

An Example (II)

In thread Y:

```
int do_recv(void) {
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    ...
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What does `seL4_Recv` here *really* do?

An Example (II)

In thread Y:

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What does `seL4_Recv` here *really* do?

- System call, not a function call.
- Triggers a kernel entry.

An Example (II)

In thread Y:

```
int do_recv(void) {
    seL4_MessageInfo_t i;
    ...
    ...
    i = seL4_Recv(cptr, NULL);
    ...
}
```

What does `seL4_Recv` here *really* do?

- System call, not a function call.
- Triggers a kernel entry.
 - There is a *specification* for that.

The seL4 Kernel: Event Handlers

seL4 is an *event reactive* kernel.

It consists of a small number of *event handlers*.

The seL4 design takes this to extremes.

Each event handler is an entry point from assembly to C.

Each function terminates, and returns out of C entirely.

Thus we can model each one as a function, $state \rightarrow state$.

Functional Correctness of the seL4 Kernel

Each kernel entry is a function $\text{state} \rightarrow \text{state}$.

The functional correctness proof guarantees that these functions implement the `call_kernel` function.

definition

```
call_kernel ::= ``event  $\Rightarrow$  (unit, ...) s_monad'' where
call_kernel ev  $\equiv$  do
    handle_event ev <handle>
        ( $\lambda$  ..)
    schedule;
    activate_thread
od
```

seL4_Recv causes a kernel entry.

definition

```
call_kernel ::= ``event  $\Rightarrow$  (unit, ...) s_monad'' where
```

```
call_kernel ev  $\equiv$  do
```

```
    handle_event ev <handle>
```

```
        ( $\lambda$  _ . ...)
```

```
    schedule;
```

```
    activate_thread
```

```
od
```

```
handle_event (SyscallEvent SysRecv) =
```

```
without_preemption (handle_recv True)
```

\therefore seL4_Recv \approx call to handle_recv.

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```
    schedule;
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od
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handle_event (SyscallEvent SysRecv) =
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- But when do they *finish*?

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```
    schedule;
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```
od
```

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handle_event (SyscallEvent SysRecv) =
```

```
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```

\therefore seL4_Recv \approx call to handle_recv.

- But when do they *finish*?
- The schedule function might not pick Y.

handle_recv ≈

1. Walk C-space and look up capability.
2. Check that the capability can receive.
 - Is an Endpoint or Notify capability.
 - Has Receive/Read rights.
3. Is there a blocked sender?
 - **No:** block this thread as a receiver.
 - **Yes:**
do_ipc_transfer sender endpoint badge grant receiver

n.b.: This is very simplified and omits a lot of cases.

Recap: Example

In thread X:

```
int do_send(void) {
    seL4_MessageInfo_t i;
    ...
    i = mk_send_info();
    i = seL4_Send(cptr, i);
    ...
}
```

In thread Y:

```
int do_recv(void) {
    seL4_MessageInfo_t i;
    ...
    ...
    i = seL4_Recv(cptr, NULL);
    ...
}
```

What does this do?

- Both threads enter the kernel, do syscall capability checks.
- Either X or Y also causes an IPC transfer and completes both syscalls.

Splitting by Example

Can we split the IPC transfer?

```
do_ipc_transfer sender endpoint badge grant receiver
```



1. X's IPC send action.
 - Part of seL4_Send.
2. Y's IPC receive action.
 - Part of seL4_Recv.

Splitting by Example

Can we split the IPC transfer?

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 - Part of seL4_Send.
2. Y's IPC receive action.
 - Part of seL4_Recv.

Let's hear about the Kernel/User project.

Splitting the Spec: Why?

Let's come back to:

Why would we want to split the spec?

Client Timelines

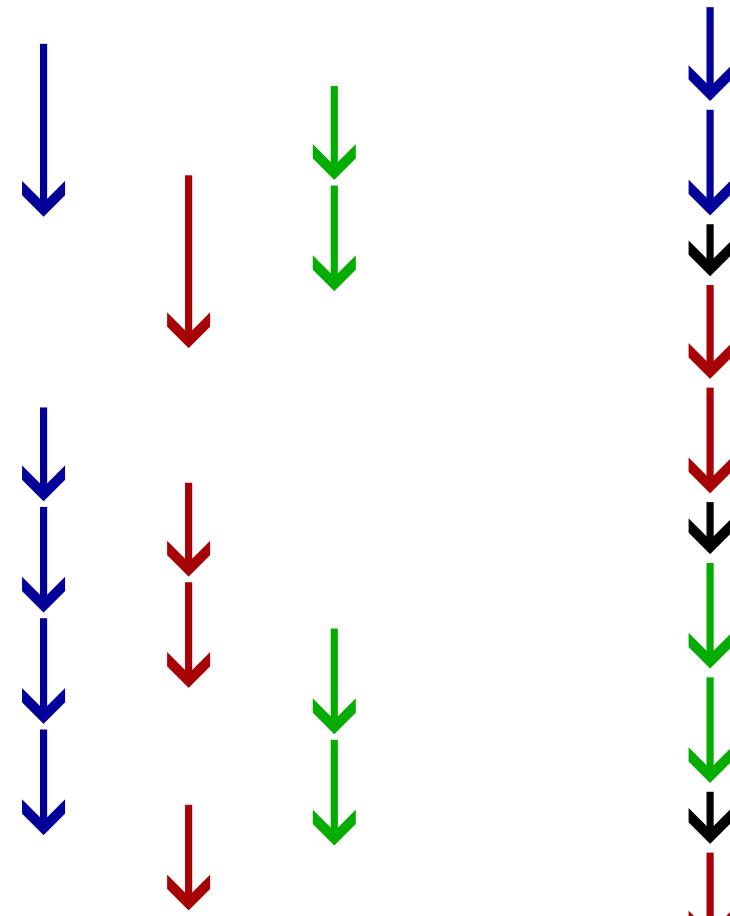
(Recap of OS lecture 2.)

Logical perspective:

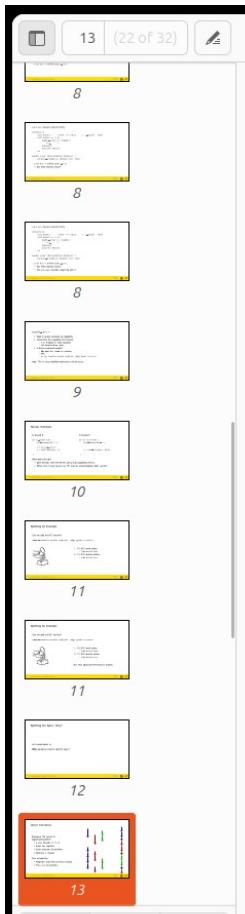
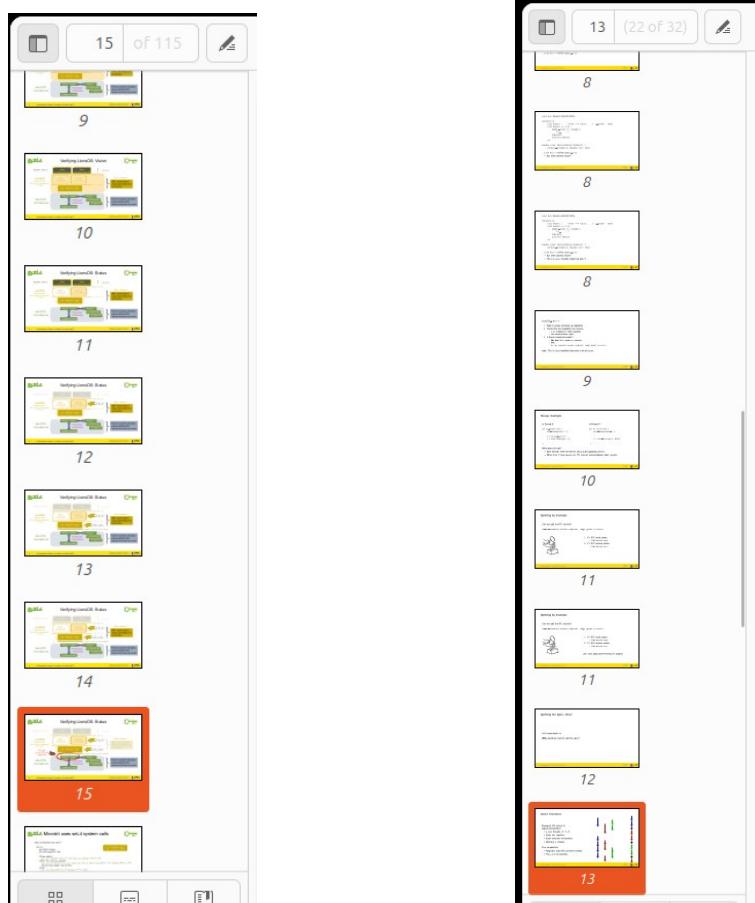
- 3 user threads, X , Y , Z .
- Each has registers.
- Each executes instructions.
- Memory is shared.

True perspective:

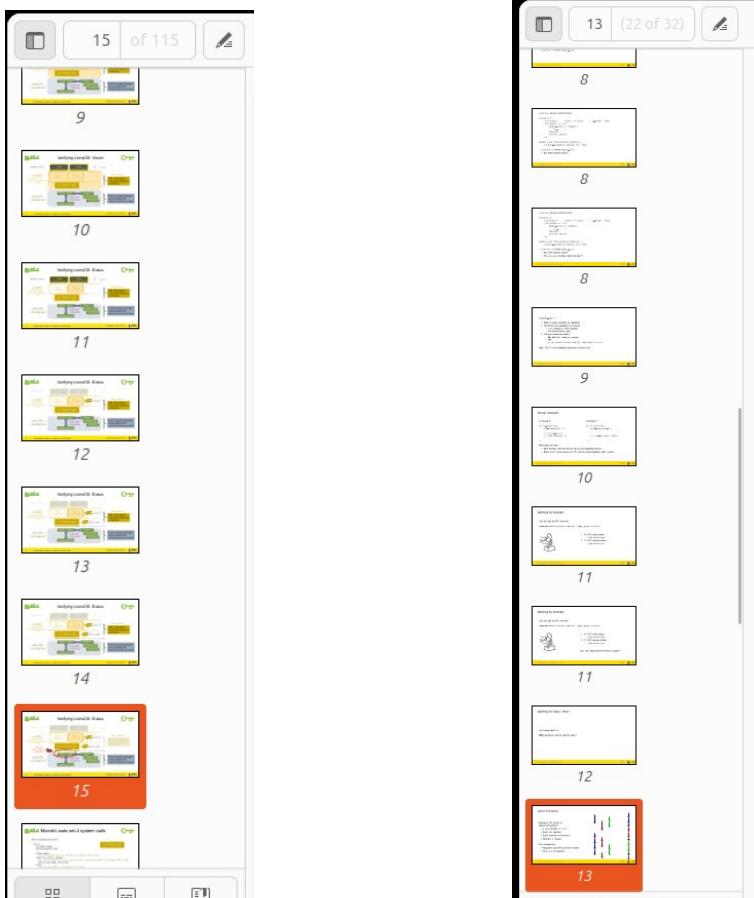
- Registers and CPU are time-shared.
- The μ -kernel switches.



A Metaphor



A Metaphor



Multiple lists of instructions, but just one talk.

Questions about the validity of the talk need to be addressed to one of these timelines.

Verifying Client Timelines

We want to verify a client program.

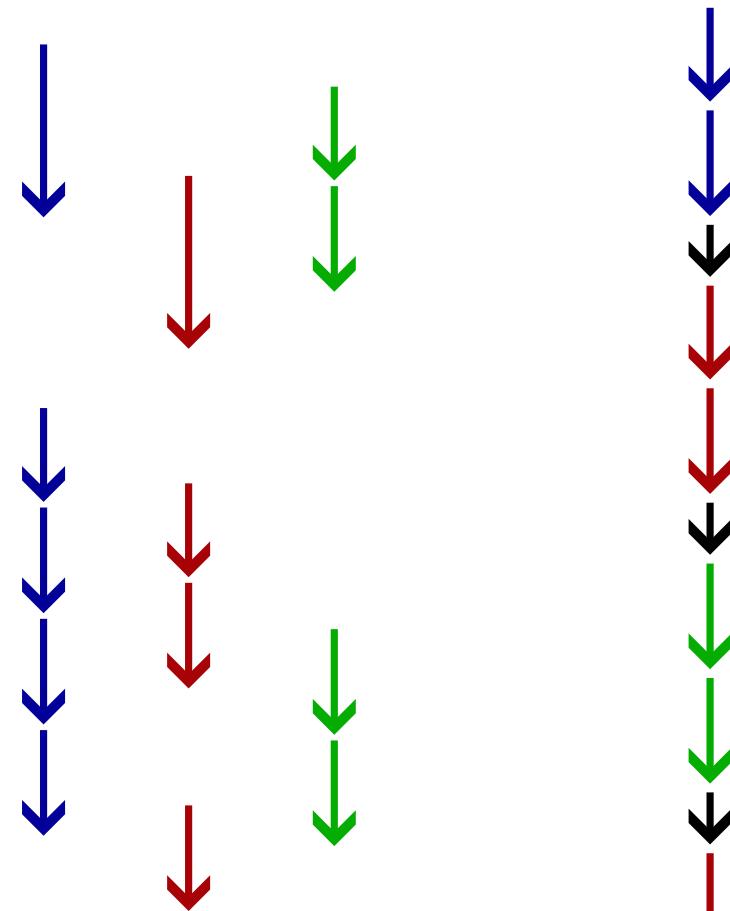
Clients run *within* these logical timelines.

It would help to have a model that exposes these timelines.

Executions of seL4 fit awkwardly with the logical timelines.

Obvious options:

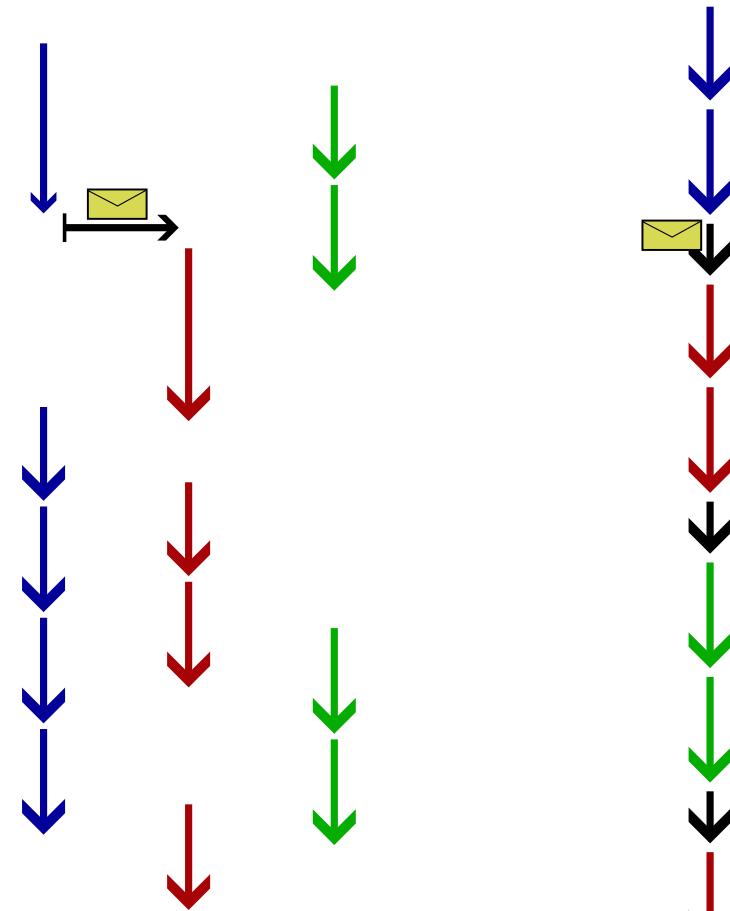
- Put μ -kernel on its own timeline.
- Put system calls in the timeline of the caller.

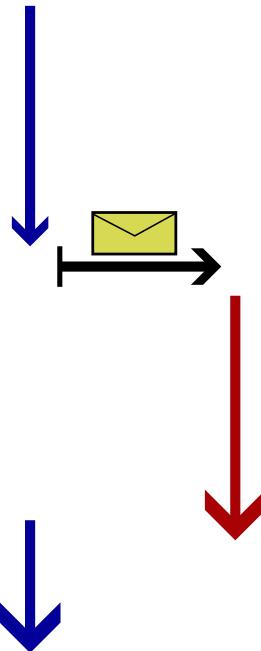


Inter-Timeline Actions

Timeline-crossing events cause additional complications.

- Synchronous seL4 message sends.
- Asynchronous seL4 notifications.





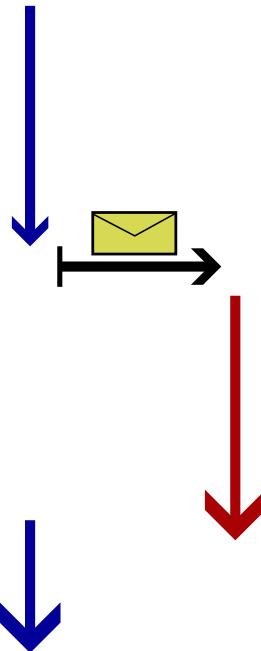
From our example: X makes a synchronous send to Y .

The seL4 “integrity” proof compares X ’s authority to what it can do:

- Assume that Y was blocked, and X causes the transfer.
- X gets a very conditional right to modify Y .
 - X can save a sent message to Y .

The blocking system call by Y ends *in* an event from X ’s timeline.

Verifying a simple IPC example is difficult; we are not aware of such a verification.



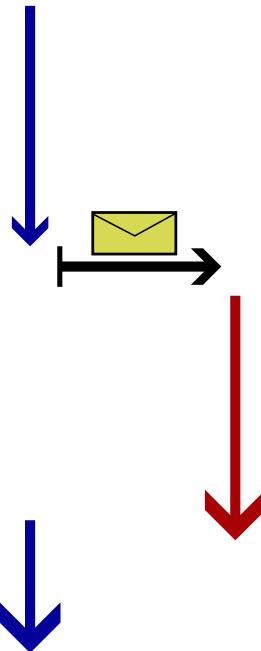
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From our example: X makes a synchronous send to Y .

The seL4 “integrity” proof compares X ’s authority to what it can do:

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The blocking system call by Y ends *in* an event from X ’s timeline.

Verifying a simple IPC example is difficult; we are not aware of such a verification.

Proposed diagnosis: these are all *symptoms* of the mismatch between the kernel timeline and the user timelines.

Splitting: How?

```
definition
  call_kernel :: ``event ==> (unit, ...) s_monad'' where
    call_kernel ev ≡ do
      handle_event ev <handle>
        (λ_. ...)
      schedule;
      activate_thread
    od
```

```
definition
  call_kernel_step :: ``event ==> (next_step, ...) s_monad'' where
    call_kernel_step ev ≡ do
      handle_event ev <handle>
        (λ_. ...)
      return (Next_Step Schedule_Next);
    od
```

Splitting

Desired properties:

- Chaining the transitions yields original spec.
 - Preserves refinement to existing implementation.
- Intermediate states satisfy kernel invariants.
- “Integrity” security property is simpler and stronger.
 - X may only modify structures it controls.
- Selecting events on timeline X makes sense.
 - Yields a model against which program X can be verified.

Splitting the Example

handle_recv_step ≈

1. Check Y 's syscall arguments and look up endpoint.
2. Sync_Sender_Unblock: remove X from endpoint.
3. Sync_Sender_Gen_Message: fetch message from X .
4. Sync_Receiver_Accept: save message to Y .
5. Sync_Sender_Cleanup: possibly clean up X Reply caps.
6. Sync_Receiver_Accept: possibly update Y scheduler state.

Thanks to ReplyRecv, there can be more than 10 split steps per kernel entry.

This order is partly chosen to agree with the existing abstract spec.
It is already somewhat re-ordered though.

Re-ordering transfer/thread-set

We do prove that two operations can be re-ordered:

- `do_ipc_transfer` sender endpoint badge grant receiver
- `set_thread_state` thread Running

This is because they access independent parts of the abstract spec state.

Setting a thread state uses:

- The `tcb_state` field of TCB heap objects.
- The current-thread pointer.
- The `scheduler_action` element of the “extended” state.

...

Re-ordering transfer/thread-set

Setting a thread state uses:

- The `tcb_state` field of TCB heap objects.
- The current-thread pointer.
- The `scheduler_action` element of the “extended” state.

IPC transfers use:

- Registers.
 - The “machine” state.
- Frame contents.
 - Architecture-specific heap objects.
- Capabilities.
 - CNode (capability container) heap objects.
 - The CDT and is-original global databases.
 - The `cdt_list` field of the “extended” state.
 - Capability slots of TCB heap objects.

Status

Desired properties:

- Chaining the transitions yields original spec.
 - Proven and then broken again.
- Intermediate states satisfy kernel invariants.
 - Mostly done.
- “Integrity” security property is simpler and stronger.
 - To do.
- Divided model makes sense.
 - Requires a re-factor.
- Selecting events on timeline X makes sense.
 - To do.

Cross to: Kernel/User

Let's cross to Rob's talk and hear the status of the Kernel/User gap project.

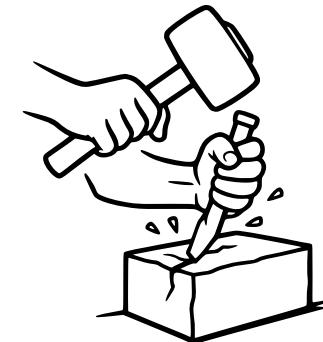
Conclusion

Two projects on connecting the seL4 abstract spec to users.

Spec splitting:

- Problem: mismatch between kernel and user timelines.
- Need user timelines to verify user programs.
- Proposal: subdivide kernel steps.
- Substantial work in progress on subdivision.
- To-do: work with derived user spec.

Also kernel/user proof integration.





School of Computer Science & Engineering
Trustworthy Systems Group

Verifying Kernel–Userland Integration for LionsOS

Dr Rob Sison

Senior Research Associate, UNSW Sydney
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The verified seL4 OS microkernel



seL4: World's first
OS kernel with
correctness proof!

But: seL4 is proved
functionally correct in
some senses, but not
others needed



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Abstract Model

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Proofs machine-checked
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Abstract Model incl. "doesn't crash"

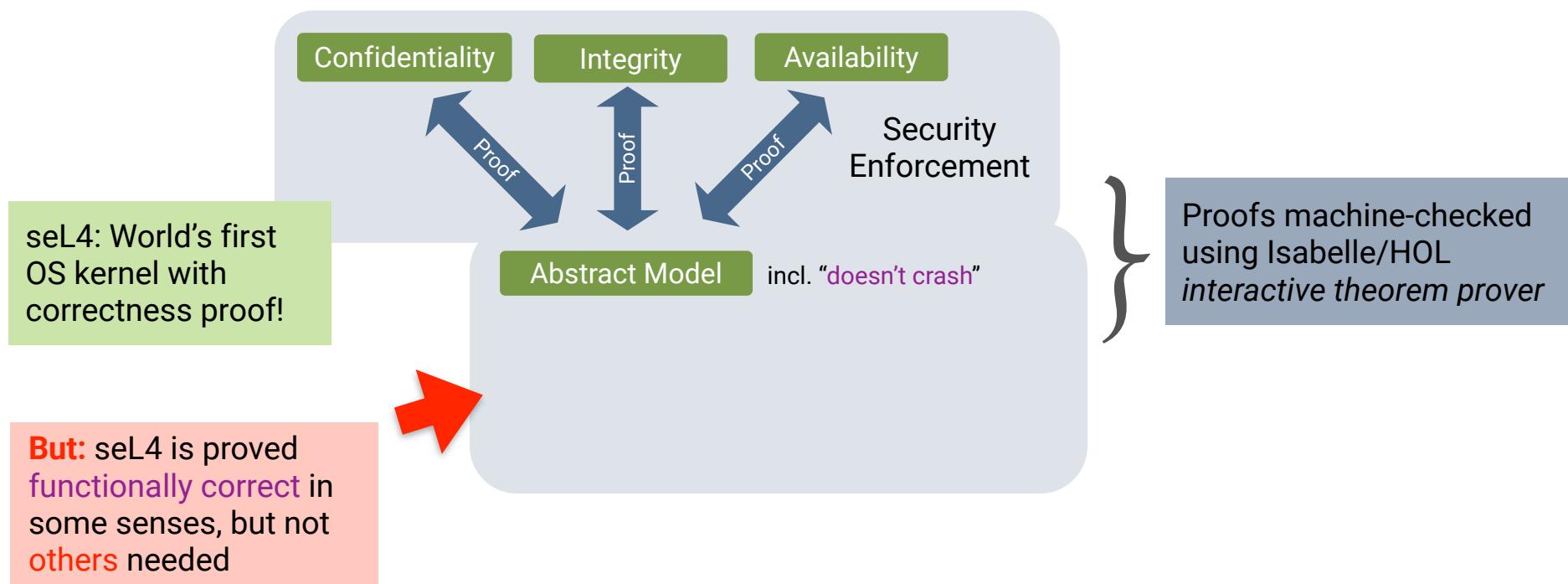
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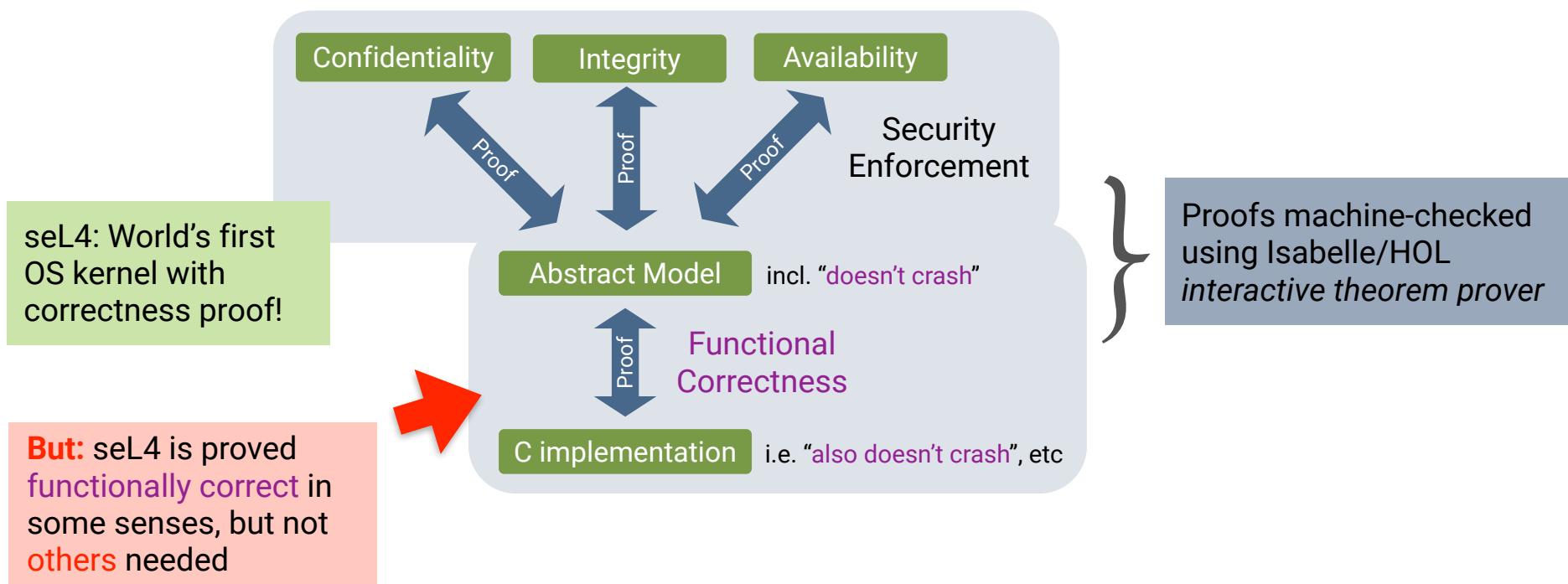


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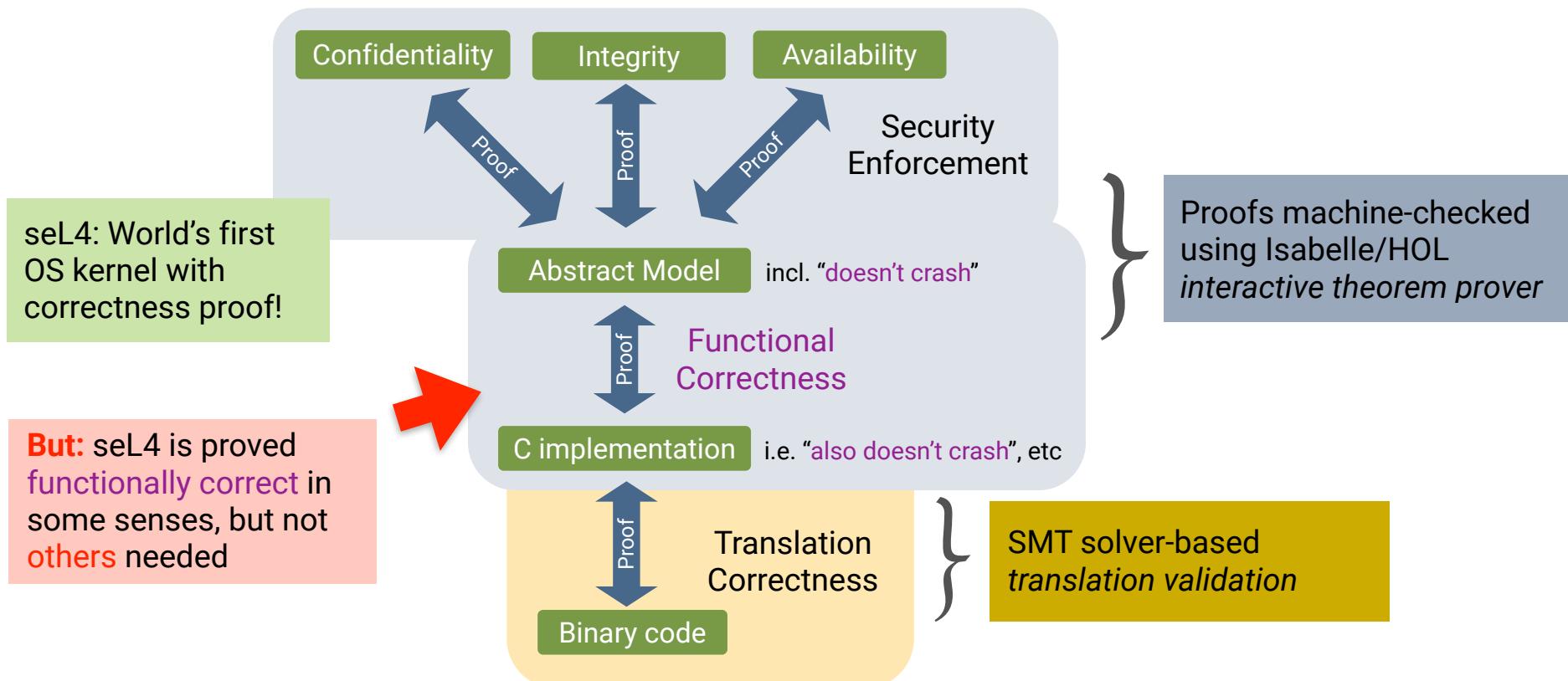


The verified seL4 OS microkernel





The verified seL4 OS microkernel





Verifying LionsOS: Vision

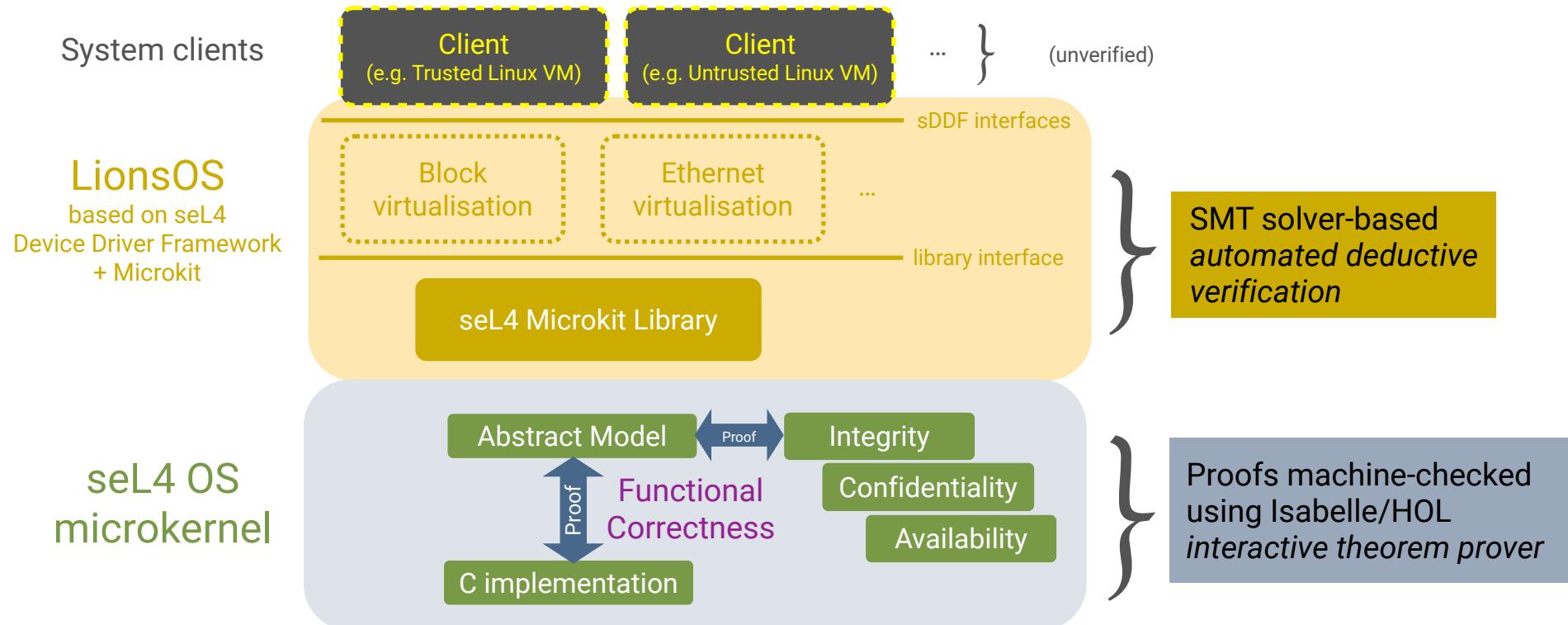


sel4 OS
microkernel



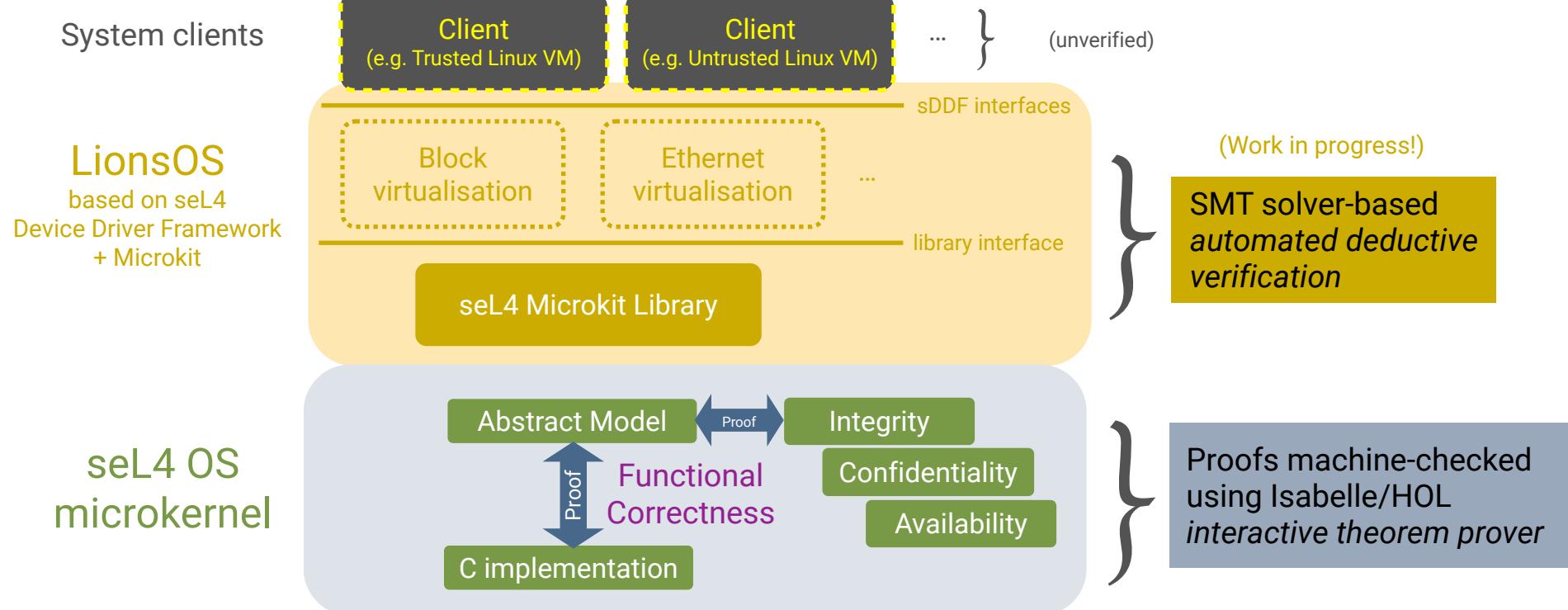


Verifying LionsOS: Vision



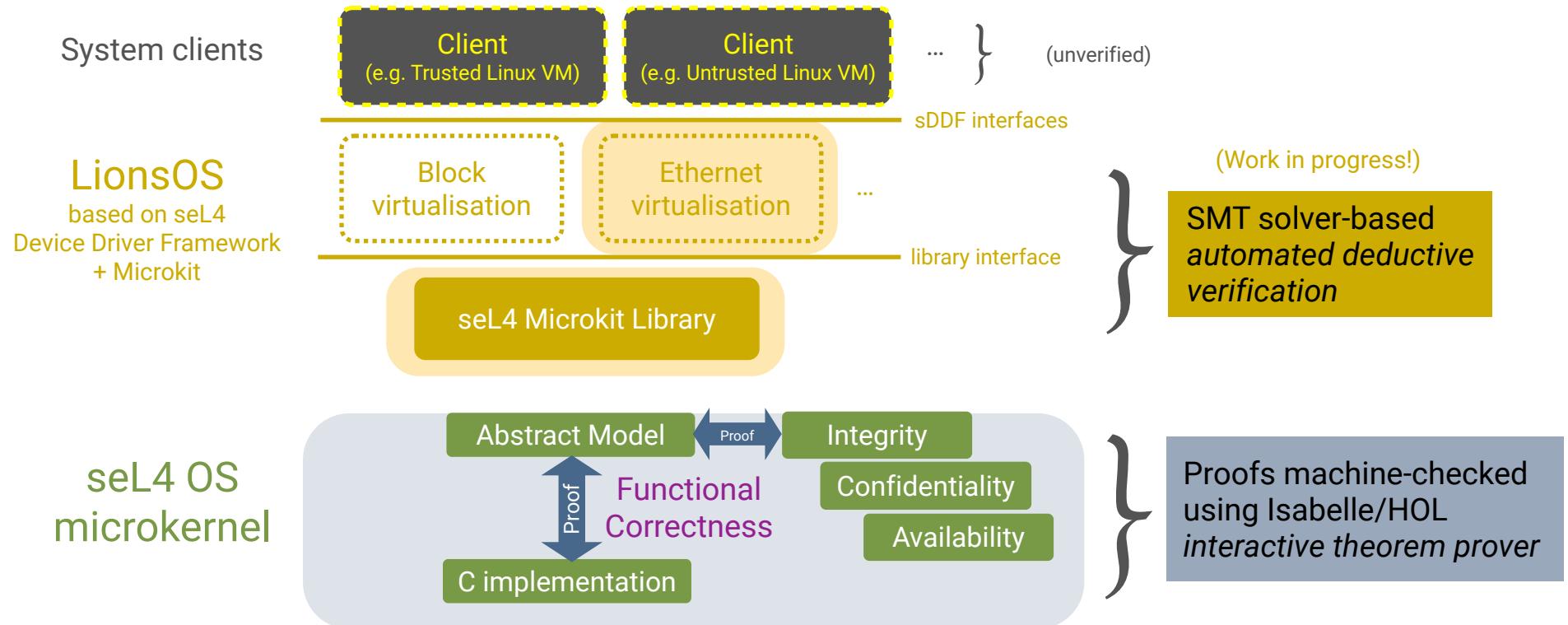


Verifying LionsOS: Vision



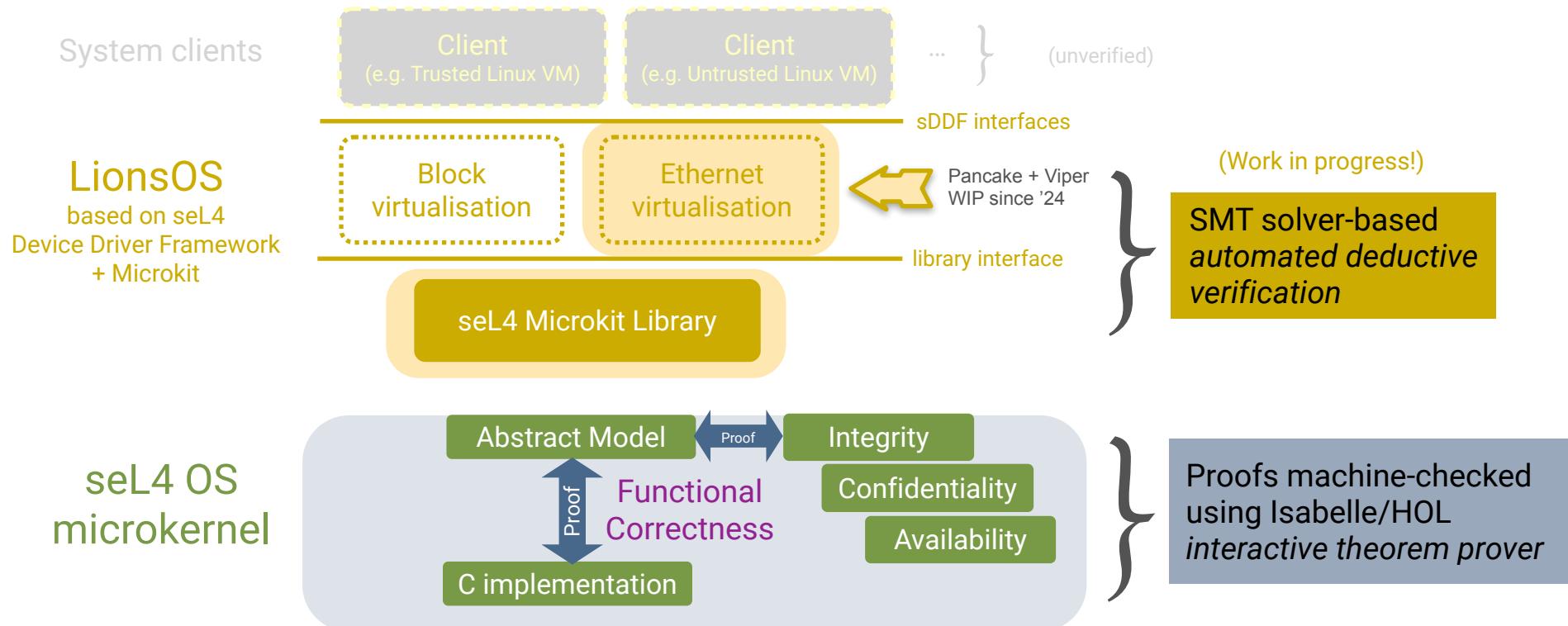


Verifying LionsOS: Status



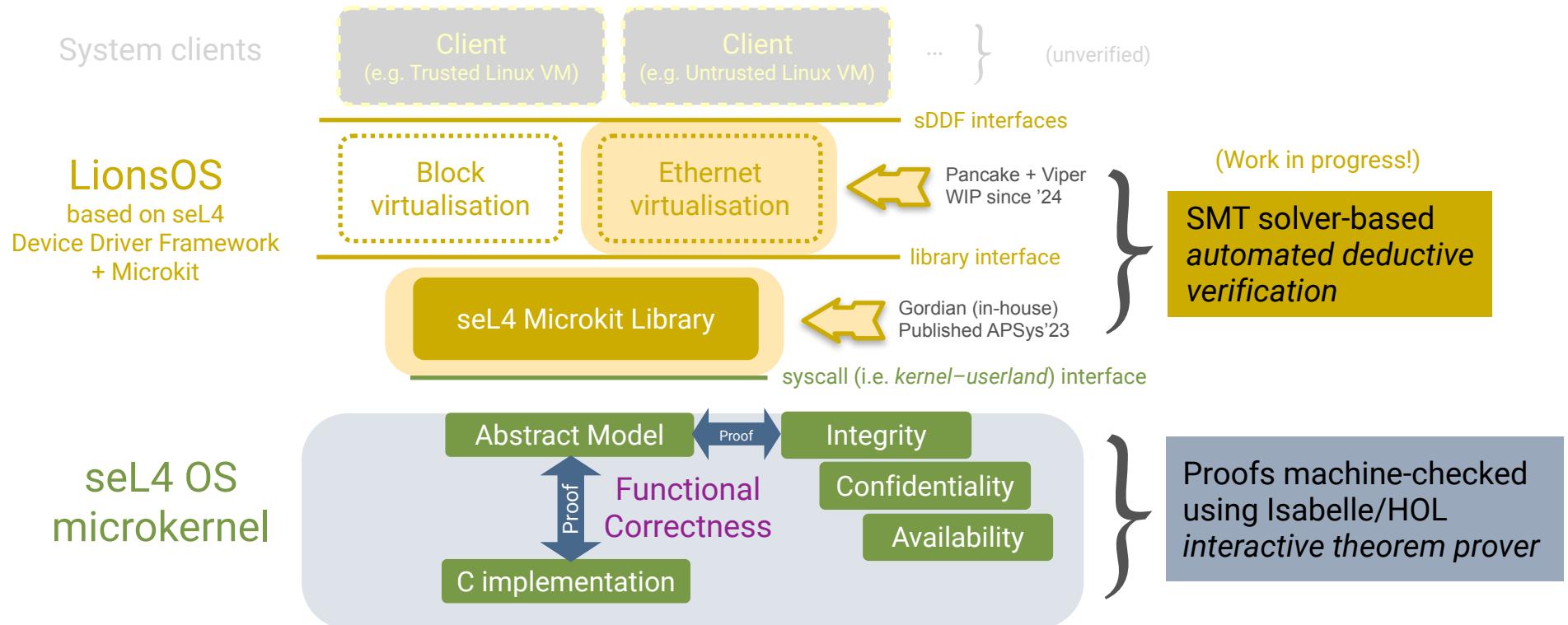


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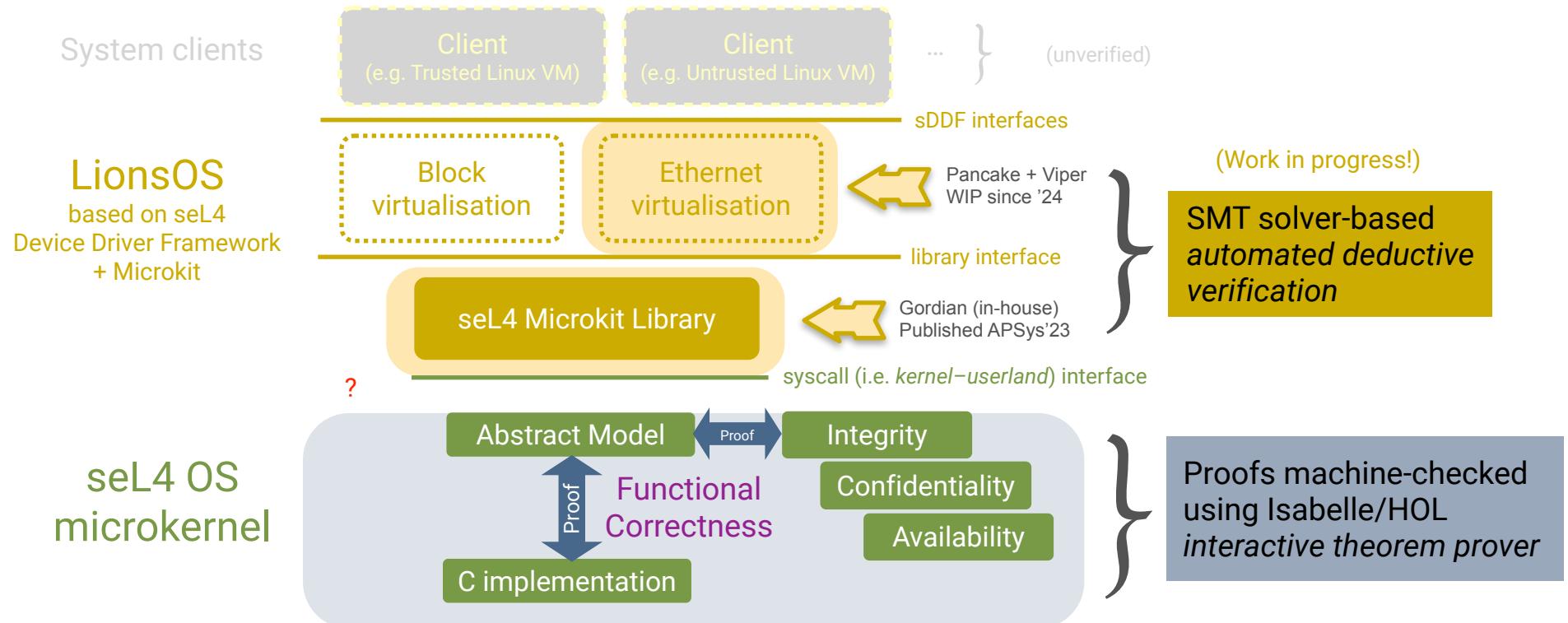


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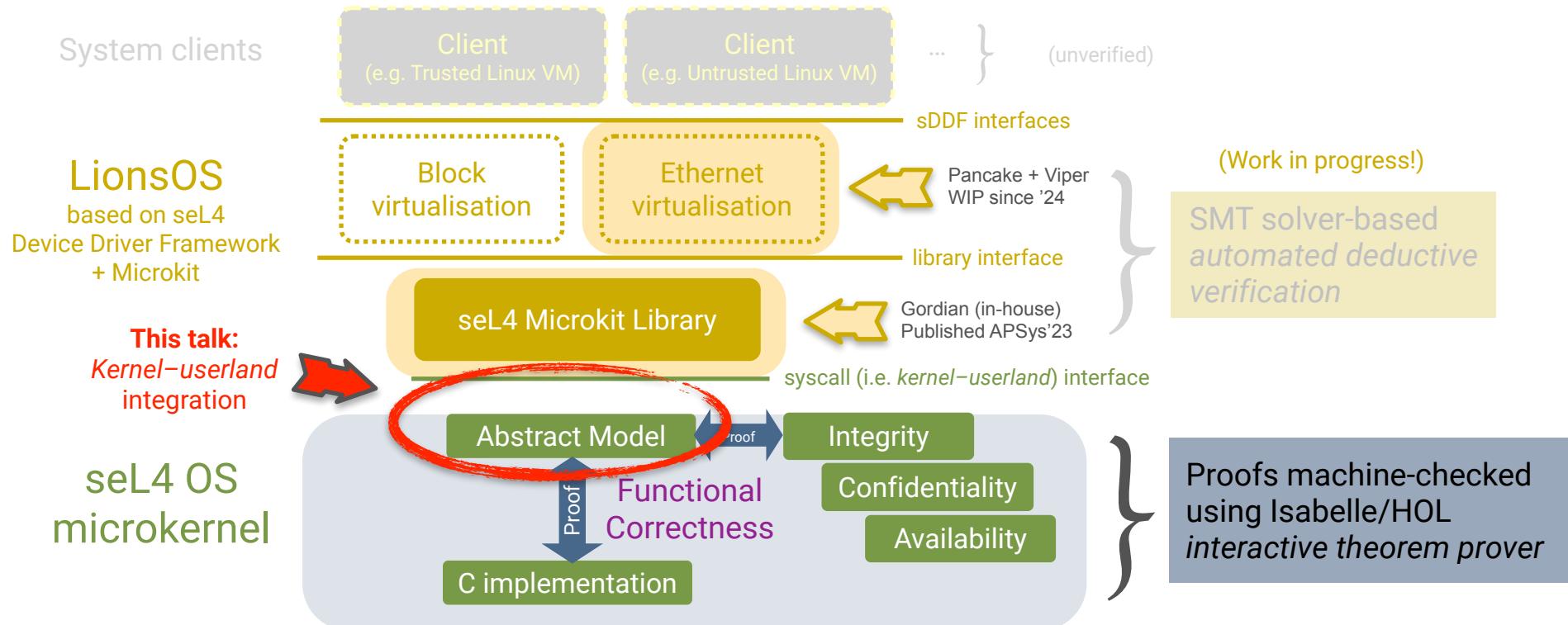


Verifying LionsOS: Status





Verifying LionsOS: Status





Microkit uses seL4 system calls



```
static void handler_loop(void) {
    ...
    for (;;) {
        seL4_Word badge;
        seL4_MessageInfo_t tag;

        if (have_reply) {
            tag = seL4_ReplyRecv(INPUT_CAP, reply_tag, &badge, REPLY_CAP);
        } else if (microkit_have_signal) {
            tag = seL4_NBSSendRecv(microkit_signal_cap, microkit_signal_msg, INPUT_CAP, &badge, REPLY_CAP);
            microkit_have_signal = seL4_False;
        } else {
            tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
        }
        ...
    }
}
```

seL4 Microkit Library

syscall (i.e. *kernel-userland*) interface



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        }  
        ...  
    }  
}
```

seL4 Microkit Library

syscall (i.e. *kernel-userland*) interface



Microkit assumes seL4's syscalls work



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```

Hoare triples:
 $\{\{ \text{Pre} \}\} f \{\{ \text{Post} \}\}$

seL4 Microkit Library

• sel4 Microkit assumes seL4's syscalls work

```
static void handler_loop(void) {  
    ...  
    {{ R }} ↗ Precondition  
    if (have_reply) {  
        ...  
    } else {
```

Hoare triples:
 $\{\{ \text{Pre} \}\} f \{\{ \text{Post} \}\}$

seL4 Microkit Library

```
        tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
```

```
    }  
    {{ S }} ↘ Postcondition  
}
```

syscall (i.e. *kernel-userland*) interface



Microkit assumes seL4's syscalls work



```
static void handler_loop(void) {
    ...
    {{ R }} ↗ Precondition
    if (have_reply) {
        ...
    } else {
        {{ R && !have_reply && !microkit_have_signal }}
    }
}
```

Hoare triples:
{{ Pre }} f {{ Post }}

seL4 Microkit Library

```
tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
```

```
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...
}
```

syscall (i.e. *kernel-userland*) interface



Microkit assumes seL4's syscalls work



```
static void handler_loop(void) {
    ...
    {{ R }} ↗ Precondition
    if (have_reply) {
        ...
    } else {
        {{ R && ! have_reply && ! microkit_have_signal }}
    }
    ↙ Precond. // if R && ... => P, assume
    {{ P }}
    tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
    ↗ Postcond. {{ Q }}
    ...
    {{ S }} ↗ Postcondition
}
```

Hoare triples:
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syscall (i.e. *kernel-userland*) interface



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        {{ Q }} ↗ Postcond. // if Q => S, conclude
        {{ S }}
    }
    {{ S }} ↗ Postcondition
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Hoare triples:
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        ↗ {{ Q }}
        // if Q => S, conclude
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    }
    {{ S }}
    ...
    ↗ Postcondition
}
```

Hoare triples:
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seL4 Microkit Library

Precond.

Postcond.

syscall (i.e. *kernel-userland*) interface



Microkit assumes seL4's syscalls work



```
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    ↗ Precondition
    {{ R }}
    if (have_reply) {
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    } else {
        {{ R && ! have_reply && ! microkit_have_signal }}
        // if R && ... => P, assume
        ↗ {{ P }}
        tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
        ↗ {{ Q }}
        // if Q => S, conclude
        {{ S }}
    }
    {{ S }} // done
    ↗ Postcondition ✓
}
```

Hoare triples:
{{ Pre }} f {{ Post }}

seL4 Microkit Library

Precond.

Postcond.



Microkit assumes seL4's syscalls work



```
static void handler_loop(void) {
    ...
    {{ R }} Precondition
    if (have_reply) {
        {{ R && ... }} ... {{ S }}
    } else {
        Precond. {{ R && ! have_reply && ! microkit_have_signal }}
        // if R && ... => P, assume
        {{ P }}
        tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
        Postcond. {{ Q }}
        // if Q => S, conclude
        {{ S }}
    }
    {{ S }} // done
    ...
    Postcondition ✓
}
```

Hoare triples:
{{ Pre }} f {{ Post }}

seL4 Microkit Library



Microkit assumes seL4's syscalls work



But is it
true?

```
static void handler_loop(void) {
    ...
    {{ R }} Precondition
    if (have_reply) {
        {{ R && ... }} ... {{ S }}
    } else {
        Precond. {{ R && ! have_reply && ! microkit_have_signal }}
        // if R && ... => P, assume
        {{ P }}
        tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
        Postcond. {{ Q }}
        // if Q => S, conclude
        {{ S }}
    }
    {{ S }} // done
    ...
}
```

Postcondition ✓

Hoare triples:
{{ Pre }} f {{ Post }}

seL4 Microkit Library



Microkit's assumptions need verifying!



```
static void handler_loop(void) { ...
    {{ R && ! have_reply && ! microkit_have_signal }}
    // if R && ... => P, assume
    {{ P }}
    tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
    {{ Q }}
    // if Q => S, conclude
    {{ S }}
    ...
}
```

syscall (i.e. *kernel–userland*) interface

seL4 Microkit Library

seL4 OS Microkernel
Abstract Model



Microkit's assumptions need verifying!



```
static void handler_loop(void) { ...  
    {{ R && ! have_reply && ! microkit_have_signal }}  
    // if R && ... => P, assume  
    {{ P }}  
    tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);  
    {{ Q }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
}
```

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

definition call_kernel :: "event \Rightarrow (unit, ...) s_monad" **where**

```
call_kernel ev  $\equiv$  do  
    handle_event ev ...;  
    schedule;  
    activate_thread  
od
```

seL4 OS Microkernel
Abstract Model



Microkit's assumptions need verifying!



```
static void handler_loop(void) { ...  
    {{ R && ! have_reply && ! microkit_have_signal }}  
    // if R && ... => P, assume  
    {{ P }}  
    tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);  
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    // if Q => S, conclude  
    {{ S }}  
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}
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seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

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    od  
    {{ Q }} ?
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seL4 OS Microkernel
Abstract Model



Microkit's assumptions need verifying!



```
static void handler_loop(void) { ...  
    {{ R && ! have_reply && ! microkit_have_signal }}  
    // if R && ... => P, assume  
    {{ P }}  
    tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);  
    {{ Q }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
}
```

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

```
definition call_kernel :: "event  $\Rightarrow$  (unit, ...) s_monad" where  
    {{ invs }}  
    call_kernel ev  $\equiv$  do  
        handle_event ev ...;  
        schedule;  
        activate_thread  
    od  
    {{ invs }} incl. "doesn't crash" ✓
```

seL4 OS Microkernel
Abstract Model



Microkit's assumptions need verifying!



```
static void handler_loop(void) { ...  
    {{ R && ! have_reply && ! microkit_have_signal }}  
    // if R && ... => P, assume  
    {{ P }}  
    tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);  
    {{ Q }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
}
```

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

definition call_kernel :: "event \Rightarrow (unit, ...)" s_monad" **where**

 {{ P }} {{ invs }}

 call_kernel ev \equiv do
 handle_event ev ...;
 schedule;
 activate_thread

 od

 {{ Q }} ?

 {{ invs }} incl. "doesn't crash"



seL4 OS Microkernel
Abstract Model



Microkit's assumptions need verifying!



```
static void handler_loop(void) { ...  
    {{ R && ! have_reply && ! microkit_have_signal }}  
    // if R && ... => P, assume  
    {{ P }}  
    tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);  
    {{ Q }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
}
```

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

definition call_kernel :: "event \Rightarrow (unit, ...)" s_monad" **where**

```
    {{ P }}  
    call_kernel ev  $\equiv$  do  
        handle_event ev ...;  
        schedule;  
        activate_thread  
    od  
    {{ Q }} ? 
```

seL4 OS Microkernel
Abstract Model



Microkit's assumptions need verifying!



```
static void handler_loop(void) { ...
    {{ R && ! have_reply && ! microkit_have_signal }}
    // if R && ... => P, assume
    {{ P }}
    tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
    {{ Q }}
    // if Q => S, conclude
    {{ S }}
    ...
}
```

————— syscall (i.e. *kernel–userland*) interface

```
definition call_kernel :: "event => (unit, ...) s_monad" where
{{ P }}=> {{ P' && cap_reg1 == INPUT_CAP && cap_reg2 == REPLY_CAP }}
    call_kernel ev ≡ do
        handle_event ev ...;
        schedule;
        activate_thread
    od
{{ Q }}<= {{ Q' && badge_reg == ? }}
```

seL4 Microkit Library

Note: libsel4 wrappers do this register marshalling - not focusing on it for now!



seL4 OS Microkernel
Abstract Model



Microkit's assumptions need verifying!



```
static void handler_loop(void) { ...
  {{ R && ! have_reply && ! microkit_have_signal }}
  // if R && ... => P, assume
  {{ P }}
  tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
  {{ Q }}
  // if Q => S, conclude
  {{ S }}
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  call_kernel ev ≡ do
    handle_event ev ...;
    schedule;
    activate_thread
  od
{{ Q }}<= {{ Q' && badge_reg == ? }}
```

seL4 Microkit Library

Note: libsel4 wrappers do this register marshalling - not focusing on it for now!



seL4 OS Microkernel Abstract Model

Question:

Is proving a Hoare triple over one
call_kernel entry always enough?



Microkit's assumptions need verifying!



```
static void handler_loop(void) { ...
  {{ R && ! have_reply && ! microkit_have_signal }}
  // if R && ... => P, assume
  {{ P }}
  tag = seL4_Recv(INPUT_CAP, &badge, REPLY_CAP);
  {{ Q }}
  // if Q => S, conclude
  {{ S }}
...
}
  _____ syscall (i.e. kernel-userland) interface
definition call_kernel :: "event => (unit, ...) s_monad" where
{{ P }}=> {{ P' && cap_reg1 == INPUT_CAP && cap_reg2 == REPLY_CAP }}
  call_kernel ev ≡ do
    handle_event ev ...;
    schedule;
    activate_thread
  od
{{ Q }} X {{ Q' && badge_reg == ? }}
```

seL4 Microkit Library

Note: libsel4 wrappers do this register marshalling - not focusing on it for now!



seL4 OS Microkernel Abstract Model

Question:

Is proving a Hoare triple over one
call_kernel entry always enough?

No.



System calls can block



Process A

```
static void handler_loop(void) { ...  
    {{ R && ... }}  
    // if R && ... => P, assume  
    {{ P_A }}  
    tag = seL4_Recv(...);  
    {{ Q_A }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
}
```

seL4 Microkit Library

Blocking seL4_Recv call

```
    {{ P_A }} => {{ P' && ... }}  
        call_kernel ev ≡ do  
            handle_event ev ...;  
            schedule;  
            activate_thread  
        od  
    {{ Q_A }} X {{ Q' && ... }}
```

syscall (i.e. *kernel-userland*)
interface

seL4 OS Microkernel
Abstract Model



System calls can block



Process A

```
static void handler_loop(void) { ...  
    {{ R && ... }}  
    // if R && ... => P, assume  
    {{ P_A }}  
    tag = seL4_Recv(...);  
    {{ Q_A }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
}
```

Process B

seL4 Microkit Library

syscall (i.e. *kernel-userland*)
interface

Blocking seL4_Recv call

```
    {{ P_A }} => {{ P' && ... }}  
        call_kernel ev ≡ do  
            handle_event ev ...;  
            schedule;  
            activate_thread // B  
        od  
    {{ Q' && ... }}
```

seL4 OS Microkernel
Abstract Model



System calls can block



Process A

```
static void handler_loop(void) { ...  
    {{ R && ... }}  
    // if R && ... => P, assume  
    {{ P_A }}  
    tag = seL4_Recv(...);  
    {{ Q_A }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
}
```

Process B

Blocking `seL4_Recv` call

```
    {{ P_A }} => {{ P' && ... }}  
        call_kernel ev ≡ do  
            handle_event ev ...;  
            schedule;  
            activate_thread // B  
        od  
    {{ Q' && ... }}
```

Unlocking `seL4_Signal` call

seL4 Microkit Library

syscall (i.e. *kernel-userland*)
interface

seL4 OS Microkernel
Abstract Model



System calls can block



Process A

```
static void handler_loop(void) { ...  
    {{ R && ... }}  
    // if R && ... => P, assume  
    {{ P_A }}  
    tag = seL4_Recv(...);  
    {{ Q_A }}  
    // if Q => S, conclude  
    {{ S }}  
    ...
```

Process B

```
static inline void  
microkit_notify(microkit_channel ch) { ...  
    {{ P_B }}  
    seL4_Signal(... + ch);  
    {{ Q_B }}  
}
```

seL4 Microkit Library

syscall (i.e. *kernel-userland*)
interface

Blocking seL4_Recv call

```
    {{ P_A }} => {{ P' && ... }}  
        call_kernel ev ≡ do  
            handle_event ev ...;  
            schedule;  
            activate_thread // B  
        od  
    {{ Q' && ... }}
```

Unlocking seL4_Signal call

seL4 OS Microkernel
Abstract Model



System calls can block



Process A

```
static void handler_loop(void) { ...  
    {{ R && ... }}  
    // if R && ... => P, assume  
    {{ P_A }}  
    tag = seL4_Recv(...);  
    {{ Q_A }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
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```

Process B

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static inline void  
microkit_notify(microkit_channel ch) { ...  
    {{ P_B }}  
    seL4_Signal(... + ch);  
    {{ Q_B }}  
}
```

Verifying these is
an unsolved problem*

seL4 Microkit Library

* to the best of our knowledge, and
when they block on other processes
(not just I/O!)

syscall (i.e. *kernel-userland*)
interface

Blocking seL4_Recv call

```
    {{ P_A }} => {{ P' && ... }}  
    call_kernel ev ≡ do  
        handle_event ev ...;  
        schedule;  
        activate_thread // B  
    od  
    {{ Q' && ... }}
```

Unlocking seL4_Signal call

seL4 OS Microkernel
Abstract Model



System calls can block

Verifying these is
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Process A

```
static void handler_loop(void) { ...  
    {{ R && ... }}  
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    {{ P_A }}  
    tag = seL4_Recv(...);  
    {{ Q_A }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
}
```

Blocking `seL4_Recv` call

```
    {{ P_A }} => {{ P' && ... }}  
        call_kernel ev ≡ do  
            handle_event ev ...;  
            schedule;  
            activate_thread // B  
        od  
    {{ Q' && ... }}
```

Process B

```
static inline void  
microkit_notify(microkit_channel ch) { ...  
    {{ P_B }}  
    seL4_Signal(... + ch);  
    {{ Q_B }}  
}
```

seL4 Microkit Library

* to the best of our knowledge, and
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syscall (i.e. *kernel-userland*)
interface

→ Unblocking `seL4_Signal` call

```
    {{ P_B }} => {{ P" && ... }}  
        call_kernel ev ≡ do  
            handle_event ev ...;  
            schedule;  
            activate_thread  
        od  
    {{ Q" && ... }}
```

seL4 OS Microkernel
Abstract Model



System calls can block



Process A

```
static void handler_loop(void) { ...  
    {{ R && ... }}  
    // if R && ... => P, assume  
    {{ P_A }}  
    tag = seL4_Recv(...);  
    {{ Q_A }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
}
```

Blocking seL4_Recv call

```
    {{ P_A }} => {{ P' && ... }}  
        call_kernel ev ≡ do  
            handle_event ev ...;  
            schedule;  
            activate_thread // B  
        od  
    {{ Q' && ... }}
```

Process B

```
static inline void  
microkit_notify(microkit_channel ch) { ...  
    {{ P_B }}  
    seL4_Signal(... + ch);  
    {{ Q_B }}  
}
```

Verifying these is
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seL4 Microkit Library

* to the best of our knowledge, and
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syscall (i.e. *kernel-userland*)
interface

→ Unblocking seL4_Signal call

```
    {{ P_B }} => {{ P" && ... }}  
        call_kernel ev ≡ do  
            handle_event ev ...;  
            schedule;  
            activate_thread // A  
        od  
    {{ Q" && ... }} => {{ Q_A }}
```

seL4 OS Microkernel
Abstract Model



System calls can block

Verifying these is
an unsolved problem*



Process A

```
static void handler_loop(void) { ...  
    {{ R && ... }}  
    // if R && ... => P, assume  
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    tag = seL4_Recv(...);  
    {{ Q_A }}  
    // if Q => S, conclude  
    {{ S }}  
    ...  
}
```

Blocking seL4_Recv call

```
    {{ P_A }} => {{ P' && ... }}  
        call_kernel ev ≡ do  
            handle_event ev ...;  
            schedule;  
            activate_thread // B  
        od  
    {{ Q' && ... }}
```

Process B

```
static inline void  
microkit_notify(microkit_channel ch) { ...  
    {{ P_B }}  
    seL4_Signal(... + ch);  
    {{ Q_B }}  
}
```

seL4 Microkit Library

* to the best of our knowledge, and
when they block on other processes
(not just I/O!)

syscall (i.e. *kernel-userland*)
interface

→ Unblocking seL4_Signal call

```
    {{ P_B }} => {{ P" && ... }}  
        call_kernel ev ≡ do  
            handle_event ev ...;  
            schedule;  
            activate_thread // A  
        od  
    {{ Q" && ... }} => {{ Q_A }}
```

seL4 OS Microkernel
Abstract Model



System calls can block



Process A

```
static void handler_loop(void) { ...
    {{ R && ... }}
    // if R && ... => P, assume
    {{ P_A }}
    tag = seL4_Recv(...);
    {{ Q_A }}
    // if Q => S, conclude
    {{ S }}
    ...
}
```

Blocking seL4_Recv call

```
{{ P_A }} => {{ P' && ... }}
call_kernel ev ≡ do
    handle_event ev ...;
? schedule;
activate_thread // X
od
{{ Q' && ... }}
```

Process B

```
static inline void
microkit_notify(microkit_channel ch) { ...
    {{ P_B }}
    sel4_Signal(... + ch);
    {{ Q_B }}
}
```

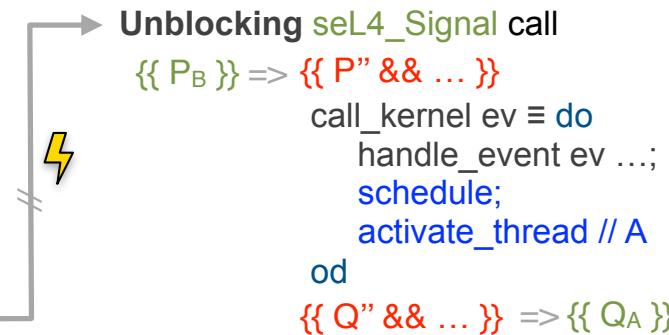
Verifying these is
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seL4 Microkit Library

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syscall (i.e. *kernel-userland*)
interface

seL4 OS Microkernel
Abstract Model





System calls can block



Process A

```
static void handler_loop(void) { ...
    {{ R && ... }}
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    {{ P_A }}
    tag = seL4_Recv(...);
    {{ Q_A }}
    // if Q => S, conclude
    {{ S }}
    ...
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```

Blocking seL4_Recv call

```
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call_kernel ev ≡ do
    handle_event ev ...;
? schedule;
activate_thread // X
od
{{ Q' && ... }}
```

Process B

```
static inline void
microkit_notify(microkit_channel ch) { ...
    {{ P_B }}
    sel4_Signal(... + ch);
    {{ Q_B }}
}
```

Verifying these is
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seL4 Microkit Library

* to the best of our knowledge, and
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syscall (i.e. *kernel-userland*)
interface

Unlocking seL4_Signal call

```
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call_kernel ev ≡ do
    handle_event ev ...;
schedule;
activate_thread // A
od
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```

seL4 OS Microkernel
Abstract Model



System calls can block

Verifying these is
an unsolved problem*



Process A

```
static void handler_loop(void) { ...
    {{ R && ... }}
    // if R && ... => P, assume
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Process B

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static inline void
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    sel4_Signal(... + ch);
    {{ Q_B }}
}
```

seL4 Microkit Library

Blocking seL4_Recv call

```
{{ P_A }} => {{ P' && ... }}
call_kernel ev ≡ do
    handle_event ev ...;
? schedule;
activate_thread // X
od
{{ Q' && ... }}
```

Unlocking seL4_Signal call

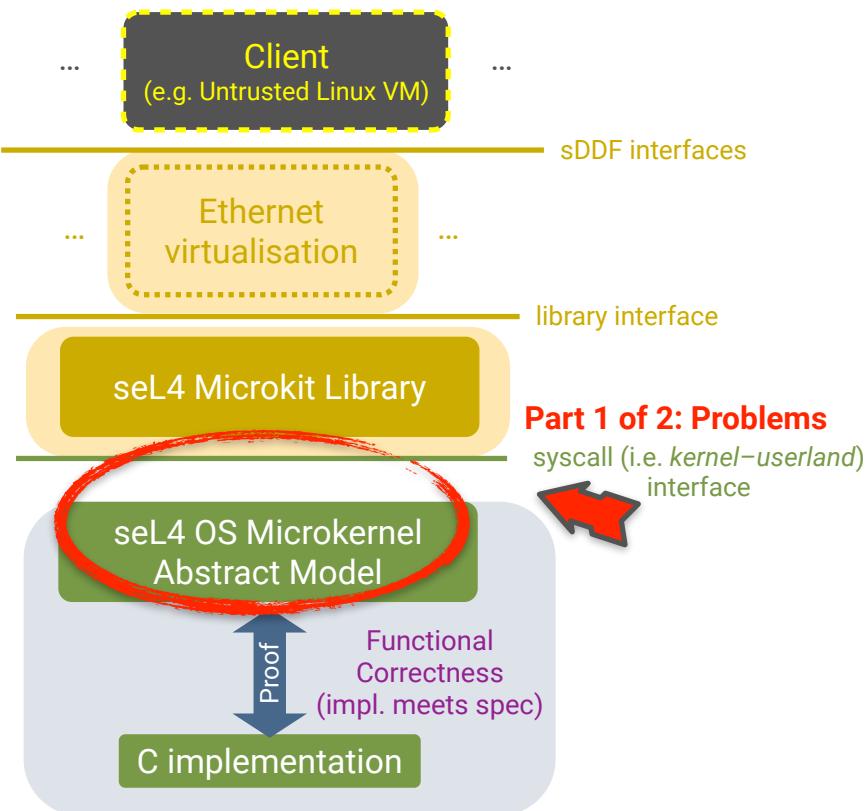
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syscall (i.e. *kernel-userland*)
interface

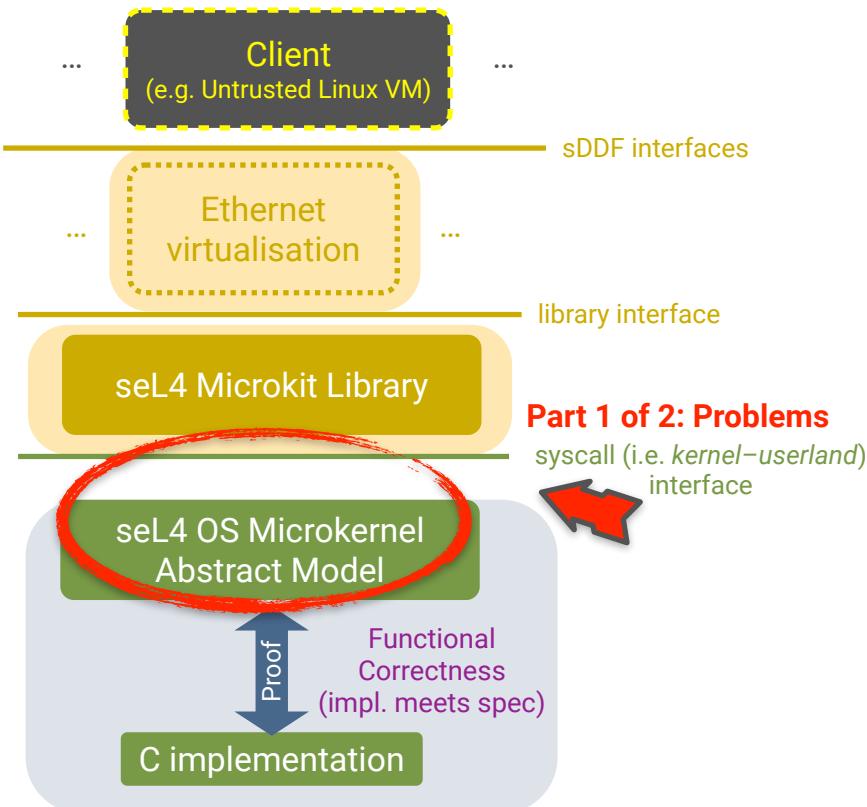
seL4 OS Microkernel
Abstract Model

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• sel4 Summary: Kernel–userland gap so far

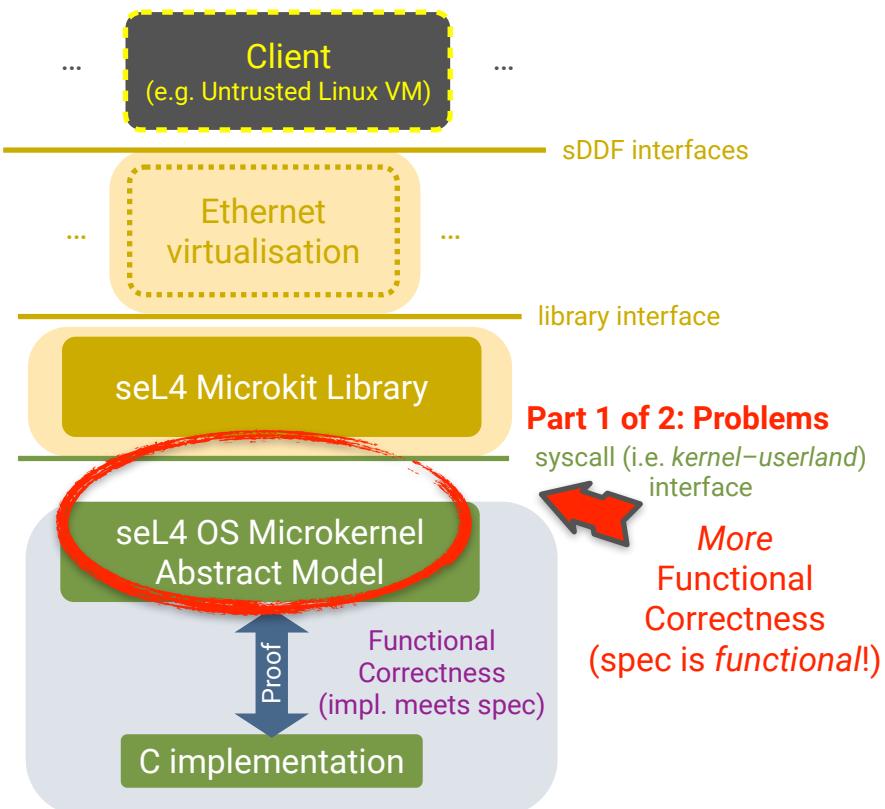


• sel4 Summary: Kernel–userland gap so far



- Microkit assumes syscall **functional specs** as Hoare triples

• sel4 Summary: Kernel–userland gap so far

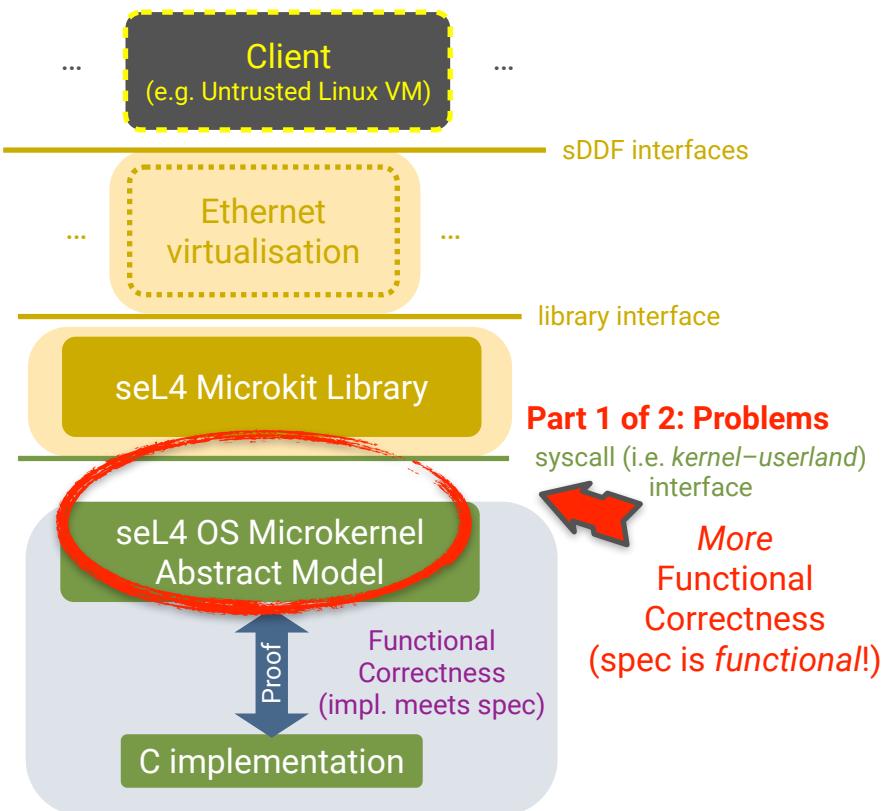


- Microkit assumes syscall **functional specs** as Hoare triples

Part 1 of 2: Problems
syscall (i.e. kernel–userland)
interface

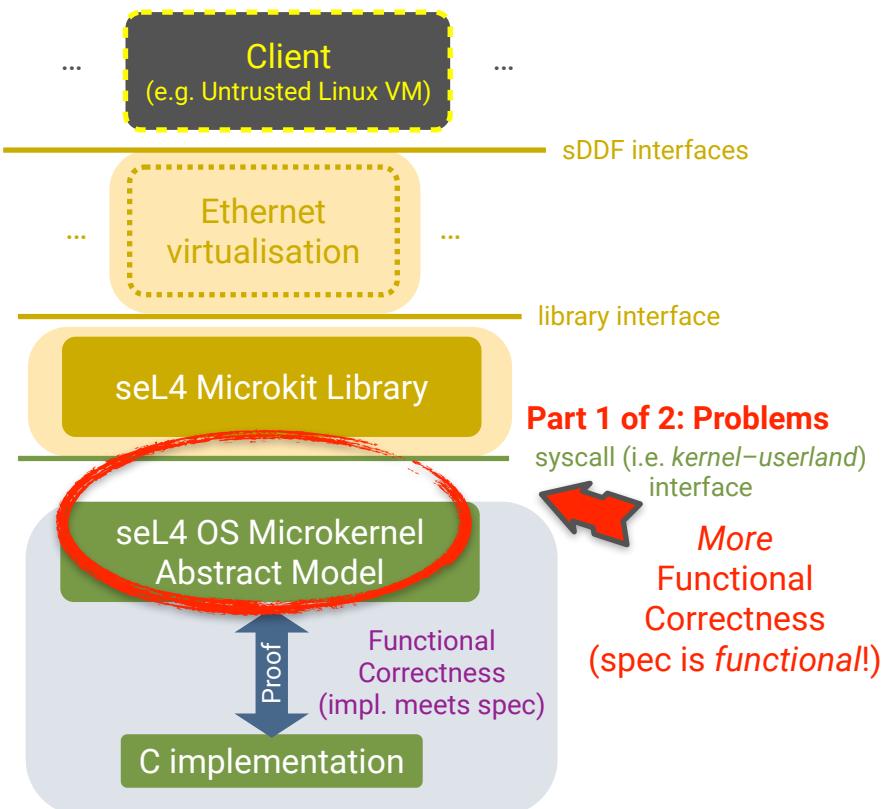
More
Functional
Correctness
(spec is *functional!*)

• sel4 Summary: Kernel–userland gap so far



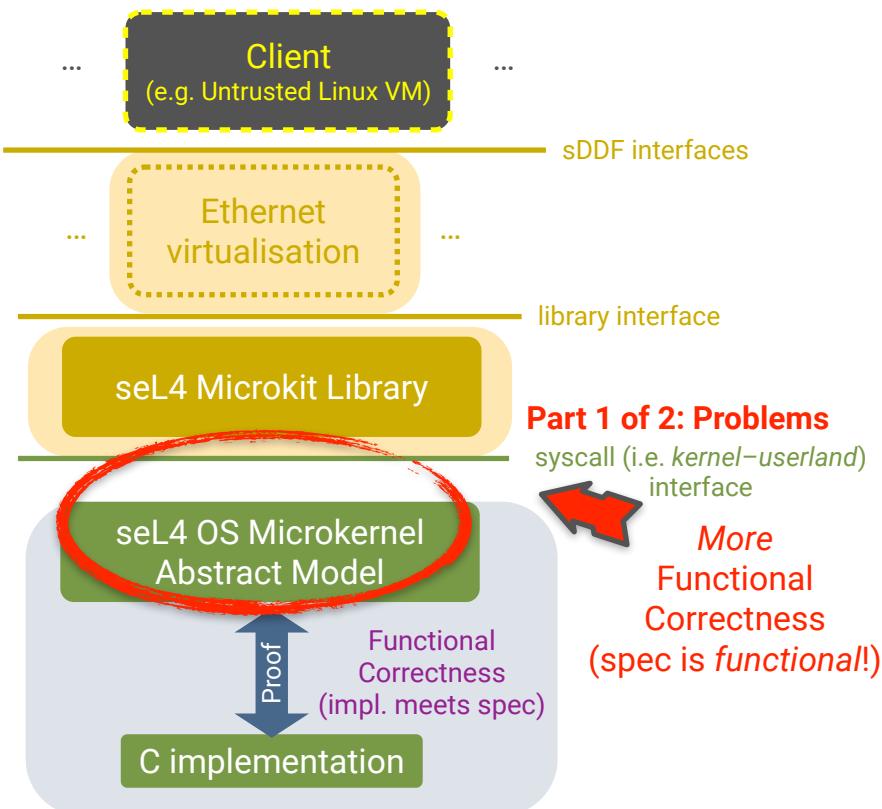
- Microkit assumes syscall **functional specs** as Hoare triples
- We now **need to prove seL4's Abstract Model satisfies them!**
(Then we'll know its C implementation does, too.)

• sel4 Summary: Kernel–userland gap so far



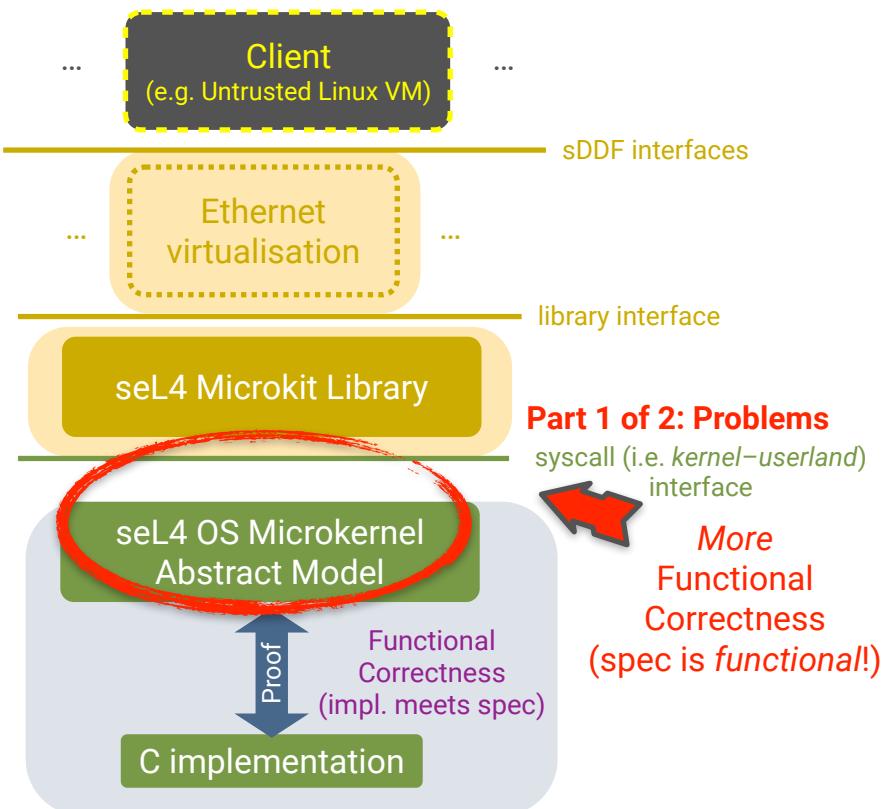
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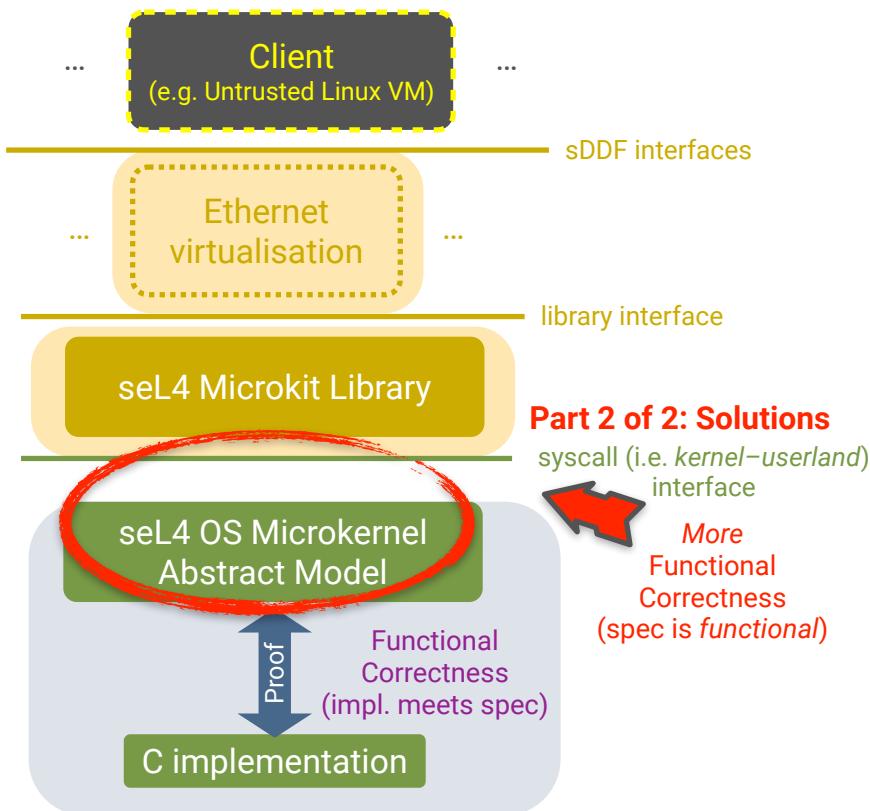
- Microkit assumes syscall **functional specs** as Hoare triples
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- We handwave some register marshalling (for now)
- Blocking syscalls may require Hoare triples for up to $2 + n$ kernel entries (finite n):
 - 1 **Blocking** call (e.g. Recv)
 - n **Irrelevant** calls or interrupts
 - 1 **Unblocking** call (e.g. Signal)

• sel4 Summary: Kernel–userland gap so far



- Microkit assumes syscall **functional specs** as Hoare triples
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- Verifying syscalls like these is **an open problem**

seL4 Towards kernel–userland functional proofs



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Towards kernel–userland functional proofs



seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

seL4 OS Microkernel
Abstract Model



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

seL4 OS Microkernel
Abstract Model



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ P \} \} \text{ seL4_Recv } \{\{ Q \} \}$

Process B

$\{\{ P' \} \} \text{ seL4_Signal } \{\{ Q' \} \}$

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

seL4 OS Microkernel
Abstract Model



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ \lambda s. P s \} \} \text{ seL4_Recv } \{\{ \lambda s. Q s \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{ seL4_Signal } \{\{ \lambda s. Q' s \} \}$

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Abstract Model



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Process B

$\{\{ \lambda s. P' s \} \} \text{ seL4_Signal } \{\{ \lambda s. Q' s \} \}$

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

$\{\{ P \&& \dots \} \}$
call_kernel
 $\{\{ Q \&& \dots \} \}$

$\{\{ P' \&& \dots \} \}$
call_kernel
 $\{\{ Q' \&& \dots \} \}$

seL4 OS Microkernel
Abstract Model



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ \lambda s. P s \} \} \text{ seL4_Recv } \{\{ \lambda s. Q s \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{ seL4_Signal } \{\{ \lambda s. Q' s \} \}$

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

$\{\{ P \&& \dots \} \}$
call_kernel
 $\{\{ Q \&& \dots \} \}$

Eliding register side-conds
to save space...

$\{\{ P' \&& \dots \} \}$
call_kernel
 $\{\{ Q' \&& \dots \} \}$

seL4 OS Microkernel
Abstract Model



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ \lambda s. P s \} \} \text{ seL4_Recv } \{\{ \lambda s. Q s \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{ seL4_Signal } \{\{ \lambda s. Q' s \} \}$

Read:
 ks_of = “kernel state of”

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

seL4 OS Microkernel
Abstract Model



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ \lambda s. P s \} \} \text{seL4_Recv } \{\{ \lambda s. Q s \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{seL4_Signal } \{\{ \lambda s. Q' s \} \}$

Read:
 ks_of = “kernel state of”

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

seL4 OS Microkernel
Abstract Model

- For a correctly initialised Microkit system, no $X \neq Y$ should possess the *capabilities* to change *most parts* of ($\text{ks_of } Y s$).



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ \lambda s. P s \} \} \text{ seL4_Recv } \{\{ \lambda s. Q s \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{ seL4_Signal } \{\{ \lambda s. Q' s \} \}$

Read:
 ks_of = “kernel state of”

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

seL4 OS Microkernel
Abstract Model

- For a correctly initialised Microkit system, no $X \neq Y$ should possess the *capabilities* to change *most parts* of ($\text{ks_of } Y s$).

$\text{ks_of } p s = \{$
 $\text{thread_cnode } p s,$
 $\text{bound_notification } p s,$
 $\text{mapped_writable } p s,$
 $\text{not_writable_others } p s,$
 $\text{recv_oracle } s (\text{bound_notification } p s) (\text{thread_cnode } p s),$
 $\lambda \text{ch. ntfn_status } s (\text{thread_cnode } p s) \text{ ch}$
 $\}$



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ \lambda s. P s \} \} \text{ seL4_Recv } \{\{ \lambda s. Q s \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{ seL4_Signal } \{\{ \lambda s. Q' s \} \}$

Read:
 ks_of = “kernel state of”

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

seL4 OS Microkernel
Abstract Model

- For a correctly initialised Microkit system, no $X \neq Y$ should possess the *capabilities* to change *most parts* of $(\text{ks_of } Y s)$.



$\left\{ \begin{array}{l} \text{ks_of } p s = () \\ \text{thread_cnode } p s, \\ \text{bound_notification } p s, \\ \text{mapped_writable } p s, \\ \text{not_writable_others } p s, \\ \text{recv_oracle } s (\text{bound_notification } p s) (\text{thread_cnode } p s), \\ \lambda ch. \text{ntfn_status } s (\text{thread_cnode } p s) ch \end{array} \right.$



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ \lambda s. P s \} \} \text{seL4_Recv } \{\{ \lambda s. Q s \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{seL4_Signal } \{\{ \lambda s. Q' s \} \}$

Read:
 ks_of = “kernel state of”

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

seL4 OS Microkernel
Abstract Model

- For a correctly initialised Microkit system, no $X \neq Y$ should possess the *capabilities* to change *most parts* of $(\text{ks_of } Y s)$.



$\left\{ \begin{array}{l} \text{ks_of } p s = () \\ \text{thread_cnode } p s, \\ \text{bound_notification } p s, \\ \text{mapped_writable } p s, \\ \text{not_writable_others } p s, \\ \text{recv_oracle } s (\text{bound_notification } p s) (\text{thread_cnode } p s), \\ \lambda \text{ch. ntfn_status } s (\text{thread_cnode } p s) \text{ ch} \end{array} \right\} \text{cap state, thread init!}$



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ \lambda s. P s \} \} \text{seL4_Recv } \{\{ \lambda s. Q s \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{seL4_Signal } \{\{ \lambda s. Q' s \} \}$

Read:
ks_of = "kernel state of"

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

seL4 OS Microkernel
Abstract Model

- For a correctly initialised Microkit system, no $X \neq Y$ should possess the *capabilities* to change *most parts* of $(\text{ks_of } Y s)$.



$\left\{ \begin{array}{l} \text{ks_of } p s = (\\ \quad \text{thread_cnode } p s, \\ \quad \text{bound_notification } p s, \\ \quad \text{mapped_writable } p s, \\ \quad \text{not_writable_others } p s, \\ \quad \text{recv_oracle } s (\text{bound_notification } p s) (\text{thread_cnode } p s), \\ \quad \lambda \text{ch. ntfn_status } s (\text{thread_cnode } p s) \text{ ch} \\) \end{array} \right. \begin{array}{l} \} \text{ cap state, thread init!} \\ \} \text{ memory mappings!} \end{array}$



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ \lambda s. P s \} \} \text{seL4_Recv } \{\{ \lambda s. Q s \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{seL4_Signal } \{\{ \lambda s. Q' s \} \}$

Read:
 ks_of = “kernel state of”

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

seL4 OS Microkernel
Abstract Model

- For a correctly initialised Microkit system, no $X \neq Y$ should possess the *capabilities* to change *most parts* of $(\text{ks_of } Y s)$.
- But we still have to prove when it *does* (i.e. **Unblocking**) or *doesn't* (i.e. **Irrelevant**).

$\left\{ \begin{array}{l} \text{ks_of } p s = () \\ \text{thread_cnode } p s, \\ \text{bound_notification } p s, \\ \text{mapped_writable } p s, \\ \text{not_writable_others } p s, \\ \text{recv_oracle } s (\text{bound_notification } p s) (\text{thread_cnode } p s), \\ \lambda \text{ch. ntfn_status } s (\text{thread_cnode } p s) \text{ ch} \end{array} \right\}$

cap state, thread init!
memory mappings!



Towards kernel–userland functional proofs



- It helps that Microkit's assumptions are on *per-process* projections of the kernel state:

Process A

$\{\{ \lambda s. P s \} \} \text{seL4_Recv } \{\{ \lambda s. Q s \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{seL4_Signal } \{\{ \lambda s. Q' s \} \}$

Read:
 ks_of = “kernel state of”

seL4 Microkit Library

syscall (i.e. *kernel–userland*) interface

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

seL4 OS Microkernel
Abstract Model

- For a correctly initialised Microkit system, no $X \neq Y$ should possess the *capabilities* to change *most parts* of $(\text{ks_of } Y s)$.



$\left\{ \begin{array}{l} \text{ks_of } p s = (\\ \quad \text{thread_cnode } p s, \\ \quad \text{bound_notification } p s, \\ \quad \text{mapped_writable } p s, \\ \quad \text{not_writable_others } p s, \\ \quad \text{recv_oracle } s (\text{bound_notification } p s) (\text{thread_cnode } p s), \\ \quad \lambda \text{ch. ntfn_status } s (\text{thread_cnode } p s) \text{ ch} \end{array} \right. \begin{array}{l} \} \text{ cap state, thread init!} \\ \} \text{ memory mappings!} \end{array}$

- But we still have to prove when it *does* (i.e. **Unblocking**) or *doesn't* (i.e. **Irrelevant**).

sel4 What we've done

- Defined state projections



Process A
 $\{\{ \lambda s. P s \} \} \text{seL4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

Process B
 $\{\{ \lambda s. P' s \} \} \text{seL4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

Read:
ks_of = "kernel state of"

seL4 Microkit Library

syscall (i.e. *kernel-userland*) interface

seL4 OS Microkernel
Abstract Model

Microkit-facing state

$\text{ks_of } p s : \{$
→ $\text{thread_cnode } p s,$ } cap state, thread init!
→ $\text{bound_notification } p s,$ } memory mappings!
→ $\text{mapped_writable } p s,$
→ $\text{not_writable_others } p s,$
→ $\text{recv_oracle } s (\text{bound_notification } p s) (\text{thread_cnode } p s),$
→ $\lambda \text{ch. ntfn_status } s (\text{thread_cnode } p s) \text{ ch}$
}

sel4 What we've done

- Defined state projections

Process A
 $\{\{\lambda s. P\ s\}\} \text{seL4_Recv } \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$
 call_kernel
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$

Process B
 $\{\{\lambda s. P'\ s\}\} \text{seL4_Signal } \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$
 call_kernel
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$

Read:
 $\text{ks_of} = \text{"kernel state of"}$

seL4 Microkit Library

syscall (i.e. *kernel-userland*) interface

seL4 OS Microkernel Abstract Model

Microkit-facing state

$\text{ks_of } p\ s : ()$

$\rightarrow \text{thread_cnode } p\ s,$
 $\rightarrow \text{bound_notification } p\ s,$
 $\rightarrow \text{mapped_writable } p\ s,$
 $\rightarrow \text{not_writable_others } p\ s,$
 $\rightarrow \text{recv_oracle } p\ s \ (\text{bound_notification } p\ s) \ (\text{thread_cnode } p\ s),$
 $\rightarrow \lambda \text{ch. ntfn_status } p\ s \ (\text{thread_cnode } p\ s) \ \text{ch}$
 $)$

Abstract Model state

$\} \text{ cap state, thread init! }$

$\} \text{ memory mappings! }$

sel4 What we've done

- Defined state projections
- Verifying Hoare triples on calls

Read:
ks_of = "kernel state of"

Process A

$\{\{ \lambda s. P s \} \} \text{seL4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{seL4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel
Abstract Model

ks_of p s = (**Abstract Model state**
 $\text{thread_cnode } | s,$
 $\text{bound_notification } | s,$ } cap state, thread init!
 $\text{mapped_writable } | s,$
 $\text{not_writable_others } | s,$ } memory mappings!
 $\text{recv_oracle } | s, \text{bound_notification } p s)$ (thread_cnode p s),
 $\lambda \text{ch. ntfn_status } | s, \text{thread_cnode } p s) \text{ ch}$
)

• sel4 What we've done

- Defined state projections
- Verifying Hoare triples on calls

Read:
ks_of = "kernel state of"

Process A

$\{\{ \lambda s. P s \} \} \text{sel4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{sel4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel
Abstract Model

```
call_kernel ev ≡ do
    handle_event ev ...;
    schedule;
    activate_thread
od
```

ks_of p s = (**Abstract Model state**
 $\text{thread_cnode } | s,$
 $\text{bound_notification } | s,$ } cap state, thread init!
 $\text{mapped_writable } | s,$
 $\text{not_writable_others } | s,$ } memory mappings!
 $\text{recv_oracle } | s, \text{bound_notification } p s) (\text{thread_cnode } p s),$
 $\lambda \text{ch. ntfn_status } | s (\text{thread_cnode } p s) \text{ ch}$
)



sel4 What we've done

- Defined state projections
- Verifying Hoare triples on calls

Read:
ks_of = "kernel state of"

Process A

$\{\{ \lambda s. P s \} \} \text{seL4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
 call_kernel
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

Process B

$\{\{ \lambda s. P' s \} \} \text{seL4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
 call_kernel
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel
Abstract Model

```
call_kernel ev ≡ do
    handle_event ev ...;
    schedule;
    activate_thread } we'll come back to this
od
```

ks_of p s = (**Abstract Model state**)
 $\text{thread_cnode } | s,$
 $\text{bound_notification } | s,$ } cap state, thread init!
 $\text{mapped_writable } | s,$
 $\text{not_writable_others } | s,$ } memory mappings!
 $\text{recv_oracle } | s, \text{bound_notification } p s) (\text{thread_cnode } p s),$
 $\lambda \text{ch. ntfn_status } | s (\text{thread_cnode } p s) \text{ ch}$
)



sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{\lambda s. P\ s\}\} \text{seL4_Recv } \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$
 call_kernel
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$

Process B

$\{\{\lambda s. P'\ s\}\} \text{seL4_Signal } \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$
 call_kernel
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel
Abstract Model

```
call_kernel ev ≡ do
  handle_event ev ...; ←
  schedule;
  activate_thread } we'll come back to this
od
```

ks_of p s = (**Abstract Model state**)
 $\text{thread_cnode } | s,$
 $\text{bound_notification } | s,$ } cap state, thread init!
 $\text{mapped_writable } | s,$
 $\text{not_writable_others } | s,$ } memory mappings!
 $\text{recv_oracle } | s, \text{ bound_notification } p\ s, (\text{thread_cnode } p\ s),$
 $\lambda \text{ch. ntfn_status } | s, (\text{thread_cnode } p\ s) \text{ ch}$
)

sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{\lambda s. P\ s\}\} \text{seL4_Recv } \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$
 handle_recv
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$

Process B

$\{\{\lambda s. P'\ s\}\} \text{seL4_Signal } \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$
 call_kernel
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel
Abstract Model

call_kernel ev ≡ do
 $\text{handle_event ev ...; }$ ←
 schedule;
 activate_thread } we'll come back to this
od

ks_of p s = (**Abstract Model state**
 $\text{thread_cnode } | s,$
 $\text{bound_notification } | s,$ } cap state, thread init!
 $\text{mapped_writable } | s,$
 $\text{not_writable_others } | s,$ } memory mappings!
 $\text{recv_oracle } | s, \text{ bound_notification } p\ s, \text{ (thread_cnode } p\ s),$
 $\lambda \text{ch. ntfn_status } | s, \text{ (thread_cnode } p\ s) \text{ ch}$
)

sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{\lambda s. P\ s\}\} \text{seL4_Recv} \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$ ✓ “Nonblocking”
 handle_recv
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$

Process B

$\{\{\lambda s. P'\ s\}\} \text{seL4_Signal} \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$
 call_kernel
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$

seL4 Microkit Library

syscall (i.e. *kernel-userland*) interface

seL4 OS Microkernel
Abstract Model

call_kernel ev ≡ do
 $\text{handle_event ev ...;}$ ←
 schedule;
 activate_thread } we'll come back to this
od

ks_of p s = (**Abstract Model state**
 $\text{thread_cnode } | s,$
 $\text{bound_notification } | s,$ } cap state, thread init!
 $\text{mapped_writable } | s,$
 $\text{not_writable_others } | s,$ } memory mappings!
 $\text{recv_oracle } | s, \text{bound_notification } p\ s, (\text{thread_cnode } p\ s),$
 $\lambda \text{ch. ntfn_status } | s, (\text{thread_cnode } p\ s) \text{ ch}$
)

sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{\lambda s. P\ s\}\} \text{seL4_Recv} \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$ ✓ “Nonblocking”
 handle_recv
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$

Process B

$\{\{\lambda s. P'\ s\}\} \text{seL4_Signal} \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$ Blocking
 call_kernel
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$

seL4 Microkit Library

syscall (i.e. *kernel-userland*) interface

seL4 OS Microkernel Abstract Model

call_kernel ev ≡ do
 handle_event ev ...;
 schedule;
 activate_thread } we'll come back to this
 od

ks_of p s = (**Abstract Model state**
 thread_cnode | s,
 bound_notification | s, } cap state, thread init!
 mapped_writable | s, } memory mappings!
 not_writable_others | s,
 recv_oracle | s, (bound_notification p s) (thread_cnode p s),
 λch. ntfn_status | s (thread_cnode p s) ch
)

sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{\lambda s. P\ s\}\} \text{seL4_Recv} \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$ ✓ “Nonblocking”
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$ Blocking

Process B

$\{\{\lambda s. P'\ s\}\} \text{seL4_Signal} \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$ call_kernel
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$ Blocking
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$ Unblock

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

```
call_kernel ev ≡ do
  handle_event ev ...; ←
  schedule;
  activate_thread } we'll come back to this
od
```

ks_of p s = (**Abstract Model state**
 thread_cnode | s,
 bound_notification | s, } cap state, thread init!
 mapped_writable | s,
 not_writable_others | s, } memory mappings!
 recv_oracle | s, (bound_notification p s) (thread_cnode p s),
 λch. ntfn_status | s (thread_cnode p s) ch)

sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{\lambda s. P\ s\}\} \text{seL4_Recv } \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$ ✓ “Nonblocking”
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$ ✓ Blocking

Process B

$\{\{\lambda s. P'\ s\}\} \text{seL4_Signal } \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$ call_kernel
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$ Blocking
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$ Unblock

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

```
call_kernel ev ≡ do
  handle_event ev ...; ←
  schedule;
  activate_thread } we'll come back to this
od
```

ks_of p s = (**Abstract Model state**
 thread_cnode | s,
 bound_notification | s, } cap state, thread init!
 mapped_writable | s,
 not_writable_others | s, } memory mappings!
 recv_oracle | s, (bound_notification p s) (thread_cnode p s),
 λch. ntfn_status | s (thread_cnode p s) ch
)

sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{ \lambda s. P s \} \} \text{seL4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$ ✓ “Nonblocking”
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$ ✓ Blocking

Process B

$\{\{ \lambda s. P' s \} \} \text{seL4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$ send_signal
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$ ⚡ Unblocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

call_kernel ev ≡ do
 handle_event ev ...; ←
 schedule;
 activate_thread } we'll come back to this
 od

ks_of p s = (**Abstract Model state**
 thread_cnode | s,
 bound_notification | s, } cap state, thread init!
 mapped_writable | s, } memory mappings!
 not_writable_others | s,
 recv_oracle | s, (bound_notification p s) (thread_cnode p s),
 λch. ntfn_status | s (thread_cnode p s) ch)

sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{ \lambda s. P s \} \} \text{seL4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$
 handle_recv
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$

“Nonblocking”
✓ Blocking

Process B

$\{\{ \lambda s. P' s \} \} \text{seL4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$
 send_signal
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$

Blocking
█ Unblocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

call_kernel ev ≡ do
 $\text{handle_event ev ...;}$
 schedule;
 activate_thread } we'll come back to this
od

Abstract Model state

```

ks_of p s = (
  thread_cnode | s,
  bound_notification | s,
  mapped_writable | s,
  not_writable_others | s,
  recv_oracle | s (bound_notification p s) (thread_cnode p s),
  λch. ntfn_status | s (thread_cnode p s) ch
)

```

sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{\lambda s. P\ s\}\} \text{seL4_Recv } \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$ handle_recv
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$ Blocking

Process B

$\{\{\lambda s. P'\ s\}\} \text{seL4_Signal } \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$ send_signal
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$ Unblocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

What we proved:

ks_of p s = ()
 thread_cnode p s,
 bound_notification p s, } cap state, thread init!
 mapped_writable p s,
 not_writable_others p s, } memory mappings!
 recv_oracle s (bound_notification p s) (thread_cnode p s),
 lch. ntnf_status s (thread_cnode p s) ch

sel4 What we've done

- Defined state projections
- Verifying Hoare triples on calls

Read:
 ks_of = "kernel state of"

Process A

$\{\{\lambda s. P\ s\}\} \text{seL4_Recv} \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$ ✓ "Nonblocking"
 handle_recv
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$ ✓ Blocking

Process B

$\{\{\lambda s. P'\ s\}\} \text{seL4_Signal} \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$ send_signal
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$ ✓ Blocking
 $\hat{\text{Un}}\text{Blocking}$

seL4 Microkit Library

syscall (i.e. *kernel-userland*) interface

seL4 OS Microkernel Abstract Model

What we proved:

- More precise cap lookup lemmas

$\text{ks_of } p\ s = \{$
 $\text{thread_cnode } p\ s,$
 $\text{bound_notification } p\ s,$ } cap state, thread init!
 $\text{mapped_writable } p\ s,$
 $\text{not_writable_others } p\ s,$ } memory mappings!
 $\text{recv_oracle } s (\text{bound_notification } p\ s) (\text{thread_cnode } p\ s),$
 $\lambda \text{ch. ntfn_status } s (\text{thread_cnode } p\ s) \text{ ch}$
 ⌞



sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{\lambda s. P\ s\}\} \text{seL4_Recv } \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$ "Nonblocking"
 $\{\{\lambda s. \text{handle_recv}\}$
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$ Blocking

Process B

$\{\{\lambda s. P'\ s\}\} \text{seL4_Signal } \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$ Blocking
 $\{\{\lambda s. \text{send_signal}\}$
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$ Unblocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

What we proved:

- More precise cap lookup lemmas
- handle_recv, as required:
 - **does not modify** most ks_of fields

ks_of p s = {
 $\text{thread_cnode } p\ s,$
 $\text{bound_notification } p\ s,$ } cap state, thread init!
 $\text{mapped_writable } p\ s,$
 $\text{not_writable_others } p\ s,$ } memory mappings!
 $\text{recv_oracle } s \ (\text{bound_notification } p\ s) \ (\text{thread_cnode } p\ s),$
 $\lambda \text{ch. ntfn_status } s \ (\text{thread_cnode } p\ s) \ \text{ch}$

sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{ \lambda s. P s \} \} \text{ sel4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (\text{ks_of } A s) \} \}$ ✓ “Nonblocking”
 handle_recv
 $\{\{ \lambda s. Q (\text{ks_of } A s) \} \}$ ✓ Blocking

Process B

$\{\{ \lambda s. P' s \} \} \text{ sel4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (\text{ks_of } B s) \} \}$ send_signal
 $\{\{ \lambda s. Q' (\text{ks_of } B s) \} \}$ ⚡ Unblocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

What we proved:

- More precise cap lookup lemmas
- handle_recv, as required:
 - **does not modify** most ks_of fields
 - returns **recv_oracle**-“predicted” badge in “Nonblocking” case
 - updates **ntfn_status** in Blocking case

ks_of p s = {
 $\text{thread_cnode } p s,$
 $\text{bound_notification } p s,$ } cap state, thread init!
 $\text{mapped_writable } p s,$
 $\text{not_writable_others } p s,$ } memory mappings!
recv_oracle s (bound_notification p s) (thread_cnode p s),
 $\lambda \text{ch. ntnf_status } s (\text{thread_cnode } p s) \text{ ch}$

sel4 What we've done



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{\lambda s. P\ s\}\} \text{seL4_Recv} \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$ ✓ “Nonblocking”
 handle_recv
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$ ✓ Blocking

Process B

$\{\{\lambda s. P'\ s\}\} \text{seL4_Signal} \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$ send_signal
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$ Blocking ✓ Unblocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

What we proved:

- More precise cap lookup lemmas
- handle_recv, as required:
 - **does not modify** most ks_of fields
 - returns **recv_oracle**-“predicted” badge in “Nonblocking” case
 - updates **ntfn_status** in Blocking case
- Lifting helpers for state projections

Read:
 ks_of = “kernel state of”

$\text{ks_of}\ p\ s = \{$

$\text{thread_cnode}\ p\ s,$ } **cap state, thread init!**
 $\text{bound_notification}\ p\ s,$ } **memory mappings!**
 $\text{mapped_writable}\ p\ s,$ }
 $\text{not_writable_others}\ p\ s,$ }
 $\text{recv_oracle}\ s\ (\text{bound_notification}\ p\ s)\ (\text{thread_cnode}\ p\ s),$
 $\lambda\text{ch. ntnf_status}\ s\ (\text{thread_cnode}\ p\ s)\ \text{ch}$

• sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{ \lambda s. P s \} \} \text{sel4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (ks_of A s) \} \}$
handle_recv
 $\{\{ \lambda s. Q (ks_of A s) \} \}$

✓ “Nonblocking”
✓ Blocking

Process B

$\{\{ \lambda s. P' s \} \} \text{sel4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (ks_of B s) \} \}$
send_signal
 $\{\{ \lambda s. Q' (ks_of B s) \} \}$

Blocking
█ Unblocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

- Proving & generalising their composition

• sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{ \lambda s. P s \} \} \text{sel4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (ks_of A s) \} \}$
handle_recv
 $\{\{ \lambda s. Q (ks_of A s) \} \}$

“Nonblocking”
Blocking

Process B

$\{\{ \lambda s. P' s \} \} \text{sel4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (ks_of B s) \} \}$
send_signal
 $\{\{ \lambda s. Q' (ks_of B s) \} \}$

Blocking
Unblocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

- Proving & generalising their composition

sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{\lambda s. P\ s\}\} \text{sel4_Recv } \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$
handle_recv
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$

“Nonblocking”
Blocking

Process B

$\{\{\lambda s. P'\ s\}\} \text{sel4_Signal } \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$
send_signal
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$

Blocking
Unblocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

- Proving & generalising their composition

$\{\{\lambda s. P\ s\}\}$
`sel4_SomeCall`
 $\{\{\lambda s. Q\ s\}\}$

sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{ \lambda s. P s \} \} \text{ sel4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (ks_of A s) \} \}$
handle_recv
 $\{\{ \lambda s. Q (ks_of A s) \} \}$

“Nonblocking”
Blocking

Process B

$\{\{ \lambda s. P' s \} \} \text{ sel4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (ks_of B s) \} \}$
send_signal
 $\{\{ \lambda s. Q' (ks_of B s) \} \}$

Blocking
Unlocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

Read:
ks_of = “kernel state of”

- Proving & generalising their composition

$\{\{ \lambda s. P s \} \}$
sel4_SomeCall
 $\{\{ \lambda s. Q s \} \}$

Blocking A

sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{ \lambda s. P s \} \} \text{ sel4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (ks_of A s) \} \}$
handle_recv
 $\{\{ \lambda s. Q (ks_of A s) \} \}$

“Nonblocking”
Blocking

Process B

$\{\{ \lambda s. P' s \} \} \text{ sel4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (ks_of B s) \} \}$
send_signal
 $\{\{ \lambda s. Q' (ks_of B s) \} \}$

Blocking
Unlocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

Read:
ks_of = “kernel state of”

- Proving & generalising their composition

$\{\{ \lambda s. P s \} \}$
sel4_SomeCall
 $\{\{ \lambda s. Q s \} \}$

Blocking A

Unlocking B

sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{ \lambda s. P s \} \} \text{ sel4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (ks_of A s) \} \}$
handle_recv
 $\{\{ \lambda s. Q (ks_of A s) \} \}$

“Nonblocking”
Blocking

Process B

$\{\{ \lambda s. P' s \} \} \text{ sel4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (ks_of B s) \} \}$
send_signal
 $\{\{ \lambda s. Q' (ks_of B s) \} \}$

Blocking
Unlocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

Read:
ks_of = “kernel state of”

- Proving & generalising their composition

$\{\{ \lambda s. P s \} \}$
sel4_SomeCall
 $\{\{ \lambda s. Q s \} \}$

Blocking A



Unblocking B

sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{ \lambda s. P s \} \} \text{ sel4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (ks_of A s) \} \}$ handle_recv
 $\{\{ \lambda s. Q (ks_of A s) \} \}$

“Nonblocking”
 ✓ Blocking

Process B

$\{\{ \lambda s. P' s \} \} \text{ sel4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (ks_of B s) \} \}$ send_signal
 $\{\{ \lambda s. Q' (ks_of B s) \} \}$

syscall (i.e. *kernel-userland*) interface

Blocking
 Blocking

Unblocking

sel4 Microkit Library

sel4 OS Microkernel Abstract Model

- Proving & generalising their composition

$\{\{ \lambda s. P s \} \}$
 sel4_SomeCall
 $\{\{ \lambda s. Q s \} \}$

Blocking A

⚡⚡
 C, D, E ... X, Y, Z
 Irrelevant

Unblocking B

sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Process A

$\{\{ \lambda s. P s \} \} \text{ sel4_Recv } \{\{ \lambda s. Q s \} \}$

$\{\{ \lambda s. P (ks_of A s) \} \}$
handle_recv
 $\{\{ \lambda s. Q (ks_of A s) \} \}$

“Nonblocking”
Blocking

Process B

$\{\{ \lambda s. P' s \} \} \text{ sel4_Signal } \{\{ \lambda s. Q' s \} \}$

$\{\{ \lambda s. P' (ks_of B s) \} \}$
send_signal
 $\{\{ \lambda s. Q' (ks_of B s) \} \}$

Blocking
Unlocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel Abstract Model

Read:
ks_of = “kernel state of”

- Proving & generalising their composition

$\{\{ \lambda s. P s \} \} \rightarrow \{\{ \lambda s. P (ks_of A s) \} \}$
sel4_SomeCall Blocking A
 $\{\{ \lambda s. Q s \} \}$

C, D, E ... X, Y, Z
Irrelevant

Unblocking B

sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Read:
ks_of = "kernel state of"

Process A

$\{\{\lambda s. P\ s\}\} \text{sel4_Recv } \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$
handle_recv
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$

✓ "Nonblocking"
✓ Blocking

Process B

$\{\{\lambda s. P'\ s\}\} \text{sel4_Signal } \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$
send_signal
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$

syscall (i.e. *kernel-userland*) interface

sel4 Microkit Library

Blocking

Unblocking

sel4 OS Microkernel Abstract Model

- Proving & generalising their composition

$\{\{\lambda s. P\ s\}\} \rightarrow \{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$
seL4_SomeCall Blocking A
 $\{\{\lambda s. Q\ s\}\}$ $\{\{\lambda s. R\ (\text{ks_of } A\ s) \& \& P' (\text{ks_of } B\ s)\}\}$

⚡⚡ ⚡⚡⚡
C, D, E ... X, Y, Z
Irrelevant

Unblocking B

sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Read:
 ks_of = "kernel state of"

Process A

$\{\{\lambda s. P\ s\}\} \text{sel4_Recv } \{\{\lambda s. Q\ s\}\}$

$\{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$
 handle_recv
 $\{\{\lambda s. Q\ (\text{ks_of } A\ s)\}\}$

✓ "Nonblocking"
 ✓ Blocking

Process B

$\{\{\lambda s. P'\ s\}\} \text{sel4_Signal } \{\{\lambda s. Q'\ s\}\}$

$\{\{\lambda s. P'\ (\text{ks_of } B\ s)\}\}$
 send_signal
 $\{\{\lambda s. Q'\ (\text{ks_of } B\ s)\}\}$

Blocking
 ⚡ Unblocking

sel4 Microkit Library

syscall (i.e. *kernel-userland*) interface

sel4 OS Microkernel
 Abstract Model

- Proving & generalising their composition

$\{\{\lambda s. P\ s\}\} \rightarrow \{\{\lambda s. P\ (\text{ks_of } A\ s)\}\}$
 seL4_SomeCall Blocking A
 $\{\{\lambda s. Q\ s\}\}$ $\{\{\lambda s. R\ (\text{ks_of } A\ s) \&& P'\ (\text{ks_of } B\ s)\}\}$

⚡⚡ ⚡⚡⚡
 C, D, E ... X, Y, Z
 Irrelevant

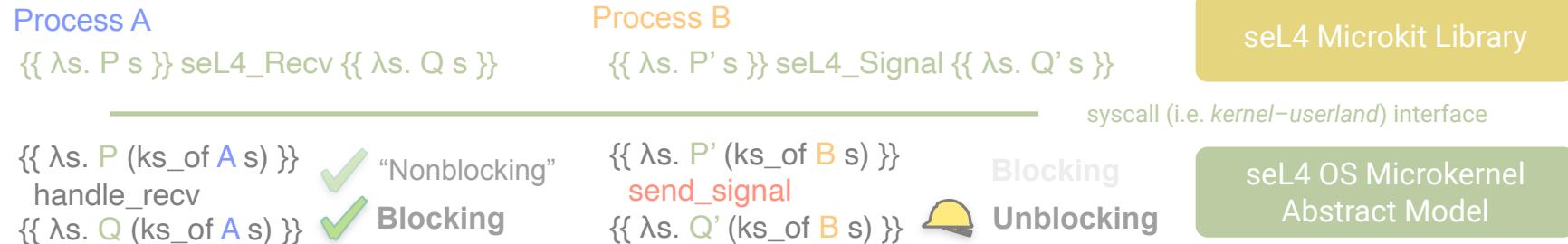
$\{\{\lambda s. R\ (\text{ks_of } A\ s) \&& P'\ (\text{ks_of } B\ s)\}\}$
 Unblocking B

sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

Read:
 ks_of = "kernel state of"



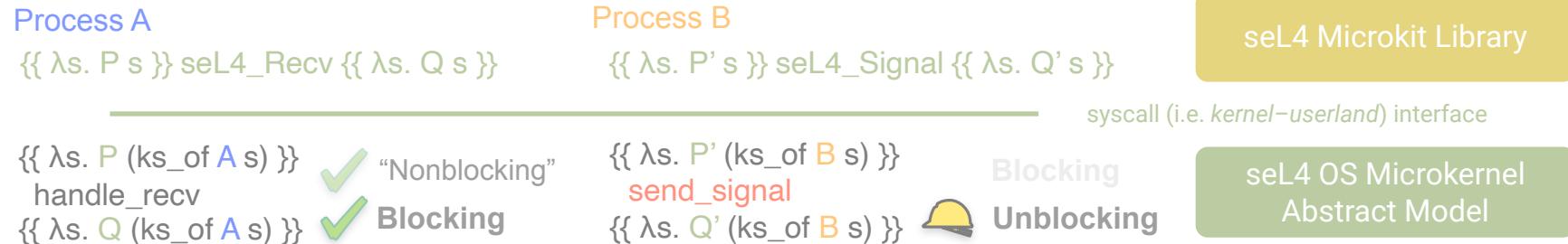
- Proving & generalising their composition



sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls



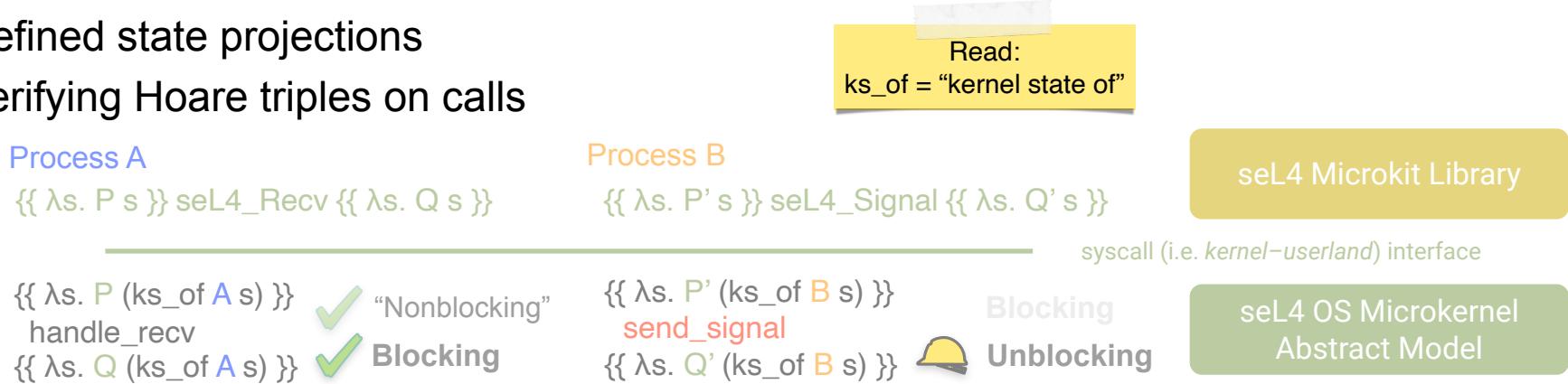
- Proving & generalising their composition



sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls



- Proving & generalising their composition

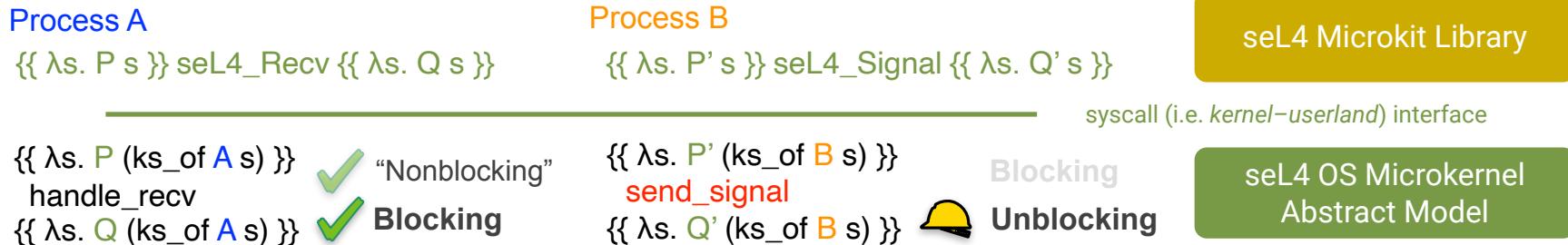


sel4 What we've done & plan to do



- Defined state projections
- Verifying Hoare triples on calls

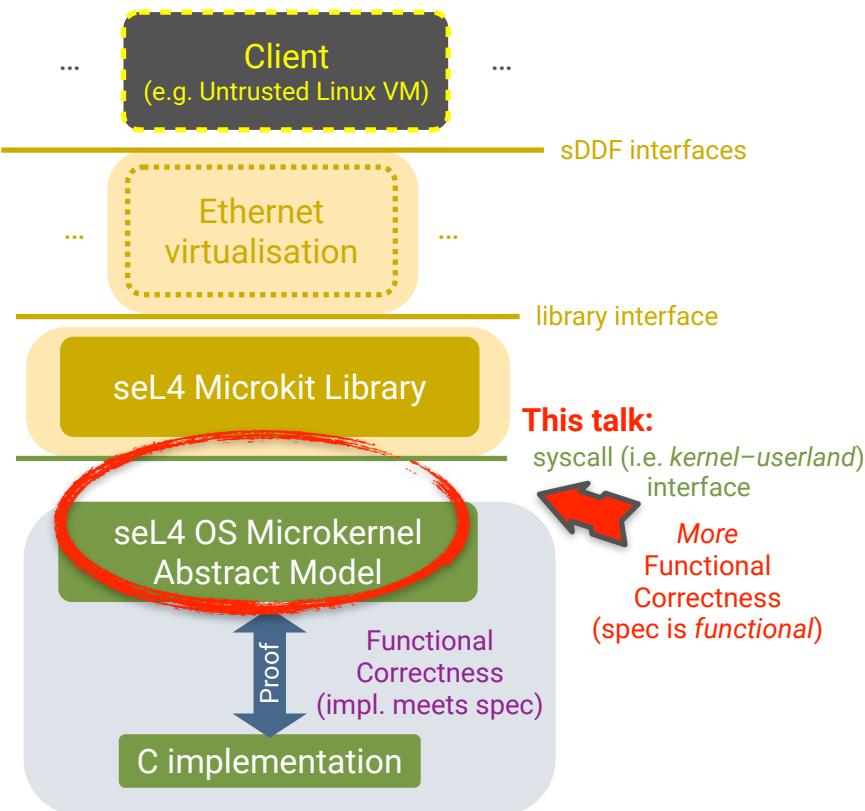
Read:
ks_of = "kernel state of"



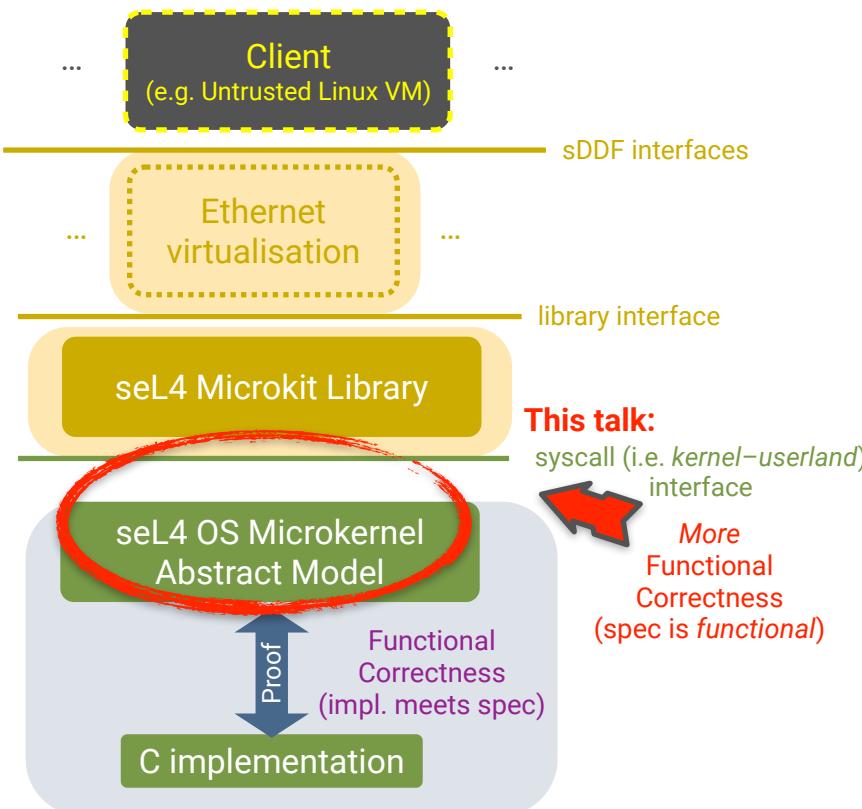
- Proving & generalising their composition



seL4 Towards kernel–userland functional proofs

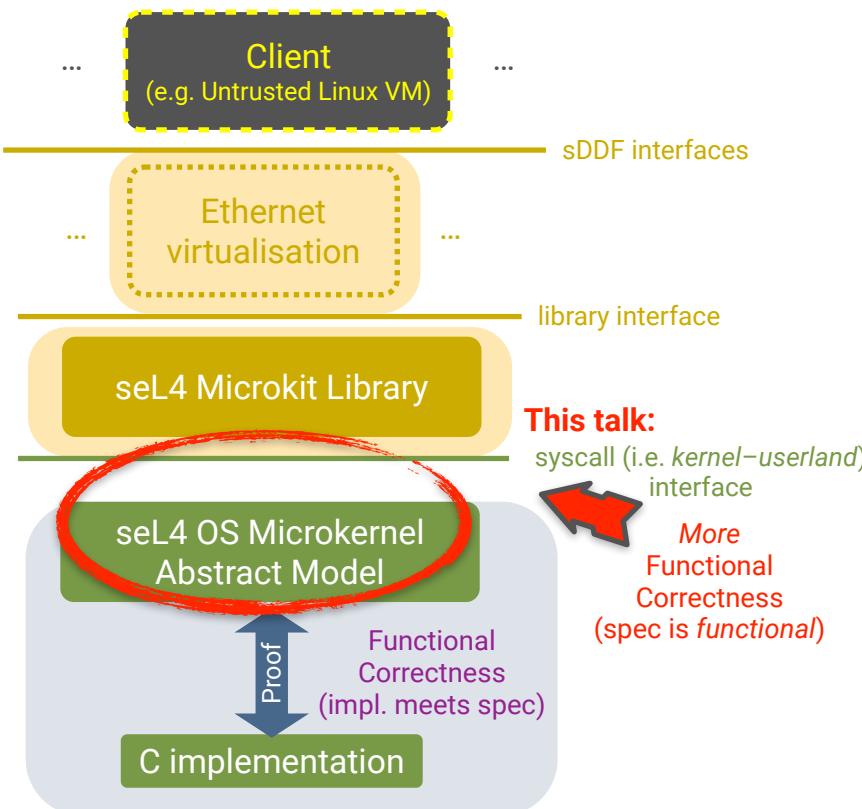


• sel4 Towards kernel–userland functional proofs



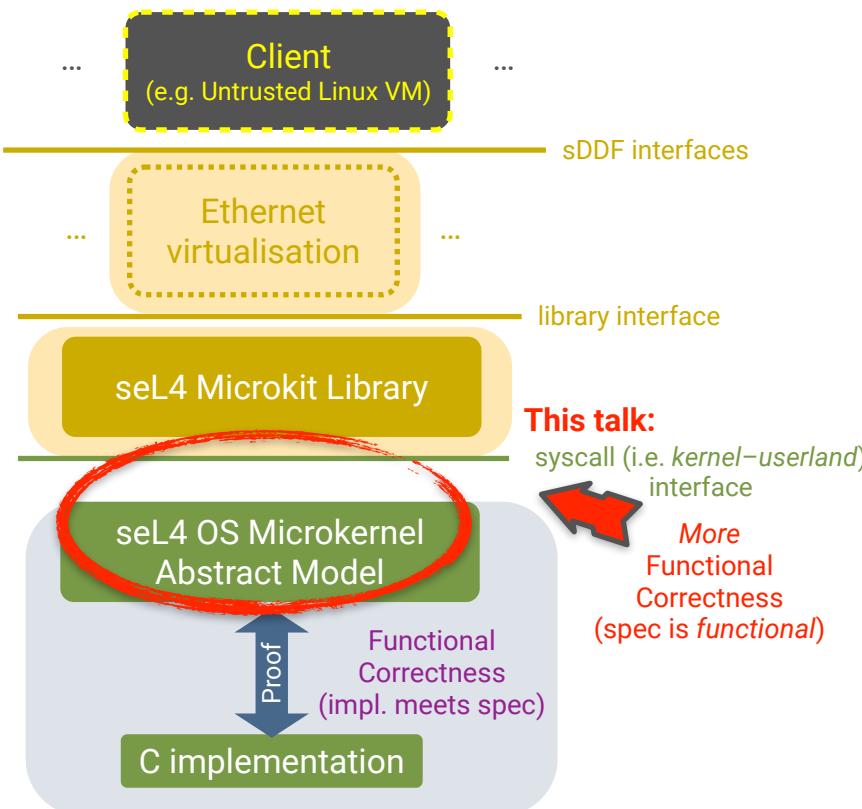
- Microkit assumes syscall **functional specs** as Hoare triples
- We **need to prove sel4's Abstract Model satisfies them!** (Then **we'll know its C implementation does, too.**)
- We handwave some register marshalling (for now)
- Blocking syscalls may require Hoare triples for up to $2 + n$ kernel entries (finite n):
 - 1 **Blocking** call (e.g. Recv)
 - n **Irrelevant** calls or interrupts
 - 1 **Unblocking** call (e.g. Signal)
- **Verifying syscalls like these is an open problem, but:**

• sel4 Towards kernel–userland functional proofs



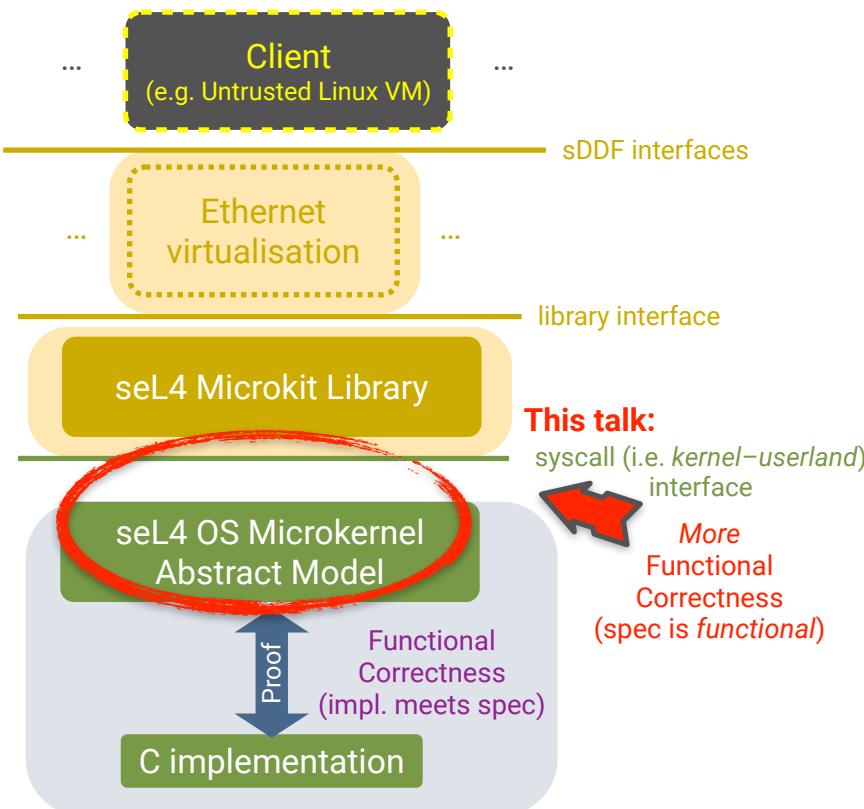
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 - 1 **Blocking** call (e.g. Recv)
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 - 1 **Unblocking** call (e.g. Signal)
- **Verifying syscalls like these is an open problem, but:**
 - We're verifying their constituent triples

• sel4 Towards kernel–userland functional proofs



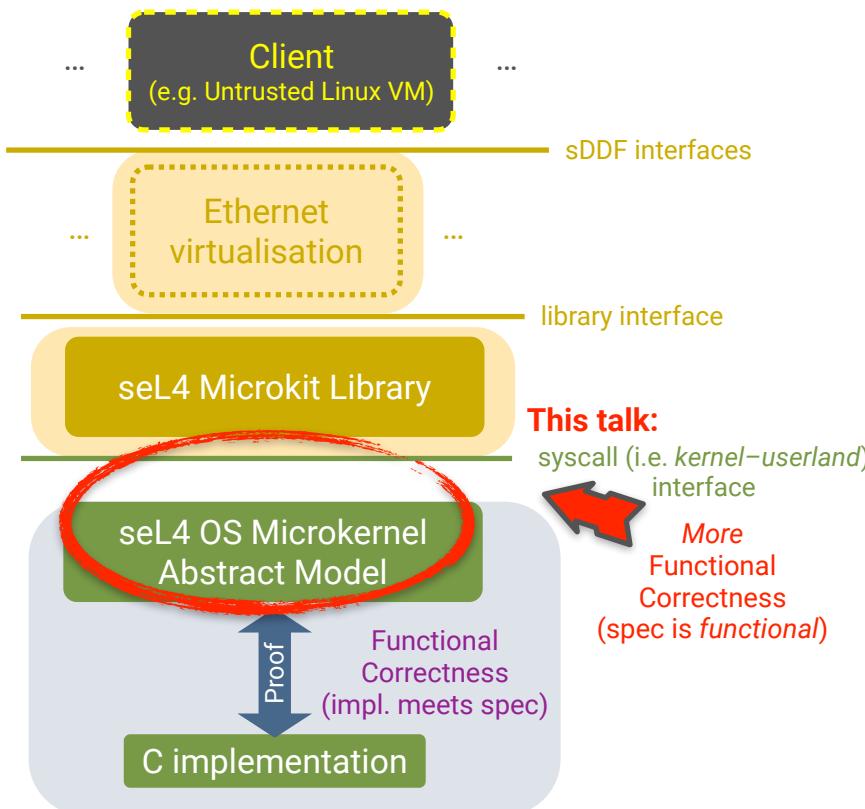
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 - 1 **Blocking** call (e.g. Recv)
 - n **Irrelevant** calls or interrupts
 - 1 **Unblocking** call (e.g. Signal)
- Verifying syscalls like these is **an open problem, but:**
 - We're verifying their constituent triples
 - We're generalising their composition

• sel4 Towards kernel–userland functional proofs



- Microkit assumes syscall **functional specs** as Hoare triples
- We **need to prove sel4's Abstract Model satisfies them!** (Then **we'll know its C implementation does, too.**)
- We handwave some register marshalling (for now)
- Blocking syscalls may require Hoare triples for up to $2 + n$ kernel entries (finite n):
 - 1 **Blocking** call (e.g. Recv)
 - n **Irrelevant** calls or interrupts
 - 1 **Unblocking** call (e.g. Signal)
- Verifying syscalls like these is **an open problem, but:**
 - We're verifying their constituent triples
 - We're generalising their composition
 - Microkit's strict requirements help us here

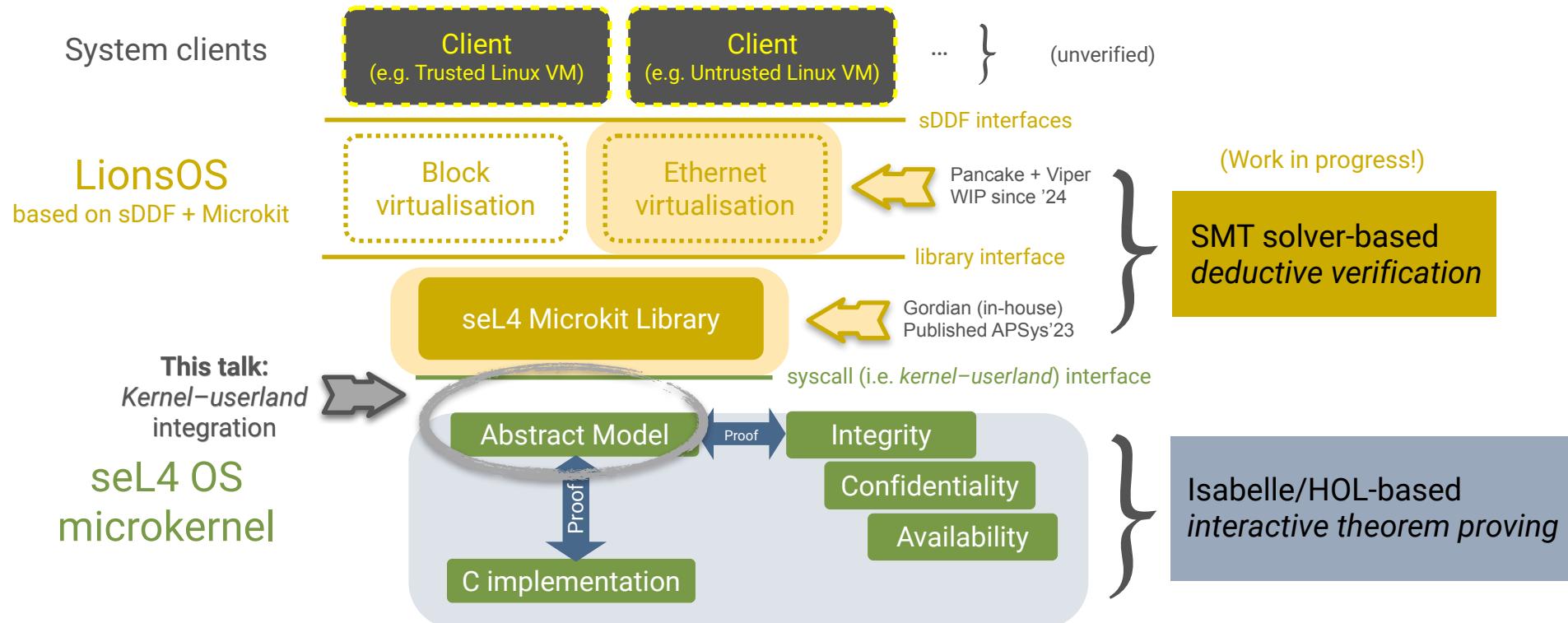
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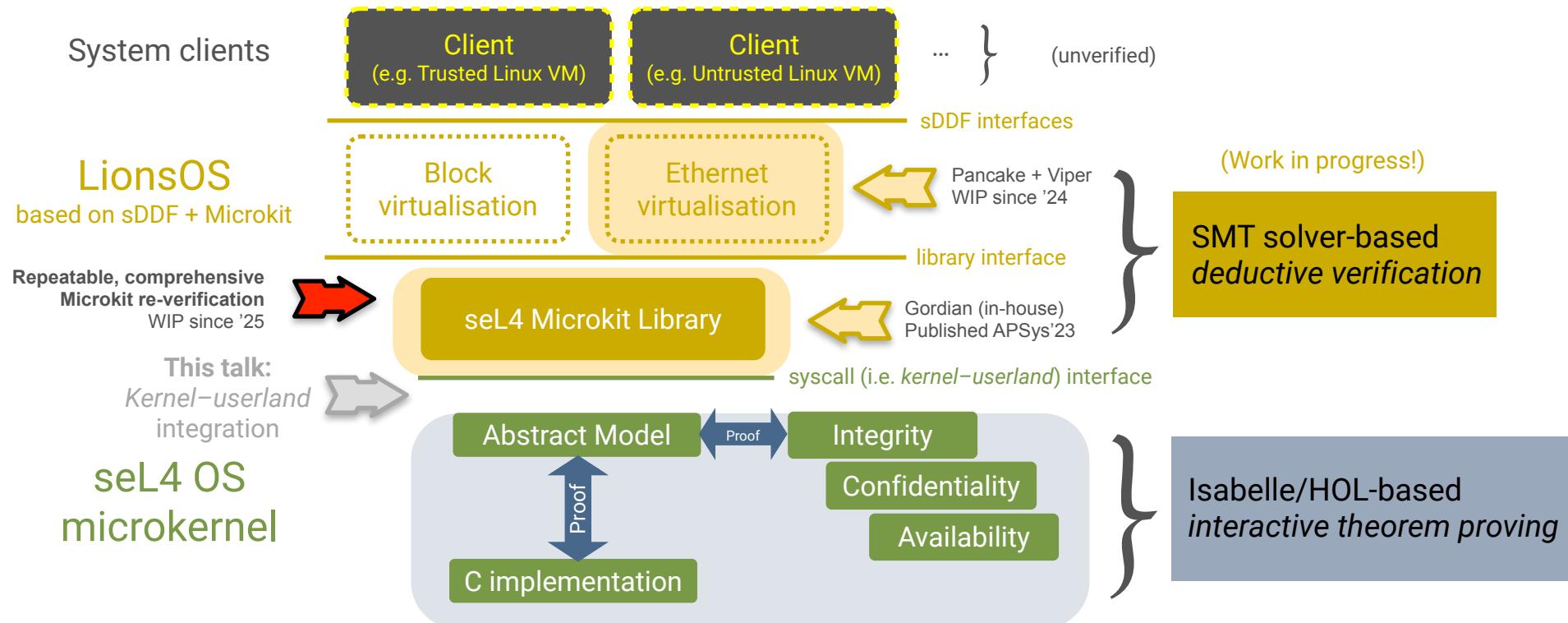


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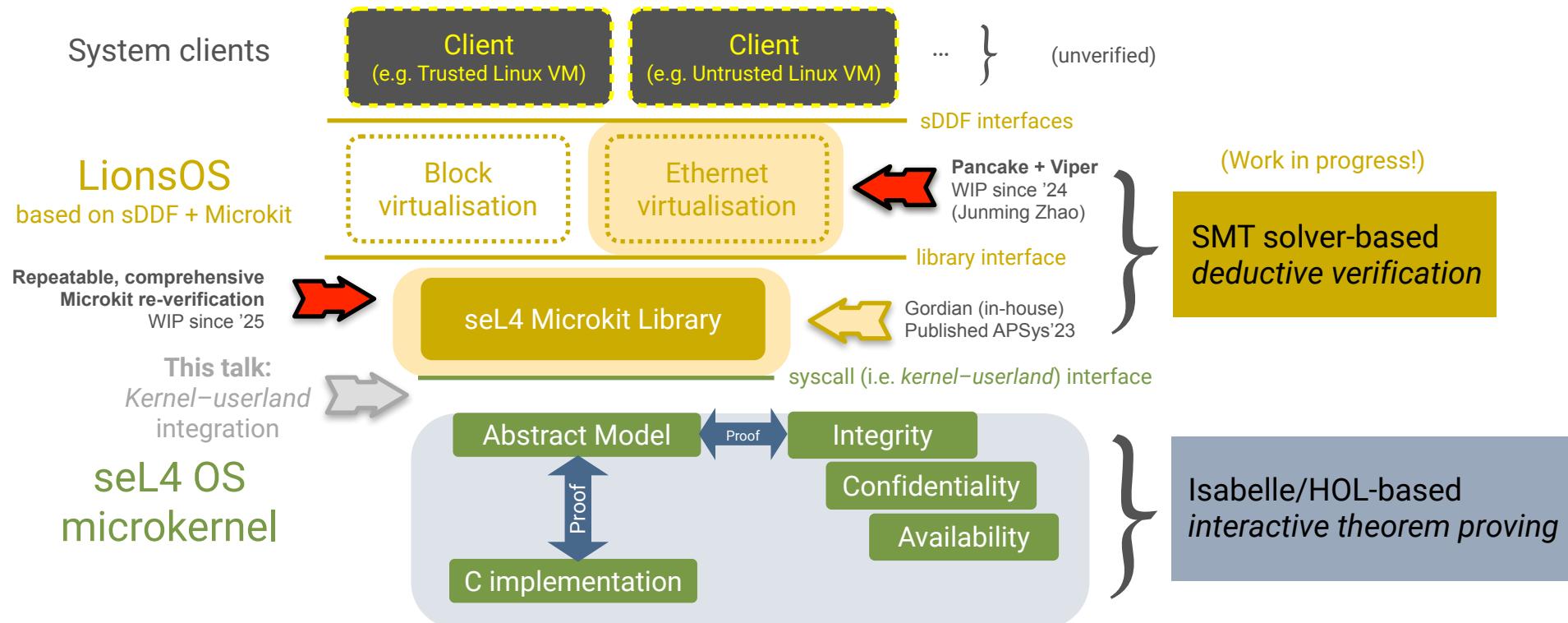


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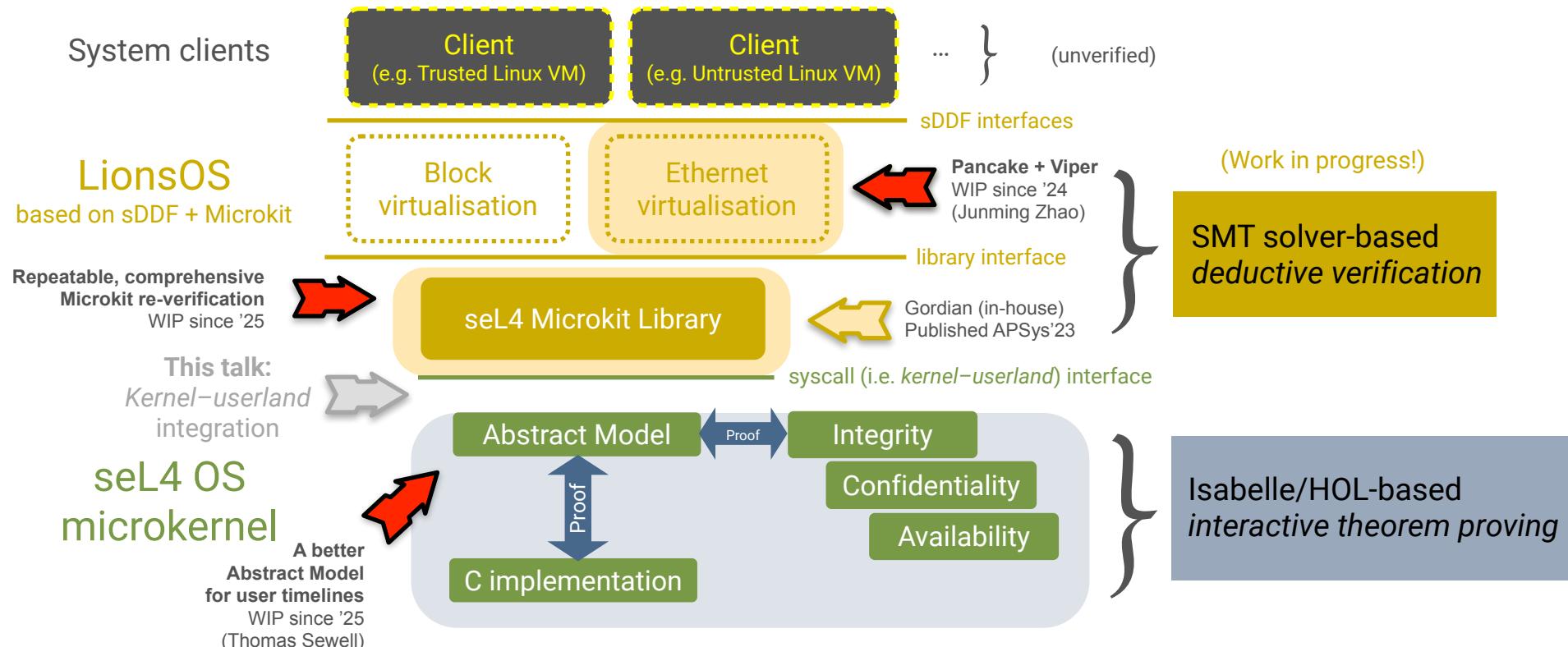


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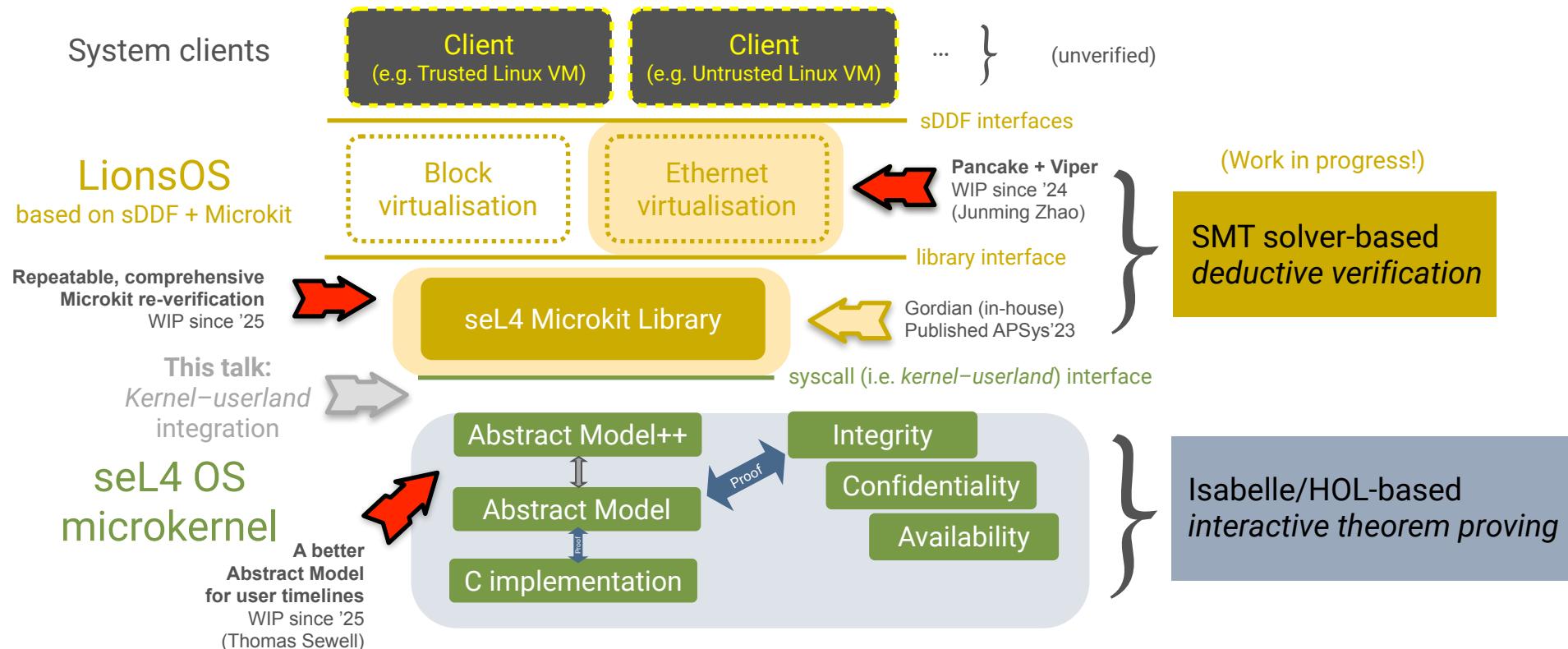


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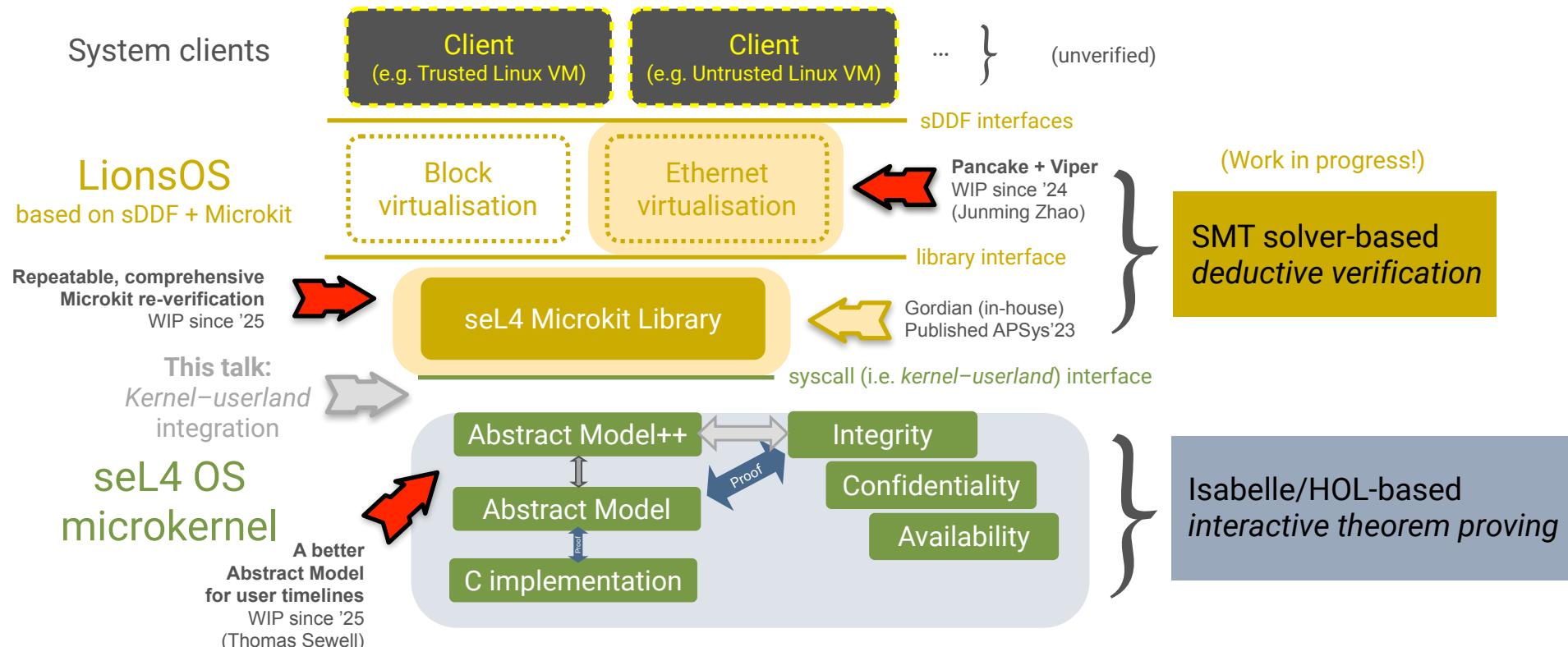


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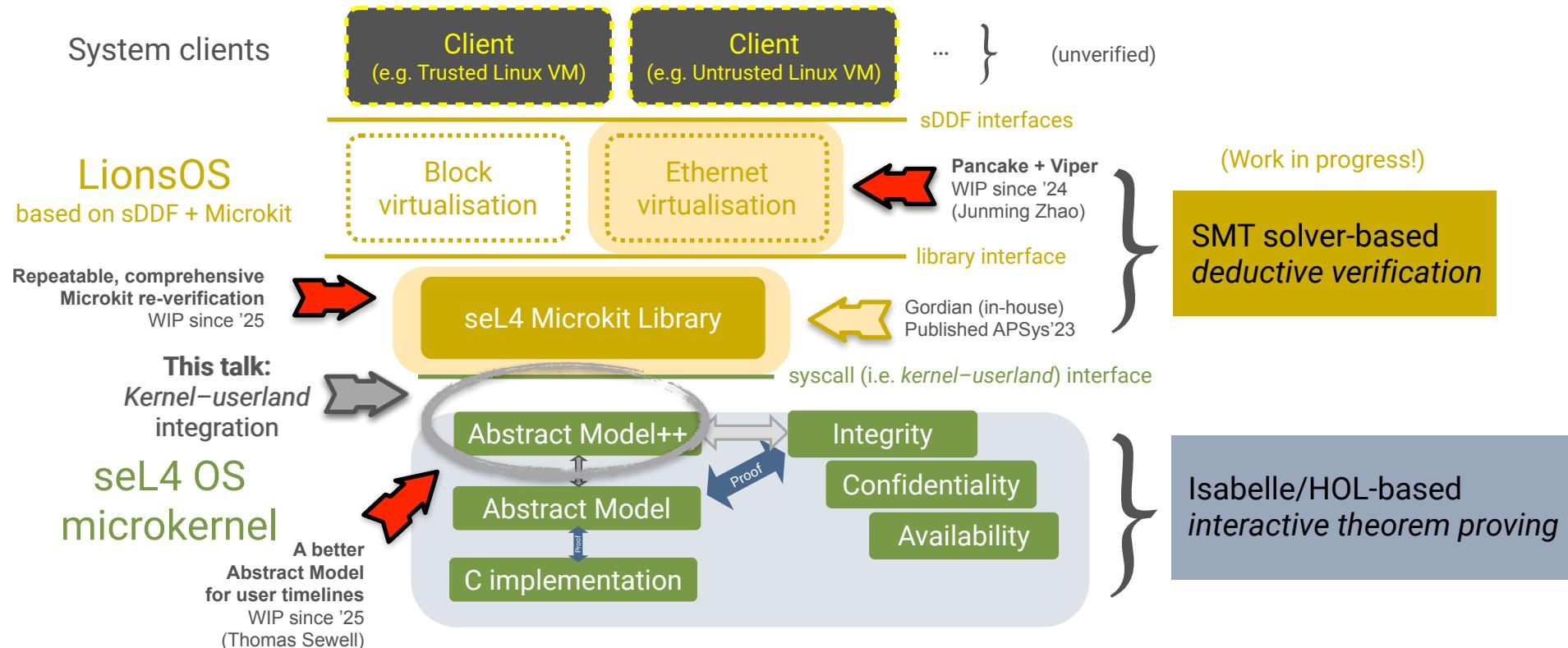


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