

Homework 2

- All homework must be turned in on PDF format. This can be scanned or typed in any paper size, but the format must be PDF and the file must be readable. This document can be modified for your homework submission. An additional homework template is available on Canvas to assist you in creating your answers, and content from lecture notes can be used.
- All final answers must be circled or in green.
- All homework must have a name on the top of **every** page.
- Submission errors (not in PDF, illegible, etc.) will not be re-graded.

Problem 1

Convert the following decimal (base-10) numbers into **binary** (base-2). Results should be accurate to within 0.01_{10} .

1. Convert -121.625_{10} into hexadecimal.
2. Convert -121_7 into hexadecimal (hint: go through base 10). Problem 2

① -121.625_{10}

$$\begin{array}{r}
 121 \\
 \underline{64} \\
 57 \\
 \underline{32} \\
 25 \\
 \underline{16} \\
 9 \\
 \underline{8} \\
 1 \\
 \underline{0}
 \end{array}$$

$$\begin{array}{r}
 0.625 \\
 \underline{0.5} \quad 2^1 \\
 0.125 \\
 \underline{0.125} \quad 2^3 \\
 0
 \end{array}$$

$$\Rightarrow -121.625 = -1111001.101_2$$

$$\Rightarrow -1111001.101_2$$

$$\Rightarrow -79. A_{16}$$

$$(2) -121_9 \Rightarrow -(x_9^0 + 2x_9^1 + 1x_9^2) = -(1 + 14 + 49)_{10} = -64_{10}$$

$$-64_{10} \Rightarrow -1006000_2 \Rightarrow -40_{16}$$

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Perform the following arithmetic problems.

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1. $143_7 + 153_7$ (perform the operation and express your answer in base-7).
2. $1AE_{16} - 2F3_{16}$ (perform the operation and express your answer in base-16).
3. $10110111_2 \times 10010001_2$ (perform the operation and express your answer in base-2).

① $143_7 + 153_7$

$$\begin{array}{r} 1 \\ 143 \\ + 153 \\ \hline 326 \end{array} \Rightarrow 326_7$$

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② $1AE_{16} - 2F3_{16}$

$$\begin{array}{r} 1 \\ 2F3 \\ - 1AE \\ \hline 145 \end{array} \Rightarrow -145_{16}$$

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③ $10110111_2 \times 10010001_2$

$$\begin{array}{r} \Rightarrow 10110111 \\ \times 10010001 \\ \hline 10110111 \\ 00000000 \\ 00000000 \\ 10110111 \\ 00000000 \\ \hline 11001111010011 \end{array} \Rightarrow 11001111010011_2$$

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Problem 3

Give the **base-2, 8-bit signed magnitude**, and **8-bit 2's complement** representation of the following numbers. Note any irregularities in your answer and work.

1. 0_{10}
2. 128_{10}
3. -128_{10}
4. 127_{10}
5. -127_{10}
6. -52_{10}

① $0_{10} \rightarrow 0_2$

00000000_2

2's Comp.
 $11111111_2 + 00000001_2$
 $\rightarrow 00000000_2$
 overflow

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② $128_{10} \rightarrow 2^7 = 10000000_2$

10000000_2

2's Comp.
 $01111111_2 + 00000001_2$
 $\rightarrow 10000000_2$ overflow

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③ $-128_{10} = -2^7 = -10000000_2$

10000000_2

2's Comp.
 $01111111_2 + 00000001_2$
 $\rightarrow 10000000_2$

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④ 127_{10}

11111111_2

2's Comp.
 01111111_2

127
64
63
32
31
16
15
8
7
4
3
2
1
0

127

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⑤ -127_{10}

127
64
63
32
31
16
8
4
2
1
0

-1111111_2

$\Rightarrow 0111111_2$

2's comp

$1000000_2 + 0000001_2$

$\Rightarrow 1000001_2$

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⑥ -52

52
32
20
16
4
0

-110100_2

$\Rightarrow 00110100_2$

2's Comp

$11001011_2 + 00000001_2$

Invert

$\Rightarrow 11001100_2$

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