# Dynamic Scheduling of Workflow for Makespan and Robustness improvement in the IaaS Cloud

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**SUMMARY**      The Infrastructure-as-a-Service (IaaS) cloud is attracting applications due to the scalability, dynamic resource provision, and pay-as-you-go cost model. Scheduling scientific workflow in the IaaS cloud is faced with uncertainties like resource performance variations and unknown failures. A schedule is said to be robust if it is able to absorb some degree of the uncertainties during the workflow execution. In this paper, we propose a novel workflow scheduling algorithm called Dynamic Earliest-Finish-Time (DEFT) in the IaaS cloud improving both makespan and robustness. DEFT is a dynamic scheduling containing a set of list scheduling loops invoked when some tasks complete successfully and release resources. In each loop, unscheduled tasks are ranked, a best virtual machine (VM) with minimum estimated earliest finish time for each task is selected. A task is scheduled only when all its parents complete, and the selected best VM is ready. Intermediate data is sent from the finished task to each of its child and the selected best VM before the child is scheduled. Experiments show that DEFT can produce shorter makespans with larger robustness than existing typical list and dynamic scheduling algorithms in the IaaS cloud.
*key words:   dynamic workflow scheduling, the IaaS cloud, makespan, robustness*

## 1.   Introduction

Over the decades, cloud computing has emerged as a new distributed computing system due to features like application scalability, heterogeneous resources, dynamic resource provisioning, and pay-as-you-go cost model. In the IaaS model of cloud computing, resources are provided in the form of VMs, which are dynamically managed, monitored, maintained, and governed by market principles. Applications can benefit from virtually unlimited resources with minimum hardware investment. As a result, scientific workflows, which are usually modeled as Directed Acyclic Graphs (DAG) with data dependencies among tasks and present applications of high throughput, computation, and complex large scale data analysis, are increasingly adopting cloud computing.

Workflow scheduling is regarded as one of the major challenges in scientific workflow management in the IaaS cloud. Scheduling is defined as mapping tasks to the computing resources by optimizing performance metrics such as execution time and cost [1]. Problem of workflow scheduling usually is NP-hard. Various heuristic and meta-heuristic approaches have been developed to solve the workflow scheduling in the heterogeneous computing system, Grids, and Cloud [1]–[4]. The majority of these approaches can pro-

duce good schedules given that the state of resources is static. However, in the IaaS cloud, there are uncertainties a scheduler needs to deal with. Resource performance variations affect the overall workflow performances. If a resource slows down, the tasks scheduled and queued on that resource have to wait to be executed, consequently impact the start time of other dependent tasks and increase the overall makespan. Failures caused by hardware failures, software failures, interferences between cohosted VMs [5], etc. are also inevitable in such large complex distributed systems and may affect the overall workflow performances. Dynamic scheduling can deal with the uncertainties by scheduling a task only when it becomes ready, namely, when all the tasks that the current task depends upon have completed their execution. It considers runtime state of the system and is adaptive in nature.

In this paper, we present a dynamic workflow scheduling algorithm in the IaaS cloud, called Dynamic Earliest-Finish-Time (DEFT). DEFT contains a set of list scheduling loops, which are invoked when some tasks complete and release resources. In each loop, the unscheduled tasks are sorted, a VM with minimum estimated earliest finish time is selected for each unscheduled task. Ready tasks are scheduled, while other tasks keep the VM selection records, and intermediate data is sent from finished tasks to their children according to the task-VM record. Coefficient of Variation (CV) is used in this paper for the robustness to measure how DEFT will schedule workflows with stable makespans in the IaaS cloud with uncertainties. Experiment results show that DEFT not only minimizes the workflow makespans but also produces schedules with larger robustness against uncertainties in the IaaS cloud.

The remainder structure of the paper is as follows. Section 2 discusses the related work. Section 3 describes the models of the system, problem definitions and attributes, and the measurement of robustness. Section 4 presents the details of DEFT, discusses the complexity of the algorithm, and illustrates the algorithm with an example. The simulation results will be presented in Section 5. And section 6 gives the conclusion and future work.

## 2.   Related work

The DAG-based workflow scheduling problem keeps evolving with computational platforms, from the age of homogeneous systems, to heterogeneous systems, Grids, and Cloud [7]. Due to its NP-hard nature, most of algorithms are

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heuristic based and can be classified into three categories: list algorithms, clustering algorithms and task duplication based algorithms. List scheduling algorithms are generally preferred since they generate good quality schedules with less complexity [7]. HEFT (Heterogeneous Earliest Finish Time) [6], CPOP (Critical Path on a Processor) [6], PETS (low complexity Performance Effective Task Scheduling) [7], HCPT (Heterogeneous Critical Parent Trees) [8], HPS (High-Performance task Scheduling) [9], Lookahead [10], SDBATS (Standard Deviation-Based Algorithm for Task Scheduling) [11], and PEFT (Predict Earliest Finish Time algorithm) [12] are typical list algorithms. HEFT, CPOP, HCPT, SDBATS, Lookahead and PEFT have two phases, including a task prioritizing phase to decide scheduling sequence of tasks, and a processor selection phase to assign a processor to each task sequentially for a minimum makespan. HPS and PETS have a level sorting phase to sort tasks into groups that can be executed in parallel before the task prioritizing and the processor selection phase. HEFT is well-known and frequently referenced with its lower time complexity, and PEFT is the latest excellent DAG scheduling algorithm with the same time complexity as HEFT. The above algorithms perform well in the static environment supposing that the resource is always available and the performance is static.

In practice, especially in dynamic IaaS cloud, such static schedulers seldom lead to good performances since the actual task execution time at runtime usually deviate a lot from their static predictions estimated before the workflow execution. Some static DAG schedulers try to deal with the unpredictability by assuming the resource computing rate or task execution time variation to follow a specific distribution. H. Arabnejad and J. Barbosa [13] model the computing rate variation of each leased VM by introducing a degradation percentage based on a normal distribution. X. Tang et al. [14] assume the processing time and the communication time to be independent and follow the exponential distribution or the normal distribution estimated by building a historic table and using statistical profiling. D. Poola et al. [15] model the task execution time variation as a normal distribution with a mean value of zero. However, it is difficult to specify analytically the exact distribution of the VM computing rate or the task execution time in the IaaS cloud. W. Zheng and R. Sakellariou [16], [17] solve the problem by using a non-analytical Monte Carlo method. The method first samples from the input space consisting of the random task execution time predictions of the given application, then generates a long list of different static schedules by employing a specific static scheduling heuristic. The schedule with minimum mean makespan of all the input samples is selected. The result of the algorithm is affected by the range of sample space, the number of samples, and the number of static schedules.

Some dynamic scheduling algorithms are developed dealing with uncertainties by scheduling or rescheduling a task in the runtime. Q. Zheng [18] proposes an offline scheduler and makes adaptations during runtime based on the current information about the task start and completion times. It alleviates the chain effect caused by task overruns by rescheduling tasks to faster resources if the predecessors are likely to increase the makespan. However, it does not reschedule tasks to faster resources for smaller makespans since the rescheduling only happens after the overruns. P-HEFT (HEFT for parallel tasks) [19] applies dynamic scheduling for a batch of jobs described DAG with different arrival times. In each scheduling loop, ready tasks of different jobs are scheduled in parallel using an adaptation of HEFT. DCP-G [20] dynamically schedules ready tasks sequentially by identifying DCP (Dynamic Critical Path) of the unscheduled tasks in each scheduling loop, and selects the resource providing the minimum execution time for the task in Grids. The problem of P-HEFT and DCP-G is, all the intermediate data that should be sent as soon as a task is finished is delayed until its child is scheduled to a resource. In DEFT, intermediate data is sent when a task completes and its child has a record of a best VM. Waiting time for intermediate data will be diminished and the overall makespan will be minimized.

There is no consensus on a good definition of robustness for a schedule. Some definitions are related to the workflow deadline. L. Boloni and D. C. Marinescu [21] define the slack of a task as the amount of time that can be delayed without delaying the deadline of the workflow and define the slack of a schedule as the sum of the slacks of all the tasks of the workflow. D. Poola et al. [15] define robustness as 1) the likelihood of the workflow to finish before the given deadline or 2) the amount of time a workflow can be delayed without violating the deadline constraint. Z. Shi et al. [22] give two definitions of robustness based on tardiness of deadline and deadline miss rate. Other definitions are related to makespan, measuring the stability of the makespan for any realization of the same schedule. L. C. Canon et al. [23] measure the robustness by scheduling tasks of a DAG to a target environment several times and computing the makespan distribution. Makespan standard deviation, makespan differential entropy [21], probabilistic that the makespan is within two bounds [24], and the worst makespan it is possible to have in 99% of cases are defined and compared based on the makespan distribution. We use the same measurement by scheduling tasks of a DAG to a target environment several times and see how stable the makespans are. However, we use CV to measure robustness that is more representative and easy to compute.

## 3. Scheduling problem formulation

This section illustrates how we model the IaaS cloud, the workflow, and the scheduling problem. Then the robustness is defined.

### 3.1 Basic models and attributes

In the IaaS cloud, resources are provided by the IaaS cloud service providers to the users in the form of VMs. The

configuration of VM differs in memory, CPU measured in million instructions per second (MIPS) and OS. When a scientific workflow is submitted to the cloud, certain type of VMs are provided as a resource pool according to the user's requirement or the workflow configuration. Performances of the network and VMs of each type are considered heterogeneous.

Scientific workflow is usually modeled as a DAG with data dependencies among tasks. The DAG of workflow is represented by $G = \{V, E\}$, where $V = \{v_1, v_2, \cdots, v_n\}$ is the set of $n$ tasks of a workflow, also called nodes in this paper, and $E = \{(v_i, v_j) \mid v_i, v_j \in V\}$ is the data dependencies between these tasks. An edge $(v_i, v_j) \in E$ shows the precedence constraint that task $v_i$ should complete its execution before task $v_j$ starts, $v_i$ is called the parent of $v_j$, donated as $parent(v_j)$, and $v_j$ is called the child of $v_i$, donated as $child(v_i)$. The task without any parent is called the entry task and the task without any child is called the exit task. All the nodes from the entry nodes to the parents of $v_i$ are the predecessors of $v_i$, and all the nodes from the children of $v_i$ to the exit nodes are the successors of $v_i$.

There are some attributes used in the workflow scheduling we will refer to in this paper.

1) Computing cost is the estimated execution time to complete a task $v_i$ on $VM_j$ at time $t$, donated as $w_{ij}^t$. Average computing cost of task $v_i$ on $M$ VMs of the requested type at time $t$ is defined as:

$$\bar{w}_i^t = \sum_{j=1}^{M} w_{ij}^t \bigg/ M = \sum_{j=1}^{M} (L_i / R_j^t) \bigg/ M \qquad (1)$$

Where $L_i$ is the length of task $v_i$ in million instructions, and the $R_j^t$ is computing rate of $VM_j$ at time $t$.

2) Communication cost $c_{ij}^t$ is the average estimated time spent on transferring intermediate data from task $v_i$ to task $v_j$ based on the network performance at time $t$, defined as:

$$c_{ij}^t = D + data_{ij} / B_{ij}^t \qquad (2)$$

Where $D$ is the average latency of data transfer and $B_{ij}^t$ is data transfer rate between $VM_i^t$ hosting task $v_i$ and $VM_j^t$ hosting task $v_j$ at time $t$, $data_{ij}$ is the amount of the intermediate data that task $v_i$ sends to task $v_j$. Note that $c_{ij}^t = 0$ if tasks $v_i$ and $v_j$ are assigned to the same VM or two VMs cohosted on the same server.

3) Makespan, which is also called schedule length in some research [6], [7], [12], of a workflow is the time span from the workflow submission to the completion of the last task of the workflow.

$$makespan = \max\{FT(n_{exit})\} - ST \qquad (3)$$

Where $ST$ is the submission time of the workflow and $FT(v_i)$ is the finish time of task $v_i$. Where there is more than one exit tasks, the makespan is the maximum finish time of all the exit tasks.

Makespan is normalized for comparison. Normalized makespan, called NSL (Normalized Schedule Length) for

short, is defined as follows:

$$NSL = makespan / L_{CP_{min}} \qquad (4)$$

$$L_{CP_{min}} = \sum_{v_i \in CP_{min}} \min_{VM_j \in VM} \{w_{ij}\}$$
$$+ \sum_{\substack{v_i \in CP_{min} \\ v_k \in CP_{min} \\ v_k \in child(v_i)}} (data_{ik} / \max_{\substack{VM_j \in VM \\ VM_l \in VM}} B_{jl}) \qquad (5)$$

$L_{CP_{min}}$ is the theoretical minimum makespan of the workflow, which is the minimum length of critical path (CP) of DAG. CP is the longest path from the entry node to the exit node. The computation cost of each task is calculated by executing it on the fastest VM, and the communication cost is calculated by setting the data transfer rate to the maximum bandwidth of the network. Real makespan cannot be shorter than $L_{CP_{min}}$, and the NSL is always larger than 1.0.

4) Earliest Start Time (EST) of task $v_i$ on $VM_j$ at time $t$ is defined as:

$$EST(v_i, VM_j; t)$$
$$= \max\{Avail_j^t, \max_{v_p \in parent(v_i)} (FT(v_p) + c_{pi}^{FT(v_p)})\} \qquad (6)$$

Where $FT(v_i)$ is the finish time of task $v_i$, and $Avail_j^t$ is the earliest time when $VM_j$ is available and ready to execute task $v_i$ from time $t$. Equation(6) means that a task starts when all its parents have finished, all the data is transferred, and the VM is ready to execute it. For the entry node $EST(v_i, VM_j; ST) = ST$, where Where $ST$ is the submission time of the workflow.

5) Data Latest Transfer Time (DLTT) is the latest time that the parent $v_p$ executed on $VM_p^t$ should send intermediate data to the child $v_i$ assigned to $VM_i^t$ at time $t$ in case of not delaying the EST of $v_i$. It is the EST of $v_i$ subtracted by the data transfer cost from $VM_p^t$ to $VM_i^t$, shown as follows:

$$DLTT(v_i, VM_i^t, v_p, VM_p^t; t) = EST(v_i, VM_i; t) - c_{pi}^t \qquad (7)$$

6) Earliest Finish Time (EFT) of task $v_i$ on $VM_j$ at time $t$ is calculated as the EST of a task $v_i$ plus the computing cost of $v_i$ on $VM_j$ at time $t$:

$$EFT(v_i, VM_j; t) = EST(v_i, VM_j; t) + w_{ij}^t \qquad (8)$$

### 3.2 Measurement of robustness

Robustness of a schedule is the stability of the makespans for any realization of the same schedule. Schedule a workflow in the dynamic IaaS cloud for $N$ times, $M_i$ is the makespan of the $i^{th}$ scheduling result, CV (Coefficient of Variations) is used to measure the robustness of the scheduler in this paper, defined as the ratio of the Standard Deviation $\sigma$ to the average makespan $\mu$:

$$CV = \frac{\sigma}{\mu}$$

$$\mu = \frac{1}{N} \sum_{i=1}^{N} M_i, \sigma = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (M_i - \mu)^2} \qquad (9)$$

CV shows the extent of variability of actual makespans in relation to the average makespan. Obviously, a smaller CV means that the makespans are more likely to be close to the average value, showing a more stable distribution of the makespans. The smaller the CV is, the more robust the scheduler is. CV performs over Standard Deviation in that it does not correlate to the average value and is easy to compute as well.

## 4. The proposed DEFT scheduling algorithm

Static scheduling has obvious shortage in the dynamic IaaS cloud with uncertainties. It schedules all the tasks on the VMs at the start of the workflow. VM computing rate and network bandwidth may change in the runtime. When a VM slows down, tasks scheduled and queued on it may be delayed, consequently impact the start time of other dependent tasks and increases the overall makespans. Failed tasks may also delay successors as well as tasks queued after the failed tasks on the same VMs. In this section, we introduce a novel scheduling algorithm for the IaaS cloud with uncertainties, called Dynamic Earliest-Finish-Time algorithm (DEFT).

### 4.1 DEFT

DEFT contains a set of loops invoked whenever some tasks complete and release VMs. DEFT is based on a heuristic that if tasks considered in each loop can gain minimum makespans based on the current computing and network performance, makespan of the whole workflow can be minimized. Each scheduling scheduling loop is list based, and contains three phases, namely, tasks prioritizing, VM selection, data transfer phase.

**Task prioritizing phase.** In each scheduling loop, unscheduled tasks are prioritized using $rank_u$. It is calculated based on the current VM computing rate and network bandwidth. $rank_u$ of task $v_i$ at time $t$, donated as $rank_u(v_i; t)$, is defined as follows:

$$rank_u(v_i; t) = \bar{w}_i^t + \max_{v_j \in child(v_i)} \left[ rank_u(v_j; t) + c_{ij}^t \right] \quad (10)$$

where $\bar{w}_i^t$ is the current average computing cost of $v_i$, and $c_{ij}^t$ is the current communication cost from $v_i$ to its child $v_j$. For the exit task, $rank_u(v_{exit}; t) = 0$.

**VM Selection Phase.** Tasks are sorted by the non-increasing order of $rank_u$ values, and the task with the higher $rank_u$ is given the higher priority. Task with the higher priority can first select and record the "best" VM that allows for the minimum EFT according to equation (8). Insertion policy is used that tries to insert a task in the earliest idle time slot between two already recorded tasks on a VM, if the slot is large enough to accommodate the task.

A task is ready if all its parents are finished. When the best VM is available, the ready task can be scheduled and executed on it. Remaining tasks, including tasks which are not ready and ready tasks which are not scheduled just save the $(task, bestVM)$ record. In the next scheduling loop, if the

best VM changed based on the new runtime performance, including VM available time, task finish time, VM computing rate, network bandwidth, etc., the $(task, bestVM)$ record is updated.

**Data Transfer Phase.** For a finished task $v_i$, intermediate data from $v_i$ to each of its children $v_j$ is sent at time DLTT. DLTT is calculated based on current network bandwidth and latency between $VM_i$ hosting $v_i$ and $VM_j$ recorded as the best VM for $v_j$, according to equation (7). At each scheduling loop, record $(time, sourceTask, sourceVM, destinationTask, destinationVM, data)$ is saved, where time is $DLTT(v_j, VM_j, v_i, VM_i; t)$, source task is $v_i$, source VM is $VM_i$, destination task is $v_j$, destination VM is $VM_j$, and data is the intermediate data from $v_i$ to $v_j$. Data is sent according to the DLTT record in the runtime. If the $(task, bestVM)$ record of $v_j$ is changed after data is sent, old data is discarded and new data is sent at the new DLTT. If the new DLTT is earlier than the current time, $v_j$ will be delayed, and $EST(v_j)$ is updated as well. When a VM receives some data, it checks the $(task, bestVM)$ record list and the DLTT record list. The data is cached if the VM is the the destination, otherwise, the data is discarded. Considering the $(task, bestVM)$ record may change before a task is scheduled, and the task may fail before complete, DLTT record will not be deleted until the task complete successfully.

In data transfer phase, DLTT is calculated for all the children of finished tasks. Best VMs for the children are selected in VM selection phase. Since tasks that are not the children of the finished tasks can neither be ready nor be assigned to the earlier idle time slot before the children, there is no use to consider them. Therefore, tasks considered in each scheduling loop are the unscheduled children of the finished tasks.

Initially, all the entry nodes are ready to schedule and stored in *Scope*. A scheduling loop is invoked at the beginning or when some tasks complete and release VMs. All the unscheduled children of finished tasks are added to *Scope* (Line 3). Then $rank_u$ of each task in *Scope* is calculated based on the current computing rate and network bandwidth according to equation (10) (Line 4-5). *Readys* is updated by adding tasks whose parents are all finished (Line 6-7). Then tasks are sorted by the non-increasing order of $rank_u$ (Line 9). Best VM is selected for each task in the sorted *Scope* (Line 11). New $(task, bestVM)$ record is add to *Maps* (Line 12-13). *Maps* and *Datas* are updated if the $(task, bestVM)$ record is changed in the current loop (Line 14-16). Then ready tasks whose best VMs are available are scheduled (Line 18-19) and records are deleted from *Maps*, *Readys*, and *Scope* (Line 21). For each finished task $v_f$, DLTT from $v_f$ to each child is calculated, and $(DLTT, v_f, VM_f, v_{child}, bestVM_{child}, data)$ is added to *Datas* (Line 22-25). Record with $v_f$ as the destination task is delete from *Datas* (Line 27). Finally, data is transferred according to *Datas* in the runtime (Line 32).

### 4.2 Detailed Description of the DEFT Algorithm

In this section, we describe each step of the DEFT algorithm

in detail. Then we analyze the time complexity.

**Algorithm 1** Pseudo code of the DEFT algorithm

Input:   The workflow DAG with $n$ tasks $\{v_1, v_2, \cdots, v_n\}$
$VM = \{VM_1, VM_2, \cdots, VM_m\}$: $m$ VM in the IaaS cloud
*Fins*: tasks finished before each loop
*Scope*: list of tasks considered in each loop, initially is $\{v_{entrance}\}$
*Readys*: list of ready tasks, initially is $\{v_{entrance}\}$
*Maps*: list of (*task*, *bestVM*) map record
*Datas*: list of data transfer record

1:   **while** *Scope* is not **null do**
2:     **if** *Fins* is **not null** at time $t$ **do**
3:       update *Scope*
4:       **for** task $v_i \in$ *Scope* **do**
5:         compute $rank_u(v_i; t)$ using equation(10)
6:         **if** $v_i$ is ready
7:           *Readys* $\leftarrow v_i$
8:       **end for**
9:       sort tasks in *Scope* by non-increasing order of $rank_u$
10:      **for** task $v_i \in$ *Scope* **do**
11:        find $bestVM_i$ that minimize $EFT(v_i, bestVM_i; t)$
12:        **if** $v_i \notin$ *Maps*
13:          *Maps* $\leftarrow (v_i, bestVM_i)$
14:        **else if** $(v_i, bestVM_i) \notin$ *Maps* **do**
15:          update *bestVM* for $v_i$ in *Maps*
16:          update records whose destination is $v_i$ in *Datas*
17:        **end if**
18:        **if** $v_i \in$ *Readys* and $bestVM_i$ is available
19:          **schedule** $v_i$ to $bestVM_i$
20:      **end for**
21:      delete scheduled tasks from *Maps, Readys, Scope*
22:      **for** task $v_f \in$ *Fins* **do**
23:        **for** task $v_c \in$ child($v_f$) **do**
24:          compute $DLTT(v_c, bestVM_c, v_f, VM_f; t)$ using equation(7)
25:          *Datas* $\leftarrow (DLTT, v_f, VM_f, v_c, bestVM_c, data)$
26:        **end for**
27:        delete record whose destination is $v_f$ from *Datas*
28:      **end for**
29:    **end if**
30:    empty *Fins*
31:    *wait()*
32:    send data at time *DLTT* in *Datas*

Suppose a workflow with $n$ tasks is scheduled to $m$ VMs in the IaaS cloud. In each scheduling loop, DEFT compute $rank_u$ for the tasks in *Scope* and select the best VMs for the tasks. Since $rank_u$ defined in equation (10) is recursively calculated by traversing the DAG from the exit task to the target task, all the unscheduled tasks are considered in the task prioritizing phase. The time complexity of computing $rank_u$ in a scheduling loop is $O(k^2 m)$, for $k$ unscheduled tasks and $m$ VMs. The time complexity of VM selection phase and data transfer phase is $O(s * m)$, where $s$ is the number of tasks in *Scope* and $s \leq k$. So, the total time complexity of each loop is $O(k^2 m)$. In the worst case where there is only one task scheduled in each loop, there are $n$ scheduling loops, and the time complexity of the $l^{th}$ loop is $O((n-l)^2 * m)$. The total time complexity is $O(1^2 * m + 2^2 * m + \cdots + (n-1)^2 * m)$, that is $O(n^3 * m)$.

### 4.3  An Example

To better illustrate DEFT, we show an example comparing DEFT to PEFT [6] , DCP-G [12], and DCP-G [20] .
HEFT and PEFT are typical static algorithms using static information to generate scheduling map at the scheduling time. HEFT uses the same definition of $rank_u$ and selection strategy as ours in prioritizing phase and VM selection phase. PEFT proposes the concept of OCT (Optimistic Cost
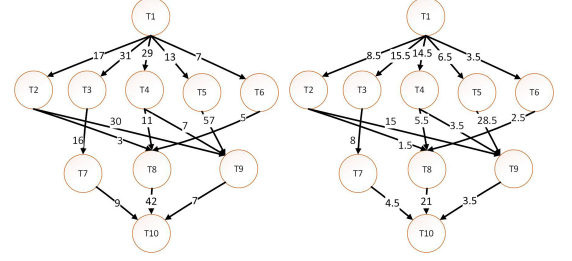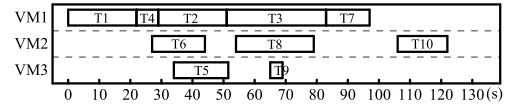


(a) Communication cost of DAG, t=0s.   (b) Communication cost of DAG, t=30s.

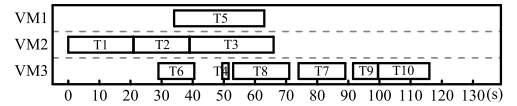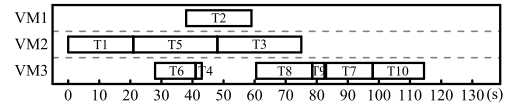|      | VM1 | VM2 | VM3(t=0) | VM3(t=30) |
|------|-----|-----|----------|-----------|
| T1   | 22  | 21  | 36       | 18        |
| T2   | 22  | 18  | 18       | 9         |
| T3   | 32  | 27  | 43       | 21.5      |
| T4   | 7   | 10  | 4        | 2         |
| T5   | 29  | 27  | 35       | 17.5      |
| T6   | 26  | 17  | 24       | 12        |
| T7   | 14  | 25  | 30       | 15        |
| T8   | 29  | 23  | 36       | 18        |
| T9   | 15  | 21  | 8        | 4         |
| T10  | 13  | 16  | 33       | 16.5      |

(c)  Computing cost matrix.
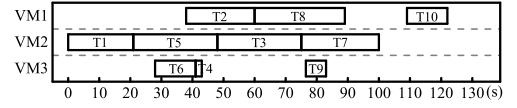


(d)  HEFT, makespan=122s.



(e)  PEFT, makespan=122s.



(f)  DCP-G, makespan=116s.



(g)  DEFT, makespan=114.5s.

**Fig. 1**   Scheduling examples of HEFT, PEFT, DCP-G, and DEFT.

Table) in the task prioritizing phases. The OCT value of a task $v_i$ on $VM_j$ is recursively defined by equation (11) by traversing the DAG from the exit task to the entry task:

$$OCT(v_i, VM_j)$$
$$= \max_{v_k \in child(v_i)} \left[ \min_{VM_p \in VM} \{OCT(v_k, VM_p) + w_{kp} + c_{ik}\} \right]$$
(11)

where $w_{kp}$ is the computing cost of $v_k$ running on $VM_p$, and $c_{ik}$ is the communication cost from $v_i$ to $v_k$. For the exit task, $OCT(v_{exit}, VM_p) = 0$ for all the $VM_p \in VM$. $c_{ik} = 0$ if $VM_j = VM_p$, or if $VM_j$ and $VM_p$ are hosted on the same server. In the VM selection phase, task $v_i$ is assigned to $VM_j$ minimizing $O_{ETF}(v_i, VM_j)$, defined by equation (12):

$$O_{EFT}(v_i, VM_j) = EFT(v_i, VM_j) + OCT(v_i, VM_j) \quad (12)$$

DCP-G selects and schedules tasks in the runtime. The task selected for scheduling is the one that is on the dynamic critical path, which has the same earliest start time and latest start time updated dynamically in the runtime, with no unmapped parent tasks and has the lowest earliest start time. The the VM with minimum execution time for that task is selected.

The scheduling results are shown in Fig.1. There are 10 tasks of a DAG workflow scheduled on 3 fully connected heterogeneous VMs. Initially, network bandwidth between VMs are the same. Communication cost and the DAG is shown in Fig.1(a). Computing cost of each task on each VM is shown in the left four columns of Fig.1(c). At t=30$s$, computing rate of VM3 doubles, and the computing cost of each task on it is shown in the right column of Fig.1(c). Transfer rates between VM3 and the other two VMs also doubles, and the communication cost of each task on it is shown in Fig.1(b).

HEFT and PEFT use initial performance to schedule tasks. Tasks are sorted and queued on the same VMs after the performance variation. Final makespan of HEFT is 122$s$ Fig.1(d), and PEFT is 122$s$ Fig.1(e). DCP-G schedules each critical task dynamically in the runtime, and the final makespan is 116$s$ Fig.1(f).

DEFT contains scheduling loops invoked dynamically in the runtime. When T6 finishes at $t = 41s$, the scheduling loop starts with the remaining task sorted as {T4, T3, T8, T7, T9, T10}. *Scope* is {T4, T3}, *Ready* is {T4, T3}. Best VM for T4 is VM3, with EST=41$s$. Then VM3's available time for T3 is at t=43$s$ (computing cost of T4 on VM3 is 2$s$), computing cost is 21.5$s$. In the scheduling loop when T1 finishes at $t = 21s$, best VM for T3 is VM2. There is no data transfer since T3 is recorded to be assigned to the same VM as T1. Therefore, if T3 is scheduled to VM3 in the scheduling loop at t=41$s$, data is sent from VM2 at $t = 41s$ and received by VM3 at $t = 56.5s$. In this case, $EST(T3, VM3; 41s) = \max\{56.5, 43\}+21.5 = 56.5+21.5 = 78s$. At $t = 41s$, VM2's available time for T3 is at t=48$s$, computing cost is 27$s$, and communication cost is 0$s$ since T3 is recorded to be assigned to the same VM as T1. In this case, $EFT(T3, VM2; 41s) = \max\{41, 48\} + 27 = 48 + 27 = 75s$. Therefore, the best VM for T3 is VM2. The final scheduling of DEFT is shown in Fig.1(g), and the makespan is 114.5$s$.

## 5. Experimental Results

In this section, we present the comparative evaluations of DEFT and PEFT, DCP-G in the IaaS cloud. We first describe experimental settings. Then we show the comparative evaluations of the three algorithms.

### 5.1 Experimental settings

We use the DynamicCloudSim [25] toolkit to simulate the IaaS cloud. DynamicCloudSim extends the CloudSim [26] simulation toolkit by introducing models for: (1) inhomogeneity in the performance of computational resources, (2) uncertainties and dynamic changes to the performance of VMs, and (3) straggler machines and failures during the task execution.

We use the default setting of the data center in DynamicCloudSim. The data center contains 100 servers of Intel Xeon E5430 2.66 GHz, 200 servers of AMD Opteron 270 2 GHz, and 200servers of AMD Opteron 2218 HE 2.6 GHz. 100 VMs are randomly hosted on the servers and allocated to random performance parameters. The default I/O throughput of VMs is 20 MB/s. The servers are fully connected. The external bandwidth of VMs is 0.25 MB/s, and the latency of data transfer is not considered.

In DynamicCloudSim, dynamic change of CPU rate of VMs, I/O throughput, are network bandwidth are simulated in the same way. The time of the next performance change is sampled from an exponential distribution with a given rate parameter, and the new value of the given characteristic is sampled from a normal distribution with the mean set to the default value of the given characteristic. Higher values in both the rate parameter of the exponential distribution and RSD (relative standard deviation) of the normal distribution correspond to higher levels of dynamics. We use the tuple $\langle change\_number, dynamic\_degree \rangle$ to donate the performance changes. Since the time of the next performance change is randomly sampled and the makespans of a workflow vary using different scheduling methods, we use the ranges of the number of changes instead of the fixed values, {1-10, 10-20, 20-30, 30-40}. The low dynamic degree is the default setting of RSD, which is 0.054 for CPU, 0.033 for I/O, and 0.04 for network bandwidth, and the high dynamic degree is RSD=0.5 for CPU, I/O, and network bandwidth. The values used in the experiments are marked: {$\langle 10, l \rangle$, $\langle 10, h \rangle$, $\langle 20, l \rangle$, $\langle 20, h \rangle$, $\langle 30, l \rangle$, $\langle 30, h \rangle$, $\langle 40, l \rangle$, $\langle 40, h \rangle$} for short.

We use the typical scientific workflow Montage, which has been repeatedly utilized for evaluating scheduling mechanisms and computational infrastructures for scientific workflow execution in the past. The DAG structure of each workflow, including task dependencies, computational characteristics, the input and output files of the tasks, etc. is described in Pegasus DAX (Directed Acyclic Graph in XML) format. Each size of the workflow, from 50 to 1000, have 20 instances generated by WorkflowGenerator [27]. Each workflow is run 100 times in the experiment, and the mean makespan and CV of the makespans are computed.

### 5.2 Evaluation results

In this section, we compare the makespan and robustness performances of PEFT, DCP-G and DEFT in the IaaS cloud.

Fig.2 shows the NSLs and robustness of the 20 workflows consisting 1000 task nodes using PEFT, DCP-G and DEFT in the default setting of performance changes. All the workflows using DEFT have smaller makespans than using PEFT, and 19 workflows using DEFT have smaller makespans than using DCP-G. DEFT can produce more robust schedules than PEFT for 19 workflows, and DCP-G for 18 workflows.
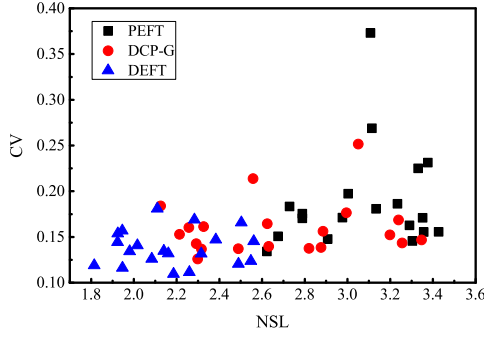
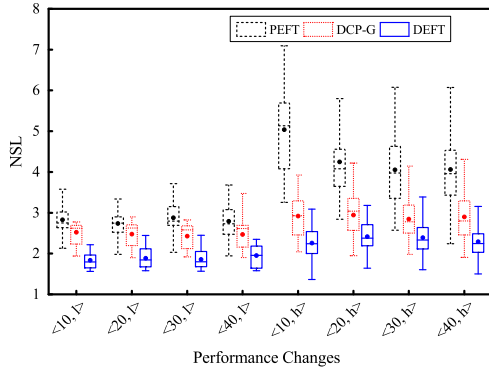**Fig. 2** Average NSL and CV in the default setting.



**Fig. 3** NSL with respect to different settings of performance changes.



**Fig. 4** CV with respect to different settings of performance changes.



**Fig. 5** Scheduling time of different workflow sizes.

Fig.3 and Fig.4 shows makespans and robustness of the three algorithms with respect to different settings of performance changes. The workflow with the minimum CV differences of the three algorithms in Fig.2 is chosen. NSLs of the workflow are 2.56 of PEFT, 2.47 of DCP-G and 1.86 of DEFT in the static environment where CPU, I/O, and network bandwidth do not vary during execution of the workflow.

Fig.3 presents the boxplots showing the minimum, 25 percent, mean, 75 percent, and maximum values of the NSL of the three scheduling methods with respect to different settings of performance changes. DEFT can always have the smallest NSLs. The average NSLs of PEFT, DCP-G, and DEFT at the low dynamic degree are 2.83, 2.52, and 1.82, respectively, for performance of CPU, I/O, and network bandwidth changes less than 10 times during the execution of the workflow, and are 2.79, 2.47, and 1.95, respectively, for performance changes over 30 times. The improvement of DEFT over PEFT and DCP-G are 35.69% and 27.78% for performance changes less than 10 times, and 30.11% and 21.05% for performance changes more than 30 times. The average NSLs of PEFT, DCP-G, and DEFT at the high dynamic degree are 5.04, 3.91, and 2.92, respectively, for performance changes less than 10 times, and 4.06, 3.65, and 2.90, respectively, for performance changes over 30 times. The improvement of DEFT over PEFT and DCP-G are 42.06% and 32.89% for performance changes less than 10 times, and 28.57% and 20.55% for performance changes over 30 times.

Fig.4 shows CVs of PEFT, DCP-G, and DEFT with respect to different settings of performance changes. CVs of DCP-G and DEFT are similar as they schedule tasks dynamically in the 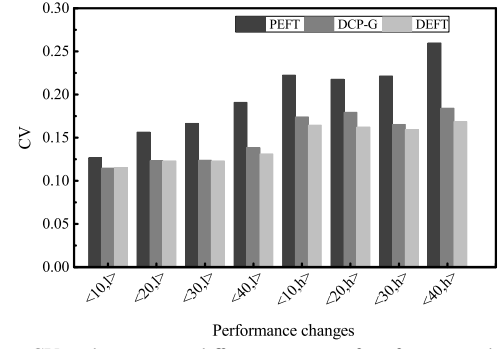runtime. The average CVs of the low dynamic degree are 0.16 of PEFT, 0.124 of DCP-G, and 0.123 of DEFT. The average CVs of the high dynamic degree are 0.23 of PEFT, 0.176 of DCP-G, and 0.164 of DEFT. The improvement of DEFT and DCP-G over PEFT are 9.36% and 8.86% for performance changes less than 10 times at the low dynamic degree, and are 29.05% and 35.03% for performance changes more than 30 times at high dynamic degree.

Scheduling time is considered as the scheduling overhead, which constitutes a significant amount of time used by the scheduler to generate the schedule. Fig.5 shows the total scheduling time of workflows with different sizes of the three scheduling methods running in the default setting of the dynamic IaaS cloud data center. It shows that the scheduling time overhead of the three methods are similar if the workflow size is small ( consisting less than 300 tasks ). With the workflow size increases, the overhead of DCP-G and DEFT increases linearly, while PEFT does not vary too much. However, it should be noticed that the average makespan of the workflows with 1000 tasks is around 7000 seconds, and the total scheduling time of the workflow is around 9 seconds. The scheduling time overhead is acceptable compared to the makespan of the workflows in our experiment. Moreover, DEFT provides a good choice for workflows with the execution time of tasks large enough to tolerant the overhead, which is about 10ms.

## 6. Conclusion and future work

Scientific workflows are increasingly adopting the IaaS cloud where computing resources are provided in the form of VMs, dynamically managed, monitored, maintained, and governed

by market principles. In this paper, we deal with the challenges of scheduling workflows to the IaaS cloud with uncertainties like resource performance variations and unknown failures. A dynamic scheduling algorithm, called DEFT, is proposed to improve both makespan and robustness. DEFT contains a set of list scheduling loops invoked when some tasks complete and release resources. In each loop, runtime informations are used to sort tasks, select VMs, and send intermediate data. Experiments show that DEFT can produce shorter makespan than existing typical list-based scheduling, PEFT, and dynamic scheduling, DCP-G. It also produces more robust schedules in the IaaS cloud with uncertainties.

Existing algorithm uses the dynamic scheduling to alleviate impact of uncertainties like the resource performance variations and unknown failures. In the future work, we will research some monitor functions to discover potential failures and a predict model to better understand the performance variations.

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