

Administrivia

- Please make sure you have obtained a Unix account. If you have very recently (i.e., since today) signed up for concurrent enrollment please email us your name, email, and SID. After we have a chance to process it, you will be able to use WebAcct, as Lab #1 specifies.
- Lab #1 is due Wednesday (end of Wednesday at midnight). Usually, labs are due Friday midnight of the week they occur. It is especially important to set up your central repository.
- If you decide not to take this course after all, please tell CalCentral ASAP, so that we can adjust the waiting list accordingly.
- HW #0 now up; due next Friday at midnight. You get credit for any submission, but we suggest you give the problems a serious try.

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Lecture #2: Let's Write a Program: Prime Numbers

Problem: want java Primes U to print prime numbers through U .

You type: java Primes 101

It types: 2 3 5 7 11 13 17 19 23 29
31 37 41 43 47 53 59 61 67 71
73 79 83 89 97 101

Definition: A *prime* number is an integer greater than 1 that has no divisors smaller than itself other than 1.

(Alternatively: $p > 1$ is prime iff $\gcd(p, x) = 1$ for all $0 < x < p$.)

Useful Facts:

- $k \leq \sqrt{N}$ iff $N/k \geq \sqrt{N}$, for $N, k > 0$.
- If k divides N then N/k divides N .

So: Try all potential divisors up to and including the square root.

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Plan

```
public class Primes {
    /** Print all primes up to ARGS[0] (interpreted as an
     * integer), 10 to a line. */
    public static void main(String[] args) {
        printPrimes(Integer.parseInt(args[0]));
    }

    /** Print all primes up to and including LIMIT, 10 to
     * a line. */
    private static void printPrimes(int limit) {
        /* For every integer, x, between 2 and LIMIT, print it if
         isPrime(x), 10 to a line. */
    }

    /** True iff X is prime */
    private static boolean isPrime(int x) {
        return /*( X is prime )*/;
    }
}
```

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Testing for Primes

```
private static boolean isPrime(int x) {
    if (x <= 1)
        return false;
    else
        return !isDivisible(x, 2); // "!" means "not"
}

/** True iff X is divisible by any positive number >=K and < X,
 * given K > 1. */
private static boolean isDivisible(int x, int k) {
    if (k >= x) // a "guard"
        return false;
    else if (x % k == 0) // "%" means "remainder"
        return true;
    else // if (k < x && x % k != 0)
        return isDivisible(x, k+1);
}
```

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Thinking Recursively

Understand and check `isDivisible(13,2)` by *tracing one level*.

```
/** True iff X is divisible by
 * some number >=K and < X,
 * given K > 1. */
private static boolean isDivisible...
if (k >= x)
    return false;
else if (x % k == 0)
    return true;
else
    return isDivisible(x, k+1);
}
```

Lesson: Comments aid understanding. Make them count!

- Call assigns $x=13$, $k=2$
- Body has form 'if ($k \geq x$) S_1 else S_2 '.
- Since $2 < 13$, we evaluate the first else.
- Check if $13 \bmod 2 = 0$; it's not.
- Left with `isDivisible(13,3)`.
- Rather than tracing it, instead use the *comment*:
- Since 13 is *not* divisible by any integer in the range 3..12 (and $3 > 1$), `isDivisible(13,3)` must be *false*, and we're done!
- Sounds like that last step begs the question. Why doesn't it?

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Iteration

- `isDivisible` is *tail recursive*, and so creates an *iterative process*.
- Traditional "Algol family" production languages have special syntax for iteration. Four equivalent versions of `isDivisible`:

```
if (k >= x)
    return false;
else if (x % k == 0)
    return true;
else
    return isDivisible(x, k+1);

while (k < x) { // !(k >= x)
    if (x % k == 0)
        return true;
    k = k+1;
    // or k += 1, or (yuch) k++
}
return false;
```

```
int k1 = k;
while (k1 < x) {
    if (x % k1 == 0)
        return true;
    k1 += 1;
}
return false;

for (int k1 = k; k1 < x; k1 += 1) {
    if (x % k1 == 0)
        return true;
}
return false;
```

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Using Facts about Primes

- We haven't used the Useful Facts from an earlier slide. Only have to check for divisors up to the square root.
- So, reimplement the iterative version of isDivisible:

```
/** True iff X is divisible by some number >=K and < X,
 *  given that K > 1, and that X is not divisible by
 *  any number >1 and <K. */
private static boolean isDivisible(int x, int k) {
    int limit = (int) Math.round(Math.sqrt(x));
    for (int k1 = k; k1 <= limit; k1 += 1) {
        if (x % k1 == 0)
            return true;
    }
    return false;
}
```

- Why the additional (blue) condition in the comment?

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Cautionary Aside: Floating Point

- In the last slide, we had

```
int limit = (int) Math.round(Math.sqrt(x));
for (int k1 = k; k1 <= limit; k1 += 1) {
    ...
}
```

intending that this would check all values of k1 up to and including the square root of x.

- Since floating-point operations yield *approximations* to the corresponding mathematical operations, you might ask the following about `(int) Math.round(Math.sqrt(x))`:
 - Is it always at least $\lfloor \sqrt{x} \rfloor$, where $\lfloor z \rfloor$ is the largest integer $\leq z$? (If not, we might miss testing \sqrt{x} when x is a perfect square.)
- As it happens, the answer is "yes" for IEEE floating-point square roots.
- Just an example of the sort of detail that must be checked in edge cases.

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Final Task: printPrimes (Simplified)

```
/** Print all primes up to and including LIMIT. */
private static void printPrimes(int limit) {
    ...
}
```

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Simplified printPrimes Solution

```
/** Print all primes up to and including LIMIT. */
private static void printPrimes(int limit) {
    for (int p = 2; p <= limit; p += 1) {
        if (isPrime(p)) {
            System.out.print(p + " ");
        }
    }
    System.out.println();
}
```

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printPrimes (full version)

```
/** Print all primes up to and including LIMIT, 10 to
 *  a line. */
private static void printPrimes(int limit) {
    int np;
    np = 0;
    for (int p = 2; p <= limit; p += 1) {
        if (isPrime(p)) {
            System.out.print(p + " ");
            np += 1;
            if (np % 10 == 0)
                System.out.println();
        }
    }
    if (np % 10 != 0)
        System.out.println();
}
```

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