#### Recreation

What is the sum of the coefficients of

$$(1 - 3x + 3x^2)^{743}(1 + 3x - 3x^2)^{744}$$

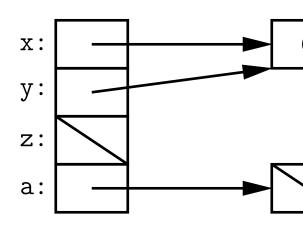
after expanding and collecting terms?

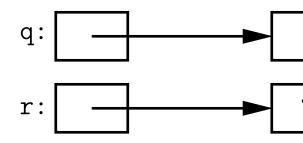
### CS61B Lecture #5: Arrays

- An array is a structured container whose components are
  - length, a fixed integer.
  - a sequence of length simple containers of the same type
     bered from 0.
  - (.length field usually implicit in diagrams.)
- Arrays are anonymous, like other structured containers.
- Always referred to with pointers.
- For array pointed to by A,
  - Length is A.length
  - Numbered component i is A[i] (i is the index)
  - Important feature: index can be any integer expression.

# A Few Samples

Java Results





```
int[] x, y, z;
String[] a;
x = new int[3];
y = x;
a = new String[3];
x[1] = 2;
y[1] = 3;
a[1] = "Hello";
```

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in+[] ~.

### Example: Accumulate Values

**Problem:** Sum up the elements of array A.

```
static int sum(int[] A) {
  int N;
  N = 0;
  for (int i = 0; i < A.length; i += 1)
     N += A[i];
  return N;
}

// For the hard-core: could have written

int N, i;
for (i=0, N=0; i<A.length; N += A[i], i += 1)
  { } // or just ;

// But please don't: it's obscure.</pre>
```

// New

for (i

N +

### Example: Insert into an Array

skunk

### (Aside) Java Shortcut

• Useful tip: Can write just 'arraycopy' by including at the to source file:

```
import static java.lang.System.arraycopy;
```

- This means "define the simple name arraycopy to be the eq of java.lang.System.arraycopy in the current source file.
- Can do the same for out so that you can write

```
out.println(...);
in place of
System.out.println(...);
```

• Finally, a declaration like

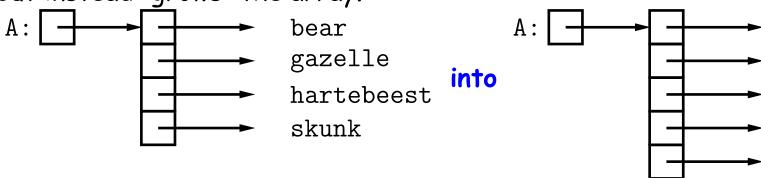
```
import static java.lang.Math.*;
```

means "take all the (public) static definitions in java.lang. Means them available in this source file by their simple nan name after the last dot)."

• Useful for functions like sin, sqrt, etc.

### Growing an Array

**Problem:** Suppose that we want to change the description at that A = insert2 (A, 2, "gnu") does not shove "skunk" off but instead "grows" the array.



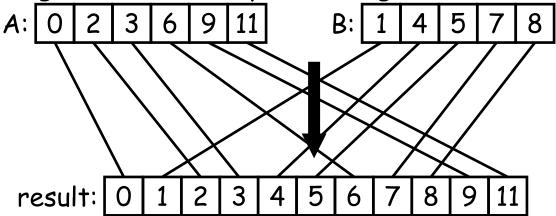
```
/** Return array, r, where r.length = ARR.length+1; r[0..K-1]
  * the same as ARR[0..K-1], r[k] = x, r[K+1..] same as ARR[K..].
static String[] insert2(String[] arr, int k, String x) {
   String[] result = new String[arr.length + 1];
   arraycopy(arr, 0, result, 0, k);
   arraycopy(arr, k, result, k+1, arr.length-k);
   result[k] = x;
   return result;
}
```

Why do we need a different return type from insert2??

# Example: Merging

Problem: Given two sorted arrays of ints, A and B, production

merge: a sorted array containing all items from A and B.



### Example: Merging Program

**Problem:** Given two sorted arrays of ints, A and B, product merge: a sorted array containing all from A and B.

**Remark:** In order to solve this recursively, it is useful to ge the original function to allow merging portions of the arrays.

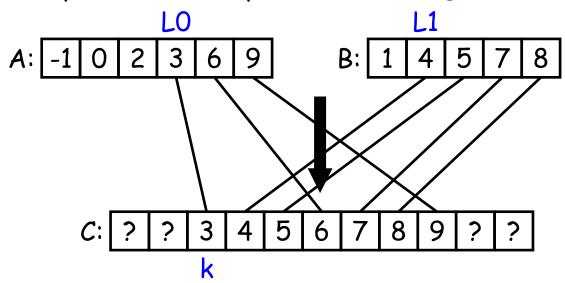
```
/** Assuming A and B are sorted, returns their merge. */
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, 0, B, 0);
}
/** The merge of A[LO..] and B[L1..] assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1) {
   int N = A.length - LO + B.length - L1; int[] C = new int[N];
   if (LO >= A.length) arraycopy(B, L1, C, O, N);
                                                            What
   else if (L1 >= B.length) arraycopy(A, L0, C, 0, N);
                                                            this ir
   else if (A[L0] <= B[L1]) {</pre>
      C[0] = A[L0]; arraycopy(mergeTo(A, L0+1, B, L1), 0, C, 1, N)
   } else {
      C[0] = B[L1]; arraycopy(mergeTo(A, L0, B, L1+1), 0, C, 1, N)
   return C;
```

### A Tail-Recursive Strategy

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorte
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, i
   ...
}
```

This last method merges part of A with part of B into part of example, consider a possible call mergeTo(A, 3, B, 1, C, 2)



```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, O, B, O, new int[A.length+B.length], O);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorte
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, i
    if (??) {
      return C;
    } else if (??) {
      C[k] = A[LO];
      return mergeTo(A, ??, B, ??, C, ??)
    } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
    }
}
```

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorte
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, i
    if (L0 >= A.length && L1 >= B.length) {
        return C;
    } else if (??) {
        C[k] = A[L0];
        return mergeTo(A, ??, B, ??, C, ??)
    } else {
        C[k] = B[L1];
        return mergeTo(A, ??, B, ??, C, ??)
    }
}
```

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, O, B, O, new int[A.length+B.length], O);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorte
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, i
    if (LO >= A.length && L1 >= B.length) {
        return C;
    } else if (L1 >= B.length || (LO < A.length && A[LO] <= B[L1])
        C[k] = A[LO];
        return mergeTo(A, ??, B, ??, C, ??)
    } else {
        C[k] = B[L1];
        return mergeTo(A, ??, B, ??, C, ??)
    }
}</pre>
```

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, O, B, O, new int[A.length+B.length], O);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorte
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, i
    if (LO >= A.length && L1 >= B.length) {
        return C;
    } else if (L1 >= B.length || (LO < A.length && A[LO] <= B[L1])
        C[k] = A[LO];
        return mergeTo(A, LO + 1, B, L1, C, k + 1);
    } else {
        C[k] = B[L1];
        return mergeTo(A, ??, B, ??, C, ??)
    }
}</pre>
```

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, O, B, O, new int[A.length+B.length], O);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorte
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, i
    if (LO >= A.length && L1 >= B.length) {
        return C;
    } else if (L1 >= B.length || (LO < A.length && A[LO] <= B[L1])
        C[k] = A[LO];
        return mergeTo(A, LO + 1, B, L1, C, k + 1);
    } else {
        C[k] = B[L1];
        return mergeTo(A, LO, B, L1 + 1, C, k + 1);
    }
}</pre>
```

#### Iterative Solution

In general, we don't use either of the previous approaches in la like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int L0, L1, k;
   L0 = L1 = k = 0;

   while (??) {
      if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
         C[k] = A[L0];
        ??
      } else {
         C[k] = B[L1];
        ??
      }
   }
   return C;
}</pre>
```

#### Iterative Solution

In general, we don't use either of the previous approaches in languages I Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int L0, L1, k;
   L0 = L1 = k = 0;

while (L0 < A.length || L1 < B.length) {
     if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
        C[k] = A[L0];
        ??
     } else {
        C[k] = B[L1];
        ??
     }
} return C;
}</pre>
```

#### Iterative Solution

In general, we don't use either of the previous approaches in languages I Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int L0, L1, k;
   L0 = L1 = k = 0;

while (L0 < A.length || L1 < B.length) {
     if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
        C[k] = A[L0];
        L0 += 1; k += 1;
     } else {
        C[k] = B[L1];
        L1 += 1; k += 1;
     }
}
return C;
}</pre>
```

#### Iterative Solution II

The same, with a for loop:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   int LO, L1;
   L0 = L1 = 0;
   for (int k = 0; k < C.length; k += 1) {
        if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
            C[k] = A[LO]; LO += 1;
        } else {
            C[k] = B[L1]; L1 += 1;
        }
   return C;
}
Invariant (true after int k = 0):
  0 \le L0 < A.length \land 0 \le L1 < B.length \land C.length = A.length + B.length
  \land C[0:k] is a permutation of A[0:L0] + B[0:L1]
  \wedge C[0:k], A, B are sorted.
```

### Alternative Solution: Removing k

Using previous invariant that k=L0+L1 simplifies things:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   int L0, L1; L0 = L1 = 0;
   while (L0 + L1 < C.length) {
      if (L1 >= B.length || (L0 < A.length && A[L0] < B[L1])) {
            C[L0 + L1] = A[L0]; L0 += 1;
      } else {
            C[L0 + L1] = B[L1]; L1 += 1;
      }
   }
   return C;
}</pre>
```

A.length+B.leng

L1

LO

0

# Multidimensional Arrays

What about two- or higher-dimensional layouts, such as

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### Multidimensional Arrays in Java

These are not primitive in Java, but we can build them as arrays of arrays:

```
int[][] A = new int[3][];
  A[0] = new int[] \{2, 3, 4, 5\};
  A[1] = new int[] {4, 9, 16, 25};
  A[2] = new int[] \{8, 27, 64, 125\};
// or
  int[][] A;
  A = new int[][] { {2, 3, 4, 5},}
                    {4, 9, 16, 25},
                                             A:
                     { 8, 27, 64, 125} };
// or
  int[][] A = { {2, 3, 4, 5},}
                {4, 9, 16, 25},
                {8, 27, 64, 125} };
// or
  int[][] A = new A[3][4];
  for (int i = 0; i < 3; i += 1)
```

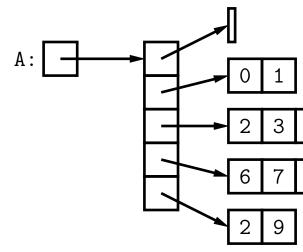
A[i][j] = (int) Math.pow(j + 2, i + 1);

for (int j = 0; j < 4; j += 1)

### Exotic Multidimensional Arrays

 Since every element of an array is independent, there is no single "widt eral:

```
int[][] A = new int[5][];
A[0] = new int[] {};
A[1] = new int[] {0, 1};
A[2] = new int[] {2, 3, 4, 5};
A[3] = new int[] {6, 7, 8};
A[4] = new int[] {9};
```



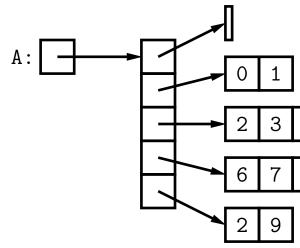
• What does this print?

```
int[][] ZERO = new int[3][];
ZERO[0] = ZERO[1] = ZERO[2] =
    new int[] {0, 0, 0};
ZERO[0][1] = 1;
System.out.println(ZERO[2][1]);
```

# Exotic Multidimensional Arrays

 Since every element of an array is independent, there is no single "widt eral:

```
int[][] A = new int[5][];
A[0] = new int[] {};
A[1] = new int[] {0, 1};
A[2] = new int[] {2, 3, 4, 5};
A[3] = new int[] {6, 7, 8};
A[4] = new int[] {9};
```



• What does this print?

```
int[][] ZERO = new int[3][];
ZERO[0] = ZERO[1] = ZERO[2] =
    new int[] {0, 0, 0};
ZERO[0][1] = 1;
System.out.println(ZERO[2][1]);
```

