CS61B Lecture #23

Today:

- Priority queues (Data Structures §6.4, §6.5)
- Range queries (§6.2)
- Java utilities: SortedSet, Map, etc.

Next topic: Hashing (Data Structures Chapter 7).

Priority Queues, Heaps

- Priority queue: defined by operations "add,"
 "find largest," "remove largest."
- Examples: scheduling long streams of actions to occur at various future times.
- Also useful for sorting (keep removing largest).
- Common implementation is the heap, a kind of tree.
- (Confusingly, this same term is used to described the pool of storage that the new operator uses. Sorry about that.)

Heaps

 A max-heap is a binary tree that enforces the

> Heap Property: Labels of both children of each node are less than node's label

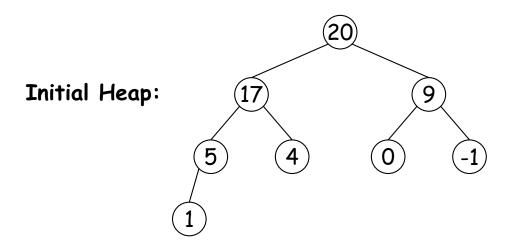
- So node at top has largest label.
- Looser than binary search property, which allows us to keep tree "bushy".
- That is, it's always valid to put the smallest nodes anywhere at the bottom of the tree.
- Thus, heaps can be made nearly complete: all but possibly the last row have as many keys as possible.
- As a result, insertion of new value and deletion of largest value always take time proportional to $\lg N$ in worst case.
- A min-heap is basically the same, but with

the minimum value at the root and children having larger values than their parents.

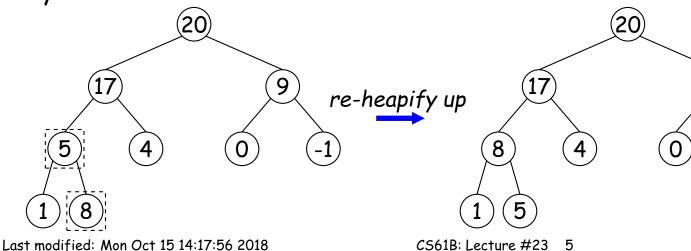
Example: Inserting into a simple heap

Data:

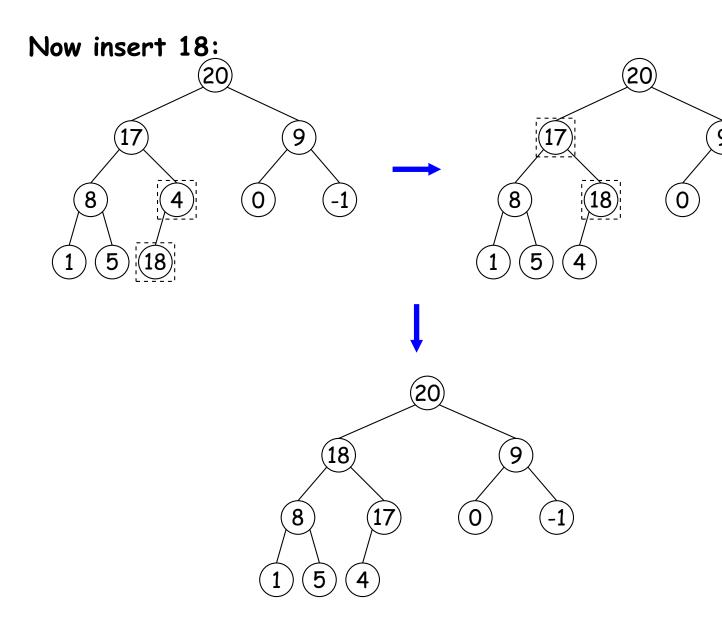
1 17 4 5 9 0 -1 20



Add 8: Dashed boxes show where heap property violated

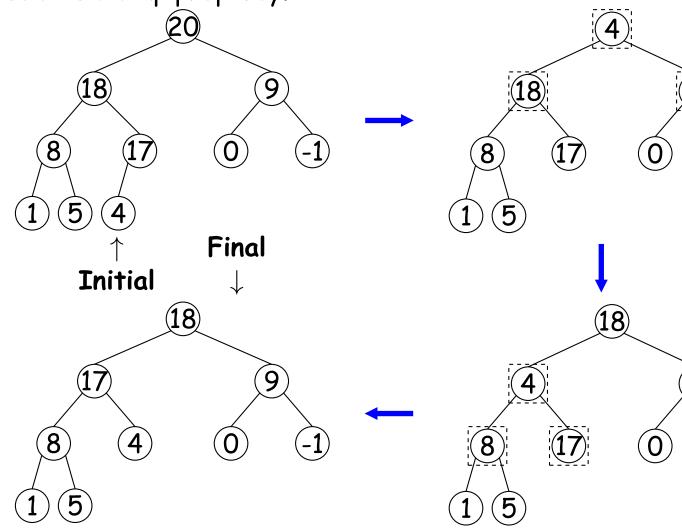


Heap insertion continued



Removing Largest from Heap

To remove largest: Move bottommost, rightmost node to top, then re-heapify down as needed (swap offending node with larger child) to reestablish heap property.

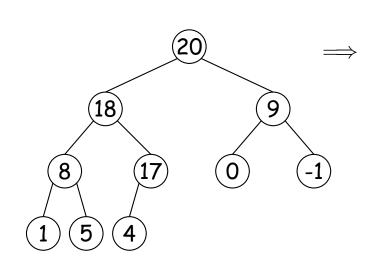


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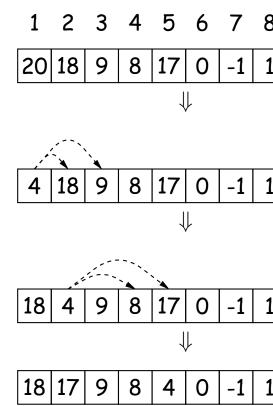
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Heaps in Arrays

- Since heaps are nearly complete (missing items only at bottom level), can use arrays for compact representation.
- Example of removal from last slide (dashed arrows show children):



Nodes stored in level order. Children of node at index #K are in 2K and 2K+1 if numbering from 1, or 2K+1 and 2K+2 if from 0.



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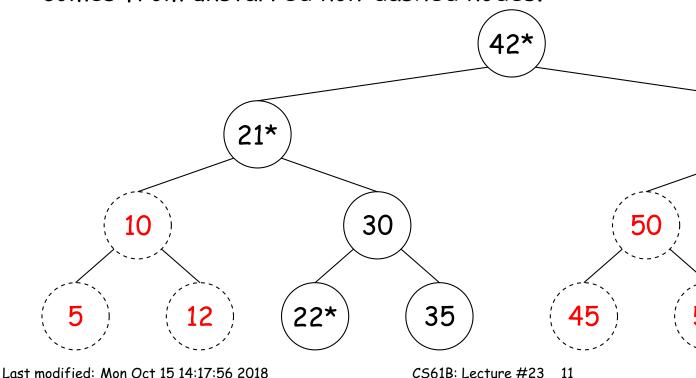
Ranges

- So far, have looked for specific items
- But for BSTs, need an ordering anyway, and can also support looking for ranges of values.
- Example: perform some action on all values in a BST that are within some range (in natural order):

```
/** Apply WHATTODO to all labels in T that are
   >= L and < U.
    * in ascending natural order. */
   static void visitRange(BST<String> T, String L,
   String U,
                             Consumer<BST<String>> whatToDo)
   {
     if (T != null) {
        int compLeft = L.compareTo(T.label ()),
            compRight = U.compareTo(T.label ());
        if (compLeft < 0)</pre>
                                               /* T. <
   label */
          visitRange (T.left(), L, U, whatToDo);
        if (compLeft <= 0 && compRight > 0) /* L <=
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```

Time for Range Queries

- Time for range query $\in O(h+M)$, where h is height of tree, and M is number of data items that turn out to be in the range.
- Consider searching the tree below for all values $25 \le x < 40$.
- ullet Dashed nodes are never looked at. Starred nodes are looked at but not output. The h comes from the starred nodes; the M comes from unstarred non-dashed nodes.



Ordered Sets and Range Queries in Java

- Class SortedSet supports range queries with views of set:
 - S.headSet(U): subset of S that is < U.
 - S.tailSet(L): subset that is \geq L.
 - S. subSet (L, U): subset that is \geq L, < U.
- Changes to views modify S.
- Attempts to, e.g., add to a headSet beyond U are disallowed.
- Can iterate through a view to process a range:

```
SortedSet<String> fauna = new TreeSet<String>
       (Arrays.asList ("axolotl", "elk", "dog",
"hartebeest", "duck"));
  for (String item : fauna.subSet ("bison", "gnu"))
      System.out.printf ("%s, ", item);
```

would print "dog, duck, elk,"

TreeSet

• Java library type TreeSet<T> requires either that T be Comparable, or that you provide a Comparator, as in:

```
SortedSet<String> rev_fauna = new TreeSet<String>(Col
```

• Comparator is a type of function object:

```
interface Comparator<T> {
     /** Return <0 if LEFT<RIGHT, >0 if LEFT>RIGHT,
else 0. */
    int compare(T left, T right);
}
```

(We'll deal with what Comparator<T extends Comparable<T>> is all about later.)

 For example, the reverseOrder comparator is defined like this:

```
return (x, y) -> y.compareTo(x);
}
```

Example of Representation: BSTSet

```
Same repre- SortedSet<String>
sentation for fauna = new
both sets and BSTSet<String>(stuff);
subset1 =
subsets.
fauna.subSet("bison", "gnu");
Pointer to BST, subset2 =
plus bounds (ifsubset1.subSet("axolotl", "dog");
any).
.size() is expensive!
```

