Recreation

What is the sum of the coefficients of

$$(1 - 3x + 3x^2)^{743}(1 + 3x - 3x^2)^{744}$$

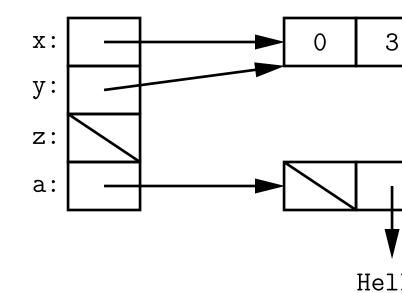
after expanding and collecting terms?

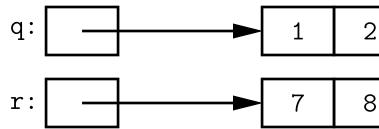
CS61B Lecture #5: Arrays

- An array is a structured container whose components are
 - length, a fixed integer.
 - a sequence of length simple containers of the same type, numbered from 0.
 - (.length field usually implicit in diagrams.)
- Arrays are anonymous, like other structured containers.
- Always referred to with pointers.
- For array pointed to by A,
 - Length is A.length
 - Numbered component i is A[i] (i is the index)
 - Important feature: index can be any integer expression.

A Few Samples

Java Results





Example: Accumulate Values

Problem: Sum up the elements of array A.

```
static int sum(int[] A) {
  int N;
  N = 0;
New (1.5) syntax
  for (int i = 0; i < A.length; i += 1)
(int x : A)
   N += A[i];
+= x;
  return N;
// For the hard-core: could have written
int N, i;
for (i=0, N=0; i<A.length; N += A[i], i +=</pre>
1)
  { } // or just ;
```

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// But please don't: it's obscure.

Example: Insert into an Array

(Aside) Java Shortcut

• Useful tip: Can write just 'arraycopy' by including at the top of the source file:

```
import static java.lang.System.arraycopy;
```

- This means "define the simple name arraycopy to be the equivalent of java.lang.System.arraycopy in the current source file."
- Can do the same for out so that you can write

```
out.println(...);
in place of
System.out.println(...);
```

• Finally, a declaration like

```
import static java.lang.Math.*;
```

means "take all the (public) static definitions in java.lang.Math and make them available in this source file by their simple names (the name after the last dot)."

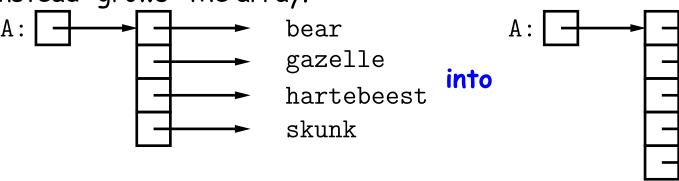
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• Useful for functions like sin, sqrt, etc.

Growing an Array

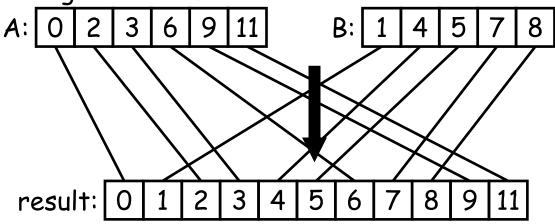
Problem: Suppose that we want to change the description above, so that A = insert2 (A, 2, "gnu") does not shove "skunk" off the end, but instead "grows" the array.



Why do we need a different return type from insert2??

Example: Merging

Problem: Given two sorted arrays of ints, A and B, produce their *merge*: a sorted array containing all items from A and B.



Example: Merging Program

Problem: Given two sorted arrays of ints, A and B, produce their *merge*: a sorted array containing all from A and B.

Remark: In order to solve this recursively, it is useful to *generalize* the original function to allow merging *portions* of the arrays.

```
/** Assuming A and B are sorted, returns their merge.
*/
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, 0, B, 0);
}
```

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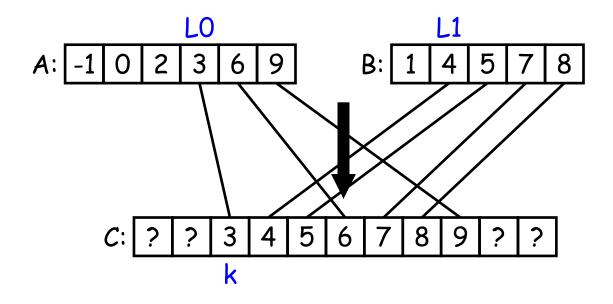
```
/** The merge of A[LO..] and B[L1..] assuming A
and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B,
int L1) {
   int N = A.length - LO + B.length - L1; int[]
                                                     is
C = new int[N];
   if (LO >= A.length) arraycopy(B, L1, this o, imple-
                                        mentation?
N);
  else if (L1 >= B.length) arraycopy(A, L0, C,
0, N);
   else if (A[L0] <= B[L1]) {</pre>
      C[0] = A[L0]; arraycopy(mergeTo(A, L0+1,
B, L1), O, C, 1, N-1);
   } else {
      C[0] = B[L1]; arraycopy(mergeTo(A, L0, B,
L1+1), 0, C, 1, N-1);
   }
   return C;
```

A Tail-Recursive Strategy

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length],
0);
}

/** Merge A[L0..] and B[L1..] into C[K..], assuming
A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int
L1, int[] C, int k){
    ...
}
```

This last method merges part of A with part of B into part of C. For example, consider a possible call mergeTo(A, 3, B, 1, C, 2)



```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length],
0);
}
/** Merge A[LO..] and B[L1..] into C[K..], assuming
A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int
L1, int[] C, int k){
   if (??) {
      return C;
   } else if (??) {
      C[k] = A[LO];
      return mergeTo(A, ??, B, ??, C, ??)
   } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
  }
}
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length],
0);
}
/** Merge A[LO..] and B[L1..] into C[K..], assuming
A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int
L1, int[] C, int k){
   if (L0 >= A.length && L1 >= B.length) {
      return C;
   } else if (??) {
      C[k] = A[LO];
      return mergeTo(A, ??, B, ??, C, ??)
   } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
  }
}
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length],
0);
}
/** Merge A[LO..] and B[L1..] into C[K..], assuming
A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int
L1, int[] C, int k){
   if (L0 >= A.length && L1 >= B.length) {
      return C;
   } else if (L1 >= B.length || (L0 < A.length &&
A[LO] <= B[L1])) {
      C[k] = A[L0];
      return mergeTo(A, ??, B, ??, C, ??)
   } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
  }
}
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length],
0);
}
/** Merge A[LO..] and B[L1..] into C[K..], assuming
A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int
L1, int[] C, int k){
   if (L0 >= A.length && L1 >= B.length) {
      return C;
   } else if (L1 >= B.length || (L0 < A.length &&
A[LO] <= B[L1])) {
      C[k] = A[L0];
      return mergeTo(A, L0 + 1, B, L1, C, k + 1);
   } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
  }
}
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length],
0);
}
/** Merge A[LO..] and B[L1..] into C[K..], assuming
A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int
L1, int[] C, int k){
   if (L0 >= A.length && L1 >= B.length) {
      return C;
   } else if (L1 >= B.length || (L0 < A.length &&
A[LO] <= B[L1])) {
      C[k] = A[L0];
      return mergeTo(A, L0 + 1, B, L1, C, k + 1);
   } else {
      C[k] = B[L1];
      return mergeTo(A, L0, B, L1 + 1, C, k + 1);
  }
}
```

Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int L0, L1, k;
   L0 = L1 = k = 0;

   while (??) {
      if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
            C[k] = A[L0];
            ??
      } else {
            C[k] = B[L1];
            ??
      }
   }
   return C;
}</pre>
```

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Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int L0, L1, k;
   L0 = L1 = k = 0;

while (L0 < A.length || L1 < B.length) {
      if (L1 >= B.length || (L0 < A.length && A[L0]) {
            C[k] = A[L0];
            ??
      } else {
            C[k] = B[L1];
            ??
      }
    }
   return C;
}</pre>
```

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Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int L0, L1, k;
   L0 = L1 = k = 0;

while (L0 < A.length || L1 < B.length) {
      if (L1 >= B.length || (L0 < A.length && A[L0]) {
            C[k] = A[L0];
            L0 += 1; k += 1;
      } else {
            C[k] = B[L1];
            L1 += 1; k += 1;
      }
    }
   return C;
}</pre>
```

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Iterative Solution II

public static int[] merge(int[] A, int[] B) {

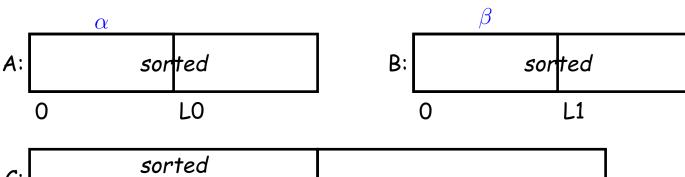
The same, with a for loop:

```
int[] C = new int[A.length + B.length];
   int LO, L1;
   L0 = L1 = 0;
   for (int k = 0; k < C.length; k += 1) {
        if (L1 >= B.length || (L0 < A.length && A[L0]
<= B[L1])) {
            C[k] = A[LO]; LO += 1;
       } else {
            C[k] = B[L1]; L1 += 1;
       }
   return C;
}
Invariant (true after int k = 0):
  0 \le L0 < A.length \land 0 \le L1 < B.length \land C.length = A.length +
  \wedge C[0:k] is a permutation of A[0:L0] + B[0:L1]
  \wedge C[0:k], A, B are sorted.
```

Alternative Solution: Removing k

Using previous invariant that k=L0+L1 simplifies things:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   int L0, L1; L0 = L1 = 0;
   while (L0 + L1 < C.length) {
      if (L1 >= B.length || (L0 < A.length && A[L0]) {
            C[L0 + L1] = A[L0]; L0 += 1;
      } else {
            C[L0 + L1] = B[L1]; L1 += 1;
      }
   }
   return C;
}</pre>
```



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Multidimensional Arrays

What about two- or higher-dimensional layouts, such as

?

Multidimensional Arrays in Java

These are not primitive in Java, but we can build them as arrays of arrays:

```
int[][] A = new int[3][];
   A[0] = new int[] \{2, 3, 4, 5\};
   A[1] = new int[] \{4, 9, 16,
25};
   A[2] = new int[] \{8, 27, 64,
125};
 // or
   int[][] A;
   A = new int[][] { {2, 3, 4,}}
5},
                         {4, 9, 16,
25},
                        A: A: 64
125} };
// or
                                                      27 64 12
   int[][] A = { {2, 3, 4, 5},}
                    {4, 9, 16, 25},
                    {8, 27, 64, 125}
};
 // or
   int[][] A = new A[3][4];
   for (int i = 0; i < 3; i += 1)
        for (int j = 0; j < 4; j
+= 1)
             A[i][j] = (int)
Math.pow(j + 2, i + 1);
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                                         CS61B: Lecture #5 29
```

Exotic Multidimensional Arrays

• Since every element of an array is independent, there is no single "width" in general:

```
int[][] A = new
int[5][];
  A[0] = new int[] {};
  A[1] = new int[] {0,
1};
  A[2] = new int[] {2,
3, 4, 5};
  A[3] = new int[] {6,
7, 8};
  A[4] = new int[] {9};
```

• What does this print?

```
int[][] ZERO = new
int[3][];
    ZERO[0] = ZERO[1] =

ZERO[2] =
        new int[] {0, 0,
0};
    ZERO[0][1] = 1;
    System.out.println(ZERO[2][1]);
```

Exotic Multidimensional Arrays

• Since every element of an array is independent, there is no single "width" in general:

```
int[][] A = new
int[5][];
  A[0] = new int[] {};
  A[1] = new int[] {0,
1};
  A[2] = new int[] {2,
3, 4, 5};
  A[3] = new int[] {6,
7, 8};
  A[4] = new int[] {9};
```

• What does this print?

```
int[][] ZERO = new
int[3][];
    ZERO[0] = ZERO[1] =
    ZERO[2] =
        new int[] {0, 0,
0};
    ZERO[0][1] = 1;
    System.out.println(ZERO[2][1]);
```