

## CS61B Lecture #4: Simple Pointer Manipulation

**Recreation** Prove that for every acute angle  $\alpha > 0$ ,

$$\tan \alpha + \cot \alpha \geq 2$$

### Announcements

- **Today:** More pointer hacking.
- **Handing in labs and homework:** We'll be lenient about accepting late homework and labs for lab1, lab2, and hw0. Just get it done: part of the point is getting to understand the tools involved. We will **not** accept submissions by email.
- We will feel free to interpret the absence of a central repository for you or a lack of a lab1 submission from you as indicating that you intend to drop the course.
- Project 0 to be released tonight.
- HW1 is released.

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## Small Test of Understanding

- In Java, the keyword **final** in a variable declaration means that the variable's value may not be changed after the variable is initialized.
- Is the following class valid?

```
public class Issue {  
  
    private final IntList aList = new IntList(0, null);  
  
    public void modify(int k) {  
        this.aList.head = k;  
    }  
}
```

Why or why not?

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## Small Test of Understanding

- In Java, the keyword **final** in a variable declaration means that the variable's value may not be changed after the variable is initialized.
- Is the following class valid?

```
public class Issue {  
  
    private final IntList aList = new IntList(0, null);  
  
    public void modify(int k) {  
        this.aList.head = k;  
    }  
}
```

Why or why not?

**Answer:** This is **valid**. Although `modify` changes the head variable of the object pointed to by `aList`, it does **not** modify the contents of `aList` itself (which is a pointer).

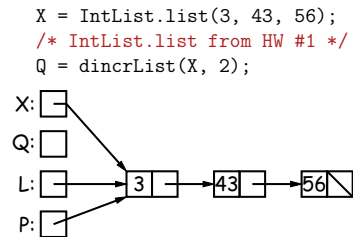
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## Destructive Incrementing

**Destructive** solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to L's items. */  
static IntList dincrList(IntList P, int n) {  
    if (P == null)  
        return null;  
    else {  
        P.head += n;  
        P.tail = dincrList(P.tail, n);  
        return P;  
    }  
}  
  
/** Destructively add N to L's items. */  
static IntList dincrList(IntList L, int n)  
{  
    // 'for' can do more than count!  
    for (IntList p = L; p != null; p = p.tail)  
        p.head += n;  
    return L;  
}
```



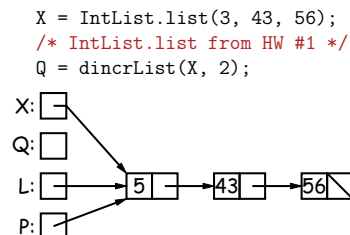
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    else {  
        P.head += n;  
        P.tail = dincrList(P.tail, n);  
        return P;  
    }  
}  
  
/** Destructively add N to L's items. */  
static IntList dincrList(IntList L, int n)  
{  
    // 'for' can do more than count!  
    for (IntList p = L; p != null; p = p.tail)  
        p.head += n;  
    return L;  
}
```



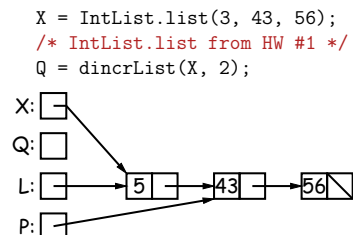
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## Destructive Incrementing

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        return null;  
    else {  
        P.head += n;  
        P.tail = dincrList(P.tail, n);  
        return P;  
    }  
}  
  
/** Destructively add N to L's items. */  
static IntList dincrList(IntList L, int n)  
{  
    // 'for' can do more than count!  
    for (IntList p = L; p != null; p = p.tail)  
        p.head += n;  
    return L;  
}
```



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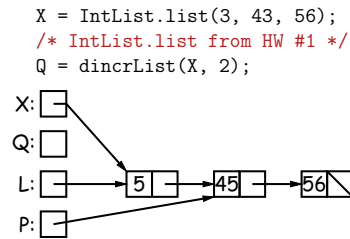
CS61B: Lecture #4 6

## Destructive Incrementing

**Destructive** solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to L's items. */
static IntList dincrList(IntList P, int n) {
    if (P == null)
        return null;
    else {
        P.head += n;
        P.tail = dincrList(P.tail, n);
        return P;
    }
}

/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
    // 'for' can do more than count!
    for (IntList p = L; p != null; p = p.tail)
        p.head += n;
    return L;
}
```



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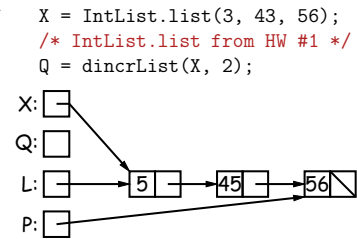
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## Destructive Incrementing

**Destructive** solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to L's items. */
static IntList dincrList(IntList P, int n) {
    if (P == null)
        return null;
    else {
        P.head += n;
        P.tail = dincrList(P.tail, n);
        return P;
    }
}

/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
    // 'for' can do more than count!
    for (IntList p = L; p != null; p = p.tail)
        p.head += n;
    return L;
}
```



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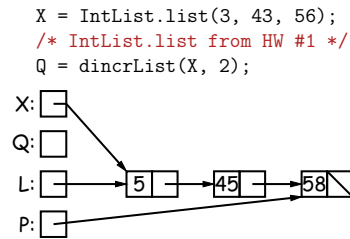
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## Destructive Incrementing

**Destructive** solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to L's items. */
static IntList dincrList(IntList P, int n) {
    if (P == null)
        return null;
    else {
        P.head += n;
        P.tail = dincrList(P.tail, n);
        return P;
    }
}

/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
    // 'for' can do more than count!
    for (IntList p = L; p != null; p = p.tail)
        p.head += n;
    return L;
}
```



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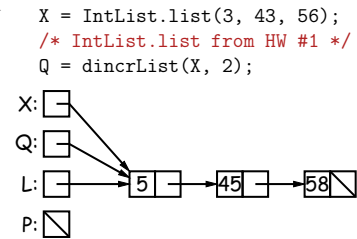
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## Destructive Incrementing

**Destructive** solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to L's items. */
static IntList dincrList(IntList P, int n) {
    if (P == null)
        return null;
    else {
        P.head += n;
        P.tail = dincrList(P.tail, n);
        return P;
    }
}

/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
{
    // 'for' can do more than count!
    for (IntList p = L; p != null; p = p.tail)
        p.head += n;
    return L;
}
```



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## Another Example: Non-destructive List Deletion

If L is the list [2, 1, 2, 9, 2], we want removeAll(L,2) to be the new list [1, 9].

```
/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return removeAll(L.tail, x);
    else
        return L.cons(removeAll(L.tail, x));
}
```

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## Another Example: Non-destructive List Deletion

If L is the list [2, 1, 2, 9, 2], we want removeAll(L,2) to be the new list [1, 9].

```
/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return removeAll(L.tail, x);
    else
        return L.cons(removeAll(L.tail, x));
}
```

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## Another Example: Non-destructive List Deletion

If L is the list [2, 1, 2, 9, 2], we want `removeAll(L,2)` to be the new list [1, 9].

```
/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return removeAll(L.tail, x);
    else
        return /*( L with all x's removed (L!=null, L.head!=x) )*/;
}
```

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## Another Example: Non-destructive List Deletion

If L is the list [2, 1, 2, 9, 2], we want `removeAll(L,2)` to be the new list [1, 9].

```
/** The list resulting from removing all instances of X from L
 * non-destructively. */
static IntList removeAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return removeAll(L.tail, x);
    else
        return new IntList(L.head, removeAll(L.tail, x));
}
```

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## Iterative Non-destructive List Deletion

Same as before, but use front-to-back iteration rather than recursion.

```
/** The list resulting from removing all instances
 * of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    for ( ; L != null; L = L.tail) {
        if (x == L.head)
            continue;
        else if (last == null)
            result = last = new IntList(L.head, null);
        else
            last = last.tail = new IntList(L.head, null);
    }
    return result;
}
```

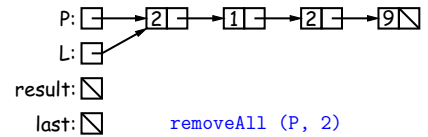
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    }
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            result = last = new IntList(L.head, null);
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            last = last.tail = new IntList(L.head, null);
    }
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}
```

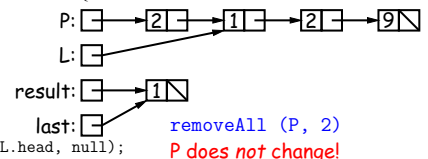
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    }
    return result;
}
```



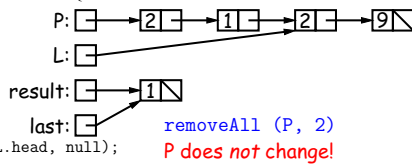
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    return result;
}
```



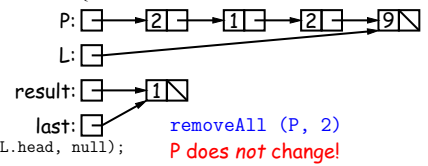
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        else if (last == null)
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        else
            last = last.tail = new IntList(L.head, null);
    }
    return result;
}
```



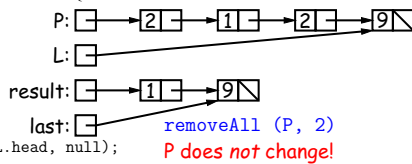
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## Iterative Non-destructive List Deletion

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        else if (last == null)
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        else
            last = last.tail = new IntList(L.head, null);
    }
    return result;
}
```



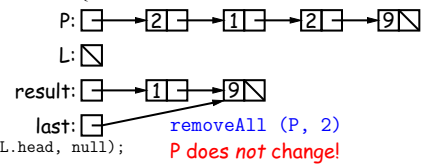
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        if (x == L.head)
            continue;
        else if (last == null)
            result = last = new IntList(L.head, null);
        else
            last = last.tail = new IntList(L.head, null);
    }
    return result;
}
```

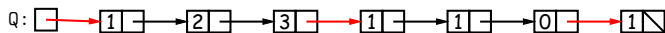


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## Destructive Deletion

→ : Original      ..... : after Q = dremoveAll (Q,1)



```
/** The list resulting from removing all instances of X from L.
 * The original list may be destroyed. */
static IntList dremoveAll(IntList L, int x) {
    if (L == null)
        return /*( null with all x's removed )*/;
    else if (L.head == x)
        return /*( L with all x's removed (L != null) )*/;
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

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## Destructive Deletion

→ : Original      ..... : after Q = dremoveAll (Q,1)



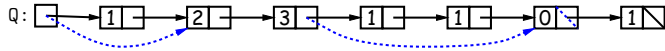
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        return /*( L with all x's removed (L != null) )*/;
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

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## Destructive Deletion

→ : Original      ..... : after Q = dremoveAll (Q,1)



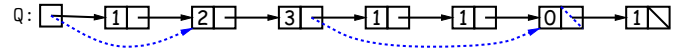
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    else if (L.head == x)
        return /*( L with all x's removed (L != null) )*/;
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

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## Destructive Deletion

→ : Original      ..... : after Q = dremoveAll (Q,1)



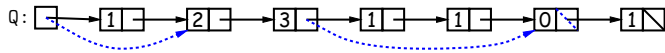
```
/** The list resulting from removing all instances of X from L.
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    else if (L.head == x)
        return /*( L with all x's removed (L != null) )*/;
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

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## Destructive Deletion

→ : Original      ..... : after Q = dremoveAll (Q,1)



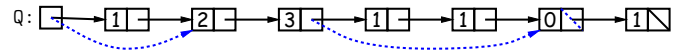
```
/** The list resulting from removing all instances of X from L.
 * The original list may be destroyed. */
static IntList dremoveAll(IntList L, int x) {
    if (L == null)
        return null;
    else if (L.head == x)
        return /*( L with all x's removed (L != null) )*/;
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

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## Destructive Deletion

→ : Original      ..... : after Q = dremoveAll (Q,1)



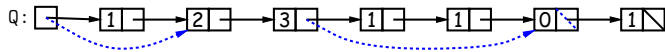
```
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 * The original list may be destroyed. */
static IntList dremoveAll(IntList L, int x) {
    if (L == null)
        return
    else if (L.head == x)
        return dremoveAll(L.tail, x);
    else {
        /*{ Remove all x's from L's tail. }*/;
        return L;
    }
}
```

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## Destructive Deletion

→ : Original      ..... : after Q = dremoveAll (Q,1)



```
/** The list resulting from removing all instances of X from L.
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static IntList dremoveAll(IntList L, int x) {
    if (L == null)
        return
    else if (L.head == x)
        return dremoveAll(L.tail, x);
    else {
        L.tail = dremoveAll(L.tail, x);
        return L;
    }
}
```

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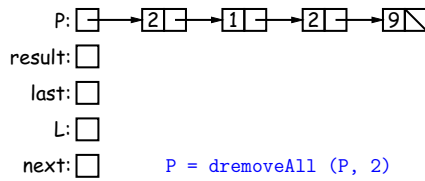
## Iterative Destructive Deletion

```
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L.tail = null;
        }
        L = next;
    }
    return result;
}
```

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## Iterative Destructive Deletion



/\*\* The list resulting from removing all X's from L

\* destructively. \*/

```
static IntList dremoveAll(IntList L, int x) {
```

```
    IntList result, last;
```

```
    result = last = null;
```

```
    while (L != null) {
```

```
        IntList next = L.tail;
```

```
        if (x != L.head) {
```

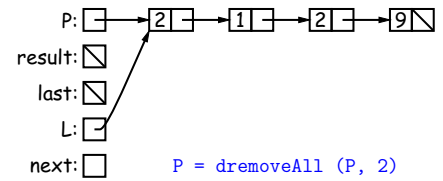
```
            if (last == null)
```

```
                result = last = L;
```

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## Iterative Destructive Deletion



/\*\* The list resulting from removing all X's from L

\* destructively. \*/

```
static IntList dremoveAll(IntList L, int x) {
```

```
    IntList result, last;
```

```
    result = last = null;
```

```
    while (L != null) {
```

```
        IntList next = L.tail;
```

```
        if (x != L.head) {
```

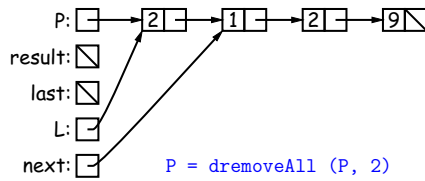
```
            if (last == null)
```

```
                result = last = L;
```

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## Iterative Destructive Deletion



/\*\* The list resulting from removing all X's from L

\* destructively. \*/

```
static IntList dremoveAll(IntList L, int x) {
```

```
    IntList result, last;
```

```
    result = last = null;
```

```
    while (L != null) {
```

```
        IntList next = L.tail;
```

```
        if (x != L.head) {
```

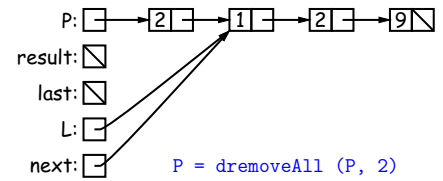
```
            if (last == null)
```

```
                result = last = L;
```

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## Iterative Destructive Deletion



/\*\* The list resulting from removing all X's from L

\* destructively. \*/

```
static IntList dremoveAll(IntList L, int x) {
```

```
    IntList result, last;
```

```
    result = last = null;
```

```
    while (L != null) {
```

```
        IntList next = L.tail;
```

```
        if (x != L.head) {
```

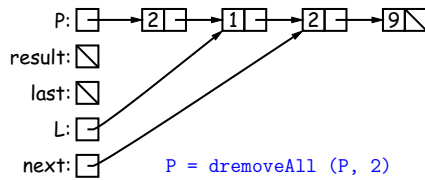
```
            if (last == null)
```

```
                result = last = L;
```

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## Iterative Destructive Deletion



/\*\* The list resulting from removing all X's from L

\* destructively. \*/

```
static IntList dremoveAll(IntList L, int x) {
```

```
    IntList result, last;
```

```
    result = last = null;
```

```
    while (L != null) {
```

```
        IntList next = L.tail;
```

```
        if (x != L.head) {
```

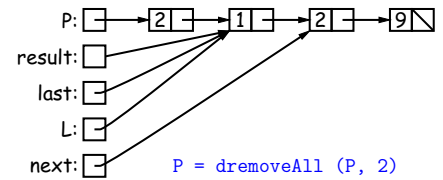
```
            if (last == null)
```

```
                result = last = L;
```

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## Iterative Destructive Deletion



/\*\* The list resulting from removing all X's from L

\* destructively. \*/

```
static IntList dremoveAll(IntList L, int x) {
```

```
    IntList result, last;
```

```
    result = last = null;
```

```
    while (L != null) {
```

```
        IntList next = L.tail;
```

```
        if (x != L.head) {
```

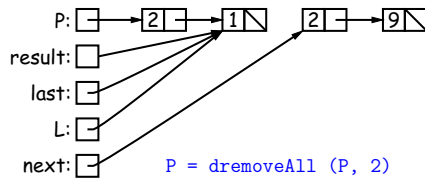
```
            if (last == null)
```

```
                result = last = L;
```

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## Iterative Destructive Deletion



```

P = dremoveAll (P, 2)

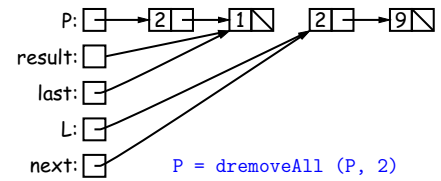
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;

```

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## Iterative Destructive Deletion



```

P = dremoveAll (P, 2)

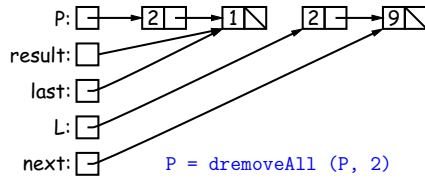
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;

```

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## Iterative Destructive Deletion



```

P = dremoveAll (P, 2)

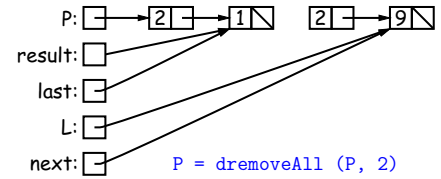
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;

```

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## Iterative Destructive Deletion



```

P = dremoveAll (P, 2)

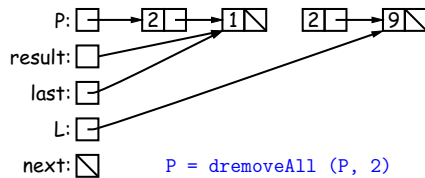
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;

```

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## Iterative Destructive Deletion



```

P = dremoveAll (P, 2)

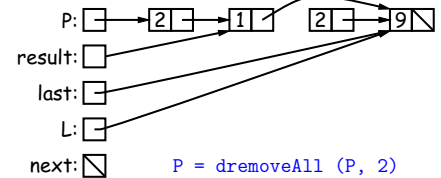
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;

```

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## Iterative Destructive Deletion



```

P = dremoveAll (P, 2)

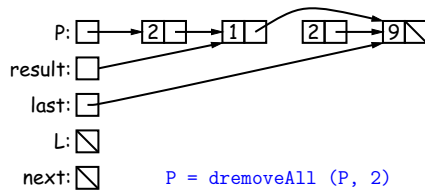
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;

```

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## Iterative Destructive Deletion



```

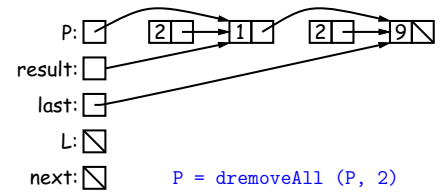
/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L = next;
        }
    }
    return result;
}

```

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## Iterative Destructive Deletion



```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L = next;
        }
    }
    return result;
}

```

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## Aside: How to Write a Loop (in Theory)

- Try to give a description of how things look on *any arbitrary iteration* of the loop.
  - This description is known as a *loop invariant*, because it is always true at the start of each iteration.
  - The loop body then must
    - Start from any situation consistent with the invariant;
    - Make progress in such a way as to make the invariant true again.
- ```

// Invariant must be true here
while (condition) { // condition must not have side-effects.
    // (Invariant will necessarily be true here.)
    loop body
    // Invariant must again be true here
}
// Invariant true and condition false.

```
- So if our loop gets the desired answer whenever *Invariant* is true and *condition* false, our job is done!

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## Relationship to Recursion

- Another way to see this is to consider an equivalent recursive procedure:

```

/** Assuming Invariant, produce a situation where Invariant
 * is true and condition is false. */
void loop() {
    // Invariant assumed true here.
    if (condition) {
        loop body
        // Invariant must be true here.
        loop()
        // Invariant true here and condition false.
    }
}

```

- Here, the invariant is the precondition of the function `loop`.
- The loop maintains the invariant while making the condition false.
- Idea is to arrange that our actual goal is implied by this post-condition.

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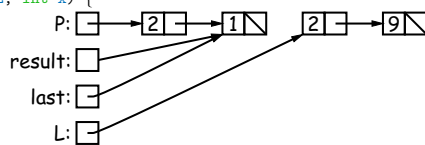
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## Example: Loop Invariant for dremoveAll

```

/** The list resulting from removing all X's from L
 * destructively. */
static IntList dremoveAll(IntList L, int x) {
    IntList result, last;
    result = last = null;
    while ** (L != null) {
        IntList next = L.tail;
        if (x != L.head) {
            if (last == null)
                result = last = L;
            else
                last = last.tail = L;
            L = next;
        }
    }
    return result;
}

```



- \*\* Invariant:**
- result points to the list of items in the final result except for those from L onward.
  - L points to an unchanged tail of the original list of items in L.
  - last points to the last item in result or is null if result is null.

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