Administrivia

- Please make sure you have obtained a Unix account. If you have very recently (i.e., since today) signed up for concurrent enrollment please email us your name, email, and SID. After we have a chance to process it, you will be able to use WebAcct, as Lab #1 specifies.
- Lab #1 is due Wednesday (end of Wednesday at midnight). Usually, labs are due Friday midnight of the week they occur. It is especially important to set up your central reppository.
- If you decide not to take this course after all, please tell CalCentral ASAP, so that we can adjust the waiting list accordingly.
- HW #0 now up; due next Friday at midnight. You get credit for any submission, but we suggest you give the problems a serious try.

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Lecture #2: Let's Write a Program: Prime Numbers

Problem: want java Primes U to print prime numbers through U.

You type: java Primes 101

It types: 2 3 5 7 11 13 17 19 23 29

31 37 41 43 47 53 59 61 67 71

73 79 83 89 97 101

Definition: A prime number is an integer greater than 1 that has no divisors smaller than itself other than 1.

(Alternatively: p > 1 is prime iff gcd(p, x) = 1for all 0 < x < p.)

Useful Facts:

- $k \leq \sqrt{N}$ iff $N/k \geq \sqrt{N}$, for N, k > 0.
- If k divides N then N/k divides N.

So: Try all potential divisors up to and including the square root.

Plan

```
public class Primes {
  /** Print all primes up to ARGS[0] (interpreted
as an
      integer), 10 to a line. */
  public static void main(String[] args) {
    printPrimes(Integer.parseInt(args[0]));
  /** Print all primes up to and including
LIMIT, 10 to
      a line. */
  private static void printPrimes(int limit)
    /*{ For every integer, x, between 2 and
LIMIT, print it if
        isPrime(x), 10 to a line. }*/
  }
  /** True iff X is prime */
  private static boolean isPrime(int x) {
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```

```
return /*( X is prime )*/;
}
```

Testing for Primes

```
private static boolean isPrime(int x) {
  if (x <= 1)
    return false;
  else
    return !isDivisible(x, 2); // "!" means
"not"
}
/** True iff X is divisible by any positive
number \geq = K and \leq X,
 * given K > 1. */
private static boolean isDivisible(int x,
int k) {
  if (k >= x)
                          // a "guard"
    return false;
  else if (x % k == 0) // "%" means "remainder"
    return true;
  else // if (k < x && x % k != 0)
    return isDivisible(x, k+1);
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```

Thinking Recursively

Understand and check isDivisible(13,2) by tracing one level.

```
/** True iff X is divisible
by
  * some number >=K and < X,
  * given K > 1. */
private static boolean
isDivisible...
  if (k >= x)
    return false;
  else if (x % k == 0)
    return true;
  else
    return isDivisible(x,
k+1);
}
```

Lesson: Comments aid understanding. Make them count!

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- Call assigns x=13, k=2
- Body has form 'if $(k \ge x)$ S_1 else S_2 '.
- ullet Since 2 < 13, we evaluate the first else.
- Check if $13 \mod 2 = 0$; it's not.
- Left with isDivisible(13,3).
- Rather than tracing it, instead use the comment:
- Since 13 is not divisible by any integer in the range 3..12 (and 3 > 1), isDivisible(13,3) mustiblectufatse, and we're done!
- Sounds like that last step begs the question.

Iteration

- isDivisible is tail recursive, and so creates an iterative process.
- Traditional "Algol family" production languages have special syntax for iteration. Four equivalent versions of isDivisible:

```
if (k >= x)
                           while (k < x) { //
                         !(k >= x)
    return false;
  else if (x \% k == 0)
                             if (x \% k == 0)
    return true;
                               return true;
                             k = |k+1|;
  else
                             // or k += 1, or
    return
                         (yuch) k++
isDivisible(x, k+1);
                           return false;
```

Using Facts about Primes

- We haven't used the Useful Facts from an earlier slide. Only have to check for divisors up to the square root.
- So, reimplement the iterative version of isDivisible:

```
/** True iff X is divisible by some number
>=K and < X,
  * given that K > 1, and that X is not
divisible by
  * any number >1 and <K. */
private static boolean isDivisible(int
  x, int k) {
  int limit = (int) Math.round(Math.sqrt(x));
  for (int k1 = k; k1 <= limit; k1 += 1)
{
   if (x % k1 == 0)
     return true;
  }
  return false;
}</pre>
```

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 Why the additional (blue) condition in the comment?

Cautionary Aside: Floating Point

In the last slide, we had

```
int limit = (int) Math.round(Math.sqrt(x));
 for (int k1 = k; k1 \le limit; k1 += 1)
{
```

intending that this would check all values of k1 up to and including the square root of x.

- Since floating-point operations yield approximations to the corresponding mathematical operations, you might ask the following about (int) Math.round(Math.sqrt(x)):
 - Is it always at least $|\sqrt{x}|$, where |z| is the largest integer $\leq z$? (If not, we might miss testing \sqrt{x} when x is a perfect square.)
- As it happens, the answer is "yes" for IEEE floating-point square roots.
- Just an example of the sort of detail that must be checked in edge cases.

Final Task: printPrimes (Simplified)

```
/** Print all primes up to and including LIMIT.
*/
private static void printPrimes(int limit)
{
```

}

Simplified printPrimes Solution

```
/** Print all primes up to and including LIMIT.
*/
private static void printPrimes(int limit)
    for (int p = 2; p <= limit; p += 1) {</pre>
        if (isPrime(p)) {
            System.out.print(p + " ");
    System.out.println();
```

printPrimes (full version)

```
/** Print all primes up to and including LIMIT,
10 to
 * a line. */
private static void printPrimes(int limit)
    int np;
    np = 0;
    for (int p = 2; p <= limit; p += 1) {</pre>
        if (isPrime(p)) {
            System.out.print(p + " ");
            np += 1;
            if (np % 10 == 0)
                System.out.println();
    if (np % 10 != 0)
        System.out.println();
```