Recreation

What is the sum of the coefficients of

$$(1 - 3x + 3x^2)^{743}(1 + 3x - 3x^2)^{744}$$

after expanding and collecting terms?

CS61B Lecture #5: Arrays

- An array is a structured container whose components are
 - length, a fixed integer.
 - a sequence of length simple containers of the same type, numbered from 0.
 - (.length field usually implicit in diagrams.)
- Arrays are anonymous, like other structured containers.
- Always referred to with pointers.
- For array pointed to by A,
 - Length is A.length
 - Numbered component i is A[i] (i is the index)
 - Important feature: index can be any integer expression.

A Few Samples

Java

Results

```
int[] x, y, z;
                                                                3
                                     x:
String[] a;
                                     y:
x = new int[3];
y = x;
                                     z:
a = new String[3];
                                     a:
x[1] = 2;
y[1] = 3;
a[1] = "Hello";
                                                             Hello
int[] q;
q = new int[] { 1, 2, 3 };
                                     q:
                                                                     3
                                                                2
// Short form for declarations:
int[] r = { 7, 8, 9 };
                                                                     9
                                     r:
```

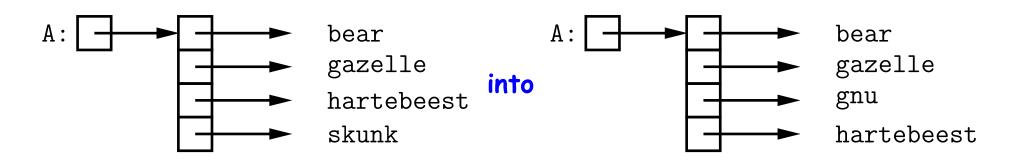
Example: Accumulate Values

Problem: Sum up the elements of array A.

```
static int sum(int[] A) {
  int N;
                                                   // New (1.5) syntax
  N = 0;
  for (int i = 0; i < A.length; i += 1)
                                                    for (int x : A)
    N += A[i];
                                                       \mathbb{N} += x;
  return N;
// For the hard-core: could have written
int N, i;
for (i=0, N=0; i<A.length; N += A[i], i += 1)</pre>
  { } // or just ;
// But please don't: it's obscure.
```

Example: Insert into an Array

Problem: Want a call like insert(A, 2, "gnu") to convert (destructively)



(Aside) Java Shortcut

• Useful tip: Can write just 'arraycopy' by including at the top of the source file:

```
import static java.lang.System.arraycopy;
```

- This means "define the simple name arraycopy to be the equivalent of java.lang.System.arraycopy in the current source file."
- Can do the same for out so that you can write

```
out.println(...);
in place of
System.out.println(...);
```

Finally, a declaration like

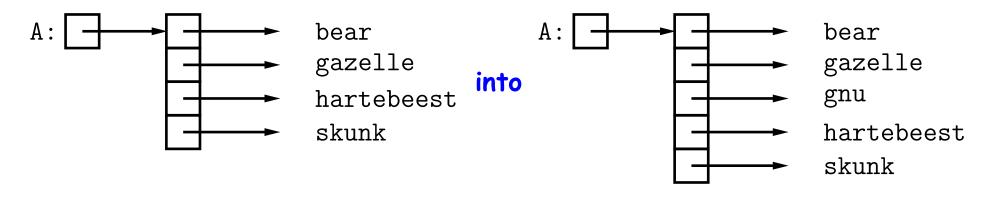
```
import static java.lang.Math.*;
```

means "take all the (public) static definitions in java.lang.Math and make them available in this source file by their simple names (the name after the last dot)."

• Useful for functions like sin, sqrt, etc.

Growing an Array

Problem: Suppose that we want to change the description above, so that A = insert2 (A, 2, "gnu") does not shove "skunk" off the end, but instead "grows" the array.

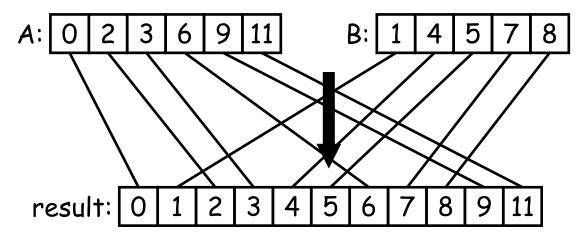


```
/** Return array, r, where r.length = ARR.length+1; r[0..K-1]
  * the same as ARR[0..K-1], r[k] = x, r[K+1..] same as ARR[K..]. */
static String[] insert2(String[] arr, int k, String x) {
  String[] result = new String[arr.length + 1];
  arraycopy(arr, 0, result, 0, k);
  arraycopy(arr, k, result, k+1, arr.length-k);
  result[k] = x;
  return result;
}
```

Why do we need a different return type from insert2??

Example: Merging

Problem: Given two sorted arrays of ints, A and B, produce their merge: a sorted array containing all items from A and B.



Example: Merging Program

Problem: Given two sorted arrays of ints, A and B, produce their merge: a sorted array containing all from A and B.

Remark: In order to solve this recursively, it is useful to generalize the original function to allow merging portions of the arrays.

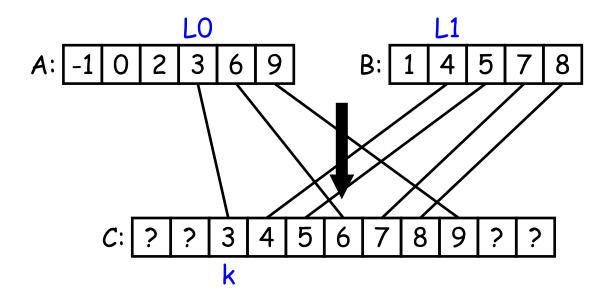
```
/** Assuming A and B are sorted, returns their merge. */
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, 0, B, 0);
/** The merge of A[LO..] and B[L1..] assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1) {
   int N = A.length - LO + B.length - L1; int[] C = new int[N];
   if (L0 >= A.length) arraycopy(B, L1, C, 0, N);
                                                           What is wrong with
   else if (L1 >= B.length) arraycopy(A, L0, C, 0, N);
                                                           this implementation?
   else if (A[L0] <= B[L1]) {</pre>
      C[0] = A[L0]; arraycopy(mergeTo(A, L0+1, B, L1), 0, C, 1, N-1);
   } else {
      C[0] = B[L1]; arraycopy(mergeTo(A, L0, B, L1+1), 0, C, 1, N-1);
   return C;
```

A Tail-Recursive Strategy

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
    ...
}
```

This last method merges part of A with part of B into part of C. For example, consider a possible call mergeTo(A, 3, B, 1, C, 2)



```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, int k){
   if (??) {
     return C;
   } else if (??) {
     C[k] = A[LO];
      return mergeTo(A, ??, B, ??, C, ??)
   } else {
      C[k] = B[L1];
     return mergeTo(A, ??, B, ??, C, ??)
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, int k){
   if (L0 \ge A.length \&\& L1 \ge B.length) {
      return C;
   } else if (??) {
     C[k] = A[LO];
      return mergeTo(A, ??, B, ??, C, ??)
   } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, int k){
   if (L0 \ge A.length \&\& L1 \ge B.length) {
      return C;
   } else if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {</pre>
      C[k] = A[LO]:
      return mergeTo(A, ??, B, ??, C, ??)
  } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, int k){
   if (L0 \ge A.length \&\& L1 \ge B.length) {
      return C;
   } else if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {</pre>
      C[k] = A[LO]:
      return mergeTo(A, L0 + 1, B, L1, C, k + 1);
   } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, int k){
   if (L0 \ge A.length \&\& L1 \ge B.length) {
      return C;
   } else if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {</pre>
      C[k] = A[LO]:
      return mergeTo(A, L0 + 1, B, L1, C, k + 1);
   } else {
      C[k] = B[L1];
      return mergeTo(A, LO, B, L1 + 1, C, k + 1);
```

Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int LO, L1, k;
   L0 = L1 = k = 0:
   while (??) {
       if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
           C[k] = A[LO];
           ??
       } else {
           C[k] = B[L1];
           ??
   return C;
```

Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, O, B, O, C, O)
   int LO, L1, k;
   L0 = L1 = k = 0;
   while (LO < A.length | L1 < B.length) {
       if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
           C[k] = A[LO];
           ??
       } else {
           C[k] = B[L1];
           ??
  return C;
```

Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int LO, L1, k;
   L0 = L1 = k = 0;
   while (LO < A.length | L1 < B.length) {
       if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
           C[k] = A[LO];
           L0 += 1; k += 1;
       } else {
          C[k] = B[L1];
          L1 += 1; k += 1;
   return C;
```

Iterative Solution II

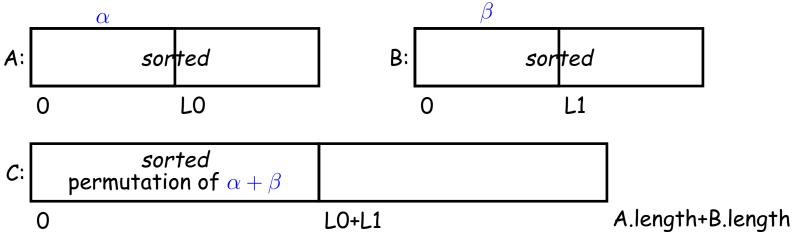
The same, with a for loop:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   int LO, L1;
   L0 = L1 = 0;
   for (int k = 0; k < C.length; k += 1) {
        if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
            C[k] = A[LO]; LO += 1;
       } else {
            C[k] = B[L1]; L1 += 1;
   return C;
Invariant (true after int k = 0):
  0 \le L0 \le A.length \land 0 \le L1 \le B.length \land C.length = A.length + B.length \land k = L0 + L1
  \wedge C[0:k] is a permutation of A[0:L0] + B[0:L1]
  \wedge C[0:k], A, B are sorted.
```

Alternative Solution: Removing k

Using previous invariant that k=L0+L1 simplifies things:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   int L0, L1; L0 = L1 = 0;
   while (L0 + L1 < C.length) {
      if (L1 >= B.length || (L0 < A.length && A[L0] < B[L1])) {
            C[L0 + L1] = A[L0]; L0 += 1;
      } else {
            C[L0 + L1] = B[L1]; L1 += 1;
      }
   }
   return C;
}</pre>
```



Multidimensional Arrays

What about two- or higher-dimensional layouts, such as

Multidimensional Arrays in Java

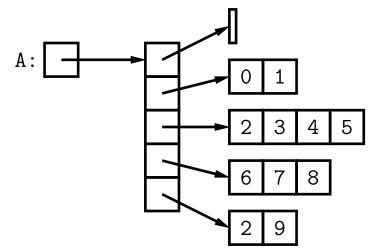
These are not primitive in Java, but we can build them as arrays of arrays:

```
int[][] A = new int[3][];
 A[0] = new int[] \{2, 3, 4, 5\};
 A[1] = new int[] \{4, 9, 16, 25\};
 A[2] = new int[] \{8, 27, 64, 125\};
// or
  int[][] A;
 A = new int[][] { {2, 3, 4, 5},}
                    {4, 9, 16, 25},
                    { 8, 27, 64, 125} };
                                                                     16 25
// or
  int[][] A = { {2, 3, 4, 5},}
                {4, 9, 16, 25},
                {8, 27, 64, 125} };
// or
  int[][] A = new A[3][4];
 for (int i = 0; i < 3; i += 1)
      for (int j = 0; j < 4; j += 1)
          A[i][j] = (int) Math.pow(j + 2, i + 1);
```

Exotic Multidimensional Arrays

• Since every element of an array is independent, there is no single "width" in general:

```
int[][] A = new int[5][];
A[0] = new int[] \{\};
A[1] = new int[] \{0, 1\};
A[2] = new int[] \{2, 3, 4, 5\};
A[3] = \text{new int}[] \{6, 7, 8\};
A[4] = new int[] \{9\};
```



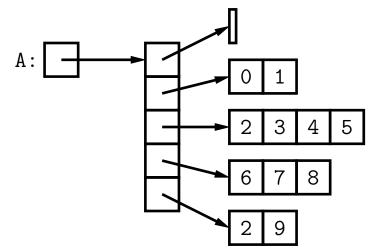
What does this print?

```
int[][] ZERO = new int[3][];
ZERO[0] = ZERO[1] = ZERO[2] =
    new int[] {0, 0, 0};
ZERO[0][1] = 1;
System.out.println(ZERO[2][1]);
```

Exotic Multidimensional Arrays

• Since every element of an array is independent, there is no single "width" in general:

```
int[][] A = new int[5][];
A[0] = new int[] {};
A[1] = new int[] {0, 1};
A[2] = new int[] {2, 3, 4, 5};
A[3] = new int[] {6, 7, 8};
A[4] = new int[] {9};
```



What does this print?

```
int[][] ZERO = new int[3][];
ZERO[0] = ZERO[1] = ZERO[2] =
    new int[] {0, 0, 0};
ZERO[0][1] = 1;
System.out.println(ZERO[2][1]);
```

