CS61B Lecture #6: More Iteration: Sort an Array

Problem. Print out the command-line arguments in lexicographic order:

```
  % java sort the quick brown fox jumped over
the lazy dog
  brown dog fox jumped lazy over quick the
the
```

Plan.

```
public class Sort {
  /** Sort and print WORDS lexicographically. */
  public static void main(String[] words) {
    sort(words, 0, words.length-1);
    print(words);
  }

  /** Sort items A[L..U], with all others unchanged.
*/
  static void sort(String[] A, int L, int U) { /*
"TOMORROW" */ }
```

```
  /** Print A on one line, separated by blanks. */
  static void print(String[] A) { /* "TOMORROW" */
}
}
```

How do We Know If It Works?

- *Unit testing* refers to the testing of individual units (methods, classes) within a program, rather than the whole program.
- In this class, we mainly use the JUnit tool for unit testing.
- Example: `AGTestYear.java` in lab #1.
- *Integration testing* refers to the testing of entire (integrated) set of modules—the whole program.
- In this course, we'll look at various ways to run the program against prepared inputs and checking the output.
- *Regression testing* refers to testing with the specific goal of checking that fixes, enhancements, or other changes have not introduced faults (regressions).

Test-Driven Development

- Idea: write tests first.
- Implement unit at a time, run tests, fix and refactor until it works.
- We're not really going to push it in this course, but it is useful and has quite a following.

Testing sort

- This is pretty easy: just give a bunch of arrays to `sort` and then make sure they each get sorted properly.
- Have to make sure we cover the necessary cases:
  - *Corner cases.* E.g., empty array, one-element, all elements the same.
  - *Representative "middle" cases.* E.g., elements reversed, elements in order, one pair of elements reversed, ...

Simple JUnit

- The JUnit package provides some handy tools for unit testing.
- The Java annotation `@Test` on a method tells the JUnit machinery to call that method.
- (An *annotation* in Java provides information about a method, class, etc., that can be examined within Java itself.)
- A collection of methods with names beginning with `assert` then allow your test cases to check conditions and report failures.
- [See example.]

Selection Sort

```
/** Sort items A[L..U], with all others unchanged
*/
static void sort(String[] A, int L, int U)
{
  if (L < U) {
    int k = /*( Index s.t. A[k] is largest in
A[L],...,A[U] )*/;
    /*{ swap A[k] with A[U] }*/;
    /*{ Sort items L to U-1 of A. }*/;
  }
}
```

And we're done! Well, OK, not quite.

Selection Sort

```
/** Sort items A[L..U], with all others unchanged
*/
static void sort(String[] A, int L, int U)
{
  if (L < U) {
    int k = indexOfLargest(A, L, U);
    /*{ swap A[k] with A[U] }*/;
    /*{ Sort items L to U-1 of A. }*/;
  }
}

/** Index k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
    ...
}
```

Selection Sort

```
/** Sort items A[L..U], with all others unchanged
*/
static void sort(String[] A, int L, int U)
{
  if (L < U) {
    int k = indexOfLargest(A, L, U);
    /*{ swap A[k] with A[U] }*/;
    sort(A, L, U-1);       // Sort items L
to U-1 of A
  }
}

/** Index k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
    ...
}
```

Selection Sort

```
/** Sort items A[L..U], with all others unchanged
*/
static void sort(String[] A, int L, int U)
{
  if (L < U) {
    int k = indexOfLargest(A, L, U);
    String tmp = A[k];  A[k] = A[U]; A[U]
= tmp;
    sort(A, L, U-1);      // Sort items L
to U-1 of A
  }
}

/** Index k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
    ...
}
```

Selection Sort

```
/** Sort items A[L..U], with all others unchanged
*/
static void sort(String[] A, int L, int U)
{
  if (L < U) {
    int k = indexOfLargest(A, L, U);
    String tmp = A[k];  A[k] = A[U]; A[U]
= tmp;
    sort(A, L, U-1);       // Sort items L
to U-1 of A
  }
}
```

What would an iterative version look like?

```
  while (?) {
    ?
  }
```

Selection Sort

```
/** Sort items A[L..U], with all others unchanged
*/
static void sort(String[] A, int L, int U)
{
  if (L < U) {
    int k = indexOfLargest(A, L, U);
    String tmp = A[k];  A[k] = A[U]; A[U]
= tmp;
    sort(A, L, U-1);       // Sort items L
to U-1 of A
  }
}
```

Iterative version:

```
  while (L < U) {
    int k = indexOfLargest(A, L, U);
    String tmp = A[k];  A[k] = A[U]; A[U]
= tmp;
    U -= 1;
  }
```

Find Largest

```
/** Index k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
  if (?)
    return i1;
  else  {


  }
}
```

Find Largest

```
/** Index k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
  if (i0 >= i1)
    return i1;
  else /* if (i0 < i1) */ {


  }
}
```

Find Largest

```
/** Index k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
  if (i0 >= i1)
    return i1;
  else /* if (i0 < i1) */ {
    int k = /*( index of largest value in
V[i0 + 1..i1] )*/;
    return /*( whichever of i0 and k has larger
value )*/;
  }
}
```

Find Largest

```
/** Index k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
  if (i0 >= i1)
    return i1;
  else /* if (i0 < i1) */ {
    int k = indexOfLargest(V, i0 + 1, i1);
    return /*( whichever of i0 and k has larger
value )*/;
  }
}
```

Find Largest

```
/** Index k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
  if (i0 >= i1)
    return i1;
  else /* if (i0 < i1) */ {
    int k = indexOfLargest(V, i0 + 1, i1);
    return (V[i0].compareTo(V[k]) > 0) ? i0
: k;
    // if (V[i0].compareTo(V[k]) > 0) return
i0; else return k;
  }
}
```

- Turning this into an iterative version is tricky: not tail recursive.
- What are the arguments to `compareTo` the first time it's called?

Iteratively Find Largest

```
/** Value k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
  if (i0 >= i1)
    return i1;
  else /* if (i0 < i1) */ {
    int k = indexOfLargest(V, i0 + 1, i1);
    return (V[i0].compareTo(V[k]) > 0) ? i0 : k;
    // if (V[i0].compareTo(V[k]) > 0) return
i0; else return k;
  }
}
```

Iterative:

```
  int i, k;
  k = ?;     // Deepest iteration
  for (i = ?; ...?; i ...?)
    k = ?;
  return k;
```

Iteratively Find Largest

```
/** Value k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
  if (i0 >= i1)
    return i1;
  else /* if (i0 < i1) */ {
    int k = indexOfLargest(V, i0 + 1, i1);
    return (V[i0].compareTo(V[k]) > 0) ? i0 : k;
    // if (V[i0].compareTo(V[k]) > 0) return
i0; else return k;
  }
}
```

Iterative:

```
  int i, k;
  k = i1;     // Deepest iteration
  for (i = ?; ...?; i ...?)
    k = ?;
  return k;
```

Iteratively Find Largest

```
/** Value k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
  if (i0 >= i1)
    return i1;
  else /* if (i0 < i1) */ {
    int k = indexOfLargest(V, i0 + 1, i1);
    return (V[i0].compareTo(V[k]) > 0) ? i0 : k;
    // if (V[i0].compareTo(V[k]) > 0) return
i0; else return k;
  }
}
```

Iterative:

```
  int i, k;
  k = i1;     // Deepest iteration
  for (i = i1 - 1; i >= i0; i -= 1)
    k = ?;
  return k;
```

Iteratively Find Largest

```
/** Value k, I0<=k<=I1, such that V[k] is
largest element among
 *  V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int
i0, int i1) {
  if (i0 >= i1)
    return i1;
  else /* if (i0 < i1) */ {
    int k = indexOfLargest(V, i0 + 1, i1);
    return (V[i0].compareTo(V[k]) > 0) ? i0 : k;
    // if (V[i0].compareTo(V[k]) > 0) return
i0; else return k;
  }
}
```

Iterative:

```
  int i, k;
  k = i1;     // Deepest iteration
  for (i = i1 - 1; i >= i0; i -= 1)
    k = (V[i].compareTo(V[k]) > 0) ? i : k;
```

```
    return k;
```

Finally, Printing

```
/** Print A on one line, separated by blanks.
*/
static void print(String[] A) {
  for (int i = 0; i < A.length; i += 1)
    System.out.print(A[i] + " ");
  System.out.println();
}

/* Java also provides a simple, specialized
syntax for looping
 * through an entire array: */
  for (String s : A)
    System.out.print(s + " ");
```

Another Problem

Given an array of integers, `A`, of length $N > 0$, find the smallest index, k, such that all elements at indices $\geq k$ and $< N - 1$ are greater than `A[`$N-1$`]`. Then rotate elements k to $N-1$ right by one. For example, if `A` starts out as

```
{ 1, 9, 4, 3, 0, 12, 11, 9, 15, 22, 12
}
```

then it ends up as

```
{ 1, 9, 4, 3, 0, 12, 11, 9, 12, 15, 22
}
```

As another example,

```
{ 1, 9, 4, 3, 0, 12, 11, 9, 15, 22, -2
}
```

would become

```
{ -2, 1, 9, 4, 3, 0, 12, 11, 9, 15, 22
}
```

What if A starts like this?

```
    { 1, 9, 4, 3, 0, 12, 11, 9, 12, 15, 22
}
```

Another Problem

Given an array of integers, `A`, of length $N > 0$, find the smallest index, k, such that all elements at indices $\geq k$ and $< N - 1$ are greater than `A[`$N-1$`]`. Then rotate elements k to $N-1$ right by one. For example, if `A` starts out as

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then it ends up as

```
{ 1, 9, 4, 3, 0, 12, 11, 9, 12, 15, 22
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```

As another example,

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}
```

would become

```
{ -2, 1, 9, 4, 3, 0, 12, 11, 9, 15, 22
}
```

What if A starts like this?

```
   { 1, 9, 4, 3, 0, 12, 11, 9, 12, 15, 22
}
```

Answer: It's unchanged. (No, the spec is not ambiguous.)

Your turn

```
public class Shove {

    /** Rotate elements A[k] to A[A.length-1] one element to the
     *  right, where k is the smallest index such that elements
     *  k through A.length-2 are all larger than A[A.length-1].
     */
    static void moveOver(int[] A) {
       // FILL IN
    }

}
```