

IFT2015 - Structures de données  
Démonstration - 2  
22 Janvier 2014

## 1 Vrai ou Faux?

1.  $O(n^2) = O(2^{2 \log_3 n})$
2.  $2^{n+1} \in O(2^n)$
3.  $\log_{10} n^2 \in O(\lg n)$
4.  $O(2^n) = O(3^n)$
5.  $2^{2n} \in O(2^n)$
6.  $f(n) \in O(n) \Rightarrow f(n) \in O(\frac{n}{\lg \lg n})$

## 2 À prouver!

1.  $\lg(n!) \in O(n \lg n)$
2.  $(n+a)^b \in O(n^b); a \in \mathbb{R}; b \in \mathbb{R}_+^*$
3.  $\max(f(n), g(n)) \in \Theta(f(n) + g(n))$
4.  $\log_a n + \frac{1}{\lg n} \in \Theta(\lg n)$
5.  $\sum_{i=1}^n i^k \in \Theta(n^{k+1})$
6. Si  $d(n)$  est dans  $O(f(n))$ , alors  $a.d(n)$  est dans  $O(f(n))$ , pour chaque constante  $a > 0$ .
7. Si  $d(n)$  est dans  $O(f(n))$  et  $f(n)$  est dans  $O(g(n))$ , alors  $d(n)$  est dans  $O(g(n))$ .

## 3 Notation asymptotique

Donnez le temps de calcul en notation asymptotique  $O$  en fonction de  $n$  des fonctions python suivantes.

1. 

```
"""Return the sum of the elements in sequence S."""
def example1(S):
    n = len(S)
    total = 0
    for j in range(n):
        # loop from 0 to n-1
        total += S[j]
    return total
```
2. 

```
"""Return the sum of the elements with even index in
sequence S."""
def example2(S):

    n = len(S)
    total = 0
    for j in range(0, n, 2):
        # note the increment of 2
        total += S[j]
    return total
```
3. 

```
"""Return the sum of the prefix sums of sequence S."""
def example3(S):
    n = len(S)
    total = 0
    for j in range(n): # loop from 0 to n-1
        for k in range(1+j): # loop from 0 to j
            total += S[k]
    return total
```
4. 

```
"""Return the sum of the prefix sums of sequence S."""
def example4(S):
    n = len(S)
    prefix = 0
    total = 0
    for j in range(n):
        prefix += S[j]
        total += prefix
    return total
```
5. 

```
"""Return the number of elements in B equal to the sum
of prefix sums in A."""
def example5(A, B):
    # assume that A and B have equal length
    n = len(A)
    count = 0
    for i in range(n):
        # loop from 0 to n-1
        total = 0
        for j in range(n):
            # loop from 0 to n-1
            for k in range(1+j):
                # loop from 0 to j
                total += A[k]
```

```
        if B[i] == total:  
            count += 1  
    return count
```