A4

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Implementation-basic

```
import numpy as np

np.random.seed(1234)
N = 10**3
x = np.random.uniform(-1, 1, size=N)
y = np.random.uniform(-1, 1, size=N)
t = np.sqrt(x**2+y**2)
pi_hat = 4*sum(t<=1)/N

print(pi_hat)</pre>
```

3.06

Time difference

```
import numpy as np
import time

start = time.time()

np.random.seed(1234)

N = 10**6

x = np.random.uniform(-1, 1, size=N)
y = np.random.uniform(-1, 1, size=N)
t = np.sqrt(x**2+y**2)
pi_hat = 4*sum(t<=1)/N

end = time.time()

print(end-start)</pre>
```

3.646251678466797

$\# { m custom}$ function

```
import numpy as np
def pi_simulator(N):
    np.random.seed(1234)
    x = np.random.uniform(-1, 1, size=N)
    y = np.random.uniform(-1, 1, size=N)
    t = np.sqrt(x**2+y**2)
    pi_hat = 4*sum(t <= 1)/N
    return(pi_hat)
print('pi_simulator(100):',pi_simulator(100))
## pi_simulator(100): 2.96
print('pi_simulator(1000):',pi_simulator(1000))
## pi_simulator(1000): 3.06
print('pi_simulator(10000):',pi_simulator(10000))
## pi_simulator(10000): 3.1352
print('pi_simulator(100000):',pi_simulator(100000))
## pi_simulator(100000): 3.13976
```

$\#\text{num_trials}$

```
import numpy as np
import pandas as pd

def pi_simulator(N):
    np.random.seed(1234)
    x = np.random.uniform(-1, 1, size=N)
    y = np.random.uniform(-1, 1, size=N)
    t = np.sqrt(x**2+y**2)
    pi_hat = 4*sum(t<=1)/N
    return(pi_hat)

num_trials = 10**np.arange(2,8)
outcome = [pi_simulator(i) for i in num_trials]
result = np.vstack((num_trials,outcome)).T
result = pd.DataFrame(result,columns=['num_trials','outcome'])
print(result)</pre>
```

```
## num_trials outcome

## 0 100.0 2.960000

## 1 1000.0 3.060000

## 2 10000.0 3.135200

## 3 100000.0 3.139760

## 4 1000000.0 3.142876

## 5 10000000.0 3.142289
```

```
#pi_simulator2
```

```
import numpy as np
import time
def pi_simulator2(N):
    start = time.time()
    np.random.seed(1234)
    x = np.random.uniform(-1, 1, size=N)
    y = np.random.uniform(-1, 1, size=N)
    t = np.sqrt(x**2+y**2)
    pi_hat = 4*sum(t <= 1)/N
    end = time.time()
    print(N)
    print('Time difference of ',end-start,'secs')
    return (pi_hat)
print([pi_simulator2(100)])
## 100
## Time difference of 0.0 secs
## [2.96]
print([pi_simulator2(1000)])
## 1000
## Time difference of 0.002991199493408203 secs
## [3.06]
print([pi_simulator2(10000)])
## 10000
## Time difference of 0.03989100456237793 secs
## [3.1352]
print([pi_simulator2(100000)])
## 100000
## Time difference of 0.34407734870910645 secs
## [3.13976]
print([pi_simulator2(1000000)])
## 1000000
## Time difference of 3.413872718811035 secs
## [3.142876]
```

print([pi_simulator2(10000000)])

```
## 10000000
## Time difference of 34.47481989860535 secs
## [3.1422888]
```

$\#pi_simulator3$

```
import numpy as np

def pi_simulator3(N):
    #np.random.seed(1234)
    x = np.random.uniform(-1, 1, size=N)
    y = np.random.uniform(-1, 1, size=N)
    t = np.sqrt(x**2+y**2)
    pi_hat = 4*sum(t<=1)/N
    return(pi_hat)

n = 100
N = 1000
np.random.seed(1234)
samples = [0]*n
for i in range(0,n):
    samples[i] = pi_simulator3(N)

print(samples[:6])</pre>
```

[3.06, 3.184, 3.12, 3.228, 3.124, 3.092]

#confidence interval

```
import numpy as np
from scipy.stats import t
def pi_simulator3(N):
    #np.random.seed(1234)
    x = np.random.uniform(-1, 1, size=N)
   y = np.random.uniform(-1, 1, size=N)
   t = np.sqrt(x**2+y**2)
    pi_hat = 4*sum(t <= 1)/N
    return(pi_hat)
n = 100
N = 1000
np.random.seed(1234)
samples = [0]*n
for i in range(0,n):
    samples[i] = pi_simulator3(N)
samples[:6]
## [3.06, 3.184, 3.12, 3.228, 3.124, 3.092]
X_bar = np.mean(samples)
s = np.sqrt((sum((X_bar-samples)**2))/(n-1))
T = t(n-1).ppf(0.975)
print('X_bar:',X_bar)
## X_bar: 3.1412000000000004
print('s:',s)
## s: 0.05271305973538881
print('T:',T)
```

T: 1.9842169515086827

#confidence interval length (Excercise 1)

```
import numpy as np
from scipy.stats import t
def pi_simulator3(N):
    #np.random.seed(1234)
    x = np.random.uniform(-1, 1, size=N)
    y = np.random.uniform(-1, 1, size=N)
   t = np.sqrt(x**2+y**2)
    pi_hat = 4*sum(t <= 1)/N
    return(pi_hat)
n = 100
N = 1000
np.random.seed(1234)
samples = [0]*n
for i in range(0,n):
    samples[i] = pi_simulator3(N)
samples[:6]
## [3.06, 3.184, 3.12, 3.228, 3.124, 3.092]
X_bar = np.mean(samples)
s = np.sqrt((sum((X_bar-samples)**2))/(n-1))
T = t(n-1).ppf(0.975)
lb = X_bar-T*s/np.sqrt(n)
ub = X_bar+T*s/np.sqrt(n)
print('lb:',lb)
## lb: 3.1307405853307158
print('ub:',ub)
## ub: 3.151659414669285
print('ub-lb:',ub-lb)
## ub-lb: 0.020918829338569367
#confidence interval length (Excercise 2)
import numpy as np
from scipy.stats import t
```

```
def pi_simulator3(N):
    #np.random.seed(1234)
    x = np.random.uniform(-1, 1, size=N)
    y = np.random.uniform(-1, 1, size=N)
   t = np.sqrt(x**2+y**2)
    pi_hat = 4*sum(t <= 1)/N
    return(pi_hat)
n = 1000
N = 10000
np.random.seed(1234)
samples = [0]*n
for i in range(0,n):
    samples[i] = pi_simulator3(N)
samples[:6]
## [3.1352, 3.1276, 3.1396, 3.1548, 3.1388, 3.1652]
X_bar = np.mean(samples)
s = np.sqrt((sum((X_bar-samples)**2))/(n-1))
T = t(n-1).ppf(0.975)
lb = X_bar-T*s/np.sqrt(n)
ub = X_bar+T*s/np.sqrt(n)
print('lb:',lb)
## lb: 3.141465340511527
print('ub:',ub)
## ub: 3.1434762594884726
print('ub-lb:',ub-lb)
```

ub-lb: 0.002010918976945497