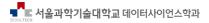
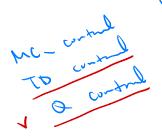
Lecture F4. MDP without Model 4

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- I. Policy iteration 3 Q-learning control
- 2 II. Policy iteration 4 Double Q-learning control





• skiier.R is loaded as follows.

```
source("../skiier.R")

## [1] "Skiier's problem is set."

## [1] "Defined are `state`, `P_normal`, `P_speed`, `R_s_a`, `q_s_a_init` (F2, p15)."

## [1] "Defined are `pi_speed`, and `pi_50` (F2, p16)."

## [1] "Defined are `simul_path()` (F2, p17)."

## [1] "Defined are `simul_step()` (F2, p18)."

## [1] "Defined are `pol_eval_MC()` (F2, p19)."

## [1] "Defined are `pol_eval_TD()` (F2, p20)."

## [1] "Defined are `pol_imp()` (F2, p20)."
```

I. Policy iteration 3 - Q-learning control

Introduction

ullet (pol_eval_MC()) MC control updates q(s,a):

$$q(s,a) \leftarrow q(s,a) + \alpha(\underline{G_t} - q(s,a)), \ \forall s,a$$

ullet (pol_eval_TD()) TD control updates q(s,a):

$$q(s,a) \leftarrow q(s,a) + \alpha(\underline{r_t} + \gamma \overline{q(s',a')} - q(s,a)), \ \forall s,a$$

• (pol_eval_Q()) Q-learning updates q(s,a):

$$q(s,a) \leftarrow q(s,a) + \alpha \underbrace{(r_t + \gamma \underset{a' \in \mathcal{A}}{\text{max}}_{a' \in \mathcal{A}} q(s',a')}_{\text{Q}} - q(s,a)), \ \forall s,a$$

- Q-learning is a variation of TD control.
 - Q-learning is greedy in a sense by taking maximum among possible future actions.
 - It is called **off-policy learning** since it may take action other than the current policy dictates.

Write pol_eval_Q()

```
pol eval TD <- function(sample_step, q_s_a, alpha) {</pre>
  s <- sample_step[1]</pre>
  a <- sample step[2]
                                              SOLYGE
  r <- sample_step[3] %>% as.numeric()
  s next <- sample step[4]
  a next <- sample step[5]
  q s a[s,a] \leftarrow q s a[s,a] + alpha*(r+q s a[s next,a next]-q s a[s,a])
  return(q s a)
                                                                                              act
pol eval Q - function(sample_step, q_s_a, alpha) {
  s <- sample step[1]
  a <- sample step[2]
  r <- sample step[3] %>% as.numeric()
  s next <- sample step[4]
 a_next <- sample_step[5] # not used here</pre>
  q_s_a[s,a] <- q_s_a[s,a] + alpha*(r+max(q_s_a[s_next,])-q_s_a[s,a]) # change here</pre>
  return(q s a)
```

```
100
Q-learning
                                    200
                                      700
num ep <- 10^5_
                                                    print(end time-beg time)
beg time <- Sys.time()</pre>
                                                    ## Time difference of 47.5 secs
qsa<-qsainit
                                                    t(pi)
pi <- pi 50
exploration rate <- 1
                                                         0 10 20 30 40 50 60 70
for (epi i in 1:num ep) {
  s now <- "0"
                                                    ## s 1 1
                                                               0
                                                                  0 1
  while (s_now != "70") {
    sample step <- simul step(pi, s now, P normal, P speed, R s a)</pre>
    q_s_a <- pol_eval_Q(sample_step, q_s_a, alpha = max(1/epi_i, 0.05))
    if (epi i %% 100 == 0) {
      pi <- pol_imp(pi, q_s_a, epsilon = exploration_rate)</pre>
    }
    s now <- sample step[4]
    exploration rate <- max(exploration rate*0.9995, 0.001)
end time <- Sys.time()</pre>
t(q s a)
##
          0
                10
                       20
                              30
                                     40
                                            50
                                                    60 70
## n -5.713 -4.760 -3.746 -2.736 -1.999 -2.000 -1.000 0
## s -5.668 -4.701 -3.947 -3.237 -1.677 -2.027 -1.815 0
```

II. Policy iteration 4 - Double Q-learning control

Why Donble Q. - update

Method

9, 2 32

ullet (pol_eval_Q()) Q-learning updates q(s,a):

$$q(s, a) \leftarrow q(s, a) + \alpha(r_t + \gamma \max_{a' \in \mathcal{A}} q(s', a') - q(s, a)), \ \forall s, a \in \mathcal{A}$$

- (pol_eval_dbl_Q()) Double Q-learning uses a pair of q-functions, q_1 () and q_2 (). I updates
 - with probability 0.5

$$\underline{q_1(s,a)} \leftarrow \underline{q_1(s,a)} + \alpha(r_t + \gamma \underline{q_2}(s', argmax_{a' \in \mathcal{A}} \ \underline{q_1(s',a')}) - q_1(s,a)), \ \forall s,a$$

with probability 0.5

$$q_2(s, a) \leftarrow q_2(s, a) + \alpha(r_t + \gamma q_1(s', argmax_{a' \in \mathcal{A}} \ q_2(s', a')) - q_2(s, a)), \ \forall s, a \in \mathcal{A}$$

• Policy is improved using $q_1(\cdot,\cdot)+q_2(\cdot,\cdot)$.

Write pol_eval_dbl_Q()

```
pol eval 0 <- function(sample step, q s a, alpha) {</pre>
  s <- sample step[1]
  a <- sample step[2]
  r <- sample step[3] %>% as.numeric()
  s next <- sample step[4]

√q s a[s,a] <- q s a[s,a] + alpha*(r+max(q s a[s next,])-q s a[s,a]) # change here</pre>
  return(q_s_a)
pol eval dbl 0 <- function(sample step, q s a 1, q s a 2, alpha) {
  s <- sample step[1]</pre>
  a <- sample step[2]
  r <- sample_step[3] %>% as.numeric()
  s next <- sample step[4]
  if (runif(1) < 0.5) { # update(q s a 1
    q s a 1[s,a] <- q s a 1[s,a] +
      alpha*(r+q_s_a_2[s_next, which.max(q_s_a_1[s_next,])]-q_s_a_1[s,a]) # change here
  } else { # update q_s_a_2
    q s a 2[s,a] \leftarrow q s a 2[s,a] +
      alpha*(r+q s a 1[s next, which.max(q s a 2[s next,])]-q s a 2[s,a]) # change here
  return(list(q_s_a_1, q_s_a_2))
```

Double Q-learning

```
num ep <- 10<sup>^</sup>X + <sup>⊀</sup> 5
                                                    print(end time-beg time)
beg time <- Sys.time() # change below
                                                    ## Time difference of 51.71 secs
qsa1 <- qsainit; qsa2 <- qsainit
                                                    t(pi)
pi <- pi 50
exploration rate <- 1
                                                         0 10 20 30 40 50 60 70
for (epi i in 1:num ep) {
  s now <- "0"
                                                    ## s 1 1 0 0 0 1 0 0
  while (s now != "70") {
    sample step <- simul_step(pi, s now, P normal, P speed, R s a)</pre>
    q_s_a <- pol_eval_dbl_Q(sample_step, q_s_a_1, q_s_a_2, alpha = max(1/epi_i, 0.) # change here
    q_s_a_1 <- q_s_a[[1]]; q_s_a_2 <- q_s_a[[2]] # change here</pre>
                                                                                   0.01
    if (epi i %% 100 == 0) {
      pi <- pol imp(pi, q s a 1+q s a 2, epsilon = exploration rate) # change here
    s now <- sample step[4]
    exploration_rate <- max(exploration_rate*0.999)
t((q s a 1 + q s a 2)/2)
##
               10
                      20
                              30
                                     40
                                            50
                                                   60 70
## n -5.69 -4.884 -3.677 -2.665 -1.650 -1.982 -1.000 0
## s -5.28 -4.639 -3.886 -3.303 -1.807 -1.617 -1.594 0
```

Exercise 1

Feel free to try different schemes for the number of iterations and exploration decaying scenarios.

"It's not that I'm so smart, it's just that I stay with problems longer. - A. Einstein"