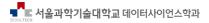
## Lecture F4. MDP without Model 4

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- I. Policy iteration 3 Q-learning control
- II. Policy iteration 4 Double Q-learning control

• skiier.R is loaded as follows.

```
source("../skiier.R")

## [1] "Skiier's problem is set."

## [1] "Defined are `state`, `P_normal`, `P_speed`, `R_s_a`, `q_s_a_init` (F2, p15)."

## [1] "Defined are `pi_speed`, and `pi_50` (F2, p16)."

## [1] "Defined are `simul_path()` (F2, p17)."

## [1] "Defined are `simul_step()` (F2, p18)."

## [1] "Defined are `pol_eval_MC()` (F2, p19)."

## [1] "Defined are `pol_eval_TD()` (F2, p20)."

## [1] "Defined are `pol_imp()` (F2, p20)."
```

I. Policy iteration 3 - Q-learning control

### Introduction

ullet (pol\_eval\_MC()) MC control updates q(s,a):

$$q(s,a) \leftarrow q(s,a) + \alpha(G_t - q(s,a)), \ \forall s,a$$

• (pol\_eval\_TD()) TD control updates q(s, a):

$$q(s,a) \leftarrow q(s,a) + \alpha(r_t + \gamma q(s',a') - q(s,a)), \ \forall s,a$$

• (pol\_eval\_Q()) Q-learning updates q(s,a):

$$q(s, a) \leftarrow q(s, a) + \alpha(r_t + \gamma max_{a' \in \mathcal{A}} q(s', a') - q(s, a)), \ \forall s, a \in \mathcal{A}$$

- Q-learning is a variation of TD control.
- Q-learning is greedy in a sense by taking maximum among possible future action.
- It is called off-policy learning since it may take action other than the current policy dictates.

## Write pol\_eval\_Q()

```
pol eval TD <- function(sample step, q s a, alpha) {
  s <- sample step[1]
  a <- sample step[2]
  r <- sample step[3] %>% as.numeric()
  s next <- sample step[4]
  a next <- sample step[5]
  q s a[s,a] \leftarrow q s a[s,a] + alpha*(r+q s a[s next,a next]-q s a[s,a])
  return(q s a)
pol eval 0 <- function(sample step, q s a, alpha) {
  s <- sample step[1]</pre>
  a <- sample step[2]
  r <- sample step[3] %>% as.numeric()
  s next <- sample step[4]
  a next <- sample step[5] # not used here
  q s a[s,a] \leftarrow q s a[s,a] + alpha*(r+max(q s a[s next,])-q s a[s,a]) # change here
  return(q s a)
```

## Q-learning

```
num ep <- 10^5
                                                    print(end time-beg time)
beg time <- Sys.time()</pre>
                                                    ## Time difference of 47.5 secs
qsa<-qsainit
                                                    t(pi)
pi <- pi 50
exploration rate <- 1
                                                         0 10 20 30 40 50 60 70
for (epi i in 1:num ep) {
                                                              1 1 0
  s now <- "0"
                                                    ## s 1 1 0 0 1 0 0 0
  while (s_now != "70") {
    sample step <- simul_step(pi, s now, P normal, P speed, R s a)</pre>
    q s a <- pol_eval_Q(sample step, q s a, alpha = max(1/epi i, 0.05))
    if (epi i %% 100 == 0) {
      pi <- pol imp(pi, q s a, epsilon = exploration rate)
    }
    s now <- sample step[4]
    exploration rate <- max(exploration rate*0.9995, 0.001)
end time <- Sys.time()</pre>
t(q s a)
##
          0
                10
                       20
                              30
                                     40
                                             50
                                                    60 70
## n -5.713 -4.760 -3.746 -2.736 -1.999 -2.000 -1.000 0
```

## s -5.668 -4.701 -3.947 -3.237 -1.677 -2.027 -1.815 0

# II. Policy iteration 4 - Double Q-learning control

### Method

ullet (pol\_eval\_Q()) Q-learning updates q(s,a):

$$q(s, a) \leftarrow q(s, a) + \alpha(r_t + \gamma max_{a' \in \mathcal{A}} q(s', a') - q(s, a)), \ \forall s, a$$

- $\bullet$  (pol\_eval\_dbl\_Q()) Double Q-learning uses a pair of q-functions,  $q_1()$  and  $q_2().$  It updates
  - with probability 0.5

$$q_1(s, a) \leftarrow q_1(s, a) + \alpha(r_t + \gamma q_2(s', argmax_{a' \in \mathcal{A}} \ q_1(s', a')) - q_1(s, a)), \ \forall s, a \in \mathcal{A}$$

with probability 0.5

$$q_2(s, a) \leftarrow q_2(s, a) + \alpha(r_t + \gamma q_1(s', argmax_{a' \in \mathcal{A}} \ q_2(s', a')) - q_2(s, a)), \ \forall s, a \in \mathcal{A}$$

• Policy is improved using  $q_1(\cdot, \cdot) + q_2(\cdot, \cdot)$ .

## Write pol\_eval\_dbl\_Q()

```
pol eval 0 <- function(sample step, q s a, alpha) {
  s <- sample step[1]</pre>
  a <- sample step[2]</pre>
  r <- sample step[3] %>% as.numeric()
  s next <- sample step[4]
  q s a[s,a] \leftarrow q s a[s,a] + alpha*(r+max(q s a[s next,])-q s a[s,a]) # change here
  return(q s a)
pol eval dbl 0 <- function(sample step, q s a 1, q s a 2, alpha) {
  s <- sample step[1]</pre>
  a <- sample step[2]
  r <- sample step[3] %>% as.numeric()
  s next <- sample step[4]
  if (runif(1) < 0.5) { # update q s a 1
    q s a 1[s,a] \leftarrow q s a 1[s,a] +
      alpha*(r+q s a 2[s next, which.max(q s a 1[s next,])]-q s a 1[s,a]) # change here
  } else { # update q s a 2
    q s a 2[s,a] \leftarrow q s a 2[s,a] +
      alpha*(r+q s a 1[s next, which.max(q s a 2[s next,])]-q s a 2[s,a]) # change here
  return(list(q s a 1, q s a 2))
```

# Double Q-learning

```
num ep <- 10^5
                                                   print(end time-beg time)
beg time <- Sys.time() # change below
                                                   ## Time difference of 51.71 secs
qsa1 <- qsainit; qsa2 <- qsainit
                                                   t(pi)
pi <- pi 50
exploration rate <- 1
                                                        0 10 20 30 40 50 60 70
for (epi i in 1:num ep) {
  s now <- "0"
                                                   ## s 1 1 0 0 0
  while (s_now != "70") {
    sample step <- simul_step(pi, s now, P normal, P speed, R s a)</pre>
    q s a <- pol eval dbl Q(sample step, q s a 1, q s a 2, alpha = max(1/epi i, 0.05)) # change here
    q_s_a_1 <- q_s_a[[1]]; q_s_a_2 <- q_s_a[[2]] # change here</pre>
    if (epi i %% 100 == 0) {
      pi <- pol imp(pi, q s a 1+q s a 2, epsilon = exploration rate) # change here
    s now <- sample step[4]
    exploration rate <- max(exploration rate*0.9995, 0.001)
t((q s a 1 + q s a 2)/2)
##
               10
                      20
                             30
                                    40
                                           50
                                                  60 70
## n -5.69 -4.884 -3.677 -2.665 -1.650 -1.982 -1.000 0
## s -5.28 -4.639 -3.886 -3.303 -1.807 -1.617 -1.594 0
```

#### Exercise 1

Feel free to try different schemes for the number of iterations and exploration decaying scenarios.

"It's not that I'm so smart, it's just that I stay with problems longer. - A. Einstein"