# F1\_Exercises

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#### Preparation (P. 9)

```
import numpy as np
import pandas as pd
states=np.arange(0,80,10).astype('str')
P_normal=pd.DataFrame(np.matrix([[0,1,0,0,0,0,0,0],
                                                        [0,0,1,0,0,0,0,0],
                                                        [0,0,0,1,0,0,0,0],
                                                        [0,0,0,0,1,0,0,0],
                                                        [0,0,0,0,0,1,0,0],
                                                        [0,0,0,0,0,0,1,0],
                                                        [0,0,0,0,0,0,0,1],
                                                        [0,0,0,0,0,0,0,1]]), index=states,columns=states)
P_speed=pd.DataFrame(np.matrix([[.1,0,.9,0,0,0,0,0],
                                                     [.1,0,0,.9,0,0,0,0],
                                                     [0,.1,0,0,.9,0,0,0],
                                                     [0,0,.1,0,0,.9,0,0],
                                                     [0,0,0,.1,0,0,.9,0],
                                                     [0,0,0,0,.1,0,0,.9],
                                                     [0,0,0,0,0,.1,0,.9],
                                                     [0,0,0,0,0,0,0,1]]), index=states, columns=states)
 R\_s\_a = pd. DataFrame (np. matrix ([-1, -1, -1, -1, 0.0, -1, -1, 0, -1.5, -1.5, -1.5, -1.5, -0.5, -1.5, -1.5, 0]). \\ reshape (len(states)) \\ reshap
R_s_a.T
                                 10
                                               20
                                                                                                                     70
                                                             30
                                                                           40
                                                                                         50
                                                                                                       60
## n -1.0 -1.0 -1.0 -1.0 0.0 -1.0 -1.0 0.0
## s -1.5 -1.5 -1.5 -0.5 -1.5 -0.0
pi_speed=pd.DataFrame(np.c_[np.repeat(0,len(states)),np.repeat(1,len(states))], index=states, columns=['n','s
pi_50=pd.DataFrame(np.c_[np.repeat(0.5,len(states)), np.repeat(0.5,len(states))],index=states, columns=['n','
pi_speed.T
                                                                                          70
                        10
                                   20
                                               30 40
                                                                     50 60
## s 1
                                      1
                                                 1
                                                                        1
pi_50.T
                                 10
                                                                                                                     70
                                               20
                                                             30
                                                                           40
                                                                                         50
                                                                                                       60
                0.5 0.5 0.5 0.5 0.5
                                                                                      0.5 0.5
## s 0.5 0.5 0.5 0.5 0.5 0.5 0.5
```

#### Simulator - $\pi^{speed}$ (P. 11)

```
pi=pi_speed
np.random.seed(1234)
history=[]
MC_N=10000
for MC_i in range(MC_N):
    s now='0'
    history_i=list(s_now)
    while s now != '70':
        if np.random.uniform(0,1) < pi.loc[s_now]['n']:</pre>
            a now='n'
            P=P_normal
        else:
            a now='s'
            P=P speed
        r_now=str(R_s_a.loc[s_now][a_now])
        s_next = states[np.argmin(P.loc[s_now].cumsum() < np.random.uniform(0,1))].item()
        history_i.extend([a_now,r_now,s_next])
        s_now=s_next
    history.append(history_i)
history_speed=history
func=np.vectorize(lambda x: ','.join(x))
pd.Series(func(history_speed[:20]))
```

```
## 0
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 1
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 2
         0,s,-1.5,0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1....
## 3
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 4
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 5
## 6
         0,s,-1.5,20,s,-1.5,10,s,-1.5,30,s,-1.5,50,s,-1...
## 7
         0, s, -1.5, 20, s, -1.5, 40, s, -0.5, 30, s, -1.5, 50, s, -1...
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 8
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 9
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 10
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 11
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 12
```

```
## 14
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 15
         0,s,-1.5,20,s,-1.5,10,s,-1.5,30,s,-1.5,50,s,-1...
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 16
## 17
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 18
                 0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## 19
## dtype: object
##
## C:\Users\User\AppData\Local\R-MINI~1\envs\R-RETI~1\lib\site-packages\numpy\core\_asarray.py:83: VisibleDep
or-tuple of lists-or-tuples-or ndarrays with different lengths or shapes) is deprecated. If you meant to do this,
     return array(a, dtype, copy=False, order=order)
```

0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70

#### Simulator - $\pi^{50}$ (P. 13)

## 13

```
pi=pi_50
np.random.seed(1234)
history=[]
MC_N=10000
for MC_i in range(MC_N):
    s now='0'
    history_i=list(s_now)
    while s_now != '70' :
        if np.random.uniform(0,1) < pi.loc[s_now]['n']:</pre>
            a_now='n'
            P=P normal
        else:
            a now='s'
            P=P_speed
        r_now=str(R_s_a.loc[s_now][a_now])
        s_next=states[np.argmin(P.loc[s_now].cumsum() < np.random.uniform(0,1))].item()</pre>
        history_i.extend([a_now,r_now,s_next])
        s_now=s_next
    history.append(history_i)
history_50=history
func=np.vectorize(lambda x: ','.join(x))
pd.Series(func(history_50[:20]))
```

```
## 0
         0,n,-1.0,10,n,-1.0,20,s,-1.5,40,n,0.0,50,s,-1....
## 1
         0,n,-1.0,10,s,-1.5,30,n,-1.0,40,s,-0.5,30,s,-1...
         0, s, -1.5, 20, n, -1.0, 30, n, -1.0, 40, s, -0.5, 60, s, -1...
## 2
## 3
         0, s, -1.5, 20, n, -1.0, 30, n, -1.0, 40, n, 0.0, 50, n, -1...
## 4
         0,n,-1.0,10,n,-1.0,20,n,-1.0,30,s,-1.5,20,s,-1...
         0,n,-1.0,10,n,-1.0,20,n,-1.0,30,n,-1.0,40,n,0....
## 5
## 6
         0, n, -1.0, 10, n, -1.0, 20, n, -1.0, 30, n, -1.0, 40, n, 0....
                  0,s,-1.5,20,s,-1.5,40,s,-0.5,60,n,-1.0,70
## 7
## 8
         0,s,-1.5,20,n,-1.0,30,s,-1.5,50,n,-1.0,60,s,-1...
## 9
         0,s,-1.5,20,s,-1.5,40,n,0.0,50,n,-1.0,60,n,-1....
         0,n,-1.0,10,s,-1.5,30,n,-1.0,40,s,-0.5,60,s,-1...
## 10
## 11
         0,s,-1.5,20,n,-1.0,30,n,-1.0,40,n,0.0,50,n,-1....
## 12
         0,n,-1.0,10,s,-1.5,30,n,-1.0,40,n,0.0,50,s,-1....
                  0,n,-1.0,10,s,-1.5,30,s,-1.5,50,s,-1.5,70
## 13
                  0,n,-1.0,10,s,-1.5,30,s,-1.5,50,s,-1.5,70
## 14
## 15
                  0,n,-1.0,10,s,-1.5,30,s,-1.5,50,s,-1.5,70
## 16
         0,s,-1.5,20,s,-1.5,40,n,0.0,50,n,-1.0,60,n,-1....
                  0,s,-1.5,20,s,-1.5,40,s,-0.5,60,n,-1.0,70
## 17
## 18
         0,n,-1.0,10,n,-1.0,20,s,-1.5,40,n,0.0,50,n,-1....
## 19
                  0,s,-1.5,20,s,-1.5,40,s,-0.5,60,s,-1.5,70
## dtype: object
##
## C:\Users\User\AppData\Local\R-MINI~1\envs\R-RETI~1\lib\site-packages\numpy\core\_asarray.py:83: VisibleDep
or-tuple of lists-or-tuples-or ndarrays with different lengths or shapes) is deprecated. If you meant to do this,
##
     return array(a, dtype, copy=False, order=order)
Implementation 1 - \pi^{speed} (vectorized) (P. 17)
pol_eval=pd.DataFrame(np.zeros((len(states),2)), index=states, columns=['count','sum'])
pol_eval.T
##
                 10
                      20
                           30
                                40
                                      50
                                           60
                                                70
```

## count 0.0

## sum

0.0

0.0

for MC\_i in range(len(history\_speed)):
 history\_i=history\_speed[MC\_i]

0.0

0.0

0.0

for j in range(0,len(history\_i),3):

0.0

0.0

pol\_eval.loc[history\_i[j]]['count']+=1

0.0

0.0

0.0 0.0 0.0 0.0

0.0

0.0

```
if j < len(history_i) :</pre>
            pol_eval.loc[history_i[j]]['sum']+=pd.Series(history_i)[range(j+2,len(history_i)-1,3)].astype('f]
        else:
            pol_eval.loc[history_i[j]]['sum']+=0
pol eval.T
##
                       10
                                20
                                        30
                                                 40
                                                         50
                                                                  60
                                                                           70
## count 11225.0 1076.0 10291.0 1887.0
                                             9485.0 2563.0
                                                              8563.0 10000.0
         -65136.0 -5619.0 -42703.0 -6539.0 -22275.5 -4472.5 -14355.0
pol_eval['sum']/pol_eval['count']
        -5.802762
## 0
        -5.222119
## 10
## 20
        -4.149548
        -3.465289
## 30
        -2.348498
## 40
        -1.745025
## 50
        -1.676398
## 60
## 70
        0.000000
## dtype: float64
Implementation 2 - \pi^{speed} (running estimate) (P. 19)
pol_eval=pd.DataFrame(np.zeros((len(states),2)), index=states, columns=['count','est'])
pol eval.T
##
                10
                     20
                               40
                                    50
                                         60
## count 0.0 0.0 0.0
                        0.0 0.0 0.0 0.0
## est
          0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0
for MC_i in range(len(history_speed)):
    history_i=history_speed[MC_i]
    for j in range(0,len(history_i),3):
        # update count
        pol_eval.loc[history_i[j]]['count']+=1
        current_cnt=pol_eval.loc[history_i[j]]['count']
        # return is the new info
```

```
if j < len(history_i):</pre>
            new_info=pd.Series(history_i)[range(j+2,len(history_i)-1,3)].astype('float').sum()
        else:
            new_info=0
        # update the last estimate with new info
        alpha=1/current_cnt
        pol_eval.loc[history_i[j]]['est']+=alpha*(new_info-pol_eval.loc[history_i[j]]['est'])
np.round(pol_eval.T,2)
##
                0
                        10
                                           30
                                                             50
                                                                      60
                                                                               70
                                  20
                                                    40
## count 11225.0 1076.00 10291.00 1887.00 9485.00 2563.00 8563.00 10000.0
## est
             -5.8
                     -5.22
                               -4.15
                                        -3.47
                                                 -2.35
                                                          -1.75
                                                                   -1.68
                                                                              0.0
Implementation 3 - \pi^{50} (vectorized) (P. 21)
pol_eval=pd.DataFrame(np.zeros((len(states),2)), index=states, columns=['count','sum'])
pol_eval.T
##
                10
                     20
                          30
                               40
                                    50
                                         60
                                              70
## count 0.0 0.0 0.0 0.0 0.0 0.0 0.0
## sum
          0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0
for MC_i in range(len(history_50)):
    history_i=history_50[MC_i]
    for j in range(0,len(history_i),3):
        pol_eval.loc[history_i[j]]['count']+=1
        if j < len(history_i) :</pre>
            pol_eval.loc[history_i[j]]['sum']+=pd.Series(history_i)[range(j+2,len(history_i)-1,3)].astype('f]
        else:
            pol_eval.loc[history_i[j]]['sum']+=0
pol_eval.T
##
                        10
                                 20
                                          30
                                                   40
                                                            50
                                                                    60
                                                                             70
## count 10863.0
                    5792.0
                             8140.0
                                      7121.0
                                               7549.0
                                                        7363.0 6991.0 10000.0
```

```
-64904.5 -29662.5 -33549.0 -24133.0 -15410.0 -14874.5 -9436.5
                                                                               0.0
## sum
pol_eval['sum']/pol_eval['count']
## 0
        -5.974823
## 10
        -5.121288
## 20
        -4.121499
        -3.388990
## 30
## 40
        -2.041330
## 50
        -2.020168
        -1.349807
## 60
## 70
         0.000000
## dtype: float64
Implementation 4 - \pi^{50} (running estimate) (P. 23)
pol_eval=pd.DataFrame(np.zeros((len(states),2)), index=states, columns=['count','est'])
pol_eval.T
##
            0
                10
                     20
                           30
                                40
                                     50
                                          60
                                               70
## count 0.0
               0.0 0.0
                         0.0 0.0 0.0 0.0
                                              0.0
          0.0 \quad 0.0 \quad 0.0 \quad 0.0 \quad 0.0 \quad 0.0 \quad 0.0
## est
for MC_i in range(len(history_50)):
    history_i=history_50[MC_i]
    for j in range(0,len(history_i),3):
        # increment count
        pol_eval.loc[history_i[j]]['count']+=1
        current_cnt=pol_eval.loc[history_i[j]]['count']
        # return is the new info
        if j < len(history_i):</pre>
            new_info=pd.Series(history_i)[range(j+2,len(history_i)-1,3)].astype('float').sum()
        else:
            new_info=0
        # update the last estimate with new info
        alpha=1/current_cnt
        pol_eval.loc[history_i[j]]['est']+=alpha*(new_info-pol_eval.loc[history_i[j]]['est'])
```

#### np.round(pol\_eval.T,2)

## count 10863.00 5792.00 8140.00 7121.00 7549.00 7363.00 6991.00 10000.0 ## est -5.97 -5.12 -4.12 -3.39 -2.04 -2.02 -1.35 0.0

"F1\_Exercises"