

- For general  $t$ , (exercise)

$$V_t(s) = \mathbb{E}[G_t | s_t = s]$$

$$= \mathbb{E}\left[\sum_{\tau=t}^n r_\tau \mid s_t = s\right]$$

$$= \mathbb{E}[r_t + r_{t+1} \dots r_n \mid s_t = s]$$

$$\underline{\mathbb{E}[r_t \mid s_t = s] = R(s)}$$

$$= R(s) + \mathbb{E}[r_{t+1} + \dots + r_n \mid s_t = s]$$

$$= R(s) + \mathbb{E}[G_{t+1} \mid s_t = s]$$

$$= R(s) + \sum_{s' \in S} P_{ss'} \mathbb{E}[G_{t+1} \mid s_{t+1} = s']$$

$$= \underline{R(s) + \sum_{s' \in S} P_{ss'} V_{t+1}(s')}$$