

# Homework #3 – Motion Estimation & Compensation

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## Objective

The goal of this homework is to implement and analyze motion estimation (ME) and motion compensation (MC) algorithms for video compression. Specifically:

1. Implement full search block matching for motion estimation with different search ranges ( $[\pm 8]$ ,  $[\pm 16]$ ,  $[\pm 32]$ ).
2. Implement motion compensation to reconstruct the frame and calculate residuals.
3. Compare the results (PSNR and runtime) for different search ranges.
4. Implement a three-step search algorithm and compare its results with the full search algorithm.

## Implementation Details

### 1. Motion Estimation (ME)

- **Algorithm:** Full Search Block Matching
- **Parameters:**
  - **Block Size:** 8x8
  - **Search Range:**  $[\pm 8]$ ,  $[\pm 16]$ ,  $[\pm 32]$
- **Method:**
  - Divide the frame into non-overlapping blocks of size 8x8.
  - For each block in the current frame, search for the best matching block in the reference frame within the specified search range.
  - Use Mean Squared Error (MSE) as the matching criterion.
- **Output:**
  - **Motion Vectors:** Displacement values (dx, dy) for each block.
  - **Residuals:** Difference between the original block and the reconstructed block.

## 2. Motion Compensation (MC)

- **Purpose:** Reconstruct the current frame using motion vectors and the reference frame.
- **Method:**
  - Use motion vectors to fetch the best matching blocks from the reference frame.
  - Combine these blocks to reconstruct the current frame.
- **Output:**
  - **Reconstructed Frame:** Approximated version of the current frame.

## 3. PSNR Evaluation

- **Purpose:** Measure the quality of the reconstructed frame.
- **Method:**
  - Calculate the Peak Signal-to-Noise Ratio (PSNR) between the original frame and the reconstructed frame.
- **Output:** PSNR value in dB.

## 4. Runtime Comparison

- **Purpose:** Compare the computational efficiency of different search ranges.
- **Method:**
  - Measure the execution time for motion estimation and motion compensation using Python's time module.
- **Output:** Runtime statistics.

## Results

```
Search Range: 8  
Full Search Time: 1.5155 seconds  
PSNR: 23.15 dB  
Search Range: 16  
Full Search Time: 5.8053 seconds  
PSNR: 25.92 dB  
Search Range: 32  
Full Search Time: 20.9858 seconds  
PSNR: 30.25 dB
```

1. search range 8:



2. search range 16:



3. search range 31:



## **Conclusion**

### **1. Search Range:**

- Increasing the search range improves PSNR but increases runtime significantly.
- A balance between search range and runtime must be considered for practical applications.

### **2. Three-Step Search:**

- Three-step search is faster than full search but may result in slightly lower PSNR.
- It is suitable for scenarios where computational efficiency is critical.

### **3. Residuals:**

- Residuals highlight the areas where motion compensation fails to perfectly reconstruct the frame.