

Problem1

1.

Code:

Hw4pr1.m

```
% hw4.1

mu1 = [0 0];
sigma1 = [1 0 ; 0 1];
mu2 = [3 0];
sigma2 = [1 0 ; 0 1];
mu3 = [0 3];
sigma3 = [1 0 ; 0 1];
p = [0.2 0.5 0.3];

sampleG = sampleDiscrete(500,p);
g1 = mvnrnd(mu1,sigma1,length(sampleG(sampleG==1)));
g2 = mvnrnd(mu2,sigma2,length(sampleG(sampleG==2)));
g3 = mvnrnd(mu3,sigma3,length(sampleG(sampleG==3)));

alldat = [g1;g2;g3]; % 500*2
errorRec = zeros(21,4);

for k = 2:5
    rp = randperm(500);
    initC = alldat(rp(1:k),:);
    nextC = zeros(size(initC,1),2);

    [nextCinfo, error] = calculateMinDistance(initC,alldat);
    errorRec(1,k-1) = sum(error);
    for ite = 1:20
        for ce = 1:k
            temp = alldat(find(nextCinfo==ce),:);
            nextC(ce,:) = mean(temp);
        end
        [nextCinfo, error] = calculateMinDistance(nextC,alldat);
        errorRec(ite+1,k-1) = sum(error);
    end
end
```

```

if (k==3)
    group1 = alldat(find(nextCinfo==1),:);
    group2 = alldat(find(nextCinfo==2),:);
    group3 = alldat(find(nextCinfo==3),:);

    subplot(1,2,1),
    scatter(group1(:,1),group1(:,2),'b'), hold on,
    scatter(group2(:,1),group2(:,2),'k'), hold on,
    scatter(group3(:,1),group3(:,2),'m'),
    title(['k=3'])

end

```

```

if (k==5)
    group1 = alldat(find(nextCinfo==1),:);
    group2 = alldat(find(nextCinfo==2),:);
    group3 = alldat(find(nextCinfo==3),:);
    group4 = alldat(find(nextCinfo==4),:);
    group5 = alldat(find(nextCinfo==5),:);

    subplot(1,2,2),
    scatter(group1(:,1),group1(:,2),'b'), hold on,
    scatter(group2(:,1),group2(:,2),'c'), hold on,
    scatter(group3(:,1),group3(:,2),'g'), hold on,
    scatter(group4(:,1),group4(:,2),'k'), hold on,
    scatter(group5(:,1),group5(:,2),'m'),
    title(['k=5'])

end

```

```

end

```

```

subplot(2,2,1), plot(errorRec(:,1)), title(['k=2']);
subplot(2,2,2), plot(errorRec(:,2)), title(['k=3']);
subplot(2,2,3), plot(errorRec(:,3)), title(['k=4']);
subplot(2,2,4), plot(errorRec(:,4)), title(['k=5']);

```

calculateMinDistance.m

```

function [x y] = calculateMinDistance(center,datapoints)

```

```

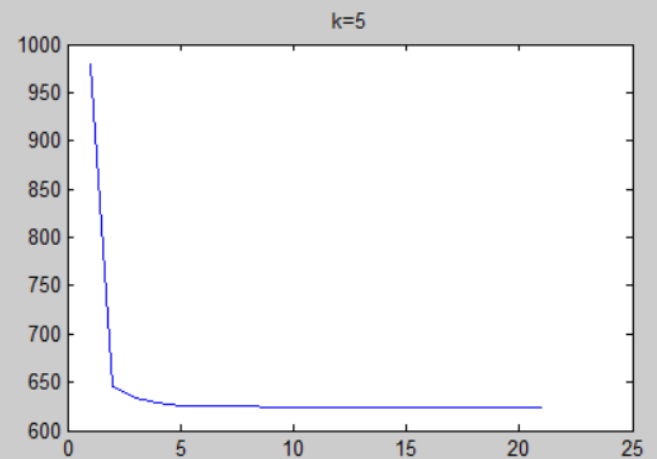
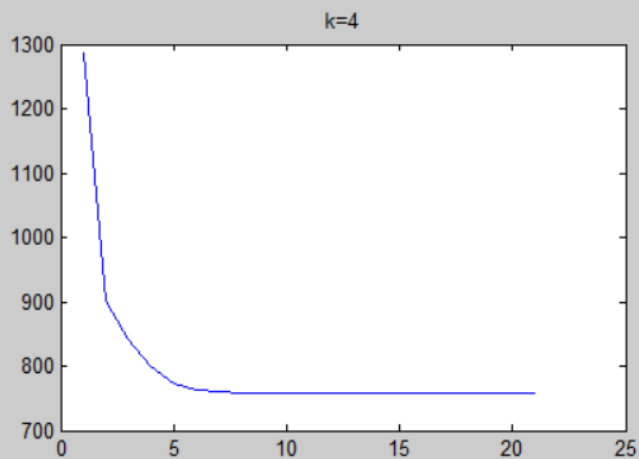
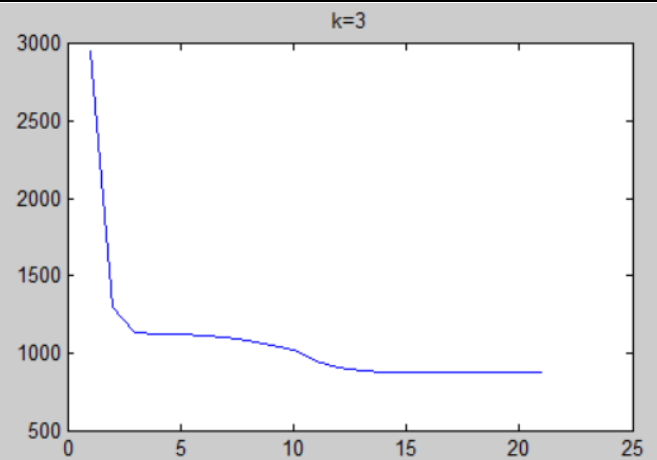
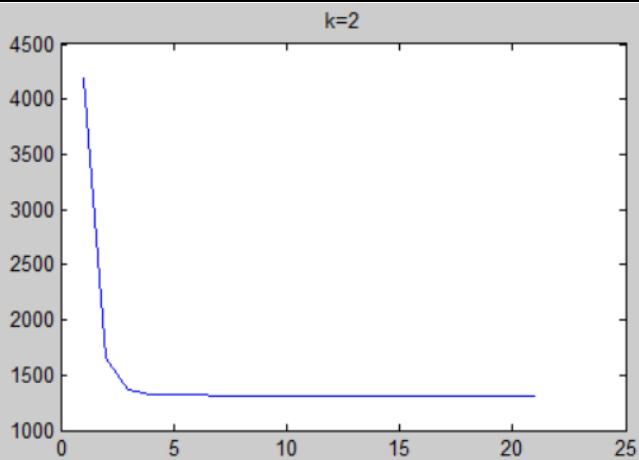
% center: m*n - m center points with n dimension
% datapoint: p*n - p points with n dimension
% x: new category information
% y: min dist information

x = zeros(size(datapoints,1),1);
y = zeros(size(datapoints,1),1);

for i = 1:size(datapoints,1)
    data = datapoints(i,:);
    repdata = repmat(data,[size(center,1) 1]); % m*n
    diff = center - repdata; % m*n
    dist = sum(diff.*diff,2); % euclidean distance
    y(i) = min(dist);
    x(i) = find(dist==min(dist));
end
end

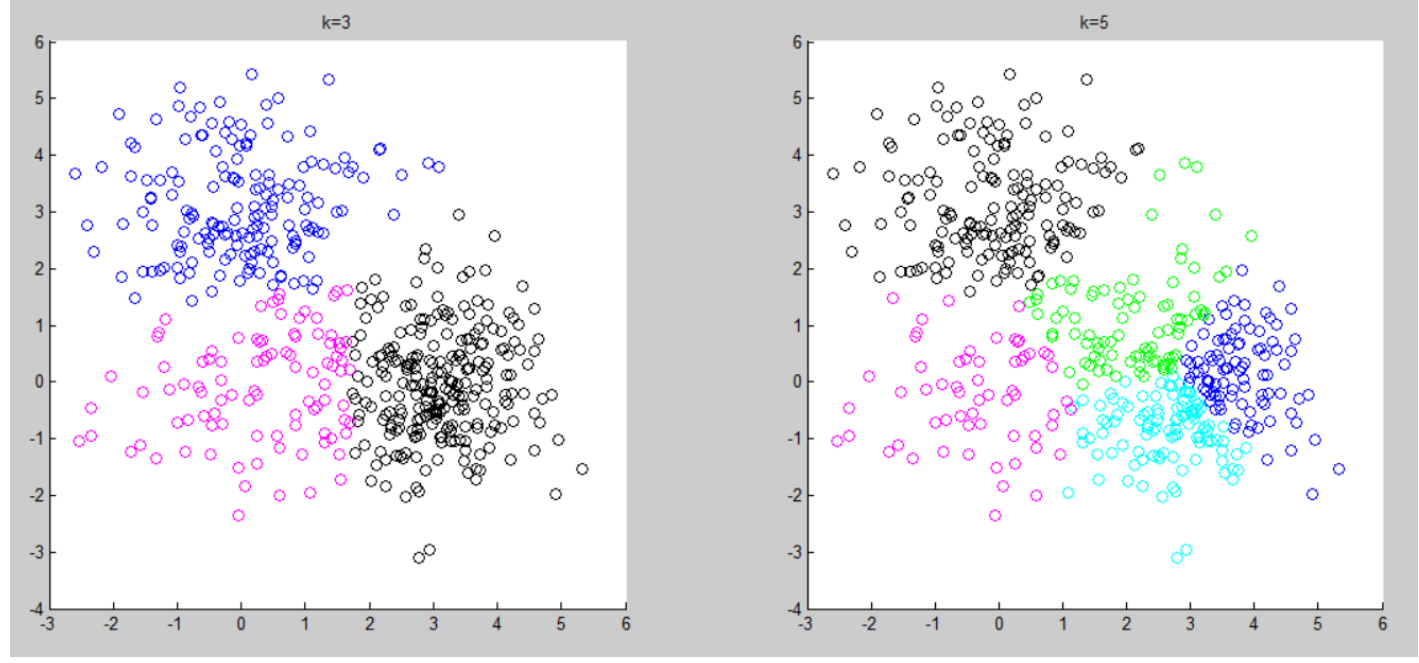
```

K=2, 3, 4, 5



2.

K=3, 5



Problem2

1.

Code:

Hw4pr2.m

```
% hw 4.2
load('movies_matlab_matrix.mat');

%%
%{
fromuser = zeros(943,1682);
for i = 1:943
    user_movie = user(i).movie_id;
    user_rating = user(i).rating;
    fromuser(i,user_movie) = user_rating;
end

frommovie = zeros(943,1682);
for i = 1:1682
    movie_user = movie(i).user_id;
    movie_rating = movie(i).rating;
    frommovie(movie_user,i) = movie_rating;
```

```

end
%}

%%
inim = zeros(1,20);
iniv = 10*eye(20);

userd = mvnrnd(inim,iniv,943);
movied = mvnrnd(inim,iniv,1682);
cst = 2.5;
rec = zeros(943,20,10);

error = zeros(100,1);
logli = zeros(100,1);

%tic

for ite = 1:100
    lg1 = 0; lg2 = 0; lg3 = 0;

    for i = 1:943
        rated = find(fromuser(i,:)~=0); % rated_number*1
        vj = movied(rated,:); % rated_number*20
        former = inv(cst+trace(vj*vj')); % 1*1
        temp = repmat((fromuser(i,rated)'),[1 20]); %repmat(rated_number*1,[1
20])

        latter = sum(temp.*vj); %
sum((rated_number*20).X(rated_number*20))=>1*20
        userd(i,:) = former*latter;

        lg2 = lg2+5*(norm(userd(i,:))^2);
    end

    for j = 1:1682
        rated = find(fromuser(:,j)~=0); % rated_number*1
        ui = userd(rated,:); % rated_number*20;
        former = inv(cst+trace(ui*ui')); % 1*1
        temp = repmat(fromuser(rated,j),[1 20]); %repmat(rated_number*1,[1 20])
        = rated_number*20
    end
end

```

```

        latter = sum(temp.*ui); %
sum((rated_number*20).X(rated_number*20))=>1*20
        movied(j,:) = former*latter;

        lg3 = lg3+5*(norm(movied(j,:))^2);
    end

    diff = zeros(943,1682);
    multi = userd*movied'; % 943*1682
    for i = 1:943
        for j = 1:1682
            if (fromuser(i,j)~=0)
                diff(i,j) = multi(i,j)-fromuser(i,j);
            end
        end
    end

    lg1 = 2*(norm(diff)^2);
    logli(ite) = -(lg1+lg2+lg3);

    errortmp = 0;
    for k = 1:5000
        diff = round(userd(ratings_test(k,1),:)* movied(ratings_test(k,2),:)) -
ratings_test(k,3);
        errortmp = errortmp + diff^2;
    end
    error(ite) = sqrt(errortmp/5000);
end

%toc

```

Hw4pr2p2.m

```

% hw4pr2 p2

load('hw4expl.mat');
load('movies_matlab/movie_ratings.mat');

subplot(1,2,1), plot(error), title(['RMSE']);
subplot(1,2,2), plot(logli), title(['Log likelihood']);

selected_mv = [1101, 1106, 1121];

```

```

closest = zeros(3,6);
mvname = cell(3,6);
dist = zeros(3,6);

for i = 1:3
    mv = movied(selected_mv(i,:),:); % 1*20
    repmv = repmat(mv,[1682 1]); % 1682*20
    subtract = movied-repmv;
    euc = sqrt(sum(subtract.^2,2));
    [y idx] = sort(euc);
    closest(i,:) = idx(1:6);
    dist(i,:) = y(1:6);
    mvname(i,:) = movie_names(idx(1:6));
end

errorRec = zeros(21);

rp = randperm(943);
initC = userd(rp(1:30),:);
nextC = zeros(size(initC,1),20);
[nextCinfo, error] = calculateMinDistance(initC,userd);
errorRec(1) = sum(error);

k = 30;
for ite = 1:20
    for ce = 1:k
        temp = userd(find(nextCinfo==ce),:);
        nextC(ce,:) = mean(temp);
    end
    [nextCinfo, error] = calculateMinDistance(nextC,userd);
    errorRec(ite+1) = sum(error);
end

cent = [5 10 15 20 25];%1:30;
farnear = zeros(20,30);
farnear2 = zeros(20,30);
largest = zeros(10,length(cent));

```

```

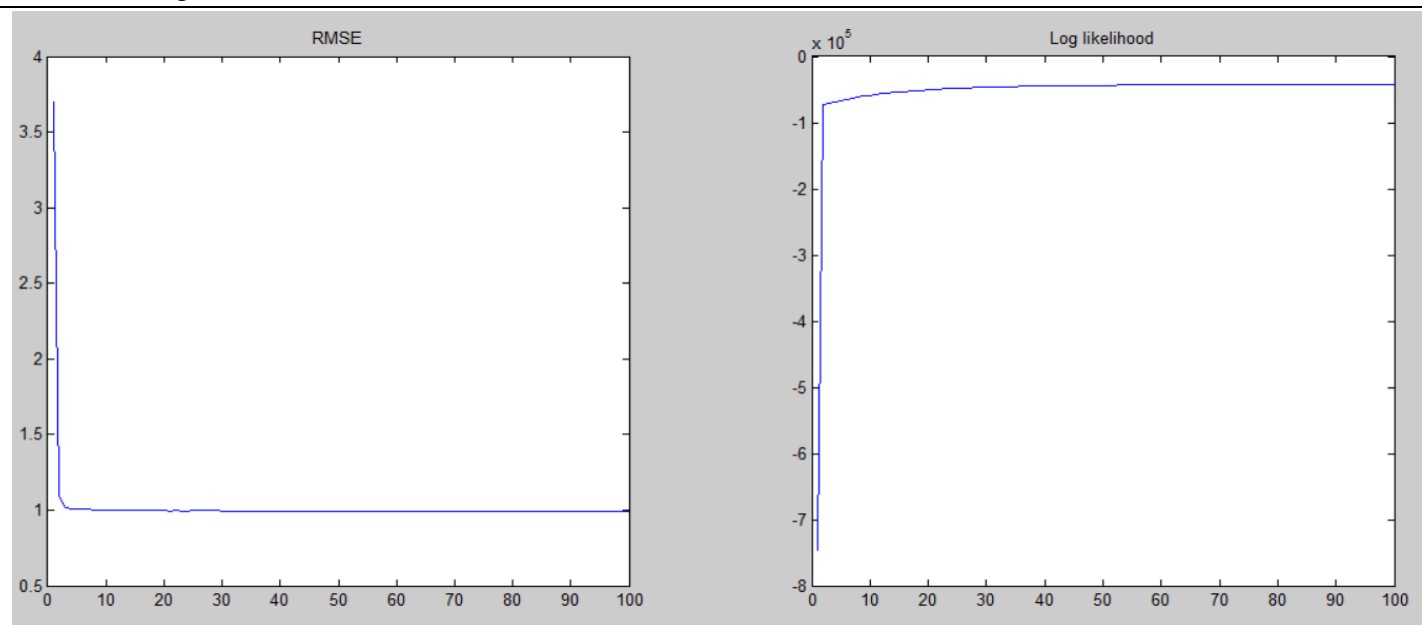
mn = cell(10,length(cent));
test = zeros(1682,length(cent));
test2 = zeros(1682,length(cent));

for i = 1:length(cent)
    curcent = nextC(cent(i,:),:);
    prod = zeros(1,1682);
    for j = 1:1682
        prod(j) = dot(curcent,movied(j,:));%current*movied';
    end
    [rank idy] = sort(prod,'descend');
    largest(:,i) = rank(1:10);
    mn(:,i) = movie_names(idy(1:10));

    test(:,i) = rank;
    test2(:,i) = idy;
    farnear(1:10,i) = rank(1:10);
    farnear(11:20,i) = rank(1673:1682);
    farnear2(1:10,i) = idy(1:10);
    farnear2(11:20,i) = idy(1673:1682);
end

```

RMSE & Loglikelihood



2.

Selected movie index: 1101, 1106, 1121

Selected Movie	'Six Degrees of Separation (1993)'	'Newton Boys, The (1998)'	'Umbrellas of Cherbourg, The (Parapluies de Cherbourg, Les) (1964)'
Closest Movies 1~5	'Horseman on the Roof, The (Hussard sur le toit, Le) (1995)'	'Of Human Bondage (1934)'	'Star Kid (1997)'
	'My Left Foot (1989)'	'Head Above Water (1996)'	'Shanghai Triad (Yao a yao yao dao waipo qiao) (1995)'
	'Brassed Off (1996)'	'Something to Talk About (1995)'	'Bananas (1971)'
	'Streetcar Named Desire, A (1951)'	'Tetsuo II: Body Hammer (1992)'	'Platoon (1986)'
	'Top Hat (1935)'	'Bean (1997)'	'Flirting With Disaster (1996)'

Distance	0.0013	0.0003	0.0034
	0.0014	0.0035	0.0038
	0.0015	0.0043	0.0052
	0.0023	0.0047	0.0053
	0.0029	0.0049	0.0054

3.

Chosen centroid: [5, 10, 15, 20, 25]

'Pather Panchali (1955)'	'Pather Panchali (1955)'	'Pather Panchali (1955)'	'Pather Panchali (1955)'	'Pather Panchali (1955)'
'Close Shave, A (1995)'	'Close Shave, A (1995)'	'Close Shave, A (1995)'	'Close Shave, A (1995)'	'Close Shave, A (1995)'
'Wrong Trousers, The (1993)'	'Wrong Trousers, The (1993)'	'Wrong Trousers, The (1993)'	'Wrong Trousers, The (1993)'	'Wrong Trousers, The (1993)'
'Casablanca (1942)'	'Casablanca (1942)'	'Casablanca (1942)'	'Casablanca (1942)'	'Casablanca (1942)'
'Schindler"s List (1993)'	'Schindler"s List (1993)'	'Schindler"s List (1993)'	'Schindler"s List (1993)'	'Schindler"s List (1993)'
'Wallace & Gromit: The Best of Aardman Animation (1996)'	'Wallace & Gromit: The Best of Aardman Animation (1996)'	'Wallace & Gromit: The Best of Aardman Animation (1996)'	'Wallace & Gromit: The Best of Aardman Animation (1996)'	'Wallace & Gromit: The Best of Aardman Animation (1996)'
'Shawshank	'Shawshank	'Shawshank	'Shawshank	'Shawshank

Redemption, The (1994)'	Redemption, The (1994)'	Redemption, The (1994)'	Redemption, The (1994)'	Redemption, The (1994)'
'Rear Window (1954)'	'Rear Window (1954)'	'Rear Window (1954)'	'Rear Window (1954)'	'Rear Window (1954)'
'12 Angry Men (1957)'	'12 Angry Men (1957)'	'12 Angry Men (1957)'	'12 Angry Men (1957)'	'12 Angry Men (1957)'
'Star Wars (1977)'	'Star Wars (1977)'	'Star Wars (1977)'	'Star Wars (1977)'	'Star Wars (1977)'

Dot product value:				
3.3590	4.3395	4.1992	4.6688	6.0182
3.3554	4.3348	4.1946	4.6637	6.0117
3.3427	4.3184	4.1787	4.6460	5.9889
3.3361	4.3099	4.1702	4.6368	5.9771
3.3252	4.2958	4.1568	4.6217	5.9575
3.3061	4.2712	4.1330	4.5952	5.9234
3.2988	4.2617	4.1239	4.5850	5.9103
3.2539	4.2037	4.0677	4.5226	5.8198
3.2484	4.1965	4.0608	4.5149	5.8199
3.2434	4.1902	4.0547	4.5081	5.8111