

**[WORKING TITLE] Improved Perception-Driven  
Semi-Structured Image Vectorization via a  
Machine-Learning-Based Approach**

**A Special Problem by**

**Sean Francis N. Ballais**

**2015-04562**

**BS CS**

**Presented to the Faculty of the  
Division of Natural Sciences and Mathematics**

**In Partial Fulfillment of the Requirements  
For the Degree of  
Bachelor of Science in Computer Science**

**University of the Philippines Visayas  
TACLOBAN COLLEGE  
Tacloban City**

**Month Year**

This special problem, entitled “[**WORKING TITLE**]  
**IMPROVED PERCEPTION-DRIVEN SEMI-STRUCTURED IMAGE VECTORIZATION VIA A MACHINE-LEARNING-BASED APPROACH**”,  
prepared and submitted by **SEAN FRANCIS N. BALLAIS**,  
in partial fulfillment of the requirements for the degree of  
**BACHELOR OF SCIENCE IN COMPUTER SCIENCE** is  
hereby accepted.

---

PROF. VICTOR M. ROMERO II  
Special Problem Adviser

Accepted as partial fulfillment of the requirements for the degree of  
**BACHELOR OF SCIENCE IN COMPUTER SCIENCE.**

---

DR. EULITO V. CASAS JR.  
Chair, DNSM

# Acknowledgements

First of all I would like to thank the Lord for his guidance during the course of my research and for making this thesis possible. I would like to thank my family who served as my inspiration, and never failed to support me all throughout my studies. Thanks to ...

# Abstract

Although the abstract is the first thing that appears in the thesis, it is best written last after you have written your conclusion. It should contain spell out your thesis problem and describe your solution clearly.

Make sure your abstract fits in one page !

# Table of Contents

<b>Acknowledgements</b>	<b>iii</b>
<b>Abstract</b>	<b>iv</b>
<b>Table of Contents</b>	<b>vi</b>
<b>List of Tables</b>	<b>vii</b>
<b>List of Figures</b>	<b>viii</b>
<b>1 Introduction</b>	<b>1</b>
1.1 The Problems of Raster Graphics . . . . .	3
1.2 Vectorization To The Rescue . . . . .	5
<b>2 Review of Related Literature</b>	<b>9</b>
2.1 Image Upscaling . . . . .	9
Non-Adaptive Techniques . . . . .	10
Adaptive Techniques . . . . .	12
Super Resolution Methods . . . . .	12
2.2 Vectorization of Images . . . . .	12
Natural Images Vectorization . . . . .	13
Vectorization of Semi-Structured Images and Pixel Art . . . . .	14
<b>3 Research Question or Problem Statement</b>	<b>15</b>
<b>4 Objectives</b>	<b>17</b>
<b>5 Describing How You Solved the Problem or Answered the Question</b>	<b>18</b>
<b>6 Describing How You Validated Your Approach.</b>	<b>19</b>

	vi
7 Stating Your Results and Drawing Insights From Them.	20
8 Summarizing Your Thesis and Drawing Your Conclusions.	21
A What should be in the Appendix	22
Bibliography	23

# List of Tables

# List of Figures

- 1.1 When zoomed in enough, each individual pixel of a raster image is visible. Meme image obtained from <http://thesismemes.tumblr.com/post/73483120281>. . . . . 2
- 1.2 Different interpolation algorithms will produce different results. As seen in the image, the quality will also differ, from an image looking blocky to an image looking blurry. Cat meme image obtained from <https://www.hercampus.com/school/uwindsor/school-thoughts-told-grumpy-cat-memes>. . . . .
- 1.3 Zooming in closely at the same image, but one being in raster format (top right) and the other in vector (though hand-drawn; bottom left), quickly reveals the quality differences of both image formats. Raster images will show you individual pixels when close enough, but vectors will remain smooth. . . . . 6



# Chapter 1

## Introduction

In computer graphics, most images are typically stored as a sequence of dots in a rectangular grid (see Fig. 1.1). Each dot is called a pixel, a small part of an image that holds one specific colour. Photographs, also called natural images [12], are one of, if not the most, common images that are stored in this manner. Many digital forms of art or any graphics work, such as paintings, posters, and icons, are also stored the same. Digital images stored in this manner are called *raster images*. These images are stored in various image formats. The most commonly used formats are JPEG, GIF, BMP, TIFF, and PNG. Each have their pros and cons, from quality of the resulting image to the file size. Nevertheless, they all still accomplish the task of holding raster image data. Everything you see in the displays of devices such as laptops and mobile devices is a raster image. Computer displays are collections of pixels, in the common definition of a dot on the screen, which computers map images to to be able display them. This is the reason why **all displayed** images are raster images.

A positive aspect of raster images is their simplicity. As mentioned earlier, raster images consists of a grid of pixels (also called a pixel matrix in other literature [22]). This pixel grid can simply be assigned a combination of colour values to create an



Figure 1.1: When zoomed in enough, each individual pixel of a raster image is visible. Meme image obtained from <http://thesismemes.tumblr.com/post/73483120281>.

image. As such, working with raster images can be analogous to painting in the real world [5]. Given the right combinations of colours, we can produce natural images, i.e. photographs [12]. Intuitively, this means that we can store fine details in a raster image [18]. This is in contrast to *vector images*, which use a series of points and mathematical calculations to form lines and shapes. Vector images are unable to display lush colour depth and keep granularity, as found in raster images, as they use solid colours or gradients [5][6]. There are studies that have been conducted in improving and utilizing *gradient meshes*, a vector graphics primitive that allows for intricate colour gradients in regular quadrilateral meshes first introduced by Adobe Illustrator, to produce photorealistic vector images. However, as noted in the paper by Jian, S, Liang, L., Wen, F., and Shum, H., simple gradient meshes are insufficient to keep the fine details of images [7][18]. It is also important to mention that vector graphics, despite represented as mathematical calculations, are still converted to

raster format in a process called *rasterization* for it to be displayed on-screen, since many modern screens are raster displays [19].

## 1.1 The Problems of Raster Graphics

With all the pros raster graphics have, it does not mean raster graphics are not without their caveats. Raster graphics have their own disadvantages which could affect the image quality and their use.

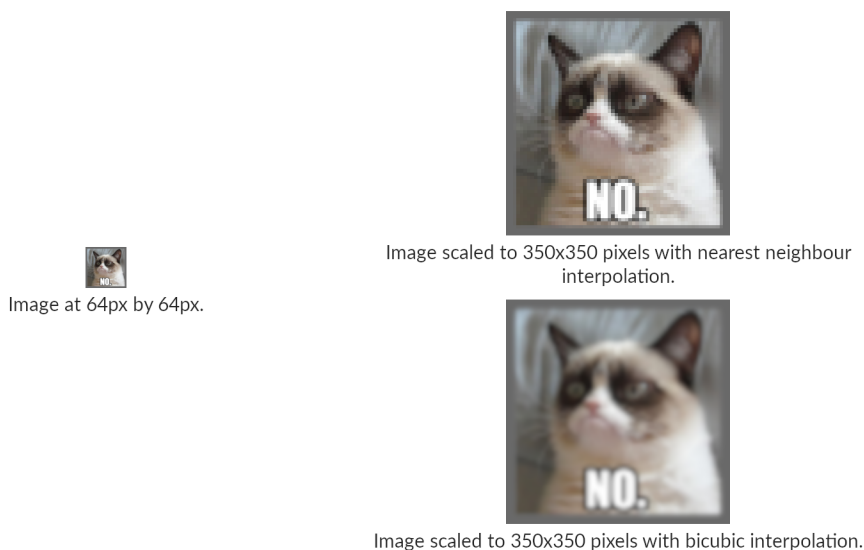


Figure 1.2: Different interpolation algorithms will produce different results. As seen in the image, the quality will also differ, from an image looking blocky to an image looking blurry. Cat meme image obtained from <https://www.hercampus.com/school/uwindsor/school-thoughts-told-grumpy-cat-memes>.

Raster graphics are **resolution-dependent**. This simply means that raster images are in their highest quality in the resolution they are initially created in and attempting to scale it up will gradually degrade the quality of the image as the image size or resolution grows larger. Rasters only have a finite number of pixels. Increasing

the size of an image (also called upsampling [12] or single-image super resolution [24]) would entail moving the individual pixels into different locations depending on the scaling factor, the distance the individual pixels will be moved to horizontally and vertically. Upsampling will create empty pixels in between the shifted pixels when there is nothing done to substitute the empty pixels. This will create an unusable image [10]. We can utilize interpolation to fill these empty pixels with colour. *Classical* image upsampling approaches approximate colour and intensity values of these empty pixels are calculated based on the values of surrounding pixels, typically the shifted pixels. However, the specifics are dependent on the interpolation algorithm used in upscaling the images. Commonly used classical interpolation methods for resizing images include Nearest-Neighbour, Linear Interpolation, and Cubic Interpolation, which most, if not all, are readily available in popular raster image editing applications, such as Adobe Photoshop [2] and GIMP [1]. The results produced by these interpolation algorithms typically suffer from blurring of sharp edges and ringing artifacts due to the fact that the algorithms do not assume anything about the data [14][16]. See Fig. 1.2 for an example of blurring caused by scaling. There are adaptive image scaling techniques that consider image features such as edge information and texture to scale images with better quality than the classical methods. Examples of adaptive techniques are content-aware image resizing, seam curving, and warping-based methods. These techniques have their downsides as they take more computational time than their non-adaptive counterparts and may produce unexpected or even unsatisfactory results [16]. One of the latest advancements in upscaling images involves the use of artificial intelligence, specifically *neural networks*, as found in the works of AI Gigapixel and by Yang, C. Ma, C. and Yang, M.. They produce high quality upscaled images

and is a significant improvement over previous non-AI based upscaling techniques. However, they require high-end expensive hardware to produce results in the shortest amount of time possible. In the case of AI Gigapixel, a laptop with an integrated graphics card takes 20 minutes to produce a final high resolution image. For the work by Yang. C, Ma.C., and Yang. M., they utilized an Nvidia Titan Xp, a high-end GPU that costs \$1,200 as of November 18, 2018 [4], to upscale a 520x520px image 2x, 4x, and 8x its size, and took 0.8s, 2.1s, and 4.4s, respectively, to complete [23][20].

## 1.2 Vectorization To The Rescue

Vectorization is the process of converting raster images into vector images [25]. Vector graphics uses collections of geometric primitives, such as points, curves, and points, and mathematical calculations to form an image [5]. Unlike raster graphics which uses a large pixel matrix (which will require large spaces without using proper image compression), vector graphics are able to smoothly scale to different resolutions, large or small, without any degradation in image quality [22][7]. This makes them **resolution-independent**. Vector graphics innately have this property due to their reliance on mathematics, instead of context-free pixel grids. Each primitive have their own mathematic formulas which, obviously, stay the same no matter what the size of an image is. As such, the primitives can simply be re-rendered whenever the image is scaled [5][6]. Vector graphics also allow for easier editing [12][18], as you only need to modify individual polygons, lines, and curves, instead of dealing with individual pixels like you normally would when using raster images editors.

Vectorization would often be done manually. In a study by Hoshyari, et. al. [12], each of their raster images, which includes icons and small graphic illustrations, take

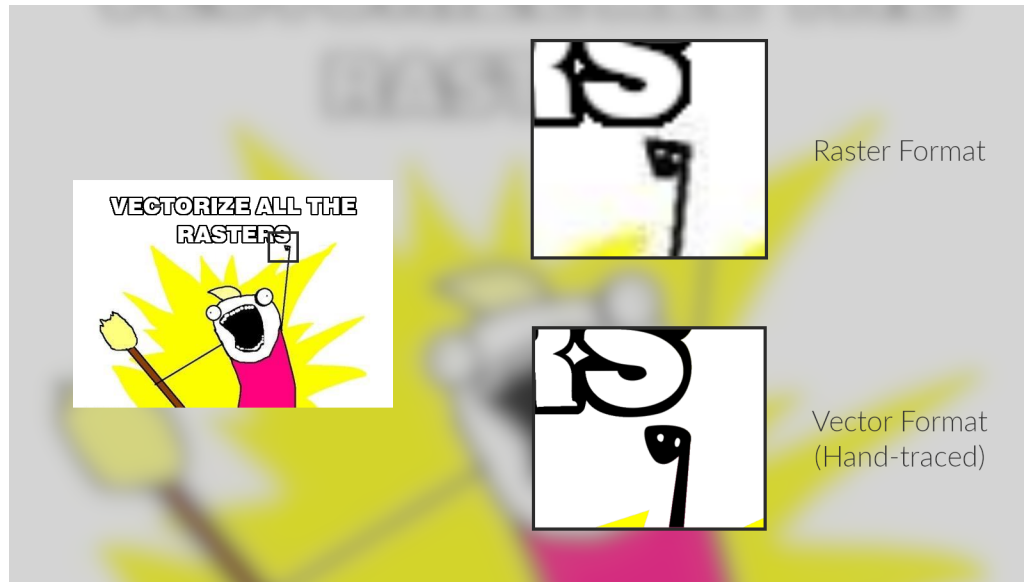


Figure 1.3: Zooming in closely at the same image, but one being in raster format (top right) and the other in vector (though hand-drawn; bottom left), quickly reveals the quality differences of both image formats. Raster images will show you individual pixels when close enough, but vectors will remain smooth.

30-45 minutes to be vectorized by an artist. More than 7 million man hours are being spent on vectorizing raster graphics in the United States every year, according to a survey in the PhD dissertation of J.R. Diebel entitled, "Bayesian image vectorization: The probabilistic inversion of vector image rasterization" [25]. Demand is, therefore, there for a robust vectorization algorithm.

Vectorization have been applied in many cases including, but not limited to, 2D maps and natural images. There are multiple methods that can be utilized in the vectorization of raster images. Their results differ from one method to another and even from one input to another, as many vectorization methods are fine tuned to specific inputs, such as those by Hoshyari, S., et. al. (semi-structured images) [12], Kopf, J. and Lischinski, D. (pixel art) [14], and Bessmeltsev, M. and Solomon, J. (line

drawings) [8]. Additionally, the ability to utilize GPUs for computational tasks has allowed parallelization of vectorization such as in the paper where a GPU was used to vectorize a video stream in real time [22].

Many vectorization methods target natural images. As noted by Hoshyari, S., et. al. many of these natural image vectorization methods utilize *image segmentation* to identify the portions of the image that will be converted into geometric primitives. These primitives are then filled with solid colors (e.g. such as what was done by Birdal, T. and Bala, E. [9]), gradient meshes (which are used in Adobe Illustrator and Corel CorelDraw [18][7]), and/or diffusion curves (such was the case in the paper by Xie, G. Sun, X., Tong, X., and Nowrouzezahrat, D. [21]). These vectorization methods produce differing results whose image qualities vary. Some results are as close as possible to the original raster image. Typically, gradient meshes and diffusion curves were utilized to achieve these results [21][18][7]. Others produce results with obvious colour segmentations, as seen in results that purely utilize solid colours (see [9] for an example).

Natural images are not the only raster images that are being vectorized. Images called semi-structured images are also candidates for image vectorization. *Semi-structured images* (SSIs) are images that consists of distinctly coloured regions and have well-defined boundaries [12]. Logos, cartoons, clip art, computer icons, and even simple graphical illustrations (such as flat 2D art) can considered to be semi-structured images. 60% of the 10 million images to be vectorized are semi-structured images [25]. This makes the demand for vectorizing these types of images evident. Various methods for vectorizing semi-structured images have been proposed by numerous papers. The common methodology of these proposals is that they attempt

to fit curves or Bezier splines on the boundaries of each region in SSIs and fill in the appropriate colour. However, each of these methods naturally have their own unique ways of fitting curves. In the work of Kopf, J., and Lischinski, D. [14], they use similarity graphs and additional intermediate steps in identifying the regions of an image, though their work is targeted at pixel art. Another paper by Yang, M., et. al. would directly optimize the shapes of individual Bezier segments connecting each boundary transition vertices to produce high fidelity vectorized images [12][25]. The work by Hoshyari, S., et. al. can be seen as a complement to the aforementioned paper. Their work utilizes human perceptual cues, primarily guided by Gestalt psychology, to produce vectorizations of semi-structured images that align much more closely to what viewers expect from a raster image [12].

An alternative method we can perform for image vectorization is to use machine learning via convolutional neural networks, a type of neural network that is well suited for image classification for their ability to learn various image features [11], to create vectorizations of semi-structured images by having the computer learn to produce Bezier curves of image region boundaries that align well with the expected vectorization. This is the method that this paper is proposing. A similar work, in that convolutional neural networks were for vectorization, to this is that of the paper of Simo-Serra, E., Iizuka, S., Sasaki, K., and Ishikawa, H. where they convert and simplify paper-and-pencil sketch drawings to vectorized images [17].



# Chapter 2

## Review of Related Literature

Image vectorization has been a long and well-researched field. One of the earliest works on the field dates back to 1982 with the paper by Jimenez, J. and Navalon, J. Their works have been focused on vectorizing digital images from natural scenes [13]. The techniques they have used, such as contour following, have been adapted in later works. Later works have made significant progress over their work and made use of hardware advancements such as GPU utilization for computational tasks.

The primary goal of vectorization is to support multiple resolutions without any loss in the original data. Vectorization is suitable for the task. However, various methods have been proposed that do not involve vectorization. In this chapter, we will explore the previous works done for vectorization and making images support larger resolutions.

### 2.1 Image Upscaling

Raster images are the common format used in representing images. Therefore, these types of images tend to be scaled to different resolutions. The process of scaling these types of images to higher resolutions is called *image upscaling* [12], and is the most

common forms of having raster images support larger resolutions. Naively scaling images would result in images with empty pixels between the shifted pixels, producing a mostly empty image. Thus, the empty pixels are coloured based on their position from, and colour and intensity values of their neighbouring pixels. This process is called *interpolation* [10]. Traditional interpolation algorithms can be classified into two types: Non-adaptive techniques, and adaptive techniques. Each of these types have their own method of resizing images and would produce different results, which may fit in with different objectives of different users [16]. Most recent works uses artificial intelligence to construct a scaled image with as little image quality loss as possible. These works uses neural networks, specifically convolutional and adversarial neural networks, to produce photorealistic upscaled versions of images with little to no distinguishable loss of image quality [23][20][15].

## Non-Adaptive Techniques

Non-adaptive interpolation techniques only scale images horizontally, vertically, or both, by a certain scaling factor, the amount in which the image will be scaled to. They do not assume anything about the underlying image data, except that it is band-limited [14]. This makes them computationally cheap [16], but also suffer from artifacts such as sharp edge blurring and ringing artifacts [14]. Nevertheless, these non-adaptive image interpolation techniques have been widely used in the industry and is standard across different raster image editing programs, such as Adobe Photoshop and GIMP [2][1]. The common non-adaptive interpolation techniques used are:

- Nearest Neighbour

- (Bi)linear Interpolation
- (Bi)cubic Interpolation

### Nearest Neighbour

Nearest Neighbour is the simplest interpolation method to understand. At the high-level, nearest neighbour simply enlarges the size of each individual pixel by a certain factor.

At the lowest level, though this **may** differ implementation-wise, the algorithm will refer back to the original unscaled version to obtain the appropriate colours for each empty pixels in between the shifted pixels in the scaled image. Each empty pixel in the scaled version will map itself to a corresponding pixel in the original image. This is done by obtaining the square coordinates of the empty pixel and dividing the coordinates by the scaling factor. Note that the coordinate system in images starts its origin from the top left, instead of the bottom left. We may acquire a decimal as a result of dividing the coordinates, of which we will floor the values. The resulting coordinates can be mapped to a pixel in the original image. We will then use the mapped pixel's colour as the colour of the empty pixel we are calculating the colour for. The interpolated pixels can be seen as a set  $I$ , as quantified by the equation below.

$$I = \{i | i = C(\lfloor \frac{e_x}{s} \rfloor, \lfloor \frac{e_y}{s} \rfloor)\}, s > 1, e \in E$$

$s$  is the scaling factor,  $C$  is the function that gets the colour of a pixel based on its coordinate, and  $E$  is the set of empty pixels that are in between the shifted pixels when naively upscaled. The resulting image will look blocky since the pixels are just

enlarged. However, this will be ideal for pixel art [10].

### **(Bi)linear and (Bi)cubic interpolation**

Both of (bi)linear and (bi)cubic interpolations schemes are fairly similar to one another. The colours between the empty pixels between them are based on the values of the colours of the shifted pixels.

Each empty pixel acquire most of their colour from the nearest shifted pixel and least from the farthest shifted pixel.

## **Adaptive Techniques**

### **Super Resolution Methods**

Super resolution methods is the process of generating high-resolution images from low-resolution image input. This allows

## **2.2 Vectorization of Images**

Various methods have been proposed throughout the years in the pursuit of supporting larger resolution without any reduction in image quality through vectorization. Typically, vectorization methods target specific inputs, such as natural images or artist drawn images, as certain methods are unsuitable for different inputs. Hoshyari, S., et. al. states that vectorizations targeted at natural images frequently produce inconsistent results when applied to artist-drawn imagery such as logos, and simple graphic illustrations [12]. No matter what the methods used are, they produce vector graphics that will vary in quality, photorealism, and artistic look (view [21], [7], and [9] for a comparison of the results of various vectorization methods).

Despite vector graphics providing a compact and alternative form of representing [22], it is important to remember that due to the inherent characteristics of vector primitives where certain fine details of raster images cannot be accurately represented in vectorized form, vector images will only be giving approximations of the details of images [18]. Nevertheless, finding the perfect balance for image level of detail and image vectorization is an endeavour that is left as an exercise for users [9].

Image vectorization can be dated as far back as the early 1990s, though experiments have started since 1982 at the earliest [13]. Commercial packages, both proprietary and open source, have image vectorization tools whose quality vary. The packages include Adobe Illustrator (Live Trace), Corel CorelDRAW (PowerTRACE), and Inkscape (based on Potrace [3]) [12]. Their wide adoption, though impressive, do not always immediately translate to quality vectorizations. The current available methods still have their own shortfalls and are still in active development. As a result, manual vectorization are still being performed in many industries that heavily require vectorizations [8].

## **Natural Images Vectorization**

Many raster images widely used today are photographs. They contain fine details and lush colour depth that are prominent in the real world. These photographs are also called natural images in digital image processing. Increasing their resolutions would entail using image upscaling techniques (see 2.1), especially the standard classical approaches. This would give the chance of producing low quality images [14] when super resolution methods are not utilized. Vectorization of these natural images are then an alternative to producing high quality higher resolution images.

Vectorization methods targeted at natural images consist the large body of work

that deals with automatic natural imagery vectorization. The core method of these algorithms involves the reliance on edge detection and/or region segmentations to cluster large quantities of pixels together into larger regions [14]. These regions are then filled with either a solid color [9], or gradients via gradient meshes [18][7] or diffusion curves[21].

## **Vectorization of Semi-Structured Images and Pixel Art**

## Chapter 3

# Research Question or Problem Statement

Engineering theses tend to refer to a “problem” to be solved where other disciplines talk in terms of a “question” to be answered. In either case, this section has three main parts:

1. a concise statement of the question that your thesis tackles
2. justification, by direct reference to Chapter 1, that your question is previously unanswered
3. discussion of why it is worthwhile to answer this question.

Item 2 above is where you analyze the information which you presented in Chapter 3. For example, maybe your problem is to “develop a Zylon algorithm capable of handling very large scale problems in reasonable time” (you would further describe what you mean by “large scale” and “reasonable time” in the problem statement). Now in your analysis of the state of the art you would show how each class of current approaches fails (i.e. can handle only small problems, or takes too much time). In

the last part of this section you would explain why having a large-scale fast Zylon algorithm is useful; e.g., by describing applications where it can be used.

Since this is one of the sections that the readers are definitely looking for, highlight it by using the word “problem” or “question” in the title: e.g. “Research Question” or “Problem Statement”, or maybe something more specific such as “The Large-Scale Zylon Algorithm Problem.”



## Chapter 4

### Objectives

This part of the manuscript aims identify the specific objectives that your thesis aims to meet. These objectives must be in alignment with the problem identified in chapter 3.

## Chapter 5

# Describing How You Solved the Problem or Answered the Question

This part of the thesis is much more free-form. It may have one or several sections and subsections. But it all has only one purpose: to convince the examiners that you answered the question or solved the problem that you set for yourself in Chapter 3. So show what you did that is relevant to answering the question or solving the problem: if there were blind alleys and dead ends, do not include these, unless specifically relevant to the demonstration that you answered the thesis question.

## Chapter 6

# Describing How You Validated Your Approach.

## Chapter 7

# Stating Your Results and Drawing Insights From Them.

## Chapter 8

# Summarizing Your Thesis and Drawing Your Conclusions.

# Appendix A

## What should be in the Appendix

What goes in the appendices? Any material which impedes the smooth development of your presentation, but which is important to justify the results of a thesis. Generally it is material that is of too nitty-gritty a level of detail for inclusion in the main body of the thesis, but which should be available for perusal by the examiners to convince them sufficiently. Examples include program listings, immense tables of data, lengthy mathematical proofs or derivations, etc.

# Bibliography

- [1] 6.22.scale image. <https://docs.gimp.org/en/gimp-image-scale.html>.
- [2] Photoshop image size and resolution. <https://helpx.adobe.com/photoshop/using/image-size-resolution.html{\#\}resampling>.
- [3] Potrace - inkscape wiki. <http://wiki.inkscape.org/wiki/index.php/Potrace>.
- [4] Titan xp graphics card with pascal architecture — nvidia geforce. <https://www.nvidia.com/en-us/titan/titan-xp/>.
- [5] Raster vs vector. [https://vector-conversions.com/vectorizing/raster\\_vs\\_vector.html](https://vector-conversions.com/vectorizing/raster_vs_vector.html), n.d.
- [6] Raster vs. vector graphics: What's the difference? <https://pixellogo.com/blogs/pixellogo-blog/raster-vs-vector-graphics>, n.d.
- [7] P. J. Barendrecht, M. Luinstra, J. Hogervorst, and J. Kosinka. Locally refinable gradient meshes supporting branching and sharp colour transitions. *The Visual Computer*, pages 949–960, 2018.
- [8] M. Bessmeltsev and J. Solomon. Vectorization of line drawings via polyvector fields. *CoRR*, abs/1801.01922, 2018.
- [9] T. Birdal and E. Bala. A novel method for vectorization. *CoRR*, abs/1403.0728, 2014.

- [10] Computerphile. Resizing images. [https://www.youtube.com/watch?v=AqscP7rc8f\\\\_}M](https://www.youtube.com/watch?v=AqscP7rc8f\\_}M), 2016.
- [11] Juan Carlos Gonzales. Use of convolutional neural networks for image classification. <https://www.apsl.net/blog/2017/11/20/use-convolutional-neural-network-image-classification/>, 2017.
- [12] S. Hoshyari, E. A. Dominici, A. Sheffer, N. Carr, Z. Wang, D. Ceylan, and I. Shen. Perception-driven semi-structured boundary vectorization. *ACM Transactions on Graphics*, 37(4):1–14, 2018.
- [13] J. Jimenez and J. Navalon. Some experiments in image vectorization. *IBM Journal of Research & Development*, volume = 26 no = 6 month =.
- [14] J. Kopf and D. Lischinski. Depixelizing pixel art. *ACM Transactions on Graphics (Proceedings of SIGGRAPH 2011)*, 30(4):99:1 – 99:8, 2011.
- [15] C. Ledig, L. Theis, F. Huszar, J. Caballero, A. Aitken, A. Tejani, J. Totz, Z. Wang, and W. Shi. Photo-realistic single image super-resolution using a generative adversarial network. *CoRR*, abs/1609.04802, 2016.
- [16] P. Parsania and P. Virparia. *International Journal of Innovative Research in Computer and Communication Engineering*, (12):7409.
- [17] E. Simo-Serra, S. Iizuka, K. Sasaki, and H. Ishikawa. Learning to simplify: Fully convolutional networks for rough sketch cleanup. *ACM Trans. Graph.*, 35(4):121:1–121:11, July 2016.
- [18] J. Sun, L. Liang, F. Wen, and H. Shum. Image vectorization using optimized gradient meshes. Association for Computing Machinery, Inc., July 2007.
- [19] Techquickie. How do vector graphics work? <https://www.youtube.com/watch?v=W2xknX3k6FY>, 2016.



- [20] Y. Wang, F. Perazzi, B. McWilliams, A. Sorkine-Hornung, O. Sorkine-Hornung, and C. Schroers. A fully progressive approach to single-image super-resolution. June 2018.
- [21] G. Xie, X. Sun, X. Tong, and D. Nowrouzezahrai. Hierarchical diffusion curves for accurate automatic image vectorization. *ACM Trans. Graph.*, 33(6):230:1–230:11, 2014.
- [22] X. Xiong, J. Feng, and B. Zhou. Real-time image vectorization on gpu. *Proceedings of the 11th Joint Conference on Computer Vision, Imaging and Computer Graphics Theory and Applications (VISIGRAPP 2016)*, 1:143–150, 2016.
- [23] A. Yang. A.i. gigapixel an inside story topaz labs. <https://topazlabs.com/a-i-gigapixel-story/>, 2018.
- [24] C. Yang, C. Ma, and M. Yang. Single-image super-resolution: A benchmark. pages 372–386. Springer International Publishing, 2014.
- [25] M. Yang, H. Chao, C. Zhang, J. Guo, L. Yuan, and J. Sun. *IEEE Transactions on Visualization and Computer Graphic*.