

## Oscillations 1

### Question 1

Consider a horizontal spring-mass system. The object of mass,  $m$ , is displaced off its equilibrium position by  $x_0$ . It is then released and the mass executes simple harmonic motion.

- (i) Sketch the displacement-time graph of the object and write down the corresponding equation.
- (ii) Sketch a velocity-time graph of the object and write down the corresponding equation.
- (iii) Sketch a restoring force-time graph of the object and write down the corresponding equation.
- (iv) Sketch a velocity-displacement graph of the object and write down the corresponding equation.
- (v) Sketch a graph to show how kinetic energy and potential energy varies with time and write down the corresponding equations.

### Question 2

A mass hangs in equilibrium from a light helical spring. It is given an initial vertical displacement of 0.1 m and released at time  $t = 0$  such that it oscillates with angular frequency of  $0.2 \text{ rad s}^{-1}$ . Determine the displacement, in m, at time  $t$ .

### Question 3

In a harbour, the rise and fall of water is simple harmonic with the time between successive high tides being 12 hours. The depth of the water in the harbour varies from 1.0 m at low tide to 3.0 m at high tide.

A ship which is stranded in the harbour at low tide ( $t = 0$ ) requires a minimum depth of 1.5 m before it can leave the harbour. How long must the ship wait (in hours) before it can leave?

### Question 4

A mass  $m$  at the end of a spring oscillates with a frequency of 0.83 Hz. When an additional 780-g mass is added to  $m$ , the frequency is 0.60 Hz. What is the value of  $m$ ?

**Answers:**

#### Question 2:

$$x = 0.1 \cos(0.2t)$$

#### Question 3:

2 hours

#### Question 4

0.85 kg