## CSCI 432 - Project Deliverable 3

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Written by Timothy A. Chan the Optimal Output-Sensitive Convex Hull Algorithm in two and three dimension is meant to help optimize the process of finding a convex hull. A convex hull is finding the smallest enclosing polygon for a set of points on a Euclidean plane that encompasses all points in the set within the polygon as well as using some of the points to define the outline. This works for Euclidean planes or Euclidean spaces.

This specific algorithm created by Chan is an improvement upon previous convex hull algorithms due to its nature of being output-sensitive. This means that the runtime depends on the output of the algorithm as well as the input. In this case the output of the algorithm is the number of vertexes in the polygon. Chan's algorithm helps to solve the problem of runtime being completely dependent on the input and saying that the size of the output or the number of vertexes in the convex has an impact on the how fast the convex can be calculated. A lot of other convex hull algorithm rely solely on the number of points in the set to determine the runtime. Chan managed to do this by elaborating and improving previous convex hull algorithms. For two dimensional Jarvis's March and Graham's Scan and for three dimensional the gift-wrapping method.

## Pseudo Code

## Algorithm 1 Hull2D

```
1: Input: P, m, H, where P \subset E^2, 3 \le m \le n, and H \ge 1
 2: Output: either incomplete or list of points
 3:
 4: partition P into subsets P_1, \ldots, P_{\lceil n/m \rceil} each of size at most m
 5: for i, \ldots \lceil n/m \rceil do
        compute conv(P_i) by Graham's scan and store its vertices in an array
    in ccw order
 7: end for
 8: p_0 \leftarrow (0, -\infty)
 9: p_1 \leftarrow the rightmost point of P
10: for k = 1, ..., H do
        for i = 1, \ldots, \lceil n/m \rceil do
11:
             compute the point q_i \in P_i that maximizes \angle p_{k-1}p_kq_i \ (q_i \neq p_k) by
12:
    performing a binary search on the vertices of conv(P_i)
13:
        p_{k+1} \leftarrow \text{the point } q \text{ from } \{q_1, \dots, q_{\lceil n/m \rceil}\} \text{ that maximizes } \angle p_{k-1} p_k q
14:
        if p_{k+1} = p_1 then
15:
          return the list \langle p_1, \ldots, p_k \rangle
16:
         end if
17:
18: end for
19: return incomplete
```

## Algorithm 2 Hull2D

```
Input: P, where P \subset E^2

2: Output: L, list of vertices in the hull for t = 1, 2, ... do

4: L \leftarrow \text{Hull2D}(P, m, H). where m = H = min\{2^{2^t}, n\} if L \neq incomplete then

6: return L end if

8: end for
```