
The R Bioc Book

SEAN DAVIS

University of Colorado Anschutz School of Medicine

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Preface

The goal of the material is NOT to teach you R or Bioconductor, but rather to provide enough groundwork to enable you to learn R and Bioconductor on your own. The idea is that we learn faster and better by developing “schemata” that allow us to organize and understand new information. When a new concept is introduced, it is easier to understand if it can be related to something we already know (see Figure 1).

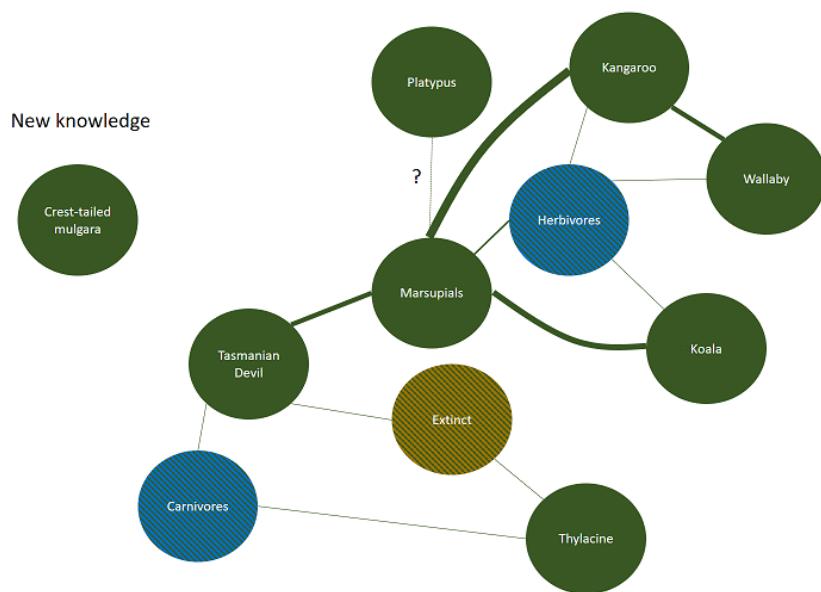


Figure 1.: Schema theory of learning. While probably not entirely applicable to how adults learn, it does highlight the importance of building on prior knowledge. When new knowledge is introduced, it is more quickly stored into long-term memory if strongly-related concepts are already available for connection.

This book is a collection of resources meant to help build your data science, statistical, and computational schemata. It is meant to be largely self-directed, but for those looking to teach data science, it can also be used as a guide for structuring a course. Material is a bit variable in terms of difficulty, prerequisites, and format which is a reflection of the organic

What are the goals?

creation of the material. See below for additional thoughts on adult learning and how it relates to this material.

What are the goals?

We can often get lost in the weeds of technical details of lessons, focusing only on the syntax and semantics of R and Bioconductor. Let's take a step back and consider the big picture. The goals are to:

1. Have a foundation for reading and writing R code to solve problems and understand data.
2. Be able to find and use online resources including AI and tutorials to solve problems and learn new concepts.
3. Be able to effectively communicate with others about R code and data science concepts.
4. Most importantly, to develop the confidence to become a self-directed learner, experimenting with concepts and practice of data science to address real-world problems.

Adult learners

Adult Learning Theory, also known as Andragogy, is the concept and practice of designing, developing, and delivering instructional experiences for adult learners. It is based on the belief that adults learn differently than children, and thus, require distinct approaches to engage, motivate, and retain information (Center 2016). The term was first introduced by Malcolm Knowles, an American educator who is known for his work in adult education (Knowles, Holton, and Swanson 2005).

One of the fundamental principles of Adult Learning Theory is that adults are self-directed learners. This means that we prefer to take control of our own learning process and set personal goals for themselves. We are motivated by our desire to solve problems or gain knowledge to improve our lives (see Figure 2). As a result, educational content for adults should be relevant and applicable to real-life situations. Furthermore, adult learners should be given opportunities to actively engage in the learning process by making choices, setting goals, and evaluating their progress.

Another key aspect of Adult Learning Theory is the role of experience. We bring a wealth of experience to the learning process, which serves as a resource for new learning. We often have well-established beliefs, values, and mental models that can influence our willingness to accept new ideas and concepts. Therefore, it is essential to acknowledge and respect our

Adult learners

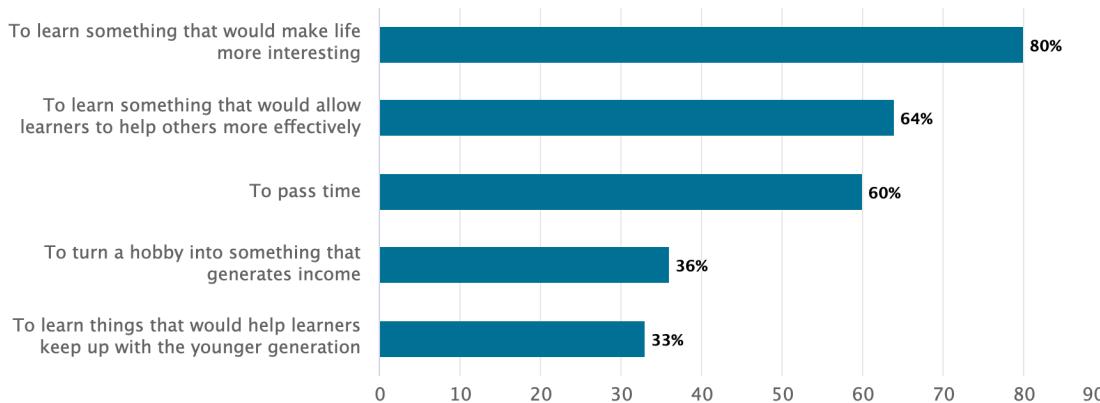


Figure 2.: Why do adults choose to learn something?

shared and unique past experiences and create an environment where we all feel comfortable sharing our perspectives.

To effectively learn as a group of adult learners, it is crucial to establish a collaborative learning environment that promotes open communication and fosters trust among participants. We all appreciate and strive for a respectful and supportive atmosphere where we can express our opinions without fear of judgment. Instructors should help facilitate discussions, encourage peer-to-peer interactions, and incorporate group activities and collaboration to capitalize on the collective knowledge of participants.

Additionally, adult learners often have multiple responsibilities outside of the learning environment, such as work and family commitments. As a result, we require flexible learning opportunities that accommodate busy schedules. Offering a variety of instructional formats, such as online modules, self-paced learning, or evening classes, can help ensure that adult learners have access to education despite any time constraints.

Adult learners benefit from a learner-centered approach that focuses on the individual needs, preferences, and interests of each participant can greatly enhance the overall learning experience. In addition, we tend to be more intrinsically motivated to learn when we have a sense of autonomy and can practice and experiment (see Figure 3) with new concepts in a safe environment.

Understanding Adult Learning Theory and its principles can significantly enhance the effectiveness of teaching and learning as adults. By respecting our autonomy, acknowledging our experiences, creating a supportive learning environment, offering flexible learning opportunities, and utilizing diverse teaching methods, we can better cater to the unique needs and preferences of adult learners.

AI is part of the solution

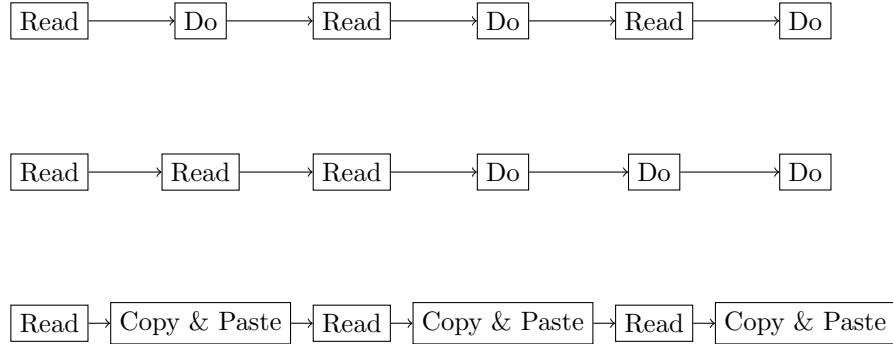


Figure 3.: How to stay stuck in data science (or anything). The “Read-Do” loop tends to deliver the best results. Too much reading between doing can be somewhat effective. Reading and simply copy-paste is probably the least effective. When working through material, experiment. Try to break things. Incorporate your own experience or applications whenever possible.

In practice, that means that we will not be prescriptive in our approach to teaching data science. We will not tell you what to do, but rather we will provide you with a variety of options and you can choose what works best for you. We will also provide you with a variety of resources and you can choose where to focus your time. Given that we cannot possibly cover everything, we will provide you with a framework for learning and you can fill in the gaps as you see fit. A key component of our success as adult learners is to gain the confidence to ask questions and problem-solve on our own.

AI is part of the solution

Artificial Intelligence (AI) is becoming an increasingly important tool in education, and it can be a powerful ally in our quest to learn data science. As it turns out, AI is excellent at helping us learn. It can provide tailored explanations, generate practice problems, and even simulate real-world scenarios for us to work through. AI can also help us find resources, summarize complex topics, and even provide feedback on our work. However, it is important to remember that AI is a tool, not a replacement for our own learning. We still need to engage with the material, ask questions, and seek out additional resources when needed. AI can help us learn more efficiently, but it cannot do the learning for us.

I encourage you to use AI tools to help you learn and to even do work for you when appropriate; AI is an excellent partner in analysis and programming. However, I also encourage you to be critical of the information that AI provides. AI is not perfect and can make mistakes. Throughout this course and book, use AI to dive deeper into the material,

AI is part of the solution

to provide additional explanations, and to generate additional depth and breadth to the material.

Part I.

Introduction

1. About R

In this chapter, we will discuss the basics of R and RStudio, two essential tools in genomics data analysis. We will cover the advantages of using R and RStudio, how to set up RStudio, and the different panels of the RStudio interface.

1.1. What is R?

R is a programming language and software environment designed for statistical computing and graphics. It is widely used by statisticians, data scientists, and researchers for data analysis and visualization. R is an open-source language, which means it is free to use, modify, and distribute. Over the years, R has become particularly popular in the fields of genomics and bioinformatics, owing to its extensive libraries and powerful data manipulation capabilities.

The R language is a dialect of the S language, which was developed in the 1970s at Bell Laboratories. The first version of R was written by Robert Gentleman and Ross Ihaka and released in 1995 (see [this slide deck](#) for Ross Ihaka's take on R's history). Since then, R has been continuously developed by the R Core Team, a group of statisticians and computer scientists. The R Core Team releases a new version of R every year.

1.2. Why use R?

There are several reasons why R is a popular choice for data analysis, particularly in genomics and bioinformatics. These include:

1. **Open-source:** R is free to use and has a large community of developers who contribute to its growth and development. [What is “open-source”?](#)
2. **Extensive libraries:** There are thousands of R packages available for a wide range of tasks, including specialized packages for genomics and bioinformatics. These libraries have been extensively tested and are available for free.
3. **Data manipulation:** R has powerful data manipulation capabilities, making it easy (or at least possible) to clean, process, and analyze large datasets.

1. About R

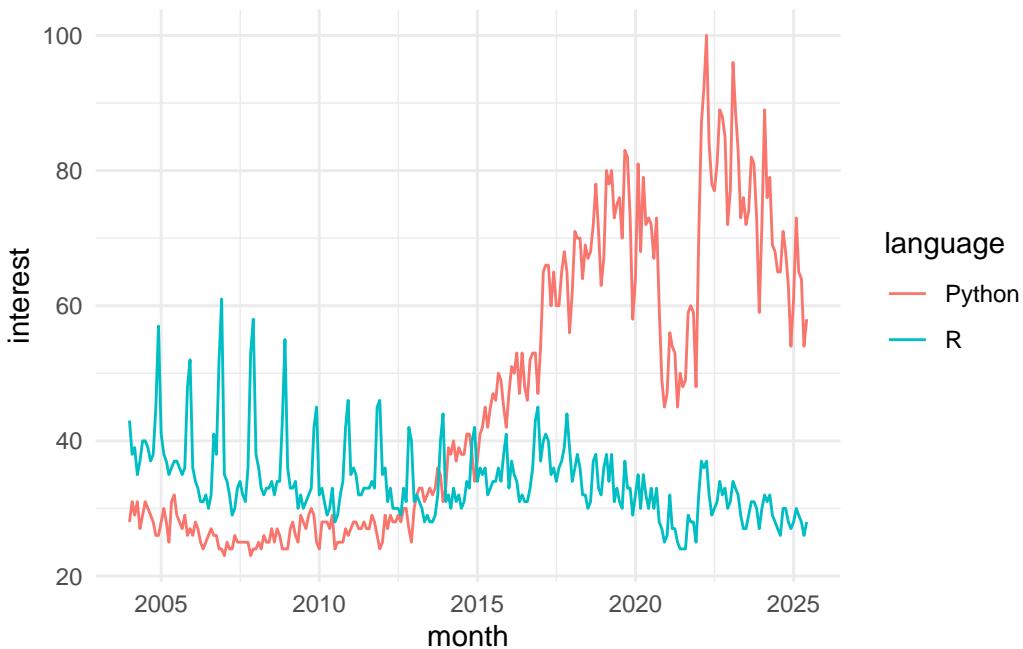


Figure 1.1.: Google trends showing the popularity of R over time based on [Google Trends](#). Note that google does not capture the context here; bioinformatics applications are still quite heavily reliant on R.

1. About R

4. **Graphics and visualization:** R has excellent tools for creating high-quality graphics and visualizations that can be customized to meet the specific needs of your analysis. In most cases, graphics produced by R are publication-quality.
5. **Reproducible research:** R enables you to create reproducible research by recording your analysis in a script, which can be easily shared and executed by others. In addition, R does not have a meaningful graphical user interface (GUI), which renders analysis in R much more reproducible than tools that rely on GUI interactions.
6. **Cross-platform:** R runs on Windows, Mac, and Linux (as well as more obscure systems).
7. **Interoperability with other languages:** R can interact with FORTRAN, C, and many other languages.
8. **Scalability:** R is useful for small and large projects.

I can develop code for analysis on my Mac laptop. I can then install the *same* code on our 20k core cluster and run it in parallel on 100 samples, monitor the process, and then update a database (for example) with R when complete. In other words, R is a powerful tool that can be used for a wide range of tasks, from small-scale data analysis to large-scale genomics and omics data science projects.

1.3. Why not use R?

- R cannot do everything.
- R is not always the “best” tool for the job.
- R will *not* hold your hand. Often, it will *slap* your hand instead.
- The documentation can be opaque (but there is documentation).
- R can drive you crazy (on a good day) or age you prematurely (on a bad one).
- Finding the right package to do the job you want to do can be challenging; worse, some contributed packages are unreliable.]{}
- R does not have a meaningfully useful graphical user interface (GUI).
- Additional languages are becoming increasingly popular for bioinformatics and biological data science, such as Python, Julia, and Rust.

1.4. R License and the Open Source Ideal

R is free (yes, totally free!) and distributed under GNU license. In particular, this license allows one to:

- Download the source code
- Modify the source code to your heart’s content

1. About R

- Distribute the modified source code and even charge money for it, but you must distribute the modified source code under the original GNU license.

This license means that R will always be available, will always be open source, and can grow organically without constraint.

1.5. Working with R

R is a programming language, and as such, it requires you to write code to perform tasks. This can be intimidating for beginners, but it is also what makes R so powerful. In R, you can write scripts to automate tasks, create functions to encapsulate complex operations, and use packages to extend the functionality of R.

R can be used interactively or as a scripting language. In interactive mode, you can enter commands directly into the R console and see the results immediately. In scripting mode, you can write a series of commands in a script file and then execute the entire script at once. This allows you to save your work, reuse code, and share your analysis with others.

In the next section, we will discuss how to set up RStudio, an integrated development environment (IDE) for R that makes it easier to write and execute R code. However, you can use R without RStudio if you prefer to work in the R console or another IDE. RStudio is not required to use R, but it does provide a more user-friendly interface and several useful features that can enhance your R programming experience.

2. RStudio

RStudio is an integrated development environment (IDE) for R. It provides a graphical user interface (GUI) for R, making it easier to write and execute R code. RStudio also provides several other useful features, including a built-in console, syntax-highlighting editor, and tools for plotting, history, debugging, workspace management, and workspace viewing. RStudio is available in both free and commercial editions; the commercial edition provides some additional features, including support for multiple sessions and enhanced debugging.

2.1. Getting started with RStudio

To get started with RStudio, you first need to install both R and RStudio on your computer. Follow these steps:

1. Download and install R from the [official R website](#).
2. Download and install RStudio from the [official RStudio website](#).
3. Launch RStudio. You should see the RStudio interface with four panels.

i R versions

RStudio works with all versions of R, but it is recommended to use the latest version of R to take advantage of the latest features and improvements. You can check your R version by running `version` (no parentheses) in the R console.

You can check the latest version of R on the [R-project website](#).

2.2. The RStudio Interface

RStudio's interface consists of four panels (see Figure 2.1):

- **Console** This panel displays the R console, where you can enter and execute R commands directly. The console also shows the output of your code, error messages, and other information.

2. RStudio

- **Source** This panel is where you write and edit your R scripts. You can create new scripts, open existing ones, and run your code from this panel.
- **Environment** This panel displays your current workspace, including all variables, data objects, and functions that you have created or loaded in your R session.
- **Plots, Packages, Help, and Viewer** These panels display plots, installed packages, help files, and web content, respectively.

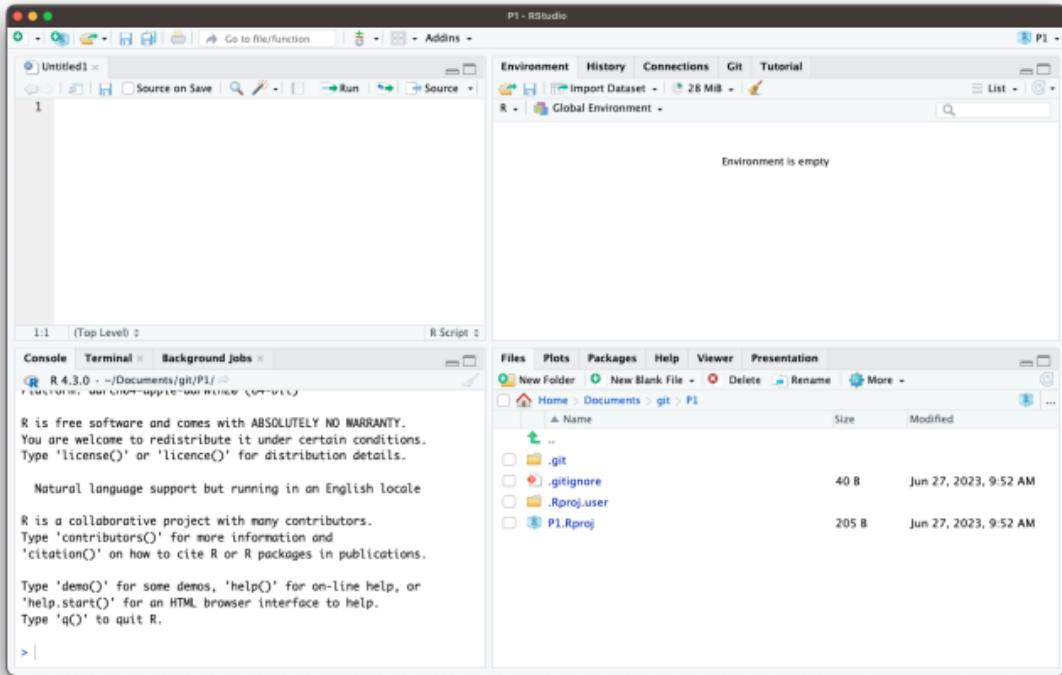


Figure 2.1.: The RStudio interface. In this layout, the **source** pane is in the upper left, the **console** is in the lower left, the **environment** panel is in the top right and the **viewer/help/files** panel is in the bottom right.

i Do I need to use RStudio?

No. You can use R without RStudio. However, RStudio makes it easier to write and execute R code, and it provides several useful features that are not available in the basic R console. Note that the only part of RStudio that is actually interacting with R directly is the console. The other panels are simply providing a GUI that enhances

2. RStudio

the user experience.

Customizing the RStudio Interface

You can customize the layout of RStudio to suit your preferences. To do so, go to **Tools > Global Options > Appearance**. Here, you can change the theme, font size, and panel layout. You can also resize the panels as needed to gain screen real estate (see Figure 2.2).

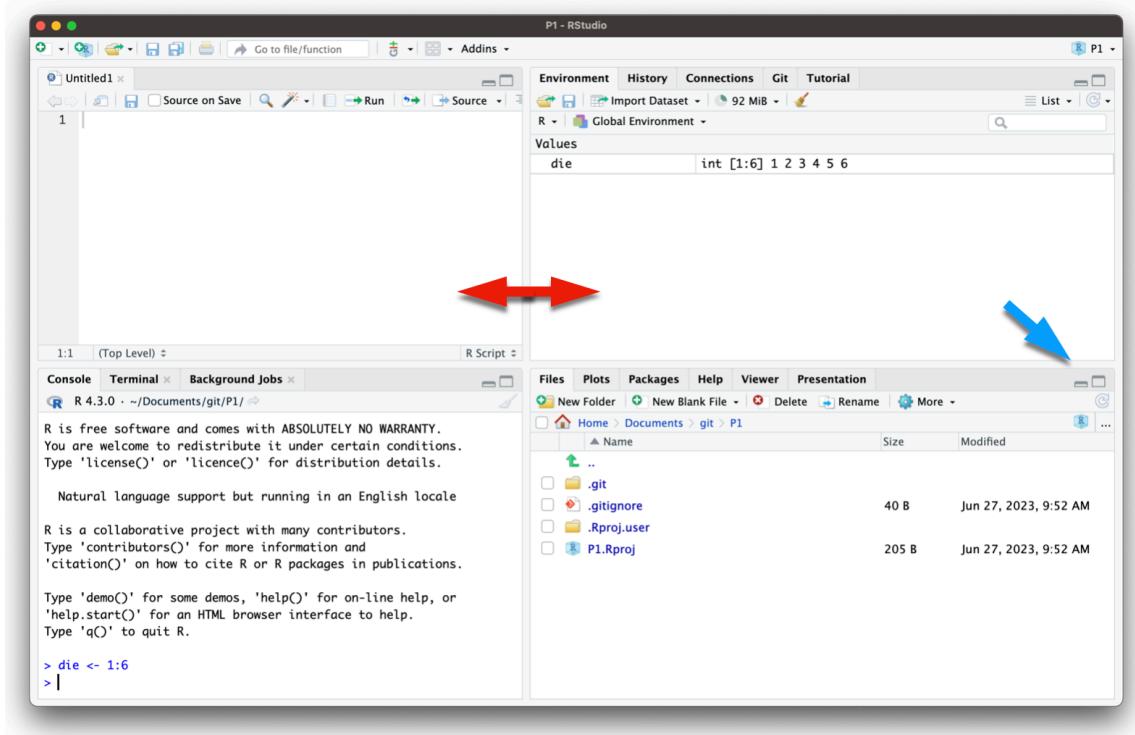


Figure 2.2.: Dealing with limited screen real estate can be a challenge, particularly when you want to open another window to, for example, view a web page. You can resize the panes by sliding the center divider (red arrows) or by clicking on the minimize/maximize buttons (see blue arrow).

In summary, R and RStudio are powerful tools for genomics data analysis. By understanding the advantages of using R and RStudio and familiarizing yourself with the RStudio interface, you can efficiently analyze and visualize your data. In the following chapters, we will delve deeper into the functionality of R, Bioconductor, and various statistical methods to help you gain a comprehensive understanding of genomics data analysis.

2. RStudio

2.3. Alternatives to RStudio

While RStudio is a popular choice for R development, there are several alternatives you can consider:

1. **Jupyter Notebooks:** Jupyter Notebooks provide an interactive environment for writing and executing R code, along with rich text support for documentation. You can use the IRKernel to run R code in Jupyter.

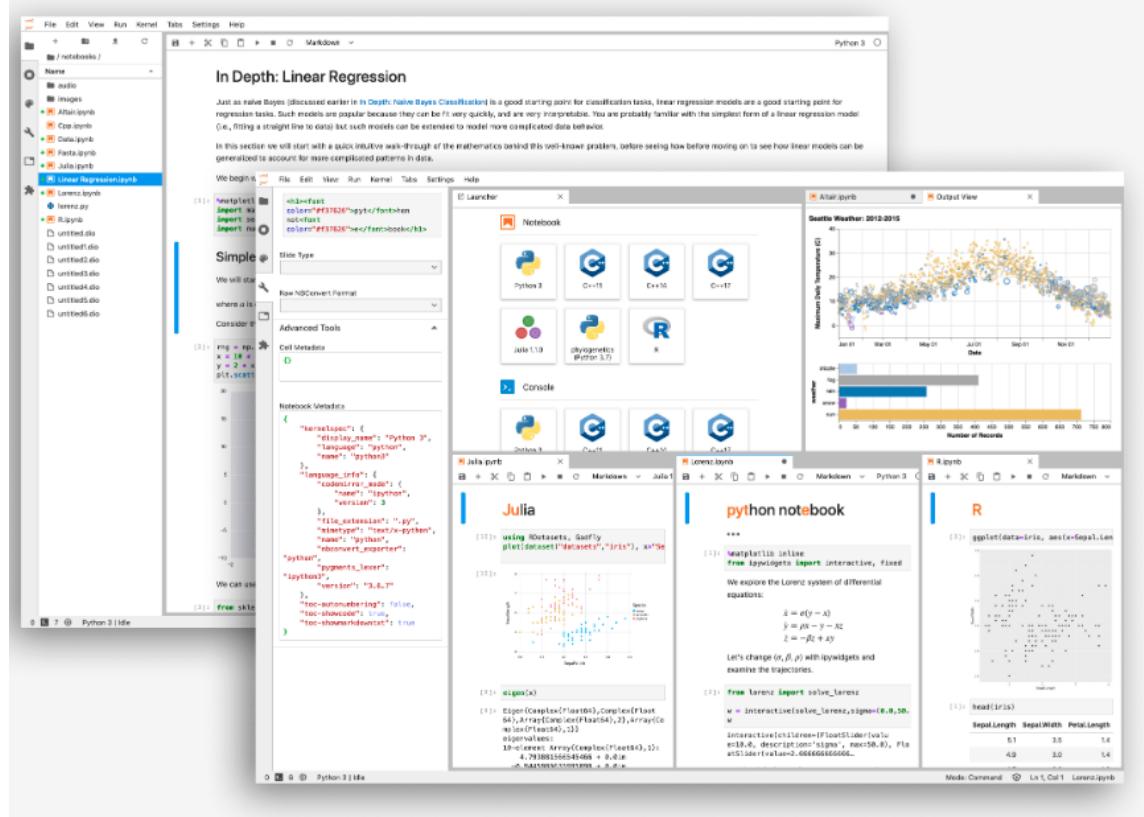


Figure 2.3.: Jupyter Notebook interface. This is an interactive environment for writing and executing R code, along with rich text support for documentation.

2. **Visual Studio Code:** With the R extension for Visual Studio Code, you can write and execute R code in a lightweight editor. This setup provides features like syntax highlighting, code completion, and integrated terminal support.

2. RStudio

The screenshot shows the RStudio interface. On the left, the 'R' pane displays the file structure and code for 'data_analysis.R'. The main workspace shows a terminal window with R code and output, and a plot titled 'Residuals vs Leverage' showing standardized residuals versus leverage. Below the plot are four smaller diagnostic plots.

```

data_analysis.R > ...
1 library(data.table)
2
3 set.seed(123)
4 n <- 1000
5 dt <- data.table(id = 1:n)
6 dt[, x1 := rnorm(.N, mean = 0, sd = 2)]
7 dt[, x2 := runif(.N, min = -1, max = 1)]
8 dt[, y := 2 * x1 + x2 + 0.5 + rnorm(.N)]
9
10 model <- lm(y ~ x1 + x2, data = dt)
11
12 summary(model)
13 plot(model)
14

> library(data.table)
> set.seed(123)
> n <- 1000
> dt <- data.table(id = 1:n)
> dt[, x1 := rnorm(.N, mean = 0, sd = 2)]
> dt[, x2 := runif(.N, min = -1, max = 1)]
> dt[, y := 2 * x1 + x2 + 0.5 + rnorm(.N)]
> model <- lm(y ~ x1 + x2, data = dt)
> summary(model)

Call:
lm(formula = y ~ x1 + x2, data = dt)

Residuals:
    Min      1Q  Median      3Q     Max 
-1.5437 -0.3164 -0.01093  0.34316  1.61131 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -0.0007077  0.4155577  -0.051   0.959    
x1           1.9855840  0.0076404 252.563 <2e-16 ***  
x2           1.0224384  0.0266384  38.382 <2e-16 ***  
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.4919 on 997 degrees of freedom
Multiple R-squared:  0.9851, Adjusted R-squared:  0.9851 
F-statistic: 3.298e+04 on 2 and 997 DF,  p-value: < 2.2e-16

> plot(model)
> 
```

Figure 2.4.: Visual Studio Code (VSCode) with the R extension. This is a lightweight alternative to RStudio that provides syntax highlighting, code completion, and integrated terminal support.

3. **Positron Workbench:** This is a commercial IDE that supports R and Python. It provides a similar interface to RStudio but with additional features for data science workflows, including support for multiple languages and cloud integration.

2. RStudio

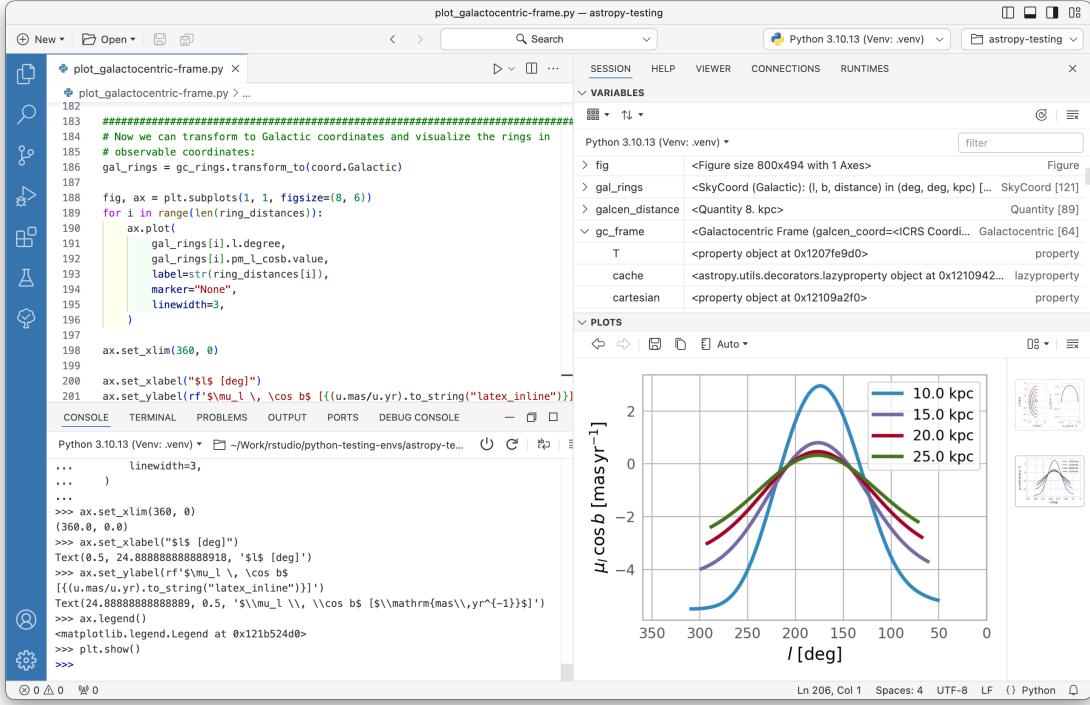


Figure 2.5.: Positron Workbench interface. This IDE supports R and Python, providing a similar interface to RStudio with additional features for data science workflows.

4. **Command Line R:** For those who prefer a minimalist approach, you can use R directly from the command line. This method lacks the GUI features of RStudio but can be efficient for quick tasks, scripting, automation, or when working on remote servers.

Each of these alternatives has its own strengths and weaknesses, so you may want to try a few to see which one best fits your workflow. All are available for free, and you can install them alongside RStudio if you wish to use multiple environments. Each can be installed in Windows, Mac, and Linux.

3. R mechanics

3.1. Starting R

We've installed R and RStudio. Now, let's start R and get going. How to start R depends a bit on the operating system (Mac, Windows, Linux) and interface. In this course, we will largely be using an Integrated Development Environment (IDE) called *RStudio*, but there is nothing to prohibit using R at the command line or in some other interface (and there are a few).

3.2. RStudio: A Quick Tour

The RStudio interface has multiple panes. All of these panes are simply for convenience except the "Console" panel, typically in the lower left corner (by default). The console pane contains the running R interface. If you choose to run R outside RStudio, the interaction will be *identical* to working in the console pane. This is useful to keep in mind as some environments, such as a computer cluster, encourage using R without RStudio.

- Panes
- Options
- Help
- Environment, History, and Files

3.3. Interacting with R

The only meaningful way of interacting with R is by typing into the R console. At the most basic level, anything that we type at the command line will fall into one of two categories:

1. Assignments

```
x = 1  
y <- 2
```

3. R mechanics

2. Expressions

```
1 + pi + sin(42)
```

```
[1] 3.225071
```

The assignment type is obvious because either the `<-` or `=` are used. Note that when we type expressions, R will return a result. In this case, the result of R evaluating `1 + pi + sin(42)` is 3.2250711.

The standard R prompt is a “`>`” sign. When present, R is waiting for the next expression or assignment. If a line is not a complete R command, R will continue the next line with a “`+`”. For example, typing the following with a “Return” after the second “`+`” will result in R giving back a “`+`” on the next line, a prompt to keep typing.

```
1 + pi +
sin(3.7)
```

```
[1] 3.611757
```

R can be used as a glorified calculator by using R expressions. Mathematical operations include:

- Addition: `+`
- Subtraction: `-`
- Multiplication: `*`
- Division: `/`
- Exponentiation: `^`
- Modulo: `%%`

The `^` operator raises the number to its left to the power of the number to its right: for example `3^2` is 9. The modulo returns the remainder of the division of the number to the left by the number on its right, for example 5 modulo 3 or `5 %% 3` is 2.

3.3.1. Expressions

```
5 + 2
28 %% 3
3^2
5 + 4 * 4 + 4 ^ 4 / 10
```

3. R mechanics

Note that R follows order-of-operations and groupings based on parentheses.

```
5 + 4 / 9  
(5 + 4) / 9
```

3.3.2. Assignment

While using R as a calculator is interesting, to do useful and interesting things, we need to assign *values* to *objects*. To create objects, we need to give it a name followed by the assignment operator `<-` (or, entirely equivalently, `=`) and the value we want to give it:

```
weight_kg <- 55
```

`<-` is the assignment operator. Assigns values on the right to objects on the left, it is like an arrow that points from the value to the object. Using an `=` is equivalent (in nearly all cases). Learn to use `<-` as it is good programming practice.

Objects can be given any name such as `x`, `current_temperature`, or `subject_id` (see below). You want your object names to be explicit and not too long. They cannot start with a number (`2x` is not valid but `x2` is). R is case sensitive (e.g., `weight_kg` is different from `Weight_kg`). There are some names that cannot be used because they represent the names of fundamental functions in R (e.g., `if`, `else`, `for`, see [here](#) for a complete list). In general, even if it's allowed, it's best to not use other function names, which we'll get into shortly (e.g., `c`, `T`, `mean`, `data`, `df`, `weights`). When in doubt, check the help to see if the name is already in use. It's also best to avoid dots (.) within a variable name as in `my.dataset`. It is also recommended to use nouns for variable names, and verbs for function names.

When assigning a value to an object, R does not print anything. You can force to print the value by typing the name:

```
weight_kg
```

```
[1] 55
```

Now that R has `weight_kg` in memory, which R refers to as the “global environment”, we can do arithmetic with it. For instance, we may want to convert this weight in pounds (weight in pounds is 2.2 times the weight in kg).

3. R mechanics

```
2.2 * weight_kg
```

```
[1] 121
```

We can also change a variable's value by assigning it a new one:

```
weight_kg <- 57.5  
2.2 * weight_kg
```

```
[1] 126.5
```

This means that assigning a value to one variable does not change the values of other variables. For example, let's store the animal's weight in pounds in a variable.

```
weight_lb <- 2.2 * weight_kg
```

and then change `weight_kg` to 100.

```
weight_kg <- 100
```

What do you think is the current content of the object `weight_lb`, 126.5 or 220?

You can see what objects (variables) are stored by viewing the Environment tab in Rstudio. You can also use the `ls()` function. You can remove objects (variables) with the `rm()` function. You can do this one at a time or remove several objects at once. You can also use the little broom button in your environment pane to remove everything from your environment.

```
ls()  
rm(weight_lb, weight_kg)  
ls()
```

What happens when you type the following, now?

```
weight_lb # oops! you should get an error because weight_lb no longer exists!
```

3.4. Rules for Names in R

R allows users to assign names to objects such as variables, functions, and even dimensions of data. However, these names must follow a few rules.

- Names may contain any combination of letters, numbers, underscore, and ":"
- Names may not start with numbers, underscore.
- R names are case-sensitive.

Examples of valid R names include:

```
pi  
x  
camelCaps  
my_stuff  
MY_Stuff  
this.is.the.name.of.the.man  
ABC123  
abc1234asdf  
.hi
```

3.5. Resources for Getting Help

There is extensive built-in help and documentation within R. A separate page contains a collection of [additional resources](#).

If the name of the function or object on which help is sought is known, the following approaches with the name of the function or object will be helpful. For a concrete example, examine the help for the `print` method.

```
help(print)  
help('print')  
?print
```

If the name of the function or object on which help is sought is *not* known, the following from within R will be helpful.

```
help.search('microarray')  
RSiteSearch('microarray')  
apropos('histogram')
```

3. R mechanics

There are also tons of online resources that Google will include in searches if online searching feels more appropriate.

I strongly recommend using `help("newfunction")` for all functions that are new or unfamiliar to you.

There are also many open and free resources and reference guides for R.

- [Quick-R](#): a quick online reference for data input, basic statistics and plots
- R reference card [PDF](#) by Tom Short
- Rstudio [cheatsheets](#)

4. Up and Running with R

In this chapter, we’re going to get an introduction to the R language, so we can dive right into programming. We’re going to create a pair of virtual dice that can generate random numbers. No need to worry if you’re new to programming. We’ll return to many of the concepts here in more detail later.

To simulate a pair of dice, we need to break down each die into its essential features. A die can only show one of six numbers: 1, 2, 3, 4, 5, and 6. We can capture the die’s essential characteristics by saving these numbers as a group of values in the computer. Let’s save these numbers first and then figure out a way to “roll” our virtual die.

4.1. The R User Interface

The RStudio interface is simple. You type R code into the bottom line of the RStudio console pane and then click Enter to run it. The code you type is called a *command*, because it will command your computer to do something for you. The line you type it into is called the *command line*.

When you type a command at the prompt and hit Enter, your computer executes the command and shows you the results. Then RStudio displays a fresh prompt for your next command. For example, if you type `1 + 1` and hit Enter, RStudio will display:

```
> 1 + 1  
[1] 2  
>
```

You’ll notice that a `[1]` appears next to your result. R is just letting you know that this line begins with the first value in your result. Some commands return more than one value, and their results may fill up multiple lines. For example, the command `100:130` returns 31 values; it creates a sequence of integers from 100 to 130. Notice that new bracketed numbers appear at the start of the second and third lines of output. These numbers just mean that the second line begins with the 14th value in the result, and the third line begins with the 25th value. You can mostly ignore the numbers that appear in brackets:

4. Up and Running with R

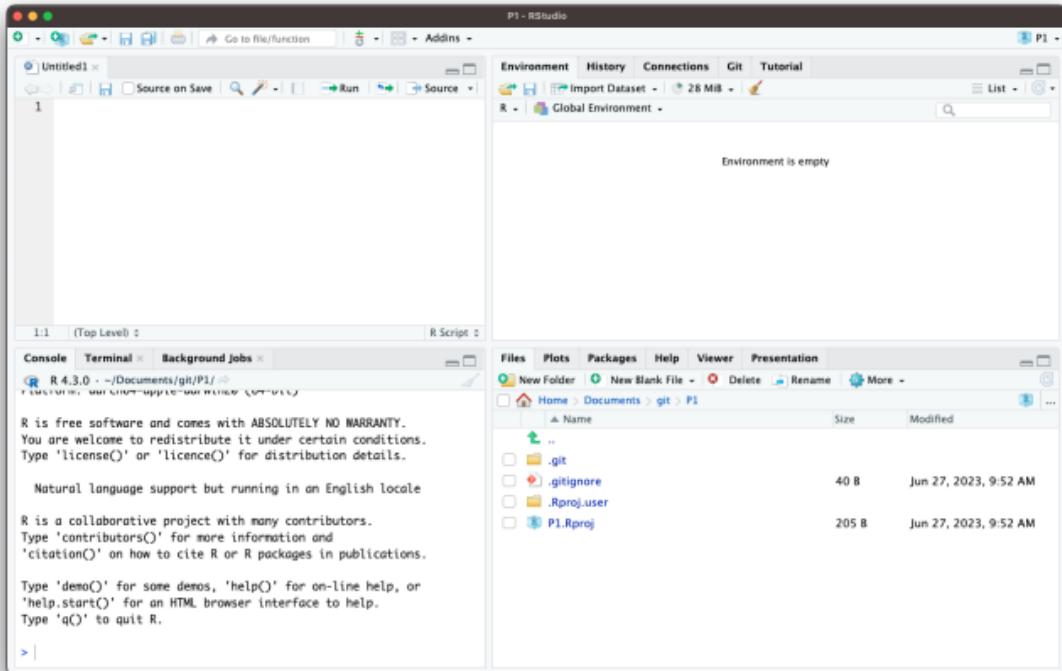


Figure 4.1.: Your computer does your bidding when you type R commands at the prompt in the bottom line of the console pane. Don't forget to hit the Enter key. When you first open RStudio, the console appears in the pane on your left, but you can change this with **File > Tools > Global Options** in the menu bar.

4. Up and Running with R

```
> 100:130
[1] 100 101 102 103 104 105 106 107 108 109 110 111 112
[14] 113 114 115 116 117 118 119 120 121 122 123 124 125
[25] 126 127 128 129 130
```

Tip

The colon operator (:) returns every integer between two integers. It is an easy way to create a sequence of numbers.

When do we compile?

In some languages, like C, Java, and FORTRAN, you have to compile your human-readable code into machine-readable code (often 1s and 0s) before you can run it. If you've programmed in such a language before, you may wonder whether you have to compile your R code before you can use it. The answer is no. R is a dynamic programming language, which means R automatically interprets your code as you run it.

If you type an incomplete command and press Enter, R will display a + prompt, which means R is waiting for you to type the rest of your command. Either finish the command or hit Escape to start over:

```
> 5 -
+
+ 1
[1] 4
```

If you type a command that R doesn't recognize, R will return an error message. If you ever see an error message, don't panic. R is just telling you that your computer couldn't understand or do what you asked it to do. You can then try a different command at the next prompt:

```
> 3 % 5
Error: unexpected input in "3 % 5"
>
```

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💡 Tip

Whenever you get an error message in R, consider googling the error message. You'll often find that someone else has had the same problem and has posted a solution online. Simply cutting-and-pasting the error message into a search engine will often work

Once you get the hang of the command line, you can easily do anything in R that you would do with a calculator. For example, you could do some basic arithmetic:

```
2 * 3
```

```
[1] 6
```

```
4 - 1
```

```
[1] 3
```

```
# this obeys order-of-operations  
6 / (4 - 1)
```

```
[1] 2
```

💡 Tip

R treats the hashtag character, #, in a special way; R will not run anything that follows a hashtag on a line. This makes hashtags very useful for adding comments and annotations to your code. Humans will be able to read the comments, but your computer will pass over them. The hashtag is known as the *commenting symbol* in R.

❗ Cancelling commands

Some R commands may take a long time to run. You can cancel a command once it has begun by pressing **ctrl + c** or by clicking the “stop sign” if it is available in Rstudio. Note that it may also take R a long time to cancel the command.

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4.1.1. An exercise

That's the basic interface for executing R code in RStudio. Think you have it? If so, try doing these simple tasks. If you execute everything correctly, you should end up with the same number that you started with:

1. Choose any number and add 2 to it.
2. Multiply the result by 3.
3. Subtract 6 from the answer.
4. Divide what you get by 3.

```
10 + 2
```

```
[1] 12
```

```
12 * 3
```

```
[1] 36
```

```
36 - 6
```

```
[1] 30
```

```
30 / 3
```

```
[1] 10
```

4.2. Objects

Now that you know how to use R, let's use it to make a virtual die. The `:` operator from a couple of pages ago gives you a nice way to create a group of numbers from one to six. The `:` operator returns its results as a **vector** (we are going to work with vectors in more detail), a one-dimensional set of numbers:

```
1:6  
## 1 2 3 4 5 6
```

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That's all there is to how a virtual die looks! But you are not done yet. Running `1:6` generated a vector of numbers for you to see, but it didn't save that vector anywhere for later use. If we want to use those numbers again, we'll have to ask your computer to save them somewhere. You can do that by creating an R *object*.

R lets you save data by storing it inside an R object. What is an object? Just a name that you can use to call up stored data. For example, you can save data into an object like `a` or `b`. Wherever R encounters the object, it will replace it with the data saved inside, like so:

```
a <- 1  
a
```

```
[1] 1
```

```
a + 2
```

```
[1] 3
```

What just happened?

1. To create an R object, choose a name and then use the less-than symbol, `<`, followed by a minus sign, `-`, to save data into it. This combination looks like an arrow, `<-`. R will make an object, give it your name, and store in it whatever follows the arrow. So `a <- 1` stores 1 in an object named `a`.
2. When you ask R what's in `a`, R tells you on the next line.
3. You can use your object in new R commands, too. Since `a` previously stored the value of 1, you're now adding 1 to 2.

Assignment vs expressions

Everything that you type into the R console can be assigned to one of two categories:

- Assignments
- Expressions

An expression is a command that tells R to do something. For example, `1 + 2` is an expression that tells R to add 1 and 2. When you type an expression into the R console, R will evaluate the expression and return the result. For example, if you type `1 + 2` into the R console, R will return 3. Expressions can have “side effects”

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but they don't explicitly result in anything being added to R memory.

```
5 + 2
```

```
[1] 7
```

```
28 %% 3
```

```
[1] 1
```

```
3^2
```

```
[1] 9
```

```
5 + 4 * 4 + 4 ^ 4 / 10
```

```
[1] 46.6
```

While using R as a calculator is interesting, to do useful and interesting things, we need to assign values to objects. To create objects, we need to give it a name followed by the assignment operator `<-` (or, entirely equivalently, `=`) and the value we want to give it:

```
weight_kg <- 55
```

So, for another example, the following code would create an object named `die` that contains the numbers one through six. To see what is stored in an object, just type the object's name by itself:

```
die <- 1:6  
die
```

```
[1] 1 2 3 4 5 6
```

When you create an object, the object will appear in the environment pane of RStudio, as shown in Figure 4.2. This pane will show you all of the objects you've created since opening RStudio.

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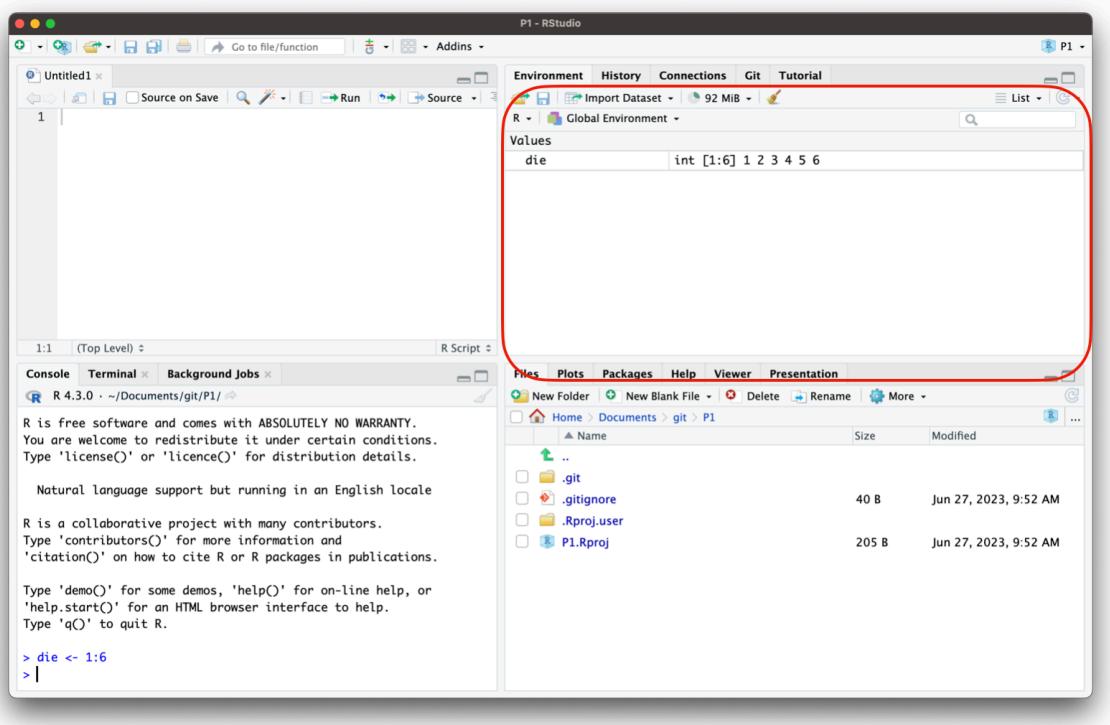


Figure 4.2.: Assignment creates an object in the environment pane.

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You can name an object in R almost anything you want, but there are a few rules. First, a name cannot start with a number. Second, a name cannot use some special symbols, like `^`, `!`, `$`, `@`, `+`, `-`, `/`, or `*`:

Good names	Names that cause errors
a	1trial
b	\$
FOO	^mean
my_var	2nd
.day	!bad

Capitalization matters

R is case-sensitive, so `name` and `Name` will refer to different objects:

```
> Name = 0
> Name + 1
[1] 1
> name + 1
Error: object 'name' not found
```

The error above is a common one!

Finally, R will overwrite any previous information stored in an object without asking you for permission. So, it is a good idea to *not* use names that are already taken:

```
my_number <- 1
```

```
my_number
```

```
[1] 1
```

```
my_number <- 999
```

```
my_number
```

```
[1] 999
```

You can see which object names you have already used with the function `ls`:

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```
ls()
```

Your environment will contain different names than mine, because you have probably created different objects.

You can also see which names you have used by examining RStudio's environment pane.

We now have a virtual die that is stored in the computer's memory and which has a name that we can use to refer to it. You can access it whenever you like by typing the word `die`.

So what can you do with this die? Quite a lot. R will replace an object with its contents whenever the object's name appears in a command. So, for example, you can do all sorts of math with the die. Math isn't so helpful for rolling dice, but manipulating sets of numbers will be your stock and trade as a data scientist. So let's take a look at how to do that:

```
die - 1
```

```
[1] 0 1 2 3 4 5
```

```
die / 2
```

```
[1] 0.5 1.0 1.5 2.0 2.5 3.0
```

```
die * die
```

```
[1] 1 4 9 16 25 36
```

R uses *element-wise execution* when working with a *vector* like `die`. When you manipulate a set of numbers, R will apply the same operation to each element in the set. So for example, when you run `die - 1`, R subtracts one from each element of `die`.

When you use two or more vectors in an operation, R will line up the vectors and perform a sequence of individual operations. For example, when you run `die * die`, R lines up the two `die` vectors and then multiplies the first element of vector 1 by the first element of vector 2. R then multiplies the second element of vector 1 by the second element of vector 2, and so on, until every element has been multiplied. The result will be a new vector the same length as the first two {Figure 4.3}.

If you give R two vectors of unequal lengths, R will repeat the shorter vector until it is as long as the longer vector, and then do the math, as shown in Figure 4.4. This isn't a

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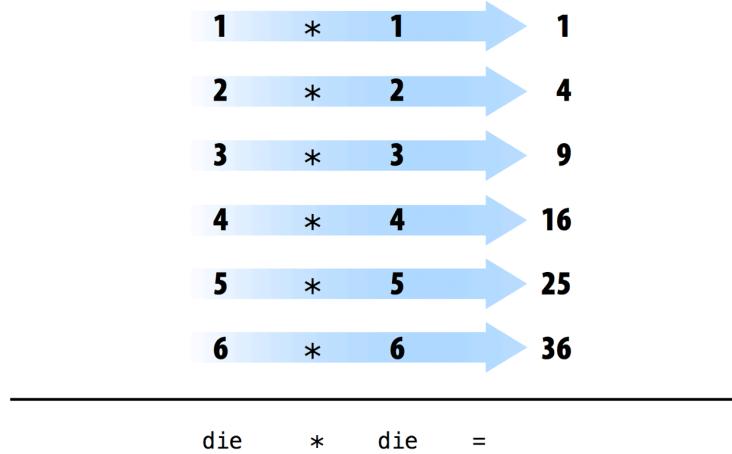


Figure 4.3.: “When R performs element-wise execution, it matches up vectors and then manipulates each pair of elements independently.”

permanent change—the shorter vector will be its original size after R does the math. If the length of the short vector does not divide evenly into the length of the long vector, R will return a warning message. This behavior is known as *vector recycling*, and it helps R do element-wise operations:

```
1:2
```

```
[1] 1 2
```

```
1:4
```

```
[1] 1 2 3 4
```

```
die
```

```
[1] 1 2 3 4 5 6
```

```
die + 1:2
```

```
[1] 2 4 4 6 6 8
```

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```
die + 1:4
```

Warning in die + 1:4: longer object length is not a multiple of shorter object length

```
[1] 2 4 6 8 6 8
```

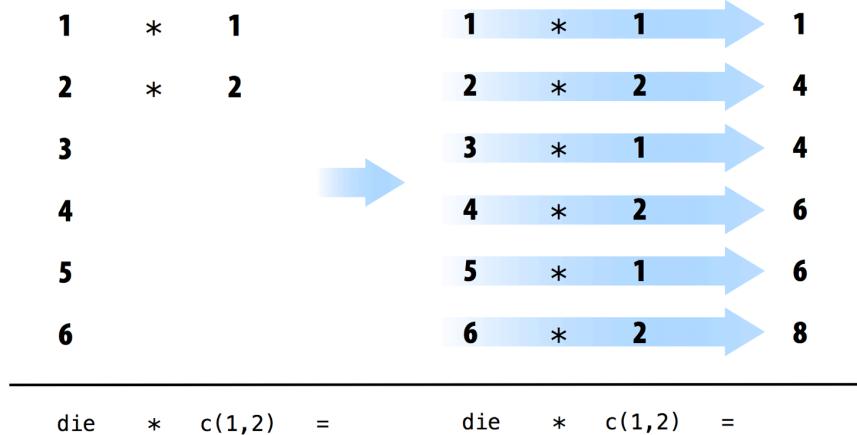


Figure 4.4.: “R will repeat a short vector to do element-wise operations with two vectors of uneven lengths.”

Element-wise operations are a very useful feature in R because they manipulate groups of values in an orderly way. When you start working with data sets, element-wise operations will ensure that values from one observation or case are only paired with values from the same observation or case. Element-wise operations also make it easier to write your own programs and functions in R.

! Element-wise operations are not matrix operations

It is important to know that operations with vectors are not the same that you might expect if you are expecting R to perform “matrix” operations. R can do inner multiplication with the `%*%` operator and outer multiplication with the `%o%` operator:

```
# Inner product (1*1 + 2*2 + 3*3 + 4*4 + 5*5 + 6*6)
die %*% die
# Outer product
die %o% die
```

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Now that you can do math with your `die` object, let's look at how you could "roll" it. Rolling your die will require something more sophisticated than basic arithmetic; you'll need to randomly select one of the die's values. And for that, you will need a *function*.

4.3. Functions

R has many functions and puts them all at our disposal. We can use functions to do simple and sophisticated tasks. For example, we can round a number with the `round` function, or calculate its factorial with the `factorial` function. Using a function is pretty simple. Just write the name of the function and then the data you want the function to operate on in parentheses:

```
round(3.1415)
```

```
[1] 3
```

```
factorial(3)
```

```
[1] 6
```

The data that you pass into the function is called the function's *argument*. The argument can be raw data, an R object, or even the results of another R function. In this last case, R will work from the innermost function to the outermost Figure 4.5.

```
mean(1:6)
```

```
[1] 3.5
```

```
mean(die)
```

```
[1] 3.5
```

```
round(mean(die))
```

```
[1] 4
```

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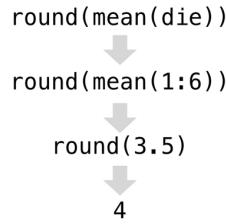


Figure 4.5.: “When you link functions together, R will resolve them from the innermost operation to the outermost. Here R first looks up die, then calculates the mean of one through six, then rounds the mean.”

Returning to our die, we can use the `sample` function to randomly select one of the die’s values; in other words, the `sample` function can simulate rolling the `die`.

The `sample` function takes *two* arguments: a vector named `x` and a number named `size`. `sample` will return `size` elements from the vector:

```
sample(x = 1:4, size = 2)
```

```
[1] 3 1
```

To roll your die and get a number back, set `x` to `die` and sample one element from it. You’ll get a new (maybe different) number each time you roll it:

```
sample(x = die, size = 1)
```

```
[1] 1
```

```
sample(x = die, size = 1)
```

```
[1] 1
```

```
sample(x = die, size = 1)
```

```
[1] 2
```

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Many R functions take multiple arguments that help them do their job. You can give a function as many arguments as you like as long as you separate each argument with a comma.

You may have noticed that I set `die` and `1` equal to the names of the arguments in `sample`, `x` and `size`. Every argument in every R function has a name. You can specify which data should be assigned to which argument by setting a name equal to data, as in the preceding code. This becomes important as you begin to pass multiple arguments to the same function; names help you avoid passing the wrong data to the wrong argument. However, using names is optional. You will notice that R users do not often use the name of the first argument in a function. So you might see the previous code written as:

```
sample(die, size = 1)
```

```
[1] 6
```

Often, the name of the first argument is not very descriptive, and it is usually obvious what the first piece of data refers to anyways.

But how do you know which argument names to use? If you try to use a name that a function does not expect, you will likely get an error:

```
round(3.1415, corners = 2)
## Error in round(3.1415, corners = 2) : unused argument(s) (corners = 2)
```

If you're not sure which names to use with a function, you can look up the function's arguments with `args`. To do this, place the name of the function in the parentheses behind `args`. For example, you can see that the `round` function takes two arguments, one named `x` and one named `digits`:

```
args(round)
```

```
function (x, digits = 0, ...)
NULL
```

Did you notice that `args` shows that the `digits` argument of `round` is already set to 0? Frequently, an R function will take optional arguments like `digits`. These arguments are considered optional because they come with a default value. You can pass a new value to an optional argument if you want, and R will use the default value if you do not. For example, `round` will round your number to 0 digits past the decimal point by default. To override the default, supply your own value for `digits`:

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```
round(3.1415)
```

```
[1] 3
```

```
round(3.1415, digits = 2)
```

```
[1] 3.14
```

```
# pi happens to be a built-in value in R  
pi
```

```
[1] 3.141593
```

```
round(pi)
```

```
[1] 3
```

You should write out the names of each argument after the first one or two when you call a function with multiple arguments. Why? First, this will help you and others understand your code. It is usually obvious which argument your first input refers to (and sometimes the second input as well). However, you'd need a large memory to remember the third and fourth arguments of every R function. Second, and more importantly, writing out argument names prevents errors.

If you do not write out the names of your arguments, R will match your values to the arguments in your function by order. For example, in the following code, the first value, `die`, will be matched to the first argument of `sample`, which is named `x`. The next value, `1`, will be matched to the next argument, `size`:

```
sample(die, 1)
```

```
[1] 5
```

As you provide more arguments, it becomes more likely that your order and R's order may not align. As a result, values may get passed to the wrong argument. Argument names prevent this. R will always match a value to its argument name, no matter where it appears in the order of arguments:

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```
sample(size = 1, x = die)
```

```
[1] 1
```

4.3.1. Sample with Replacement

If you set `size = 2`, you can *almost* simulate a pair of dice. Before we run that code, think for a minute why that might be the case. `sample` will return two numbers, one for each die:

```
sample(die, size = 2)
```

```
[1] 2 6
```

I said this “almost” works because this method does something funny. If you use it many times, you’ll notice that the second die never has the same value as the first die, which means you’ll never roll something like a pair of threes or snake eyes. What is going on?

By default, `sample` builds a sample *without replacement*. To see what this means, imagine that `sample` places all of the values of `die` in a jar or urn. Then imagine that `sample` reaches into the jar and pulls out values one by one to build its sample. Once a value has been drawn from the jar, `sample` sets it aside. The value doesn’t go back into the jar, so it cannot be drawn again. So if `sample` selects a six on its first draw, it will not be able to select a six on the second draw; six is no longer in the jar to be selected. Although `sample` creates its sample electronically, it follows this seemingly physical behavior.

One side effect of this behavior is that each draw depends on the draws that come before it. In the real world, however, when you roll a pair of dice, each die is independent of the other. If the first die comes up six, it does not prevent the second die from coming up six. In fact, it doesn’t influence the second die in any way whatsoever. You can recreate this behavior in `sample` by adding the argument `replace = TRUE`:

```
sample(die, size = 2, replace = TRUE)
```

```
[1] 6 5
```

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The argument `replace = TRUE` causes `sample` to sample *with replacement*. Our jar example provides a good way to understand the difference between sampling with replacement and without. When `sample` uses replacement, it draws a value from the jar and records the value. Then it puts the value back into the jar. In other words, `sample` replaces each value after each draw. As a result, `sample` may select the same value on the second draw. Each value has a chance of being selected each time. It is as if every draw were the first draw.

Sampling with replacement is an easy way to create *independent random samples*. Each value in your sample will be a sample of size one that is independent of the other values. This is the correct way to simulate a pair of dice:

```
sample(die, size = 2, replace = TRUE)
```

```
[1] 3 4
```

Congratulate yourself; you've just run your first simulation in R! You now have a method for simulating the result of rolling a pair of dice. If you want to add up the dice, you can feed your result straight into the `sum` function:

```
dice <- sample(die, size = 2, replace = TRUE)  
dice
```

```
[1] 2 5
```

```
sum(dice)
```

```
[1] 7
```

What would happen if you call `dice` multiple times? Would R generate a new pair of dice values each time? Let's give it a try:

```
dice
```

```
[1] 2 5
```

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```
dice
```

```
[1] 2 5
```

```
dice
```

```
[1] 2 5
```

The name `dice` refers to a *vector* of two numbers. Calling more than once does not change the favlue. Each time you call `dice`, R will show you the result of that one time you called `sample` and saved the output to `dice`. R won't rerun `sample(die, 2, replace = TRUE)` to create a new roll of the dice. Once you save a set of results to an R object, those results do not change.

However, it *would* be convenient to have an object that can re-roll the dice whenever you call it. You can make such an object by writing your own R function.

4.4. Writing Your Own Functions

To recap, you already have working R code that simulates rolling a pair of dice:

```
die <- 1:6
dice <- sample(die, size = 2, replace = TRUE)
sum(dice)
```

```
[1] 3
```

You can retype this code into the console anytime you want to re-roll your dice. However, this is an awkward way to work with the code. It would be easier to use your code if you wrapped it into its own function, which is exactly what we'll do now. We're going to write a function named `roll` that you can use to roll your virtual dice. When you're finished, the function will work like this: each time you call `roll()`, R will return the sum of rolling two dice:

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```
roll()  
## 8  
  
roll()  
## 3  
  
roll()  
## 7
```

Functions may seem mysterious or fancy, but they are *just another type of R object*. Instead of containing data, they contain code. This code is stored in a special format that makes it easy to reuse the code in new situations. You can write your own functions by recreating this format.

4.4.1. The Function Constructor

Every function in R has three basic parts: a name, a body of code, and a set of arguments. To make your own function, you need to replicate these parts and store them in an R object, which you can do with the `function` function. To do this, call `function()` and follow it with a pair of braces, {}:

```
my_function <- function() {}
```

This function, as written, doesn't do anything (yet). However, it is a valid function. You can call it by typing its name followed by an open and closed parenthesis:

```
my_function()
```

```
NULL
```

`function` will build a function out of whatever R code you place between the braces. For example, you can turn your dice code into a function by calling:

```
roll <- function() {  
  die <- 1:6  
  dice <- sample(die, size = 2, replace = TRUE)  
  sum(dice)  
}
```

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Indentation and readability

Notice each line of code between the braces is indented. This makes the code easier to read but has no impact on how the code runs. R ignores spaces and line breaks and executes one complete expression at a time. Note that in other languages like python, spacing is extremely important and part of the language.

Just hit the Enter key between each line after the first brace, {. R will wait for you to type the last brace, }, before it responds.

Don't forget to save the output of `function` to an R object. This object will become your new function. To use it, write the object's name followed by an open and closed parenthesis:

```
roll()
```

```
[1] 8
```

You can think of the parentheses as the “trigger” that causes R to run the function. If you type in a function’s name *without* the parentheses, R will show you the code that is stored inside the function. If you type in the name *with* the parentheses, R will run that code:

```
roll
```

```
function ()  
{  
  die <- 1:6  
  dice <- sample(die, size = 2, replace = TRUE)  
  sum(dice)  
}
```

```
roll()
```

```
[1] 8
```

The code that you place inside your function is known as the *body* of the function. When you run a function in R, R will execute all of the code in the body and then return the result of the last line of code. If the last line of code doesn’t return a value, neither will your function, so you want to ensure that your final line of code returns a value. One way

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to check this is to think about what would happen if you ran the body of code line by line in the command line. Would R display a result after the last line, or would it not?

Here's some code that would display a result:

```
dice  
1 + 1  
sqrt(2)
```

And here's some code that would not:

```
dice <- sample(die, size = 2, replace = TRUE)  
two <- 1 + 1  
a <- sqrt(2)
```

Again, this is just showing the distinction between expressions and assignments.

4.5. Arguments

What if we removed one line of code from our function and changed the name `die` to `bones` (just a name—don't think of it as important), like this?

```
roll2 <- function() {  
  dice <- sample(bones, size = 2, replace = TRUE)  
  sum(dice)  
}
```

Now I'll get an error when I run the function. The function **needs** the object `bones` to do its job, but there is no object named `bones` to be found (you can check by typing `ls()` which will show you the names in the environment, or memory).

```
roll2()  
## Error in sample(bones, size = 2, replace = TRUE) :  
##   object 'bones' not found
```

You can supply `bones` when you call `roll2` if you make `bones` an argument of the function. To do this, put the name `bones` in the parentheses that follow `function` when you define `roll2`:

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```
roll12 <- function(bones) {  
  dice <- sample(bones, size = 2, replace = TRUE)  
  sum(dice)  
}
```

Now `roll12` will work as long as you supply `bones` when you call the function. You can take advantage of this to roll different types of dice each time you call `roll12`.

Remember, we're rolling pairs of dice:

```
roll12(bones = 1:4)
```

```
[1] 7
```

```
roll12(bones = 1:6)
```

```
[1] 11
```

```
roll12(1:20)
```

```
[1] 8
```

Notice that `roll12` will still give an error if you do not supply a value for the `bones` argument when you call `roll12`:

```
roll12()  
## Error in sample(bones, size = 2, replace = TRUE) :  
##   argument "bones" is missing, with no default
```

You can prevent this error by giving the `bones` argument a default value. To do this, set `bones` equal to a value when you define `roll12`:

```
roll12 <- function(bones = 1:6) {  
  dice <- sample(bones, size = 2, replace = TRUE)  
  sum(dice)  
}
```

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Now you can supply a new value for `bones` if you like, and `roll2` will use the default if you do not:

```
roll2()
```

```
[1] 12
```

You can give your functions as many arguments as you like. Just list their names, separated by commas, in the parentheses that follow `function`. When the function is run, R will replace each argument name in the function body with the value that the user supplies for the argument. If the user does not supply a value, R will replace the argument name with the argument's default value (if you defined one).

To summarize, `function` helps you construct your own R functions. You create a body of code for your function to run by writing code between the braces that follow `function`. You create arguments for your function to use by supplying their names in the parentheses that follow `function`. Finally, you give your function a name by saving its output to an R object, as shown in Figure 4.6.

Once you've created your function, R will treat it like every other function in R. Think about how useful this is. Have you ever tried to create a new Excel option and add it to Microsoft's menu bar? Or a new slide animation and add it to Powerpoint's options? When you work with a programming language, you can do these types of things. As you learn to program in R, you will be able to create new, customized, reproducible tools for yourself whenever you like.

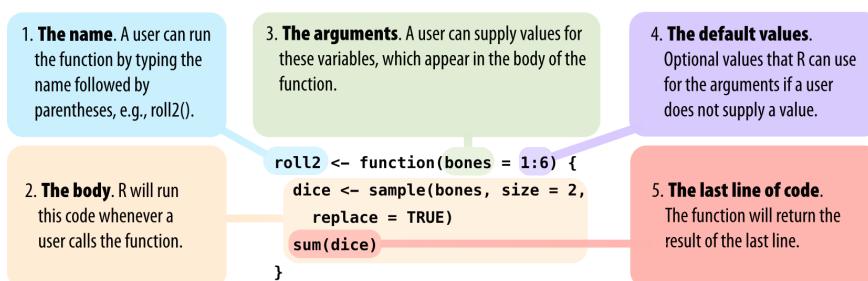


Figure 4.6.: “Every function in R has the same parts, and you can use `function` to create these parts. Assign the result to a name, so you can call the function later.”

4.6. Scripts

Scripts are code that are saved for later reuse or editing. An R script is just a plain text file that you save R code in. You can open an R script in RStudio by going to **File > New File > R script** in the menu bar. RStudio will then open a fresh script above your console pane, as shown in Figure 4.7.

I strongly encourage you to write and edit all of your R code in a script before you run it in the console. Why? This habit creates a reproducible record of your work. When you're finished for the day, you can save your script and then use it to rerun your entire analysis the next day. Scripts are also very handy for editing and proofreading your code, and they make a nice copy of your work to share with others. To save a script, click the scripts pane, and then go to **File > Save As** in the menu bar.

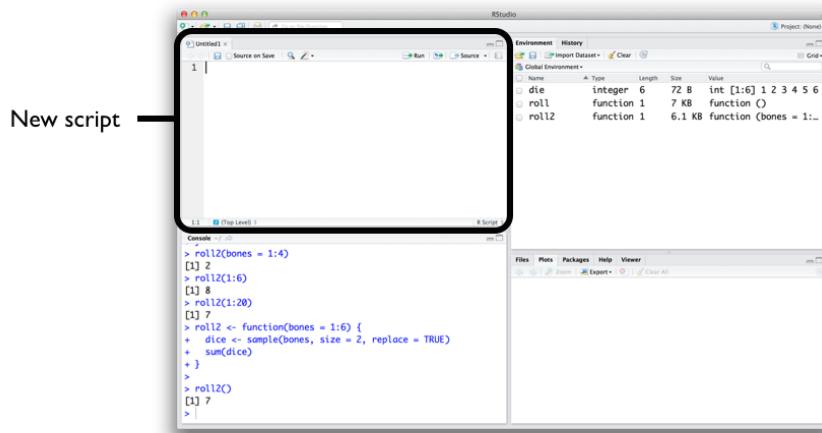


Figure 4.7.: “When you open an R Script (File > New File > R Script in the menu bar), RStudio creates a fourth pane (or puts a new tab in the existing pane) above the console where you can write and edit your code.”

RStudio comes with many built-in features that make it easy to work with scripts. First, you can automatically execute a line of code in a script by clicking the Run button at the top of the editor panel.

R will run whichever line of code your cursor is on. If you have a whole section highlighted, R will run the highlighted code. Alternatively, you can run the entire script by clicking the Source button. Don’t like clicking buttons? You can use Control + Return as a shortcut for the Run button. On Macs, that would be Command + Return.

4. Up and Running with R

If you're not convinced about scripts, you soon will be. It becomes a pain to write multi-line code in the console's single-line command line. Let's avoid that headache and open your first script now before we move to the next chapter.



Tip

Extract function

RStudio comes with a tool that can help you build functions. To use it, highlight the lines of code in your R script that you want to turn into a function. Then click **Code > Extract Function** in the menu bar. RStudio will ask you for a function name to use and then wrap your code in a **function** call. It will scan the code for undefined variables and use these as arguments.

You may want to double-check RStudio's work. It assumes that your code is correct, so if it does something surprising, you may have a problem in your code.

4.7. Summary

We've covered a lot of ground already. You now have a virtual die stored in your computer's memory, as well as your own R function that rolls a pair of dice. You've also begun speaking the R language.

The two most important components of the R language are objects, which store data, and functions, which manipulate data. R also uses a host of operators like `+`, `-`, `*`, `/`, and `<-` to do basic tasks. As a data scientist, you will use R objects to store data in your computer's memory, and you will use functions to automate tasks and do complicated calculations.

5. Packages and more dice

We now have code that allows us to roll two dice and add the results together. To keep things interesting, let's aim to weight the dice so that we can fool our friends into thinking we are lucky.

First, though, we should prove to ourselves that our dice are fair. We can investigate the behavior of our dice using two powerful and general tools;

- Simulation (or repetition or repeated sampling)
- Visualization

For the repetition part of things, we will use a built-in R function, `replicate`. For visualization, we are going to use a convenient plotting function, `qplot`. However, `qplot` does not come built into R. We must install a *package* to gain access to it.

5.1. Packages

R is a powerful language for data science and programming, allowing beginners and experts alike to manipulate, analyze, and visualize data effectively. One of the most appealing features of R is its extensive library of packages, which are essential tools for expanding its capabilities and streamlining the coding process.

An R package is a collection of reusable functions, datasets, and compiled code created by other users and developers to extend the functionality of the base R language. These packages cover a wide range of applications, such as data manipulation, statistical analysis, machine learning, and data visualization. By utilizing existing R packages, you can leverage the expertise of others and save time by avoiding the need to create custom functions from scratch.

Using others' R packages is incredibly beneficial as it allows you to take advantage of the collective knowledge of the R community. Developers often create packages to address specific challenges, optimize performance, or implement popular algorithms or methodologies. By incorporating these packages into your projects, you can enhance your productivity, reduce development time, and ensure that you are using well-tested and reliable code.

5. Packages and more dice

5.1.1. Installing R packages

To install an R package, you can use the `install.packages()` function in the R console or script. For example, to install the popular data manipulation package “dplyr,” simply type `install.packages("dplyr")`. This command will download the package from the Comprehensive R Archive Network (CRAN) and install it on your local machine. Keep in mind that you only need to install a package once, unless you want to update it to a newer version.

For those who are going to be using R for bioinformatics or biological data science, you will also want to install packages from Bioconductor, which is a repository of R packages specifically designed for bioinformatics and computational biology. To install Bioconductor packages, you can use the `BiocManager::install()` function.

To use this recommended approach, you first need to install the `BiocManager` package, which is the package manager for Bioconductor.

```
install.packages('BiocManager')
```

This is a one-time installation. After that, you can install any R, Bioconductor, rOpenSci, or even GitHub package using the `BiocManager::install()` function. For example, to install the `ggplot2` package, which is widely used for data visualization, you would run:

```
BiocManager::install("ggplot2")
```

5.1.2. Installing vs loading (library) R packages

After installing an R package, you will need to load it into your R session before using its functions. To load a package, use the `library()` function followed by the package name, such as `library(dplyr)`. Loading a package makes its functions and datasets available for use in your current R session. Note that you need to load a package every time you start a new R session.

```
library(ggplot2)
```

Now, the functionality of the `ggplot2` package is available in our R session.

💡 Installing vs loading packages

The main thing to remember is that you only need to install a package once, but you need to load it with `library` each time you wish to use it in a new R session. R will

5. Packages and more dice

unload all of its packages each time you close RStudio.



Images sourced from <https://www.wikihow.com/Change-a-Light-Bulb>

Figure 5.1.: Installing vs loading R packages.

As in {Figure 5.1}, screw in the lightbulb (eg., `BiocManager::install`) only once and then to use it, you need to turn on the switch each time you want to use it (`library`).

5.1.3. Finding R packages

Finding useful R packages can be done in several ways. First, browsing CRAN (<https://cran.r-project.org/>) and Bioconductor (more later, <https://bioconductor.org>) are an excellent starting points, as they host thousands of packages categorized by topic. Additionally, online forums like Stack Overflow and R-bloggers can provide valuable recommendations based on user experiences. Social media platforms such as Twitter, where developers and data scientists often share new packages and updates, can also be a helpful resource. Finally, don't forget to ask your colleagues or fellow R users for their favorite packages, as they may have insights on which ones best suit your specific needs.

5.2. Are our dice fair?

Well, let's review our code.

5. Packages and more dice

```
roll12 <- function(bones = 1:6) {
  dice = sample(bones, size = 2, replace = TRUE)
  sum(dice)
}
```

If our dice are fair, then each number should show up equally. What does the sum look like with our two dice?

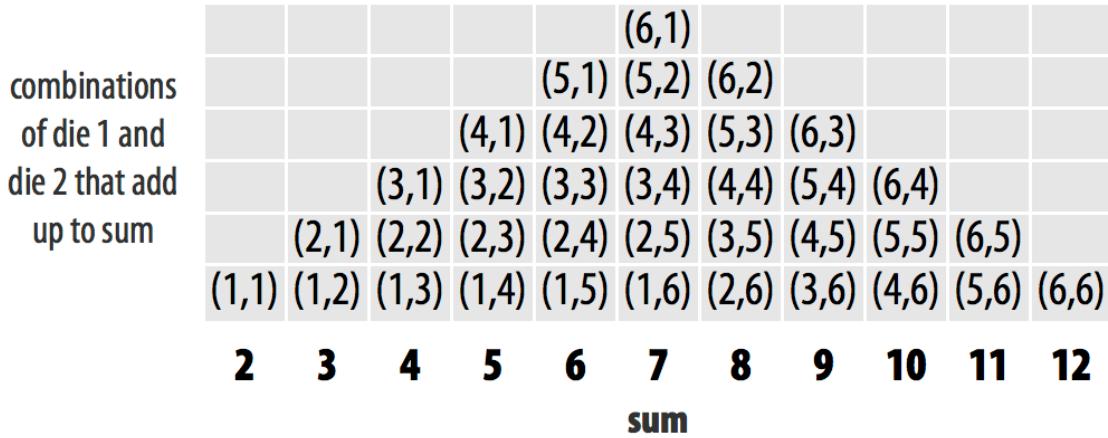


Figure 5.2.: In an ideal world, a histogram of the results would look like this

Read the help page for `replicate` (i.e., `help("replicate")`). In short, it suggests that we can repeat our dice rolling as many times as we like and `replicate` will return a *vector* of the sums for each roll.

```
rolls = replicate(n = 100, roll12())
```

What does `rolls` look like?

```
head(rolls)
```

```
[1] 4 7 5 11 7 8
```

```
length(rolls)
```

5. Packages and more dice

```
[1] 100
```

```
mean(rolls)
```

```
[1] 7.03
```

```
summary(rolls)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
2.00	5.00	7.00	7.03	9.00	12.00

This looks like it roughly agrees with our sketched out ideal histogram in Figure 5.2. However, now that we've loaded the `qplot` function from the `ggplot2` package, we can make a histogram of the data themselves.

```
qplot(rolls, binwidth=1)
```

```
Warning: `qplot()` was deprecated in ggplot2 3.4.0.
```

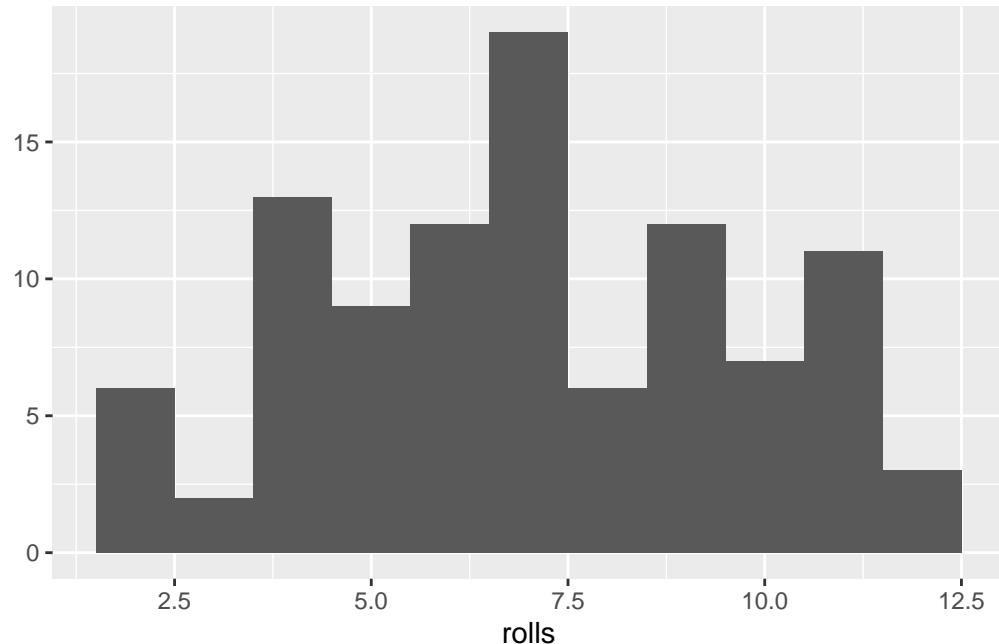


Figure 5.3.: Histogram of the sums from 100 rolls of our fair dice

5. Packages and more dice

How does your histogram look (and yours will be different from mine since we are sampling random values)? Is it what you expect?

What happens to our histogram as we increase the number of replicates?

```
rolls = replicate(n = 100000, roll2())
qplot(rolls, binwidth=1)
```

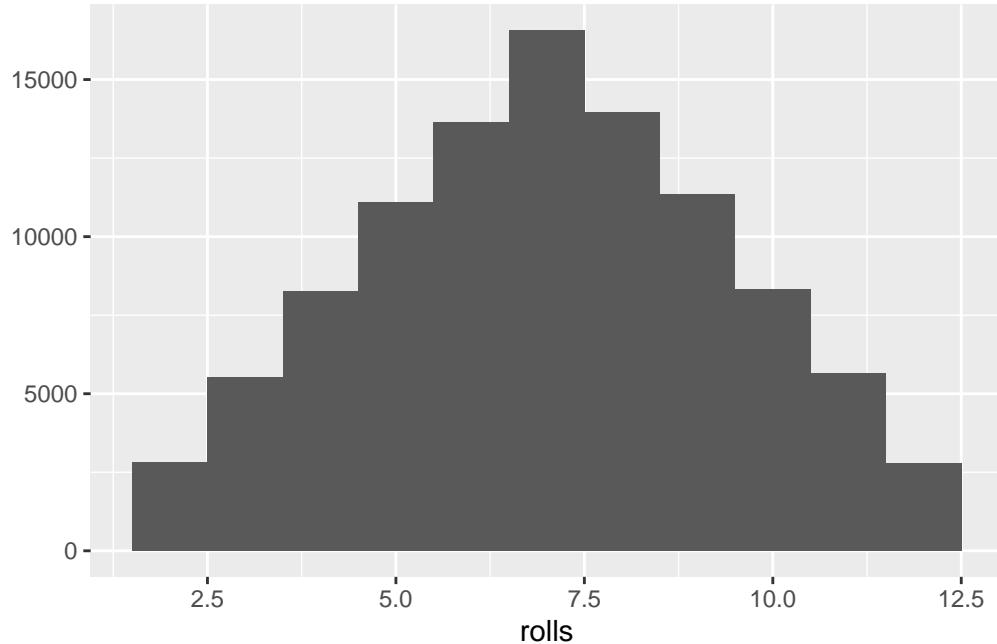


Figure 5.4.: Histogram with 100000 rolls much more closely approximates the pyramidal shape we anticipated

5.3. Bonus exercise

How would you change the `roll2` function to weight the dice?

i Hint

Read the help page for `sample` (i.e., `help("sample")`).

6. Reading and writing data files

6.1. Introduction

In this chapter, we will discuss how to read and write data files in R. Data files are essential for storing and sharing data across different platforms and applications. R provides a variety of functions and packages to read and write data files in different formats, such as text files, CSV files, Excel files. By mastering these functions, you can efficiently import and export data in R, enabling you to perform data analysis and visualization tasks effectively.

6.2. CSV files

Comma-Separated Values (CSV) files are a common file format for storing tabular data. They consist of rows and columns, with each row representing a record and each column representing a variable or attribute. CSV files are widely used for data storage and exchange due to their simplicity and compatibility with various software applications. In R, you can read and write CSV files using the `read.csv()` and `write.csv()` functions, respectively. A commonly used alternative is to use the `readr` package, which provides faster and more user-friendly functions for reading and writing CSV files.

6.2.1. Writing a CSV file

Since we are going to use the `readr` package, we need to install it first. You can install the `readr` package using the following command:

```
install.packages("readr")
```

Once the package is installed, you can load it into your R session using the `library()` function:

6. Reading and writing data files

```
library(readr)
```

Since we don't have a CSV file sitting around, let's create a simple data frame to write to a CSV file. Here's an example data frame:

```
df <- data.frame(  
  id = c(1, 2, 3, 4, 5),  
  name = c("Alice", "Bob", "Charlie", "David", "Eve"),  
  age = c(25, 30, 35, 40, 45)  
)
```

Now, you can write this data frame to a CSV file using the `write_csv()` function from the `readr` package. Here's how you can do it:

```
write_csv(df, "data.csv")
```

You can check the current working directory to see if the CSV file was created successfully. If you want to specify a different directory or file path, you can provide the full path in the `write_csv()` function.

```
# see what the current working directory is  
getwd()  
  
[1] "/Users/davsean/Documents/git/RBiocBook"  
  
# and check to see that the file was created  
dir(pattern = "data.csv")  
  
[1] "data.csv"
```

6.2.2. Reading a CSV file

Now that we have a CSV file, let's read it back into R using the `read_csv()` function from the `readr` package. Here's how you can do it:

6. Reading and writing data files

```
df2 <- read_csv("data.csv")  
  
Rows: 5 Columns: 3  
-- Column specification -----  
Delimiter: ","  
chr (1): name  
dbl (2): id, age  
  
i Use `spec()` to retrieve the full column specification for this data.  
i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

You can check the structure of the data frame `df2` to verify that the data was read correctly:

```
df2  
  
# A tibble: 5 x 3  
  id   name    age  
  <dbl> <chr>   <dbl>  
1     1 Alice    25  
2     2 Bob      30  
3     3 Charlie  35  
4     4 David   40  
5     5 Eve      45
```

The `readr` package can read CSV files with various delimiters, headers, and data types, making it a versatile tool for handling tabular data in R. It can also read CSV files directly from web locations like so:

```
df3 <- read_csv("https://data.cdc.gov/resource/pwn4-m3yp.csv")  
  
Rows: 1000 Columns: 10  
-- Column specification -----  
Delimiter: ","  
chr  (1): state  
dbl  (6): tot_cases, new_cases, tot_deaths, new_deaths, new_historic_cases, ...  
dttm (3): date_updated, start_date, end_date  
  
i Use `spec()` to retrieve the full column specification for this data.  
i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

6. Reading and writing data files

The dataset that you just downloaded is described here: [Covid-19 data from CDC](#)

6.3. Excel files

Microsoft Excel files are another common file format for storing tabular data. Excel files can contain multiple sheets, formulas, and formatting options, making them a popular choice for data storage and analysis. In R, you can read and write Excel files using the `readxl` package. This package provides functions to import and export data from Excel files, enabling you to work with Excel data in R.

6.3.1. Reading an Excel file

To read an Excel file in R, you need to install and load the `readxl` package. You can install the `readxl` package using the following command:

```
install.packages("readxl")
```

Once the package is installed, you can load it into your R session using the `library()` function:

```
library(readxl)
```

Now, you can read an Excel file using the `read_excel()` function from the `readxl` package. We don't have an excel file available, so let's download one from the internet. Here's an example:

```
download.file('https://www.w3resource.com/python-exercises/pandas/excel/SaleData.xlsx', 'Sa
```

Now, you can read the Excel file into R using the `read_excel()` function:

```
df_excel <- read_excel("SaleData.xlsx")
```

You can check the structure of the data frame `df_excel` to verify that the data was read correctly:

6. Reading and writing data files

```
df_excel
```

```
# A tibble: 45 x 8
  OrderDate      Region Manager SalesMan Item  Units Unit_price Sale_amt
  <dttm>        <chr>   <chr>   <chr>   <chr> <dbl>    <dbl>    <dbl>
1 2018-01-06 00:00:00 East    Martha  Alexander Tele~    95     1198    113810
2 2018-01-23 00:00:00 Central Hermann Shelli   Home~    50      500    25000
3 2018-02-09 00:00:00 Central Hermann Luis     Tele~    36     1198    43128
4 2018-02-26 00:00:00 Central Timothy David   Cell~    27      225    6075
5 2018-03-15 00:00:00 West    Timothy Stephen  Tele~    56     1198    67088
6 2018-04-01 00:00:00 East    Martha  Alexander Home~    60      500    30000
7 2018-04-18 00:00:00 Central Martha  Steven   Tele~    75     1198    89850
8 2018-05-05 00:00:00 Central Hermann Luis     Tele~    90     1198    107820
9 2018-05-22 00:00:00 West    Douglas Michael  Tele~    32     1198    38336
10 2018-06-08 00:00:00 East   Martha  Alexander Home~    60      500    30000
# i 35 more rows
```

The `readxl` package provides various options to read Excel files with multiple sheets, specific ranges, and data types, making it a versatile tool for handling Excel data in R.

6.3.2. Writing an Excel file

To write an Excel file in R, you can use the `write_xlsx()` function from the `writexl` package. You can install the `writexl` package using the following command:

```
install.packages("writexl")
```

Once the package is installed, you can load it into your R session using the `library()` function:

```
library(writexl)
```

The `write_xlsx()` function allows you to write a data frame to an Excel file. Here's an example:

```
write_xlsx(df, "data.xlsx")
```

6. Reading and writing data files

You can check the current working directory to see if the Excel file was created successfully. If you want to specify a different directory or file path, you can provide the full path in the `write_xlsx()` function.

```
# see what the current working directory is  
getwd()
```

```
[1] "/Users/davsean/Documents/git/RBiocBook"
```

```
# and check to see that the file was created  
dir(pattern = "data.xlsx")
```

```
[1] "data.xlsx"
```

6.4. Additional options

- Google Sheets: You can read and write data from Google Sheets using the `googlesheets4` package. This package provides functions to interact with Google Sheets, enabling you to import and export data from Google Sheets to R.
- JSON files: You can read and write JSON files using the `jsonlite` package. This package provides functions to convert R objects to JSON format and vice versa, enabling you to work with JSON data in R.
- Database files: You can read and write data from database files using the `DBI` and `RSQLite` packages. These packages provide functions to interact with various database systems, enabling you to import and export data from databases to R.

Part II.

R Data Structures

Chapter overview

Welcome to the section on R data structures! As you begin your journey in learning R, it is essential to understand the fundamental building blocks of this powerful programming language. R offers a variety of data structures to store and manipulate data, each with its unique properties and capabilities. In this section, we will cover the core data structures in R, including:

- Vectors
- Matrices
- Lists
- Data.frames

By the end of this section, you will have a solid understanding of these data structures, and you will be able to choose and utilize the appropriate data structure for your specific data manipulation and analysis tasks.

In each chapter, we will delve into the properties and usage of each data structure, starting with their definitions and moving on to their practical applications. We will provide examples, exercises, and active learning approaches to help you better understand and apply these concepts in your work.

Chapter overview

- **Vectors** : In this chapter, we will introduce you to the simplest data structure in R, the vector. We will cover how to create, access, and manipulate vectors, as well as discuss their unique properties and limitations.
- **Matrices** Next, we will explore matrices, which are two-dimensional data structures that extend vectors. You will learn how to create, access, and manipulate matrices, and understand their usefulness in mathematical operations and data organization.
- **Lists** The third chapter will focus on lists, a versatile data structure that can store elements of different types and sizes. We will discuss how to create, access, and modify lists, and demonstrate their flexibility in handling complex data structures.
- **Data.frames** Finally, we will examine data.frames, a widely-used data structure for organizing and manipulating tabular data. You will learn how to create, access, and manipulate data.frames, and understand their advantages over other data structures for data analysis tasks.

Chapter overview

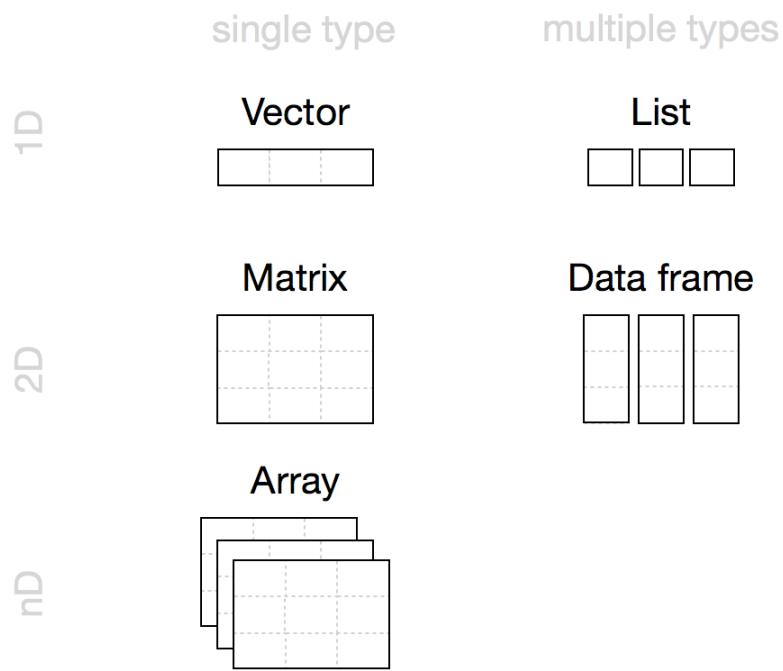


Figure 6.1.: A pictorial representation of R's most common data structures are vectors, matrices, arrays, lists, and dataframes. Figure from [Hands-on Programming with R](#).

Chapter overview

- **Arrays** While we will not focus directly on the `array` data type, which are multidimensional data structures that extend matrices, they are very similar to matrices, but with a third dimension.

As you progress through these chapters, practice the examples and exercises provided, engage in discussion, and collaborate with your peers to deepen your understanding of R data structures. This solid foundation will serve as the basis for more advanced data manipulation, analysis, and visualization techniques in R.

7. Vectors

7.1. What is a Vector?

A vector is the simplest and most basic data structure in R. It is a one-dimensional, ordered collection of elements, where all the elements are of the same data type. Vectors can store various types of data, such as numeric, character, or logical values. Figure 7.1 shows a pictorial representation of three vector examples.

Index	1	2	3	4	5	6	7
Vector	3	7	10	NA	932	127	-3
Vector	TRUE	FALSE	FALSE	TRUE	TRUE	FALSE	NA
Vector	“Cat”	“Dog”	“A”	“C”	“T”	NA	“G”
Names (Optional)	“H”	“I”	“L”	“Z”	“This”	“That”	“Other”

Figure 7.1.: “Pictorial representation of three vector examples. The first vector is a numeric vector. The second is a ‘logical’ vector. The third is a character vector. Vectors also have indices and, optionally, names.”

In this chapter, we will provide a comprehensive overview of vectors, including how to create, access, and manipulate them. We will also discuss some unique properties and rules associated with vectors, and explore their applications in data analysis tasks.

In R, even a single value is a vector with length=1.

7. Vectors

```
z = 1  
z
```

```
[1] 1
```

```
length(z)
```

```
[1] 1
```

In the code above, we “assigned” the value 1 to the variable named `z`. Typing `z` by itself is an “expression” that returns a result which is, in this case, the value that we just assigned. The `length` method takes an R object and returns the R length. There are numerous ways of asking R about what an object represents, and `length` is one of them.

Vectors can contain numbers, strings (character data), or logical values (TRUE and FALSE) or other “atomic” data types Table 7.1. *Vectors cannot contain a mix of types!* We will introduce another data structure, the R `list` for situations when we need to store a mix of base R data types.

Table 7.1.: Atomic (simplest) data types in R.

Data type	Stores
numeric	floating point numbers
integer	integers
complex	complex numbers
factor	categorical data
character	strings
logical	TRUE or FALSE
NA	missing
NULL	empty
function	function type

7.2. Creating vectors

Character vectors (also sometimes called “string” vectors) are entered with each value surrounded by single or double quotes; either is acceptable, but they must match. They are always displayed by R with double quotes. Here are some examples of creating vectors:

7. Vectors

```
# examples of vectors  
c('hello','world')
```

```
[1] "hello" "world"
```

```
c(1,3,4,5,1,2)
```

```
[1] 1 3 4 5 1 2
```

```
c(1.12341e7,78234.126)
```

```
[1] 11234100.00    78234.13
```

```
c(TRUE,FALSE,TRUE,TRUE)
```

```
[1] TRUE FALSE TRUE TRUE
```

```
# note how in the next case the TRUE is converted to "TRUE"  
# with quotes around it.  
c(TRUE,'hello')
```

```
[1] "TRUE"  "hello"
```

We can also create vectors as “regular sequences” of numbers. For example:

```
# create a vector of integers from 1 to 10  
x = 1:10  
# and backwards  
x = 10:1
```

The `seq` function can create more flexible regular sequences.

```
# create a vector of numbers from 1 to 4 skipping by 0.3  
y = seq(1,4,0.3)
```

And creating a new vector by concatenating existing vectors is possible, as well.

7. Vectors

```
# create a sequence by concatenating two other sequences
z = c(y,x)
z
```

```
[1] 1.0 1.3 1.6 1.9 2.2 2.5 2.8 3.1 3.4 3.7 4.0 10.0 9.0 8.0 7.0
[16] 6.0 5.0 4.0 3.0 2.0 1.0
```

7.3. Vector Operations

Operations on a single vector are typically done element-by-element. For example, we can add 2 to a vector, 2 is added to each element of the vector and a new vector of the same length is returned.

```
x = 1:10
x + 2
```

```
[1] 3 4 5 6 7 8 9 10 11 12
```

If the operation involves two vectors, the following rules apply. If the vectors are the same length: R simply applies the operation to each pair of elements.

```
x + x
```

```
[1] 2 4 6 8 10 12 14 16 18 20
```

If the vectors are different lengths, but one length a multiple of the other, R reuses the shorter vector as needed.

```
x = 1:10
y = c(1,2)
x * y
```

```
[1] 1 4 3 8 5 12 7 16 9 20
```

If the vectors are different lengths, but one length *not* a multiple of the other, R reuses the shorter vector as needed *and* delivers a warning.

7. Vectors

```
x = 1:10
y = c(2,3,4)
x * y
```

Warning in x * y: longer object length is not a multiple of shorter object length

```
[1] 2 6 12 8 15 24 14 24 36 20
```

Typical operations include multiplication (“*”), addition, subtraction, division, exponentiation (“ \wedge ”), but many operations in R operate on vectors and are then called “vectorized”.

Be aware of the recycling rule when working with vectors of different lengths, as it may lead to unexpected results if you’re not careful.

7.4. Logical Vectors

Logical vectors are vectors composed on only the values TRUE and FALSE. Note the all-upper-case and no quotation marks.

```
a = c(TRUE, FALSE, TRUE)

# we can also create a logical vector from a numeric vector
# 0 = false, everything else is 1
b = c(1, 0, 217)
d = as.logical(b)
d
```

```
[1] TRUE FALSE TRUE
```

```
# test if a and d are the same at every element
all.equal(a, d)
```

```
[1] TRUE
```

7. Vectors

```
# We can also convert from logical to numeric  
as.numeric(a)
```

```
[1] 1 0 1
```

7.4.1. Logical Operators

Some operators like `<`, `>`, `==`, `>=`, `<=`, `!=` can be used to create logical vectors.

```
# create a numeric vector  
x = 1:10  
# testing whether x > 5 creates a logical vector  
x > 5
```

```
[1] FALSE FALSE FALSE FALSE FALSE TRUE TRUE TRUE TRUE TRUE
```

```
x <= 5
```

```
[1] TRUE TRUE TRUE TRUE TRUE FALSE FALSE FALSE FALSE FALSE
```

```
x != 5
```

```
[1] TRUE TRUE TRUE TRUE FALSE TRUE TRUE TRUE TRUE TRUE
```

```
x == 5
```

```
[1] FALSE FALSE FALSE FALSE FALSE TRUE FALSE FALSE FALSE FALSE
```

We can also assign the results to a variable:

```
y = (x == 5)  
y
```

```
[1] FALSE FALSE FALSE FALSE FALSE TRUE FALSE FALSE FALSE FALSE
```

7.5. Indexing Vectors

In R, an index is used to refer to a specific element or set of elements in a vector (or other data structure). [R uses [and] to perform indexing, although other approaches to getting subsets of larger data structures are common in R.

```
x = seq(0,1,0.1)
# create a new vector from the 4th element of x
x[4]
```

```
[1] 0.3
```

We can even use other vectors to perform the “indexing”.

```
x[c(3,5,6)]
```

```
[1] 0.2 0.4 0.5
```

```
y = 3:6
x[y]
```

```
[1] 0.2 0.3 0.4 0.5
```

Combining the concept of indexing with the concept of logical vectors results in a very powerful combination.

```
# use help('rnorm') to figure out what is happening next
myvec = rnorm(10)

# create logical vector that is TRUE where myvec is >0.25
gt1 = (myvec > 0.25)
sum(gt1)
```

```
[1] 5
```

7. Vectors

```
# and use our logical vector to create a vector of myvec values that are >0.25  
myvec[gt1]
```

```
[1] 2.3567830 0.5266998 1.0390147 1.2989228 0.3576956
```

```
# or <=0.25 using the logical "not" operator, "!"  
myvec[!gt1]
```

```
[1] -0.9015151 -0.9194154 0.1518130 -0.2471621 -0.9175934
```

```
# shorter, one line approach  
myvec[myvec > 0.25]
```

```
[1] 2.3567830 0.5266998 1.0390147 1.2989228 0.3576956
```

7.6. Named Vectors

Named vectors are vectors with labels or names assigned to their elements. These names can be used to access and manipulate the elements in a more meaningful way.

To create a named vector, use the `names()` function:

```
fruit_prices <- c(0.5, 0.75, 1.25)  
names(fruit_prices) <- c("apple", "banana", "cherry")  
print(fruit_prices)
```

```
apple banana cherry  
0.50   0.75   1.25
```

You can also access and modify elements using their names:

```
banana_price <- fruit_prices["banana"]  
print(banana_price)
```

```
banana  
0.75
```

7. Vectors

```
fruit_prices["apple"] <- 0.6
print(fruit_prices)
```

```
apple banana cherry
0.60   0.75   1.25
```

7.7. Character Vectors, A.K.A. Strings

R uses the `paste` function to concatenate strings.

```
paste("abc","def")
```

```
[1] "abc def"
```

```
paste("abc","def",sep="THISSEP")
```

```
[1] "abcTHISSEPdef"
```

```
paste0("abc","def")
```

```
[1] "abcdef"
```

```
## [1] "abcdef"
paste(c("X","Y"),1:10)
```

```
[1] "X 1"   "Y 2"   "X 3"   "Y 4"   "X 5"   "Y 6"   "X 7"   "Y 8"   "X 9"   "Y 10"
```

```
paste(c("X","Y"),1:10,sep="_")
```

```
[1] "X_1"   "Y_2"   "X_3"   "Y_4"   "X_5"   "Y_6"   "X_7"   "Y_8"   "X_9"   "Y_10"
```

We can count the number of characters in a string.

7. Vectors

```
nchar('abc')
```

```
[1] 3
```

```
nchar(c('abc','d',123456))
```

```
[1] 3 1 6
```

Pulling out parts of strings is also sometimes useful.

```
substr('This is a good sentence.',start=10,stop=15)
```

```
[1] " good "
```

Another common operation is to replace something in a string with something (a find-and-replace).

```
sub('This','That','This is a good sentence.')
```

```
[1] "That is a good sentence."
```

When we want to find all strings that match some other string, we can use `grep`, or “grab regular expression”.

```
grep('bcd',c('abcdef','abcd','bcde','cdef','defg'))
```

```
[1] 1 2 3
```

```
grep('bcd',c('abcdef','abcd','bcde','cdef','defg'),value=TRUE)
```

```
[1] "abcdef" "abcd"    "bcde"
```

Read about the `grepl` function (`?grepl`). Use that function to return a logical vector (TRUE/FALSE) for each entry above with an `a` in it.

7.8. Missing Values, AKA “NA”

R has a special value, “NA”, that represents a “missing” value, or *Not Available*, in a vector or other data structure. Here, we just create a vector to experiment.

```
x = 1:5
```

```
x
```

```
[1] 1 2 3 4 5
```

```
length(x)
```

```
[1] 5
```

```
is.na(x)
```

```
[1] FALSE FALSE FALSE FALSE FALSE
```

```
x[2] = NA
```

```
x
```

```
[1] 1 NA 3 4 5
```

The length of `x` is unchanged, but there is one value that is marked as “missing” by virtue of being `NA`.

```
length(x)
```

```
[1] 5
```

```
is.na(x)
```

```
[1] FALSE TRUE FALSE FALSE FALSE
```

We can remove `NA` values by using indexing. In the following, `is.na(x)` returns a logical vector the length of `x`. The `!` is the logical *NOT* operator and converts `TRUE` to `FALSE` and vice-versa.

7. Vectors

```
x[!is.na(x)]
```

```
[1] 1 3 4 5
```

7.9. Exercises

1. Create a numeric vector called `temperatures` containing the following values: 72, 75, 78, 81, 76, 73.

```
temperatures <- c(72, 75, 78, 81, 76, 73, 93)
```

2. Create a character vector called `days` containing the following values: “Monday”, “Tuesday”, “Wednesday”, “Thursday”, “Friday”, “Saturday”, “Sunday”.

```
days <- c("Monday", "Tuesday", "Wednesday", "Thursday", "Friday", "Saturday", "Sunday")
```

3. Calculate the average temperature for the week and store it in a variable called `average_temperature`.

```
average_temperature <- mean(temperatures)
```

4. Create a named vector called `weekly_temperatures`, where the names are the days of the week and the values are the temperatures from the `temperatures` vector.

```
weekly_temperatures <- temperatures  
names(weekly_temperatures) <- days
```

5. Create a numeric vector called `ages` containing the following values: 25, 30, 35, 40, 45, 50, 55, 60.

```
ages <- c(25, 30, 35, 40, 45, 50, 55, 60)
```

6. Create a logical vector called `is_adult` by checking if the elements in the `ages` vector are greater than or equal to 18.

```
is_adult <- ages >= 18
```

7. Calculate the sum and product of the `ages` vector.

```
sum_ages <- sum(ages)  
product_ages <- prod(ages)
```

7. Vectors

8. Extract the ages greater than or equal to 40 from the `ages` vector and store them in a variable called `older_ages`.

```
older_ages <- ages[ages >= 40]
```

8. Matrices

A *matrix* is a rectangular collection of the same data type (see Figure 8.1). It can be viewed as a collection of column vectors all of the same length and the same type (i.e. numeric, character or logical) OR a collection of row vectors, again all of the same type and length. A *data.frame* is *also* a rectangular array. All of the columns must be the same length, but they **may be** of *different* types. The rows and columns of a matrix or data frame can be given names. However these are implemented differently in R; many operations will work for one but not both, often a source of confusion.

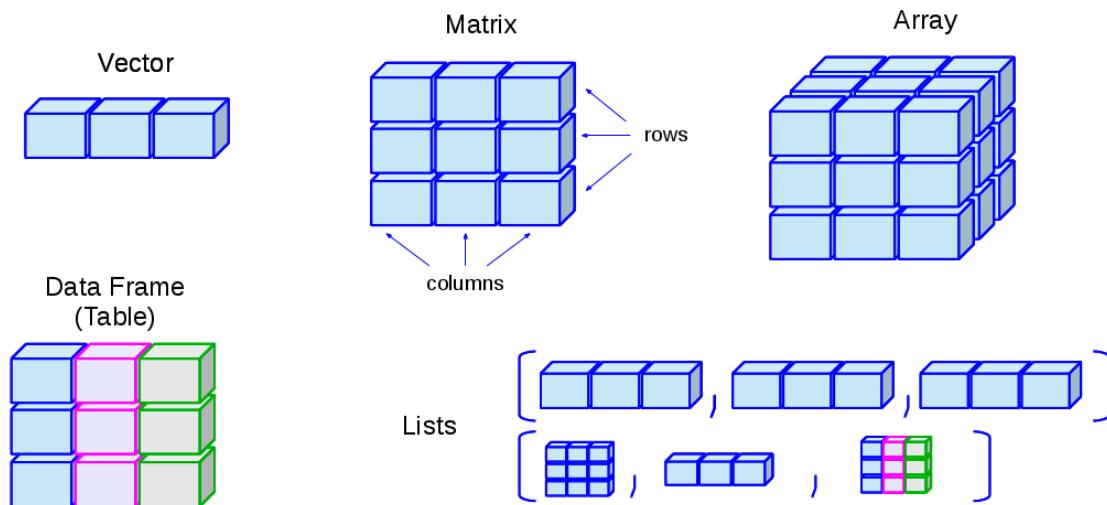


Figure 8.1.: A matrix is a collection of column vectors.

8.1. Creating a matrix

There are many ways to create a matrix in R. One of the simplest is to use the `matrix()` function. In the code below, we'll create a matrix from a vector from 1:16.

8. Matrices

```
mat1 <- matrix(1:16,nrow=4)
mat1
```

```
[,1] [,2] [,3] [,4]
[1,]    1     5     9    13
[2,]    2     6    10    14
[3,]    3     7    11    15
[4,]    4     8    12    16
```

The same is possible, but specifying that the matrix be “filled” by row.

```
mat1 <- matrix(1:16,nrow=4,byrow = TRUE)
mat1
```

```
[,1] [,2] [,3] [,4]
[1,]    1     2     3     4
[2,]    5     6     7     8
[3,]    9    10    11    12
[4,]   13    14    15    16
```

Notice the subtle difference in the order that the numbers go into the matrix.

We can also build a matrix from parts by “binding” vectors together:

```
x <- 1:10
y <- rnorm(10)
```

Each of the vectors above is of length 10 and both are “numeric”, so we can make them into a matrix. Using `rbind` binds rows (`r`) into a matrix.

```
mat <- rbind(x,y)
mat
```

```
[,1]      [,2]      [,3]      [,4]      [,5]      [,6]      [,7]      [,8]
x  1.000000 2.000000 3.000000 4.000000 5.0000000 6.0000000 7.0000000 8.0000000
y -1.383674 1.022323 1.188663 -1.068186 0.4360454 0.9917045 0.5836144 0.5213843
[,9]      [,10]
x  9.0000000 10.000000
y -0.4447755  0.781375
```

8. Matrices

The alternative to `rbind` is `cbind` that binds columns (**c**) together.

```
mat <- cbind(x,y)
mat
```

```
      x         y
[1,] 1 -1.3836742
[2,] 2  1.0223233
[3,] 3  1.1886630
[4,] 4 -1.0681859
[5,] 5  0.4360454
[6,] 6  0.9917045
[7,] 7  0.5836144
[8,] 8  0.5213843
[9,] 9 -0.4447755
[10,] 10 0.7813750
```

Inspecting the names associated with rows and columns is often useful, particularly if the names have human meaning.

```
rownames(mat)
```

```
NULL
```

```
colnames(mat)
```

```
[1] "x" "y"
```

We can also change the names of the matrix by assigning *valid* names to the columns or rows.

```
colnames(mat) = c('apples','oranges')
colnames(mat)
```

```
[1] "apples"  "oranges"
```

8. Matrices

```
mat
```

```
    apples      oranges
[1,]      1 -1.3836742
[2,]      2  1.0223233
[3,]      3  1.1886630
[4,]      4 -1.0681859
[5,]      5  0.4360454
[6,]      6  0.9917045
[7,]      7  0.5836144
[8,]      8  0.5213843
[9,]      9 -0.4447755
[10,]     10  0.7813750
```

Matrices have dimensions.

```
dim(mat)
```

```
[1] 10  2
```

```
nrow(mat)
```

```
[1] 10
```

```
ncol(mat)
```

```
[1] 2
```

8.2. Accessing elements of a matrix

Indexing for matrices works as for vectors except that we now need to include both the row and column (in that order). We can access elements of a matrix using the square bracket [indexing method. Elements can be accessed as `var[r, c]`. Here, `r` and `c` are vectors describing the elements of the matrix to select.

8. Matrices

! Important

The indices in R start with one, meaning that the first element of a vector or the first row/column of a matrix is indexed as one.

This is different from some other programming languages, such as Python, which use zero-based indexing, meaning that the first element of a vector or the first row/column of a matrix is indexed as zero.

It is important to be aware of this difference when working with data in R, especially if you are coming from a programming background that uses zero-based indexing. Using the wrong index can lead to unexpected results or errors in your code.

```
# The 2nd element of the 1st row of mat  
mat[1,2]
```

```
oranges  
-1.383674
```

```
# The first ROW of mat  
mat[1,]
```

```
apples    oranges  
1.000000 -1.383674
```

```
# The first COLUMN of mat  
mat[,1]
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

```
# and all elements of mat that are > 4; note no comma  
mat[mat>4]
```

```
[1] 5 6 7 8 9 10
```

```
## [1] 5 6 7 8 9 10
```

8. Matrices

🔥 Caution

Note that in the last case, there is no “,”, so R treats the matrix as a long vector (length=20). This is convenient, sometimes, but it can also be a source of error, as some code may “work” but be doing something unexpected.

We can also use indexing to exclude a row or column by prefixing the selection with a - sign.

```
mat[,-1]      # remove first column
```

```
[1] -1.3836742  1.0223233  1.1886630 -1.0681859  0.4360454  0.9917045  
[7]  0.5836144  0.5213843 -0.4447755  0.7813750
```

```
mat[-c(1:5),]  # remove first five rows
```

```
      apples     oranges  
[1,]       6  0.9917045  
[2,]       7  0.5836144  
[3,]       8  0.5213843  
[4,]       9 -0.4447755  
[5,]      10  0.7813750
```

8.3. Changing values in a matrix

We can create a matrix filled with random values drawn from a normal distribution for our work below.

```
m = matrix(rnorm(20), nrow=10)  
summary(m)
```

V1	V2
Min. :-1.54340	Min. :-1.4190
1st Qu.:-0.67168	1st Qu.:-0.9032
Median : 0.06123	Median :-0.1002
Mean :-0.02654	Mean :-0.2634
3rd Qu.: 0.55115	3rd Qu.: 0.1103
Max. : 1.25409	Max. : 0.9455

8. Matrices

Multiplication and division works similarly to vectors. When multiplying by a vector, for example, the values of the vector are reused. In the simplest case, let's multiply the matrix by a constant (vector of length 1).

```
# multiply all values in the matrix by 20
m2 = m*20
summary(m2)
```

V1	V2
Min. :-30.8681	Min. :-28.379
1st Qu.:-13.4336	1st Qu.:-18.064
Median : 1.2246	Median : -2.005
Mean : -0.5307	Mean : -5.267
3rd Qu.: 11.0230	3rd Qu.: 2.206
Max. : 25.0819	Max. : 18.910

By combining subsetting with assignment, we can make changes to just part of a matrix.

```
# and add 100 to the first column of m
m2[,1] = m2[,1] + 100
# summarize m
summary(m2)
```

V1	V2
Min. : 69.13	Min. :-28.379
1st Qu.: 86.57	1st Qu.:-18.064
Median :101.22	Median : -2.005
Mean : 99.47	Mean : -5.267
3rd Qu.:111.02	3rd Qu.: 2.206
Max. :125.08	Max. : 18.910

A somewhat common transformation for a matrix is to transpose which changes rows to columns. One might need to do this if an assay output from a lab machine puts samples in rows and genes in columns, for example, while in Bioconductor/R, we often want the samples in columns and the genes in rows.

```
t(m2)
```

8. Matrices

```
[,1]      [,2]      [,3]      [,4]      [,5]      [,6]      [,7]
[1,] 124.333765 125.081871 97.70854 101.300544 101.148731 106.68670 73.979815
[2,] -2.214361 -1.795608 -22.58731 -1.454317 -4.492802 10.77263 3.425541
      [,8]      [,9]      [,10]
[1,] 112.46845 69.13193 82.85241
[2,] -24.85817 18.90987 -28.37912
```

8.4. Calculations on matrix rows and columns

Again, we just need a matrix to play with. We'll use `rnorm` again, but with a slight twist.

```
m3 = matrix(rnorm(100,5,2),ncol=10) # what does the 5 mean here? And the 2?
```

Since these data are from a normal distribution, we can look at a row (or column) to see what the mean and standard deviation are.

```
mean(m3[,1])
```

```
[1] 5.585108
```

```
sd(m3[,1])
```

```
[1] 0.7807432
```

```
# or a row  
mean(m3[1,])
```

```
[1] 6.367885
```

```
sd(m3[1,])
```

```
[1] 1.459511
```

There are some useful convenience functions for computing means and sums of data in **all** of the columns and rows of matrices.

8. Matrices

```
colMeans(m3)
```

```
[1] 5.585108 5.616137 4.437312 6.001155 5.826136 6.218967 5.763700 5.683374  
[9] 5.058097 4.419581
```

```
rowMeans(m3)
```

```
[1] 6.367885 5.364585 5.475563 4.690024 4.948899 6.060900 6.223290 5.552056  
[9] 5.290125 4.636241
```

```
rowSums(m3)
```

```
[1] 63.67885 53.64585 54.75563 46.90024 49.48899 60.60900 62.23290 55.52056  
[9] 52.90125 46.36241
```

```
colSums(m3)
```

```
[1] 55.85108 56.16137 44.37312 60.01155 58.26136 62.18967 57.63700 56.83374  
[9] 50.58097 44.19581
```

We can look at the distribution of column means:

```
# save as a variable  
cmeans = colMeans(m3)  
summary(cmeans)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
4.420	5.190	5.650	5.461	5.811	6.219

Note that this is centered pretty closely around the selected mean of 5 above.

How about the standard deviation? There is not a `colSd` function, but it turns out that we can easily apply functions that take vectors as input, like `sd` and “apply” them across either the rows (the first dimension) or columns (the second) dimension.

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```
csds = apply(m3, 2, sd)
summary(csds)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
0.7807	1.6781	1.9775	1.9495	2.2203	3.0281

Again, take a look at the distribution which is centered quite close to the selected standard deviation when we created our matrix.

8.5. Exercises

8.5.1. Data preparation

For this set of exercises, we are going to rely on a dataset that comes with R. It gives the number of sunspots per month from 1749-1983. The dataset comes as a `ts` or time series data type which I convert to a matrix using the following code.

Just run the code as is and focus on the rest of the exercises.

```
data(sunspots)
sunspot_mat <- matrix(as.vector(sunspots), ncol=12, byrow = TRUE)
colnames(sunspot_mat) <- as.character(1:12)
rownames(sunspot_mat) <- as.character(1749:1983)
```

8.5.2. Questions

- After the conversion above, what does `sunspot_mat` look like? Use functions to find the number of rows, the number of columns, the class, and some basic summary statistics.

```
ncol(sunspot_mat)
nrow(sunspot_mat)
dim(sunspot_mat)
summary(sunspot_mat)
head(sunspot_mat)
tail(sunspot_mat)
```

- Practice subsetting the matrix a bit by selecting:

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- The first 10 years (rows)
- The month of July (7th column)
- The value for July, 1979 using the rowname to do the selection.

```
sunspot_mat[1:10,]  
sunspot_mat[,7]  
sunspot_mat['1979',7]
```

1. These next few exercises take advantage of the fact that calling a univariate statistical function (one that expects a vector) works for matrices by just making a vector of all the values in the matrix. What is the highest (max) number of sunspots recorded in these data?

```
max(sunspot_mat)
```

2. And the minimum?

```
min(sunspot_mat)
```

3. And the overall mean and median?

```
mean(sunspot_mat)  
median(sunspot_mat)
```

4. Use the `hist()` function to look at the distribution of all the monthly sunspot data.

```
hist(sunspot_mat)
```

5. Read about the `breaks` argument to `hist()` to try to increase the number of breaks in the histogram to increase the resolution slightly. Adjust your `hist()` and `breaks` to your liking.

```
hist(sunspot_mat, breaks=40)
```

6. Now, let's move on to summarizing the data a bit to learn about the pattern of sunspots varies by month or by year. Examine the dataset again. What do the columns represent? And the rows?

```
# just a quick glimpse of the data will give us a sense  
head(sunspot_mat)
```

7. We'd like to look at the distribution of sunspots by month. How can we do that?

```
# the mean of the columns is the mean number of sunspots per month.  
colMeans(sunspot_mat)
```

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```
# Another way to write the same thing:  
apply(sunspot_mat, 2, mean)
```

8. Assign the month summary above to a variable and summarize it to get a sense of the spread over months.

```
monthmeans = colMeans(sunspot_mat)  
summary(monthmeans)
```

9. Play the same game for years to get the per-year mean?

```
ymeans = rowMeans(sunspot_mat)  
summary(ymean)
```

10. Make a plot of the yearly means. Do you see a pattern?

```
plot(ymean)  
# or make it clearer  
plot(ymean, type='l')
```

9. Lists

9.1. The Power of a “Catch-All” Container

So far in our journey through R’s data structures, we’ve dealt with vectors and matrices. These are fantastic tools, but they have one strict rule: all their elements must be of the *same data type*. You can have a vector of numbers or a matrix of characters, but you can’t mix and match.

But what about real-world biological data? A single experiment can generate a dizzying variety of information. Imagine you’re studying a particular gene. You might have:

- The gene’s name (text).
- Its expression level across several samples (a set of numbers).
- A record of whether it’s a known cancer-related gene (a simple TRUE/FALSE).
- The raw fluorescence values from your qPCR machine (a matrix of numbers).
- Some personal notes about the experiment (a paragraph of text).

How could you possibly store all of this related, yet different, information together? You could create many separate variables, but that would be clunky and hard to manage. This is exactly the problem that **lists** are designed to solve.

A list in R is like a flexible, multi-compartment container. It’s a single object that can hold a collection of *other* R objects, and those objects can be of any type, length, or dimension. You can put vectors, matrices, logical values, and even other lists inside a single list. This makes them one of the most fundamental and powerful data structures for bioinformatics analysis.

The key features of lists are:

- **Flexibility:** They can contain a mix of any data type.
- **Organization:** You can and should *name* the elements of a list, making your data self-describing.
- **Hierarchy:** Because lists can contain other lists, you can create complex, nested data structures to represent sophisticated relationships in your data.

9.2. Creating a List

You create a list with the `list()` function. The best practice is to name the elements as you create them. This makes your code infinitely more readable and your data easier to work with.

Let's create a list to store the information for our hypothetical gene study.

```
# An experiment tracking list for the gene TP53
experiment_data <- list(
  experiment_id = "EXP042",
  gene_name = "TP53",
  read_counts = c(120, 155, 98, 210),
  is_control = FALSE,
  sample_matrix = matrix(1:4, nrow = 2, dimnames = list(c("Treated", "Untreated"), c("Replicate1", "Replicate2")))
)

# --- Function Explainer: print() ---
# The print() function displays the contents of an R object in the console.
# For a list, it shows each element and its contents. It's the default action
# when you just type the variable's name and hit Enter.
print(experiment_data)

$experiment_id
[1] "EXP042"

$gene_name
[1] "TP53"

$read_counts
[1] 120 155 98 210

$is_control
[1] FALSE

$sample_matrix
      Replicate1 Replicate2
Treated          1          3
Untreated        2          4
```

9.3. Inspecting Your List: What's Inside?

When someone hands you a tube in the lab, the first thing you do is look at the label. When R gives you a complex object like a list, you need to do the same. R provides several “introspection” functions to help you understand the contents and structure of your lists.

9.3.1. `str()`: The Structure Function

This is arguably the most useful function for inspecting any R object, especially lists.

```
# --- Function Explainer: str() ---
# The str() function provides a compact, human-readable summary of an
# object's internal "str"ucture. It's your best friend for understanding
# what's inside a list, including the type and a preview of each element.
str(experiment_data)
```

```
List of 5
$ experiment_id: chr "EXP042"
$ gene_name     : chr "TP53"
$ read_counts   : num [1:4] 120 155 98 210
$ is_control    : logi FALSE
$ sample_matrix: int [1:2, 1:2] 1 2 3 4
..- attr(*, "dimnames")=List of 2
.. ..$ : chr [1:2] "Treated" "Untreated"
.. ..$ : chr [1:2] "Replicate1" "Replicate2"
```

The output of `str()` tells us everything we need to know: it's a “List of 5”, and for each of the 5 elements, it shows the name (e.g., `experiment_id`), the data type (e.g., `chr` for character, `num` for numeric), and a preview of the content.

9.3.2. `length()`, `names()`, and `class()`

These functions give you more specific information about the list itself.

```
# --- Function Explainer: length() ---
# For a list, length() tells you how many top-level elements it contains.
length(experiment_data)
```

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```
[1] 5
```

```
# --- Function Explainer: names() ---
# The names() function extracts the names of the elements in a list as a
# character vector. It's a great way to see what you can access.
names(experiment_data)
```

```
[1] "experiment_id" "gene_name"      "read_counts"    "is_control"
[5] "sample_matrix"
```

```
# --- Function Explainer: class() ---
# The class() function tells you the type of the object itself.
# This is useful to confirm you are indeed working with a list.
class(experiment_data)
```

```
[1] "list"
```

9.4. Accessing List Elements: Getting Things Out

Okay, you've packed your experimental data into a list. Now, how do you get specific items out? This is a critical concept, and R has a few ways to do it, each with a distinct purpose.

9.4.1. The Mighty `[[...]]` and `$` for Single Items

To pull out a *single element* from a list in its original form, you use either double square brackets `[[...]]` or the dollar sign `$` (for named lists). Think of this as carefully reaching into a specific compartment of your container and taking out the item itself.

Let's use our `experiment_data` list.

```
# Get the gene name using [[...]]
gene <- experiment_data[["gene_name"]]
print(gene)
```

```
[1] "TP53"
```

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```
class(gene) # It's a character vector, just as it was when we put it in.
```

```
[1] "character"
```

```
# Get the read counts using the $ shortcut. This is often easier to read.  
reads <- experiment_data$read_counts  
print(reads)
```

```
[1] 120 155 98 210
```

```
class(reads) # It's a numeric vector.
```

```
[1] "numeric"
```

```
# The [...] has a neat trick: you can use a variable to specify the name.  
element_to_get <- "read_counts"  
experiment_data[[element_to_get]]
```

```
[1] 120 155 98 210
```

The key takeaway is that [...] and \$ extract the element. The result is the object that was stored inside the list.

9.4.2. The Subsetting [...] for New Lists

The single square bracket [...] behaves differently. It always returns a *new, smaller list* that is a subset of the original list. It's like taking a whole compartment, label and all, out of your larger container.

```
# Get the gene name using [...]  
gene_sublist <- experiment_data["gene_name"]  
  
print(gene_sublist)
```

```
$gene_name  
[1] "TP53"
```

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```
# --- Note the class! ---
# The result is another list, which contains the gene_name element.
class(gene_sublist)

[1] "list"
```

This distinction is vital. If you want to perform a calculation on an element (like finding the `mean()` of `read_counts`), you must extract it with `[...]` or `$`. If you tried `mean(experiment_data["read_counts"])`, R would give you an error because you can't calculate the mean of a list!

9.5. Modifying Lists

Your data is rarely static. You can easily add, remove, or update elements in a list after you've created it.

9.5.1. Adding and Updating Elements

You can add a new element or change an existing one by using the `$` or `[...]` assignment syntax.

```
# Add the date of the experiment
experiment_data$date <- "2024-06-05"

# Add some notes using the [...] syntax
experiment_data[["notes"]] <- "Initial pilot experiment. High variance in read counts."

# Let's update the control status
experiment_data$is_control <- TRUE

# Let's look at the structure now
str(experiment_data)
```

```
List of 7
$ experiment_id: chr "EXP042"
$ gene_name    : chr "TP53"
$ read_counts  : num [1:4] 120 155 98 210
```

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```
$ is_control      : logi TRUE
$ sample_matrix: int [1:2, 1:2] 1 2 3 4
..- attr(*, "dimnames")=List of 2
... $ : chr [1:2] "Treated" "Untreated"
... $ : chr [1:2] "Replicate1" "Replicate2"
$ date           : chr "2024-06-05"
$ notes          : chr "Initial pilot experiment. High variance in read counts."
```

9.5.2. Removing Elements

To remove an element from a list, you simply assign `NULL` to it. `NULL` is R's special object representing nothingness.

```
# We've decided the matrix isn't needed for this summary object.
experiment_data$sample_matrix <- NULL

# See the final structure of our list
str(experiment_data)
```

```
List of 6
$ experiment_id: chr "EXP042"
$ gene_name     : chr "TP53"
$ read_counts   : num [1:4] 120 155 98 210
$ is_control    : logi TRUE
$ date          : chr "2024-06-05"
$ notes          : chr "Initial pilot experiment. High variance in read counts."
```

9.6. A Biological Example: A Self-Contained Gene Record

Let's put this all together. Lists are perfect for creating self-contained records that you can easily pass to functions or combine into larger lists.

```
# --- Function Explainer: log2() ---
# The log2() function calculates the base-2 logarithm. It's very common in
# gene expression analysis to transform skewed count data to make it more
# symmetric and easier to model.

brca1_gene <- list(
```

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```
gene_symbol = "BRCA1",
full_name = "BRCA1 DNA repair associated",
chromosome = "17",
expression_log2 = log2(c(45, 50, 30, 88, 120)),
related_diseases = c("Breast Cancer", "Ovarian Cancer")
)

# Now we can easily work with this structured information

# --- Function Explainer: cat() ---
# The cat() function concatenates and prints its arguments to the console.
# Unlike print(), it allows you to seamlessly join text and variables, and
# the "\n" character is used to add a newline (a line break).
cat("Analyzing gene:", brca1_gene$gene_symbol, "\n")
```

Analyzing gene: BRCA1

```
cat("Located on chromosome:", brca1_gene$chromosome, "\n")
```

Located on chromosome: 17

```
# Calculate the average log2 expression
# --- Function Explainer: mean() ---
# The mean() function calculates the arithmetic average of a numeric vector.
avg_expression <- mean(brca1_gene$expression_log2)
cat("Average log2 expression:", avg_expression, "\n")
```

Average log2 expression: 5.881784

This simple `brca1_gene` list is now a complete, portable record. You could imagine creating a list of these gene records, creating a powerful, hierarchical database for your entire project.

10. Data Frames

While R has many different data types, the one that is central to much of the power and popularity of R is the `data.frame`. A `data.frame` looks a bit like an R matrix in that it has two dimensions, rows and columns. However, `data.frames` are usually viewed as a set of columns representing variables and the rows representing the values of those variables. Importantly, a `data.frame` may contain *different* data types in each of its columns; matrices **must** contain only one data type. This distinction is important to remember, as there are *specific* approaches to working with R `data.frames` that may be different than those for working with matrices.

10.1. Learning goals

- Understand how `data.frames` are different from matrices.
- Know a few functions for examining the contents of a `data.frame`.
- List approaches for subsetting `data.frames`.
- Be able to load and save tabular data from and to disk.
- Show how to create `data.frames` from scratch.

10.2. Learning objectives

- Load the yeast growth dataset into R using `read.csv`.
- Examine the contents of the dataset.
- Use subsetting to find genes that may be involved with nutrient metabolism and transport.
- Summarize data measurements by categories.

10.3. Dataset

The data used here are borrowed directly from the [fantastic Bioconductor tutorials](#) and are a cleaned up version of the data from [Brauer et al. Coordination of Growth Rate, Cell](#)

10. Data Frames

Cycle, Stress Response, and Metabolic Activity in Yeast (2008) Mol Biol Cell 19:352-367.

These data are from a gene expression microarray, and in this paper the authors examine the relationship between growth rate and gene expression in yeast cultures limited by one of six different nutrients (glucose, leucine, ammonium, sulfate, phosphate, uracil). If you give yeast a rich media loaded with nutrients except restrict the supply of a single nutrient, you can control the growth rate to any rate you choose. By starving yeast of specific nutrients you can find genes that:

1. Raise or lower their expression in response to growth rate. Growth-rate dependent expression patterns can tell us a lot about cell cycle control, and how the cell responds to stress. The authors found that expression of >25% of all yeast genes is linearly correlated with growth rate, independent of the limiting nutrient. They also found that the subset of negatively growth-correlated genes is enriched for peroxisomal functions, and positively correlated genes mainly encode ribosomal functions.
2. Respond differently when different nutrients are being limited. If you see particular genes that respond very differently when a nutrient is sharply restricted, these genes might be involved in the transport or metabolism of that specific nutrient.

The dataset can be downloaded directly from:

- [brauer2007_tidy.csv](#)

We are going to read this dataset into R and then use it as a playground for learning about data.frames.

10.4. Reading in data

R has many capabilities for reading in data. Many of the functions have names that help us to understand what data format is to be expected. In this case, the filename that we want to read ends in `.csv`, meaning comma-separated-values. The `read.csv()` function reads in `.csv` files. As usual, it is worth reading `help('read.csv')` to get a better sense of the possible bells-and-whistles.

The `read.csv()` function can read directly from a URL, so we do not need to download the file directly. This dataset is relatively large (about 16MB), so this may take a bit depending on your network connection speed.

```
options(width=60)
```

```
url = paste0(  
  'https://raw.githubusercontent.com',  
  '/bioconnector/workshops/master/data/brauer2007_tidy.csv'  
)  
ydat <- read.csv(url)
```

Our variable, `ydat`, now “contains” the downloaded and read data. We can check to see what data type `read.csv` gave us:

```
class(ydat)
```

```
[1] "data.frame"
```

10.5. Inspecting data.frames

Our `ydat` variable is a `data.frame`. As I mentioned, the dataset is fairly large, so we will not be able to look at it all at once on the screen. However, R gives us many tools to inspect a `data.frame`.

- Overviews of content
 - `head()` to show first few rows
 - `tail()` to show last few rows
- Size
 - `dim()` for dimensions (rows, columns)
 - `nrow()`
 - `ncol()`
 - `object.size()` for power users interested in the memory used to store an object
- Data and attribute summaries
 - `colnames()` to get the names of the columns
 - `rownames()` to get the “names” of the rows—may not be present
 - `summary()` to get per-column summaries of the data in the `data.frame`.

```
head(ydat)
```

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```

symbol systematic_name nutrient rate expression
1   SFB2          YNL049C  Glucose 0.05     -0.24
2   <NA>          YNL095C  Glucose 0.05      0.28
3   QRI7          YDL104C  Glucose 0.05     -0.02
4   CFT2          YLR115W  Glucose 0.05     -0.33
5   SS02          YMR183C  Glucose 0.05      0.05
6   PSP2          YML017W  Glucose 0.05     -0.69

                                bp
1       ER to Golgi transport
2   biological process unknown
3 proteolysis and peptidolysis
4   mRNA polyadenylation*
5           vesicle fusion*
6   biological process unknown

                                mf
1   molecular function unknown
2   molecular function unknown
3 metalloendopeptidase activity
4           RNA binding
5        t-SNARE activity
6   molecular function unknown

```

```
tail(ydat)
```

```

symbol systematic_name nutrient rate expression
198425  DOA1          YKL213C  Uracil  0.3    0.14
198426  KRE1          YNL322C  Uracil  0.3    0.28
198427  MTL1          YGR023W  Uracil  0.3    0.27
198428  KRE9          YJL174W  Uracil  0.3    0.43
198429  UTH1          YKR042W  Uracil  0.3    0.19
198430  <NA>          YOL111C  Uracil  0.3    0.04

                                bp
198425  ubiquitin-dependent protein catabolism*
198426  cell wall organization and biogenesis
198427  cell wall organization and biogenesis
198428  cell wall organization and biogenesis*
198429 mitochondrion organization and biogenesis*
198430        biological process unknown

                                mf
198425  molecular function unknown

```

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```
198426 structural constituent of cell wall
198427      molecular function unknown
198428      molecular function unknown
198429      molecular function unknown
198430      molecular function unknown
```

```
dim(ydat)
```

```
[1] 198430      7
```

```
nrow(ydat)
```

```
[1] 198430
```

```
ncol(ydat)
```

```
[1] 7
```

```
colnames(ydat)
```

```
[1] "symbol"          "systematic_name" "nutrient"
[4] "rate"            "expression"       "bp"
[7] "mf"
```

```
summary(ydat)
```

```
symbol           systematic_name      nutrient
Length:198430    Length:198430      Length:198430
Class :character  Class :character  Class :character
Mode  :character  Mode  :character  Mode  :character
```

```
rate            expression        bp
Min.   :0.0500  Min.   :-6.500000  Length:198430
1st Qu.:0.1000  1st Qu.:-0.290000  Class :character
```

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```
Median :0.2000    Median : 0.000000   Mode  :character
Mean   :0.1752    Mean   : 0.003367
3rd Qu.:0.2500    3rd Qu.: 0.290000
Max.   :0.3000    Max.   : 6.640000
               mf
Length:198430
Class :character
Mode  :character
```

In RStudio, there is an additional function, `View()` (note the capital “V”) that opens the first 1000 rows (default) in the RStudio window, akin to a spreadsheet view.

```
View(ydat)
```

10.6. Accessing variables (columns) and subsetting

In R, `data.frames` can be subset similarly to other two-dimensional data structures. The `[` in R is used to denote subsetting of any kind. When working with two-dimensional data, we need two values inside the `[]` to specify the details. The specification is `[rows, columns]`. For example, to get the first three rows of `ydat`, use:

```
ydat[1:3, ]
```

```
symbol systematic_name nutrient rate expression
1   SFB2          YNL049C  Glucose 0.05     -0.24
2   <NA>          YNL095C  Glucose 0.05      0.28
3   QRI7          YDL104C  Glucose 0.05     -0.02
                                bp
1       ER to Golgi transport
2   biological process unknown
3 proteolysis and peptidolysis
                                mf
1   molecular function unknown
2   molecular function unknown
3 metalloendopeptidase activity
```

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Note how the second number, the columns, is blank. R takes that to mean “all the columns”. Similarly, we can combine rows and columns specification arbitrarily.

```
ydat[1:3, 1:3]
```

```
symbol systematic_name nutrient
1   SFB2          YNL049C  Glucose
2   <NA>          YNL095C  Glucose
3   QRI7          YDL104C  Glucose
```

Because selecting a single variable, or column, is such a common operation, there are two shortcuts for doing so *with data.frames*. The first, the \$ operator works like so:

```
# Look at the column names, just to refresh memory
colnames(ydat)
```

```
[1] "symbol"           "systematic_name" "nutrient"
[4] "rate"              "expression"       "bp"
[7] "mf"
```

```
# Note that I am using "head" here to limit the output
head(ydat$symbol)
```

```
[1] "SFB2" NA      "QRI7" "CFT2" "SS02" "PSP2"
```

```
# What is the actual length of "symbol"?
length(ydat$symbol)
```

```
[1] 198430
```

The second is related to the fact that, in R, data.frames are also lists. We subset a list by using `[[[]]]` notation. To get the second column of `ydat`, we can use:

```
head(ydat[[2]])
```

```
[1] "YNL049C" "YNL095C" "YDL104C" "YLR115W" "YMR183C"
[6] "YML017W"
```

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Alternatively, we can use the column name:

```
head(ydat[["systematic_name"]])
```

```
[1] "YNL049C" "YNL095C" "YDL104C" "YLR115W" "YMR183C"  
[6] "YML017W"
```

10.6.1. Some data exploration

There are a couple of columns that include numeric values. Which columns are numeric?

```
class(ydat$symbol)
```

```
[1] "character"
```

```
class(ydat$rate)
```

```
[1] "numeric"
```

```
class(ydat$expression)
```

```
[1] "numeric"
```

Make histograms of: - the expression values - the rate values

What does the `table()` function do? Could you use that to look at the `rate` column given that that column appears to have repeated values?

What `rate` corresponds to the most nutrient-starved condition?

10.6.2. More advanced indexing and subsetting

We can use, for example, logical values (TRUE/FALSE) to subset data.frames.

```
head(ydat[ydat$symbol == 'LEU1', ])
```

	symbol	systematic_name	nutrient	rate	expression	bp
NA	<NA>	<NA>	<NA>	NA	NA	<NA>
NA.1	<NA>	<NA>	<NA>	NA	NA	<NA>
NA.2	<NA>	<NA>	<NA>	NA	NA	<NA>
NA.3	<NA>	<NA>	<NA>	NA	NA	<NA>
NA.4	<NA>	<NA>	<NA>	NA	NA	<NA>
NA.5	<NA>	<NA>	<NA>	NA	NA	<NA>
	mf					
NA	<NA>					
NA.1	<NA>					
NA.2	<NA>					
NA.3	<NA>					
NA.4	<NA>					
NA.5	<NA>					

```
tail(ydat[ydat$symbol == 'LEU1', ])
```

	symbol	systematic_name	nutrient	rate	expression
NA.47244	<NA>	<NA>	<NA>	NA	NA
NA.47245	<NA>	<NA>	<NA>	NA	NA
NA.47246	<NA>	<NA>	<NA>	NA	NA
NA.47247	<NA>	<NA>	<NA>	NA	NA
NA.47248	<NA>	<NA>	<NA>	NA	NA
NA.47249	<NA>	<NA>	<NA>	NA	NA
	bp	mf			
NA.47244	<NA>	<NA>			
NA.47245	<NA>	<NA>			
NA.47246	<NA>	<NA>			
NA.47247	<NA>	<NA>			
NA.47248	<NA>	<NA>			
NA.47249	<NA>	<NA>			

What is the problem with this approach? It appears that there are a bunch of NA values. Taking a quick look at the symbol column, we see what the problem.

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```
summary(ydat$symbol)
```

Length	Class	Mode
198430	character	character

Using the `is.na()` function, we can make filter further to get down to values of interest.

```
head(ydat[ydat$symbol == 'LEU1' & !is.na(ydat$symbol), ])
```

	symbol	systematic_name	nutrient	rate	expression
1526	LEU1	YGL009C	Glucose	0.05	-1.12
7043	LEU1	YGL009C	Glucose	0.10	-0.77
12555	LEU1	YGL009C	Glucose	0.15	-0.67
18071	LEU1	YGL009C	Glucose	0.20	-0.59
23603	LEU1	YGL009C	Glucose	0.25	-0.20
29136	LEU1	YGL009C	Glucose	0.30	0.03
		bp			
1526	leucine biosynthesis				
7043	leucine biosynthesis				
12555	leucine biosynthesis				
18071	leucine biosynthesis				
23603	leucine biosynthesis				
29136	leucine biosynthesis				
		mf			
1526	3-isopropylmalate dehydratase activity				
7043	3-isopropylmalate dehydratase activity				
12555	3-isopropylmalate dehydratase activity				
18071	3-isopropylmalate dehydratase activity				
23603	3-isopropylmalate dehydratase activity				
29136	3-isopropylmalate dehydratase activity				

Sometimes, looking at the data themselves is not that important. Using `dim()` is one possibility to look at the number of rows and columns after subsetting.

```
dim(ydat[ydat$expression > 3, ])
```

```
[1] 714    7
```

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Find the high expressed genes when leucine-starved. For this task we can also use `subset` which allows us to treat column names as R variables (no \$ needed).

```
subset(ydat, nutrient == 'Leucine' & rate == 0.05 & expression > 3)
```

	symbol	systematic_name	nutrient	rate	expression
133768	QDR2	YIL121W	Leucine	0.05	4.61
133772	LEU1	YGL009C	Leucine	0.05	3.84
133858	BAP3	YDR046C	Leucine	0.05	4.29
135186	<NA>	YPL033C	Leucine	0.05	3.43
135187	<NA>	YLR267W	Leucine	0.05	3.23
135288	HXT3	YDR345C	Leucine	0.05	5.16
135963	TP02	YGR138C	Leucine	0.05	3.75
135965	YR02	YBR054W	Leucine	0.05	4.40
136102	GPG1	YGL121C	Leucine	0.05	3.08
136109	HSP42	YDR171W	Leucine	0.05	3.07
136119	HXT5	YHR096C	Leucine	0.05	4.90
136151	<NA>	YJL144W	Leucine	0.05	3.06
136152	MOH1	YBL049W	Leucine	0.05	3.43
136153	<NA>	YBL048W	Leucine	0.05	3.95
136189	HSP26	YBR072W	Leucine	0.05	4.86
136231	NCA3	YJL116C	Leucine	0.05	4.03
136233	<NA>	YBR116C	Leucine	0.05	3.28
136486	<NA>	YGR043C	Leucine	0.05	3.07
137443	ADH2	YMR303C	Leucine	0.05	4.15
137448	ICL1	YER065C	Leucine	0.05	3.54
137451	SFC1	YJR095W	Leucine	0.05	3.72
137569	MLS1	YNL117W	Leucine	0.05	3.76
			bp		
133768			multidrug transport		
133772			leucine biosynthesis		
133858			amino acid transport		
135186			meiosis*		
135187			biological process unknown		
135288			hexose transport		
135963			Polyamine transport		
135965			biological process unknown		
136102			signal transduction		
136109			response to stress*		
136119			hexose transport		

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136151	response to dessication
136152	biological process unknown
136153	<NA>
136189	response to stress*
136231	mitochondrion organization and biogenesis
136233	<NA>
136486	biological process unknown
137443	fermentation*
137448	glyoxylate cycle
137451	fumarate transport*
137569	glyoxylate cycle mf
133768	multidrug efflux pump activity
133772	3-isopropylmalate dehydratase activity
133858	amino acid transporter activity
135186	molecular function unknown
135187	molecular function unknown
135288	glucose transporter activity*
135963	spermine transporter activity
135965	molecular function unknown
136102	signal transducer activity
136109	unfolded protein binding
136119	glucose transporter activity*
136151	molecular function unknown
136152	molecular function unknown
136153	<NA>
136189	unfolded protein binding
136231	molecular function unknown
136233	<NA>
136486	transaldolase activity
137443	alcohol dehydrogenase activity
137448	isocitrate lyase activity
137451	succinate:fumarate antiporter activity
137569	malate synthase activity

10.7. Aggregating data

Aggregating data, or summarizing by category, is a common way to look for trends or differences in measurements between categories. Use `aggregate` to find the mean expression

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by gene symbol.

```
head(aggregate(ydat$expression, by=list( ydat$symbol), mean))
```

```
Group.1           x
1    AAC1  0.52888889
2    AAC3 -0.21628571
3   AAD10  0.43833333
4   AAD14 -0.07166667
5   AAD16  0.24194444
6   AAD4 -0.79166667
```

```
# or
head(aggregate(expression ~ symbol, mean, data=ydat))
```

```
symbol  expression
1    AAC1  0.52888889
2    AAC3 -0.21628571
3   AAD10  0.43833333
4   AAD14 -0.07166667
5   AAD16  0.24194444
6   AAD4 -0.79166667
```

10.8. Creating a data.frame from scratch

Sometimes it is useful to combine related data into one object. For example, let's simulate some data.

```
smoker = factor(rep(c("smoker", "non-smoker"), each=50))
smoker_numeric = as.numeric(smoker)
x = rnorm(100)
risk = x + 2*smoker_numeric
```

We have two variables, `risk` and `smoker` that are related. We can make a data.frame out of them:

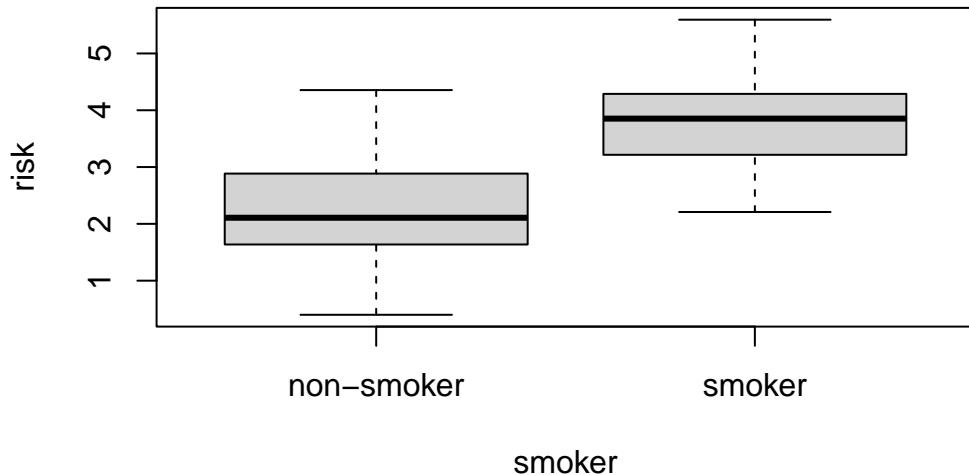
10. Data Frames

```
smoker_risk = data.frame(smoker = smoker, risk = risk)
head(smoker_risk)
```

```
smoker      risk
1 smoker 3.438347
2 smoker 3.570912
3 smoker 4.511678
4 smoker 4.131091
5 smoker 2.582227
6 smoker 4.046004
```

R also has plotting shortcuts that work with data.frames to simplify plotting

```
plot(risk ~ smoker, data=smoker_risk)
```



10.9. Saving a data.frame

Once we have a data.frame of interest, we may want to save it. The most portable way to save a data.frame is to use one of the `write` functions. In this case, let's save the data as a `.csv` file.

```
write.csv(smoker_risk, "smoker_risk.csv")
```

11. Factors

11.1. Factors

A factor is a special type of vector, normally used to hold a categorical variable—such as smoker/non-smoker, state of residency, zipcode—in many statistical functions. Such vectors have class “factor”. Factors are primarily used in Analysis of Variance (ANOVA) or other situations when “categories” are needed. When a factor is used as a predictor variable, the corresponding indicator variables are created (more later).

Note of caution that factors in R often *appear* to be character vectors when printed, but you will notice that they do not have double quotes around them. They are stored in R as numbers with a key name, so sometimes you will note that the factor *behaves* like a numeric vector.

```
# create the character vector
citizen<-c("uk","us","no","au","uk","us","us","no","au")

# convert to factor
citizenf<-factor(citizen)
citizen
```

```
[1] "uk" "us" "no" "au" "uk" "us" "us" "no" "au"
```

```
citizenf
```

```
[1] uk us no au uk us us no au
Levels: au no uk us
```

```
# convert factor back to character vector
as.character(citizenf)
```

```
[1] "uk" "us" "no" "au" "uk" "us" "us" "no" "au"
```

11. Factors

```
# convert to numeric vector  
as.numeric(citizenf)
```

```
[1] 3 4 2 1 3 4 4 2 1
```

R stores many data structures as vectors with “attributes” and “class” (just so you have seen this).

```
attributes(citizenf)
```

```
$levels  
[1] "au" "no" "uk" "us"
```

```
$class  
[1] "factor"
```

```
class(citizenf)
```

```
[1] "factor"
```

```
# note that after unclassing, we can see the  
# underlying numeric structure again  
unclass(citizenf)
```

```
[1] 3 4 2 1 3 4 4 2 1  
attr(,"levels")  
[1] "au" "no" "uk" "us"
```

Tabulating factors is a useful way to get a sense of the “sample” set available.

```
table(citizenf)
```

```
citizenf  
au no uk us  
2 2 2 3
```

Part III.

Exploratory data analysis

Imagine you're on an adventure, about to embark on a journey into the unknown. You've just been handed a treasure map, with the promise of valuable insights waiting to be discovered. This map is your data set, and the journey is exploratory data analysis (EDA).

As you begin your exploration, you start by getting a feel for the terrain. You take a broad, bird's-eye view of the data, examining its structure and dimensions. Are you dealing with a vast landscape or a small, confined area? Are there any missing pieces in the map that you'll need to account for? Understanding the overall context of your data set is crucial before venturing further.

With a sense of the landscape, you now zoom in to identify key landmarks in the data. You might look for unusual patterns, trends, or relationships between variables. As you spot these landmarks, you start asking questions: What's causing that spike in values? Are these two factors related, or is it just a coincidence? By asking these questions, you're actively engaging with the data and forming hypotheses that could guide future analysis or experiments.

As you continue your journey, you realize that the map alone isn't enough to fully understand the terrain. You need more tools to bring the data to life. You start visualizing the data using charts, plots, and graphs. These visualizations act as your binoculars, allowing you to see patterns and relationships more clearly. Through them, you can uncover the hidden treasures buried within the data.

EDA isn't a linear path from start to finish. As you explore, you'll find yourself circling back to previous points, refining your questions, and digging deeper. The process is iterative, with each new discovery informing the next. And as you go, you'll gain a deeper understanding of the data's underlying structure and potential.

Finally, after your thorough exploration, you'll have a solid foundation to build upon. You'll be better equipped to make informed decisions, test hypotheses, and draw meaningful conclusions. The insights you've gained through EDA will serve as a compass, guiding you towards the true value hidden within your data. And with that, you've successfully completed your journey through exploratory data analysis.

12. Introduction to dplyr: mammal sleep dataset

The dataset we will be using to introduce the *dplyr* package is an updated and expanded version of the mammals sleep dataset. Updated sleep times and weights were taken from V. M. Savage and G. B. West. A quantitative, theoretical framework for understanding mammalian sleep¹.

12.1. Learning goals

- Know that *dplyr* is just a different approach to manipulating data in *data.frames*.
- List the commonly used *dplyr* verbs and how they can be used to manipulate *data.frames*.
- Show how to aggregate and summarize data using *dplyr*
- Know what the piping operator, `|>`, is and how it can be used.

12.2. Learning objectives

- Select subsets of the mammal sleep dataset.
- Reorder the dataset.
- Add columns to the dataset based on existing columns.
- Summarize the amount of sleep by categorical variables using `group_by` and `summarize`.

¹A quantitative, theoretical framework for understanding mammalian sleep. Van M. Savage, Geoffrey B. West. Proceedings of the National Academy of Sciences Jan 2007, 104 (3) 1051-1056; DOI: [10.1073/pnas.0610080104](https://doi.org/10.1073/pnas.0610080104)

12. Introduction to dplyr: mammal sleep dataset

12.3. What is dplyr?

The *dplyr* package is a specialized package for working with `data.frames` (and the related `tibble`) to transform and summarize tabular data with rows and columns. For another explanation of *dplyr* see the *dplyr* package vignette: [Introduction to dplyr](#)

12.4. Why Is dplyr useful?

dplyr contains a set of functions—commonly called the *dplyr* “verbs”—that perform common data manipulations such as filtering for rows, selecting specific columns, re-ordering rows, adding new columns and summarizing data. In addition, *dplyr* contains a useful function to perform another common task which is the “split-apply-combine” concept.

Compared to base functions in R, the functions in *dplyr* are often easier to work with, are more consistent in the syntax and are targeted for data analysis around data frames, instead of just vectors.

12.5. Data: Mammals Sleep

The `msleep` (mammals sleep) data set contains the sleep times and weights for a set of mammals and is available in the `dagdata` repository on github. This data set contains 83 rows and 11 variables. The data happen to be available as a `dataset` in the `ggplot2` package. To get access to the `msleep` dataset, we need to first install the `ggplot2` package.

```
install.packages('ggplot2')
```

Then, we can load the library.

```
library(ggplot2)
data(msleep)
```

As with many datasets in R, “help” is available to describe the dataset itself.

```
?msleep
```

12. Introduction to dplyr: mammal sleep dataset

The columns are described in the help page, but are included here, also.

column name	Description
name	common name
genus	taxonomic rank
vore	carnivore, omnivore or herbivore?
order	taxonomic rank
conservation	the conservation status of the mammal
sleep_total	total amount of sleep, in hours
sleep_rem	rem sleep, in hours
sleep_cycle	length of sleep cycle, in hours
awake	amount of time spent awake, in hours
brainwt	brain weight in kilograms
bodywt	body weight in kilograms

12.6. dplyr verbs

The dplyr verbs are listed here. There are many other functions available in dplyr, but we will focus on just these.

dplyr verbs	Description
<code>select()</code>	select columns
<code>filter()</code>	filter rows
<code>arrange()</code>	re-order or arrange rows
<code>mutate()</code>	create new columns
<code>summarise()</code>	summarise values
<code>group_by()</code>	allows for group operations in the “split-apply-combine” concept

12.7. Using the dplyr verbs

The two most basic functions are `select()` and `filter()`, which selects columns and filters rows respectively. What are the equivalent ways to select columns without dplyr? And filtering to include only specific rows?

Before proceeding, we need to install the dplyr package:

12. Introduction to dplyr: mammal sleep dataset

```
install.packages('dplyr')
```

And then load the library:

```
library(dplyr)
```

```
Attaching package: 'dplyr'
```

```
The following objects are masked from 'package:stats':
```

```
filter, lag
```

```
The following objects are masked from 'package:base':
```

```
intersect, setdiff, setequal, union
```

12.7.1. Selecting columns: select()

Select a set of columns such as the `name` and the `sleep_total` columns.

```
sleepData <- select(msleep, name, sleep_total)
head(sleepData)
```

```
# A tibble: 6 x 2
  name                 sleep_total
  <chr>                <dbl>
1 Cheetah              12.1
2 Owl monkey            17
3 Mountain beaver      14.4
4 Greater short-tailed shrew 14.9
5 Cow                  4
6 Three-toed sloth     14.4
```

To select all the columns *except* a specific column, use the “-” (subtraction) operator (also known as negative indexing). For example, to select all columns except `name`:

12. Introduction to dplyr: mammal sleep dataset

```
head(select(msleep, -name))

# A tibble: 6 x 10
  genus     vore   order  conservation sleep_total sleep_rem sleep_cycle awake
  <chr>    <chr>  <chr>      <chr>        <dbl>      <dbl>      <dbl> <dbl>
1 Acinonyx  carni Carnivo~ lc           12.1       NA       NA     11.9
2 Aotus      omni  Primates <NA>        17         1.8      NA      7
3 Aplodontia herbi Rodentia nt          14.4       2.4      NA     9.6
4 Blarina    omni  Soricom~ lc           14.9       2.3     0.133    9.1
5 Bos        herbi Artiodactyl~ domesticated 4          0.7     0.667   20
6 Bradypus   herbi Pilosa  <NA>        14.4       2.2     0.767   9.6
# i 2 more variables: brainwt <dbl>, bodywt <dbl>
```

To select a range of columns by name, use the “:” operator. Note that dplyr allows us to use the column names without quotes and as “indices” of the columns.

```
head(select(msleep, name:order))

# A tibble: 6 x 4
  name              genus     vore   order
  <chr>            <chr>    <chr>  <chr>
1 Cheetah          Acinonyx  carni Carnivora
2 Owl monkey       Aotus     omni  Primates
3 Mountain beaver Aplodontia herbi Rodentia
4 Greater short-tailed shrew Blarina  omni  Soricomorpha
5 Cow               Bos       herbi Artiodactyla
6 Three-toed sloth Bradypus  herbi Pilosa
```

To select all columns that start with the character string “sl”, use the function `starts_with()`.

```
head(select(msleep, starts_with("sl")))

# A tibble: 6 x 3
  sleep_total sleep_rem sleep_cycle
  <dbl>       <dbl>      <dbl>
1     12.1       NA       NA
2      17        1.8      NA
```

12. Introduction to dplyr: mammal sleep dataset

```
3      14.4      2.4      NA
4      14.9      2.3     0.133
5       4       0.7     0.667
6      14.4      2.2     0.767
```

Some additional options to select columns based on a specific criteria include:

1. `ends_with()` = Select columns that end with a character string
2. `contains()` = Select columns that contain a character string
3. `matches()` = Select columns that match a regular expression
4. `one_of()` = Select column names that are from a group of names

12.7.2. Selecting rows: `filter()`

The `filter()` function allows us to filter rows to include only those rows that *match* the filter. For example, we can filter the rows for mammals that sleep a total of more than 16 hours.

```
filter(msleep, sleep_total >= 16)
```

```
# A tibble: 8 x 11
  name   genus vore  order conservation sleep_total sleep_rem sleep_cycle awake
  <chr>  <chr> <chr> <chr> <chr>          <dbl>      <dbl>      <dbl> <dbl>
1 Owl    Aotus  omni  Prim~ <NA>           17        1.8      NA     7
2 Long-n Dasy~ carni Cing~ lc            17.4       3.1     0.383   6.6
3 North ~ Dide~ omni  Dide~ lc            18        4.9     0.333   6
4 Big    br~ Epte~ inse~ Chir~ lc           19.7       3.9     0.117   4.3
5 Thick-~ Lutr~ carni Dide~ lc           19.4       6.6      NA     4.6
6 Little~ Myot~ inse~ Chir~ <NA>          19.9       2       0.2     4.1
7 Giant ~ Prio~ inse~ Cing~ en           18.1       6.1      NA     5.9
8 Arctic~ Sper~ herbi Rode~ lc           16.6       NA      NA     7.4
# i 2 more variables: brainwt <dbl>, bodywt <dbl>
```

Filter the rows for mammals that sleep a total of more than 16 hours *and* have a body weight of greater than 1 kilogram.

```
filter(msleep, sleep_total >= 16, bodywt >= 1)
```

12. Introduction to dplyr: mammal sleep dataset

```
# A tibble: 3 x 11
  name   genus vore  order conservation sleep_total sleep_rem sleep_cycle awake
  <chr>  <chr> <chr> <chr> <chr>       <dbl>      <dbl>      <dbl> <dbl>
1 Long-n~ Dasy~ carni Cing~ lc        17.4       3.1      0.383    6.6
2 North ~ Dide~ omni  Dide~ lc        18         4.9      0.333     6
3 Giant ~ Prio~ inse~ Cing~ en       18.1       6.1       NA        5.9
# i 2 more variables: brainwt <dbl>, bodywt <dbl>
```

Filter the rows for mammals in the Perissodactyla and Primates taxonomic order. The `%in%` operator is a logical operator that returns TRUE for values of a vector that are present in a second vector.

```
filter(msleep, order %in% c("Perissodactyla", "Primates"))
```

```
# A tibble: 15 x 11
  name   genus vore  order conservation sleep_total sleep_rem sleep_cycle awake
  <chr>  <chr> <chr> <chr> <chr>       <dbl>      <dbl>      <dbl> <dbl>
1 Owl m~ Aotus omni  Prim~ <NA>        17         1.8      NA        7
2 Grivet Cerc~ omni  Prim~ lc        10         0.7      NA       14
3 Horse Equus herbi Peri~ domesticated  2.9        0.6       1      21.1
4 Donkey Equus herbi Peri~ domesticated  3.1        0.4      NA      20.9
5 Patas~ Eryt~ omni  Prim~ lc        10.9       1.1      NA      13.1
6 Galago Gala~ omni  Prim~ <NA>        9.8        1.1      0.55    14.2
7 Human Homo omni  Prim~ <NA>        8          1.9      1.5      16
8 Mongo~ Lemur herbi Prim~ vu        9.5        0.9      NA      14.5
9 Macaque Maca~ omni  Prim~ <NA>       10.1       1.2      0.75    13.9
10 Slow ~ Nyct~ carni Prim~ <NA>       11         NA      NA        13
11 Chimp~ Pan   omni  Prim~ <NA>       9.7        1.4      1.42    14.3
12 Baboon Papio omni  Prim~ <NA>       9.4        1      0.667   14.6
13 Potto Pero~ omni  Prim~ lc        11         NA      NA        13
14 Squir~ Saim~ omni  Prim~ <NA>       9.6        1.4      NA      14.4
15 Brazi~ Tapi~ herbi Peri~ vu        4.4        1      0.9      19.6
# i 2 more variables: brainwt <dbl>, bodywt <dbl>
```

You can use the boolean operators (e.g. `>`, `<`, `>=`, `<=`, `!=`, `%in%`) to create the logical tests.

12.8. “Piping” with |>

It is not unusual to want to perform a set of operations using dplyr. The pipe operator `|>` allows us to “pipe” the output from one function into the input of the next. While there is nothing special about how R treats operations that are written in a pipe, the idea of piping is to allow us to read multiple functions operating one after another from left-to-right. Without piping, one would either 1) save each step in set of functions as a temporary variable and then pass that variable along the chain or 2) have to “nest” functions, which can be hard to read.

Here’s an example we have already used:

```
head(select(msleep, name, sleep_total))
```

```
# A tibble: 6 x 2
  name           sleep_total
  <chr>          <dbl>
1 Cheetah        12.1
2 Owl monkey     17
3 Mountain beaver 14.4
4 Greater short-tailed shrew 14.9
5 Cow            4
6 Three-toed sloth 14.4
```

Now in this case, we will pipe the `msleep` data frame to the function that will select two columns (`name` and `sleep_total`) and then pipe the new data frame to the function `head()`, which will return the head of the new data frame.

```
msleep |>
  select(name, sleep_total) |>
  head()
```

```
# A tibble: 6 x 2
  name           sleep_total
  <chr>          <dbl>
1 Cheetah        12.1
2 Owl monkey     17
3 Mountain beaver 14.4
4 Greater short-tailed shrew 14.9
5 Cow            4
6 Three-toed sloth 14.4
```

12. Introduction to dplyr: mammal sleep dataset

You will soon see how useful the pipe operator is when we start to combine many functions.

Now that you know about the pipe operator (`|>`), we will use it throughout the rest of this tutorial.

12.8.1. Arrange Or Re-order Rows Using `arrange()`

To arrange (or re-order) rows by a particular column, such as the taxonomic order, list the name of the column you want to arrange the rows by:

```
msleep |> arrange(order) |> head()
```

```
# A tibble: 6 x 11
  name   genus vore  order conservation sleep_total sleep_rem sleep_cycle awake
  <chr>  <chr> <chr> <chr>        <dbl>      <dbl>      <dbl> <dbl>
1 Tenrec  Tenre~ omni  Afro~ <NA>       15.6       2.3     NA    8.4
2 Cow     Bos    herbi Arti~ domesticated  4          0.7     0.667  20
3 Roe de~ Capr~ herbi Arti~ lc         3          NA      NA    21
4 Goat    Capri  herbi Arti~ lc         5.3       0.6     NA    18.7
5 Giraffe Gira~ herbi Arti~ cd         1.9       0.4     NA    22.1
6 Sheep   Ovis   herbi Arti~ domesticated 3.8       0.6     NA    20.2
# i 2 more variables: brainwt <dbl>, bodywt <dbl>
```

Now we will select three columns from `msleep`, arrange the rows by the taxonomic order and then arrange the rows by `sleep_total`. Finally, show the head of the final data frame:

```
msleep |>
  select(name, order, sleep_total) |>
  arrange(order, sleep_total) |>
  head()
```

```
# A tibble: 6 x 3
  name   order      sleep_total
  <chr>  <chr>      <dbl>
1 Tenrec  Afrosoricida  15.6
2 Giraffe Artiodactyla  1.9
3 Roe deer Artiodactyla  3
4 Sheep   Artiodactyla  3.8
```

12. Introduction to dplyr: mammal sleep dataset

```
5 Cow      Artiodactyla      4
6 Goat     Artiodactyla    5.3
```

Same as above, except here we filter the rows for mammals that sleep for 16 or more hours, instead of showing the head of the final data frame:

```
msleep |>
  select(name, order, sleep_total) |>
  arrange(order, sleep_total) |>
  filter(sleep_total >= 16)
```

```
# A tibble: 8 x 3
  name          order    sleep_total
  <chr>        <chr>      <dbl>
1 Big brown bat Chiroptera 19.7
2 Little brown bat Chiroptera 19.9
3 Long-nosed armadillo Cingulata 17.4
4 Giant armadillo Cingulata 18.1
5 North American Opossum Didelphimorphia 18
6 Thick-tailed opossum Didelphimorphia 19.4
7 Owl monkey       Primates   17
8 Arctic ground squirrel Rodentia 16.6
```

For something slightly more complicated do the same as above, except arrange the rows in the sleep_total column in a descending order. For this, use the function `desc()`

```
msleep |>
  select(name, order, sleep_total) |>
  arrange(order, desc(sleep_total)) |>
  filter(sleep_total >= 16)
```

```
# A tibble: 8 x 3
  name          order    sleep_total
  <chr>        <chr>      <dbl>
1 Little brown bat Chiroptera 19.9
2 Big brown bat Chiroptera 19.7
3 Giant armadillo Cingulata 18.1
4 Long-nosed armadillo Cingulata 17.4
5 Thick-tailed opossum Didelphimorphia 19.4
```

12. Introduction to dplyr: mammal sleep dataset

6	North American Opossum	Didelphimorphia	18
7	Owl monkey	Primates	17
8	Arctic ground squirrel	Rodentia	16.6

12.9. Create New Columns Using `mutate()`

The `mutate()` function will add new columns to the data frame. Create a new column called `rem_proportion`, which is the ratio of rem sleep to total amount of sleep.

```
msleep |>
  mutate(rem_proportion = sleep_rem / sleep_total) |>
  head()
```

```
# A tibble: 6 x 12
  name    genus vore  order conservation sleep_total sleep_rem sleep_cycle awake
  <chr>   <chr> <chr> <chr>           <dbl>      <dbl>      <dbl> <dbl>
1 Cheetah Acin~ carni Carn~ lc            12.1       NA        NA     11.9
2 Owl mo~ Aotus omni Prim~ <NA>          17          1.8       NA      7
3 Mounta~ Aplo~ herbi Rode~ nt            14.4       2.4       NA     9.6
4 Greate~ Blar~ omni Sori~ lc            14.9       2.3      0.133    9.1
5 Cow      Bos    herbi Arti~ domesticated 4          0.7      0.667   20
6 Three~~ Brad~ herbi Pilo~ <NA>          14.4       2.2      0.767   9.6
# i 3 more variables: brainwt <dbl>, bodywt <dbl>, rem_proportion <dbl>
```

You can add many new columns using `mutate` (separated by commas). Here we add a second column called `bodywt_grams` which is the `bodywt` column in grams.

```
msleep |>
  mutate(rem_proportion = sleep_rem / sleep_total,
        bodywt_grams = bodywt * 1000) |>
  head()
```

```
# A tibble: 6 x 13
  name    genus vore  order conservation sleep_total sleep_rem sleep_cycle awake
  <chr>   <chr> <chr> <chr>           <dbl>      <dbl>      <dbl> <dbl>
1 Cheetah Acin~ carni Carn~ lc            12.1       NA        NA     11.9
2 Owl mo~ Aotus omni Prim~ <NA>          17          1.8       NA      7
3 Mounta~ Aplo~ herbi Rode~ nt            14.4       2.4       NA     9.6
```

12. Introduction to dplyr: mammal sleep dataset

```
4 Greate~ Blar~ omni  Sori~ lc          14.9      2.3      0.133    9.1
5 Cow       Bos     herbi Arti~ domesticated   4         0.7      0.667    20
6 Three~~ Brad~ herbi Pilo~ <NA>        14.4      2.2      0.767    9.6
# i 4 more variables: brainwt <dbl>, bodywt <dbl>, rem_proportion <dbl>,
#   bodywt_grams <dbl>
```

Is there a relationship between `rem_proportion` and `bodywt`? How about `sleep_total`?

12.9.1. Create summaries: `summarise()`

The `summarise()` function will create summary statistics for a given column in the data frame such as finding the mean. For example, to compute the average number of hours of sleep, apply the `mean()` function to the column `sleep_total` and call the summary value `avg_sleep`.

```
msleep |>
  summarise(avg_sleep = mean(sleep_total))
```

```
# A tibble: 1 x 1
  avg_sleep
  <dbl>
1     10.4
```

There are many other summary statistics you could consider such `sd()`, `min()`, `max()`, `median()`, `sum()`, `n()` (returns the length of vector), `first()` (returns first value in vector), `last()` (returns last value in vector) and `n_distinct()` (number of distinct values in vector).

```
msleep |>
  summarise(avg_sleep = mean(sleep_total),
            min_sleep = min(sleep_total),
            max_sleep = max(sleep_total),
            total = n())
```

```
# A tibble: 1 x 4
  avg_sleep min_sleep max_sleep total
  <dbl>      <dbl>      <dbl> <int>
1     10.4      1.9      19.9     83
```

12.10. Grouping data: group_by()

The `group_by()` verb is an important function in dplyr. The `group_by` allows us to use the concept of “split-apply-combine”. We literally want to split the data frame by some variable (e.g. taxonomic order), apply a function to the individual data frames and then combine the output. This approach is similar to the `aggregate` function from R, but `group_by` integrates with dplyr.

Let’s do that: split the `msleep` data frame by the taxonomic order, then ask for the same summary statistics as above. We expect a set of summary statistics for each taxonomic order.

```
msleep |>
  group_by(order) |>
  summarise(avg_sleep = mean(sleep_total),
            min_sleep = min(sleep_total),
            max_sleep = max(sleep_total),
            total = n())

# A tibble: 19 x 5
# ... with 5 variables:
#   order      avg_sleep  min_sleep  max_sleep total
#   <chr>        <dbl>       <dbl>       <dbl>    <int>
# 1 Afrosoricida     15.6       15.6       15.6     1
# 2 Artiodactyla      4.52       1.9        9.1      6
# 3 Carnivora        10.1       3.5        15.8     12
# 4 Cetacea           4.5        2.7        5.6      3
# 5 Chiroptera        19.8       19.7       19.9     2
# 6 Cingulata          17.8       17.4       18.1     2
# 7 Didelphimorphia    18.7       18         19.4     2
# 8 Diprotodontia      12.4       11.1       13.7     2
# 9 Erinaceomorpha     10.2       10.1       10.3     2
# 10 Hyracoidea        5.67       5.3        6.3      3
# 11 Lagomorpha         8.4        8.4        8.4      1
# 12 Monotremata       8.6        8.6        8.6      1
# 13 Perissodactyla     3.47       2.9        4.4      3
# 14 Pilosa             14.4       14.4       14.4     1
# 15 Primates            10.5       8          17      12
# 16 Proboscidea         3.6        3.3        3.9      2
# 17 Rodentia            12.5       7          16.6     22
# 18 Scandentia          8.9        8.9        8.9      1
# 19 Soricomorpha        11.1       8.4       14.9      5
```

13. Case Study: Behavioral Risk Factor Surveillance System

13.1. A Case Study on the Behavioral Risk Factor Surveillance System

The Behavioral Risk Factor Surveillance System (BRFSS) is a large-scale health survey conducted annually by the Centers for Disease Control and Prevention (CDC) in the United States. The BRFSS collects information on various health-related behaviors, chronic health conditions, and the use of preventive services among the adult population (18 years and older) through telephone interviews. The main goal of the BRFSS is to identify and monitor the prevalence of risk factors associated with chronic diseases, inform public health policies, and evaluate the effectiveness of health promotion and disease prevention programs. The data collected through BRFSS is crucial for understanding the health status and needs of the population, and it serves as a valuable resource for researchers, policy makers, and healthcare professionals in making informed decisions and designing targeted interventions.

In this chapter, we will walk through an exploratory data analysis (EDA) of the Behavioral Risk Factor Surveillance System dataset using R. EDA is an important step in the data analysis process, as it helps you to understand your data, identify trends, and detect any anomalies before performing more advanced analyses. We will use various R functions and packages to explore the dataset, with a focus on active learning and hands-on experience.

13.2. Loading the Dataset

First, let's load the dataset into R. We will use the `read.csv()` function from the base R package to read the data and store it in a data frame called `brfss`. Make sure the CSV file is in your working directory, or provide the full path to the file.

First, we need to get the data. Either download the data from [THIS LINK](#) or have R do it directly from the command-line (preferred):

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```
download.file('https://raw.githubusercontent.com/seandavi/ITR/master/BRFSS-subset.csv',
              destfile = 'BRFSS-subset.csv')

path <- file.choose()      # look for BRFSS-subset.csv

stopifnot(file.exists(path))
brfss <- read.csv(path)
```

13.3. Inspecting the Data

Once the data is loaded, let's take a look at the first few rows of the dataset using the `head()` function:

```
head(brfss)
```

	Age	Weight	Sex	Height	Year
1	31	48.98798	Female	157.48	1990
2	57	81.64663	Female	157.48	1990
3	43	80.28585	Male	177.80	1990
4	72	70.30682	Male	170.18	1990
5	31	49.89516	Female	154.94	1990
6	58	54.43108	Female	154.94	1990

This will display the first six rows of the dataset, allowing you to get a feel for the data structure and variable types.

Next, let's check the dimensions of the dataset using the `dim()` function:

```
dim(brfss)
```

```
[1] 20000      5
```

This will return the number of rows and columns in the dataset, which is important to know for subsequent analyses.

13.4. Summary Statistics

Now that we have a basic understanding of the data structure, let's calculate some summary statistics. The `summary()` function in R provides a quick overview of the main statistics for each variable in the dataset:

```
summary(brfss)
```

```
Age           Weight          Sex            Height
Min.    :18.00   Min.    : 34.93   Length:20000   Min.    :105.0
1st Qu.:36.00   1st Qu.: 61.69   Class  :character 1st Qu.:162.6
Median  :51.00   Median  : 72.57   Mode   :character Median  :168.0
Mean    :50.99   Mean    : 75.42
3rd Qu.:65.00   3rd Qu.: 86.18
Max.    :99.00   Max.    :278.96
NA's    :139     NA's    :649      NA's   :184
Year
Min.    :1990
1st Qu.:1990
Median  :2000
Mean    :2000
3rd Qu.:2010
Max.    :2010
```

This will display the minimum, first quartile, median, mean, third quartile, and maximum for each numeric variable, and the frequency counts for each factor level for categorical variables.

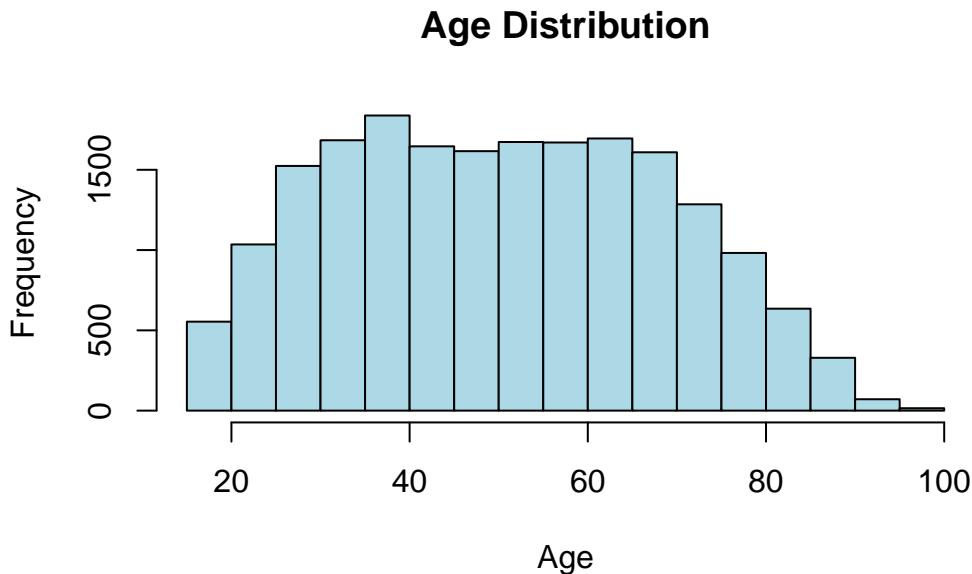
13.5. Data Visualization

Visualizing the data can help you identify patterns and trends in the dataset. Let's start by creating a histogram of the Age variable using the `hist()` function.

This will create a histogram showing the frequency distribution of ages in the dataset. You can customize the appearance of the histogram by adjusting the parameters within the `hist()` function.

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```
hist(brfss$Age, main = "Age Distribution",
     xlab = "Age", col = "lightblue")
```



💡 What are the options for a histogram?

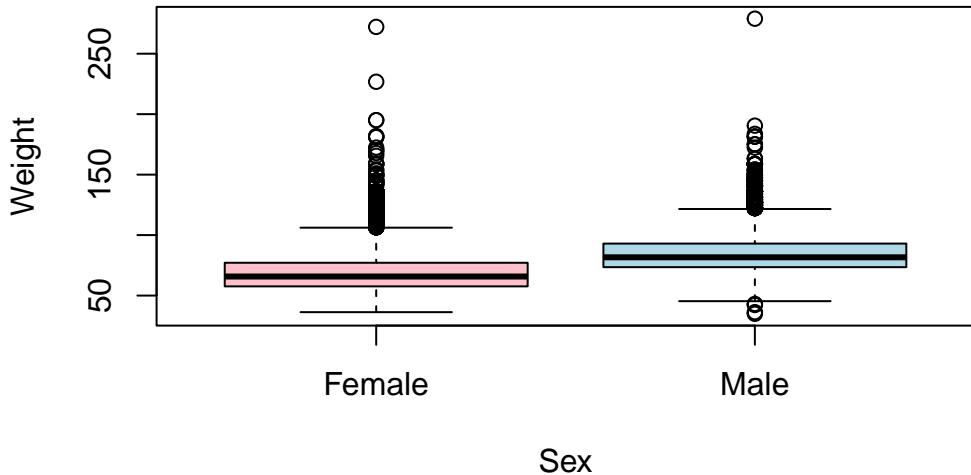
The `hist()` function has many options. For example, you can change the number of bins, the color of the bars, the title, and the x-axis label. You can also add a vertical line at the mean or median, or add a normal curve to the histogram. For more information, type `?hist` in the R console.

More generally, it is important to understand the options available for each function you use. You can do this by reading the documentation for the function, which can be accessed by typing `?function_name` or `help("function_name")` in the R console.

Next, let's create a boxplot to compare the distribution of Weight between males and females. We will use the `boxplot()` function for this. This will create a boxplot comparing the weight distribution between males and females. You can customize the appearance of the boxplot by adjusting the parameters within the `boxplot()` function.

```
boxplot(brfss$Weight ~ brfss$Sex, main = "Weight Distribution by Sex",
        xlab = "Sex", ylab = "Weight", col = c("pink", "lightblue"))
```

Weight Distribution by Sex



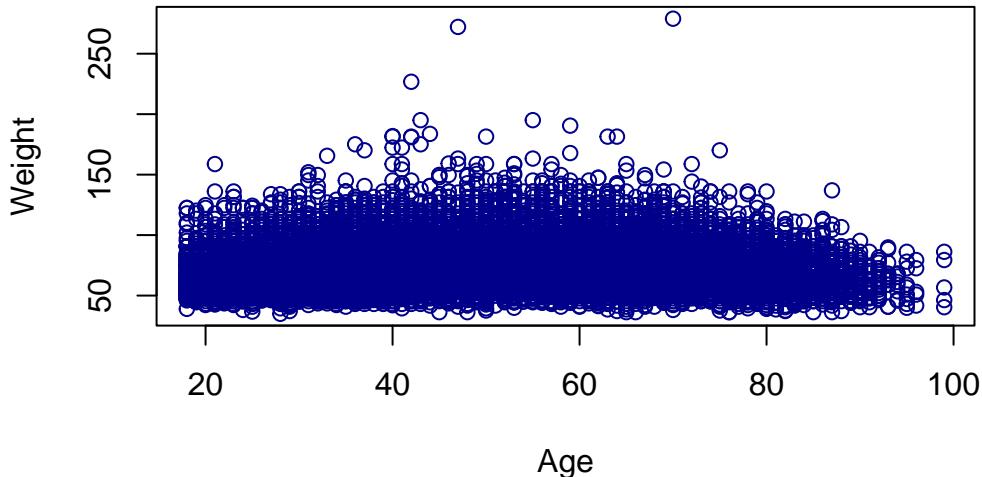
13.6. Analyzing Relationships Between Variables

To further explore the data, let's investigate the relationship between age and weight using a scatterplot. We will use the `plot()` function for this:

This will create a scatterplot of age and weight, allowing you to visually assess the relationship between these two variables.

```
plot(brfss$Age, brfss$Weight, main = "Scatterplot of Age and Weight",
     xlab = "Age", ylab = "Weight", col = "darkblue")
```

Scatterplot of Age and Weight



To quantify the strength of the relationship between age and weight, we can calculate the correlation coefficient using the `cor()` function:

This will return the correlation coefficient between age and weight, which can help you determine whether there is a linear relationship between these variables.

```
cor(brfss$Age, brfss$Weight)
```

```
[1] NA
```

Why does `cor()` give a value of NA? What can we do about it? A quick glance at `help("cor")` will give you the answer.

```
cor(brfss$Age, brfss$Weight, use = "complete.obs")
```

```
[1] 0.02699989
```

13.7. Exercises

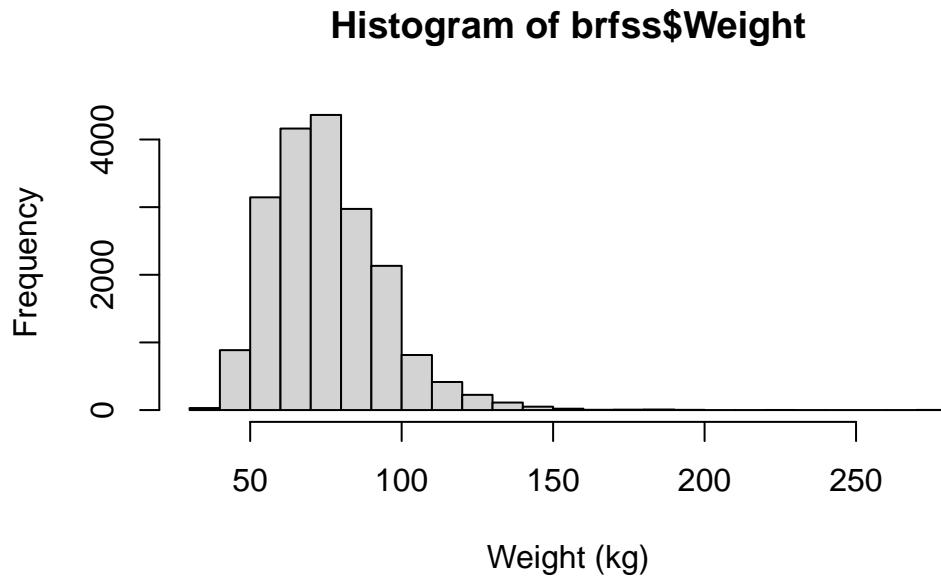
1. What is the mean weight in this dataset? How about the median? What is the difference between the two? What does this tell you about the distribution of weights in the dataset?

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```
mean(brfss$Weight, na.rm = TRUE)  
[1] 75.42455  
  
median(brfss$Weight, na.rm = TRUE)  
[1] 72.57478  
  
mean(brfss$Weight, na.rm=TRUE) - median(brfss$Weight, na.rm = TRUE)  
[1] 2.849774
```

- Given the findings about the `mean` and `median` in the previous exercise, use the `hist()` function to create a histogram of the weight distribution in this dataset. How would you describe the shape of this distribution?

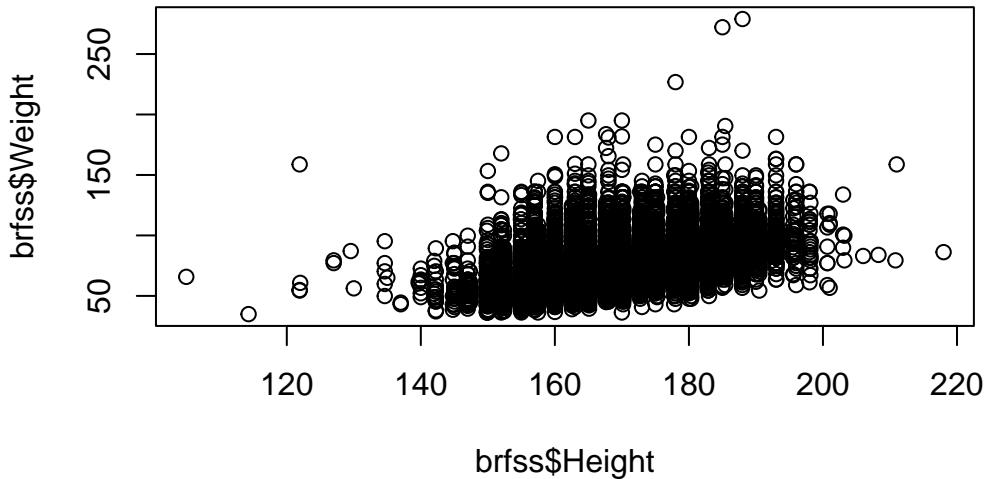
```
hist(brfss$Weight, xlab="Weight (kg)", breaks = 30)
```



- Use `plot()` to examine the relationship between height and weight in this dataset.

```
plot(brfss$Height, brfss$Weight)
```

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4. What is the correlation between height and weight? What does this tell you about the relationship between these two variables?

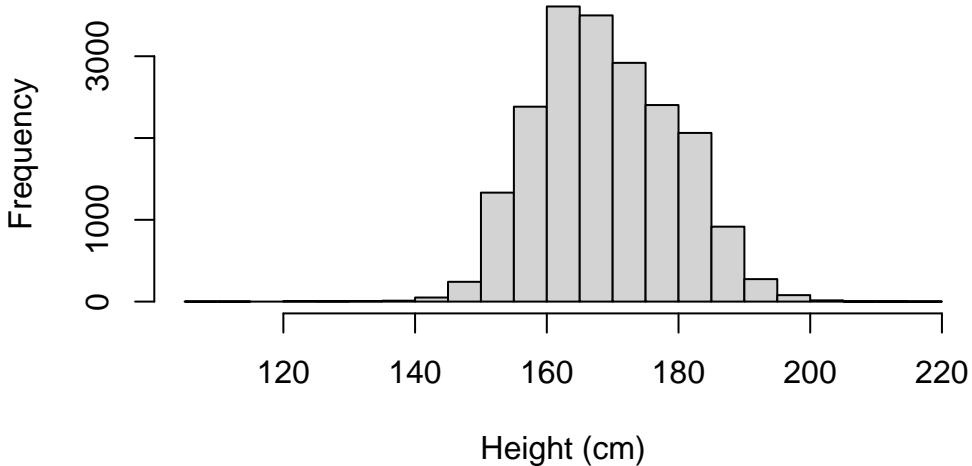
```
cor(brfss$Height, brfss$Weight, use = "complete.obs")
```

[1] 0.5140928

5. Create a histogram of the height distribution in this dataset. How would you describe the shape of this distribution?

```
hist(brfss$Height, xlab="Height (cm)", breaks = 30)
```

Histogram of brfss\$Height



13.8. Conclusion

In this chapter, we have demonstrated how to perform an exploratory data analysis on the Behavioral Risk Factor Surveillance System dataset using R. We covered data loading, inspection, summary statistics, visualization, and the analysis of relationships between variables. By actively engaging with the R code and data, you have gained valuable experience in using R for EDA and are well-equipped to tackle more complex analyses in your future work.

Remember that EDA is just the beginning of the data analysis process, and further statistical modeling and hypothesis testing will likely be necessary to draw meaningful conclusions from your data. However, EDA is a crucial step in understanding your data and informing your subsequent analyses.

13.9. Learn about the data

Using the data exploration techniques you have seen to explore the brfss dataset.

- `summary()`
- `dim()`
- `colnames()`
- `head()`
- `tail()`
- `class()`
- `View()`

You may want to investigate individual columns visually using plotting like `hist()`. For categorical data, consider using something like `table()`.

13.10. Clean data

R read `Year` as an integer value, but it's really a `factor`

```
brfss$Year <- factor(brfss$Year)
```

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13.11. Weight in 1990 vs. 2010 Females

- Create a subset of the data

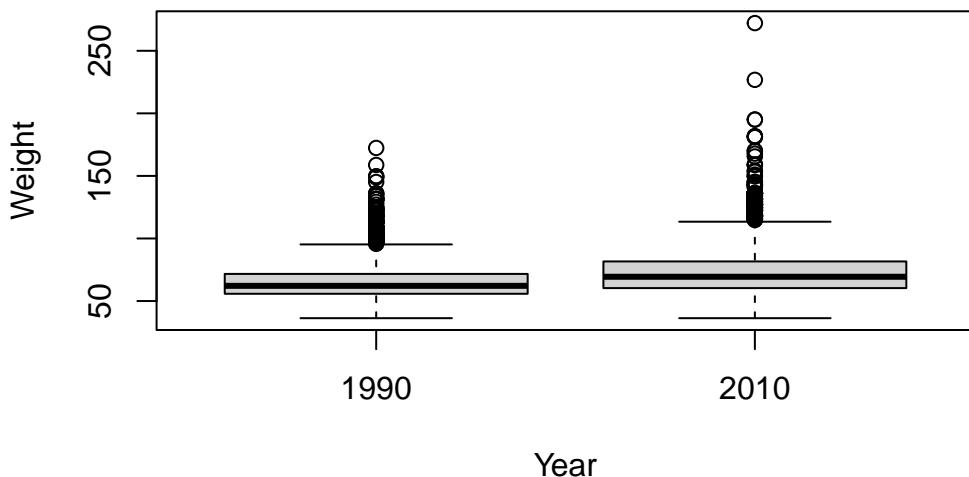
```
brfssFemale <- brfss[brfss$Sex == "Female",]  
summary(brfssFemale)
```

Age	Weight	Sex	Height
Min. :18.00	Min. : 36.29	Length:12039	Min. :105.0
1st Qu.:37.00	1st Qu.: 57.61	Class :character	1st Qu.:157.5
Median :52.00	Median : 65.77	Mode :character	Median :163.0
Mean :51.92	Mean : 69.05		Mean :163.3
3rd Qu.:67.00	3rd Qu.: 77.11		3rd Qu.:168.0
Max. :99.00	Max. :272.16		Max. :200.7
NA's :103	NA's :560		NA's :140

Year
1990:5718
2010:6321

- Visualize

```
plot(Weight ~ Year, brfssFemale)
```



13. Case Study: Behavioral Risk Factor Surveillance System

- Statistical test

```
t.test(Weight ~ Year, brfssFemale)
```

Welch Two Sample t-test

```
data: Weight by Year
t = -27.133, df = 11079, p-value < 2.2e-16
alternative hypothesis: true difference in means between group 1990 and group 2010 is not equal to 0
95 percent confidence interval:
-8.723607 -7.548102
sample estimates:
mean in group 1990 mean in group 2010
64.81838          72.95424
```

13.12. Weight and height in 2010 Males

- Create a subset of the data

```
brfss2010Male <- subset(brfss, Year == 2010 & Sex == "Male")
summary(brfss2010Male)
```

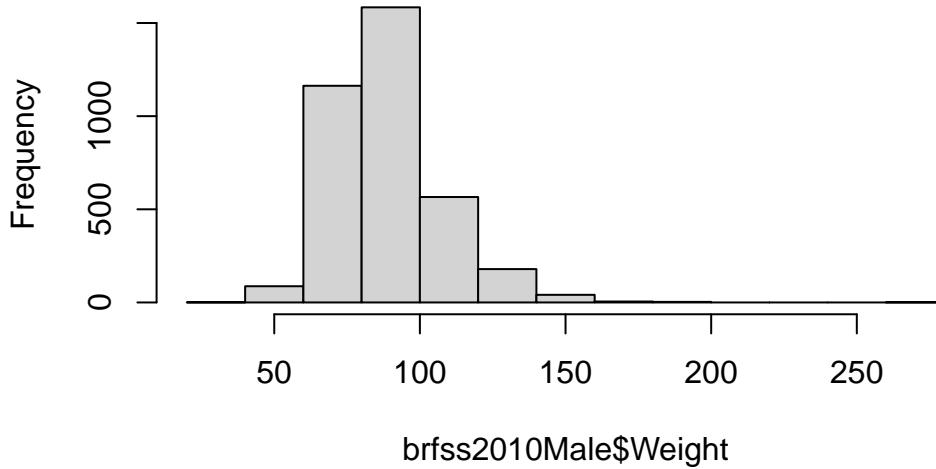
Age	Weight	Sex	Height	Year
Min. :18.00	Min. : 36.29	Length:3679	Min. :135	1990: 0
1st Qu.:45.00	1st Qu.: 77.11	Class :character	1st Qu.:173	2010:3679
Median :57.00	Median : 86.18	Mode :character	Median :178	
Mean :56.25	Mean : 88.85		Mean :178	
3rd Qu.:68.00	3rd Qu.: 99.79		3rd Qu.:183	
Max. :99.00	Max. :278.96		Max. :218	
NA's :30	NA's :49		NA's :31	

- Visualize the relationship

```
hist(brfss2010Male$Weight)
```

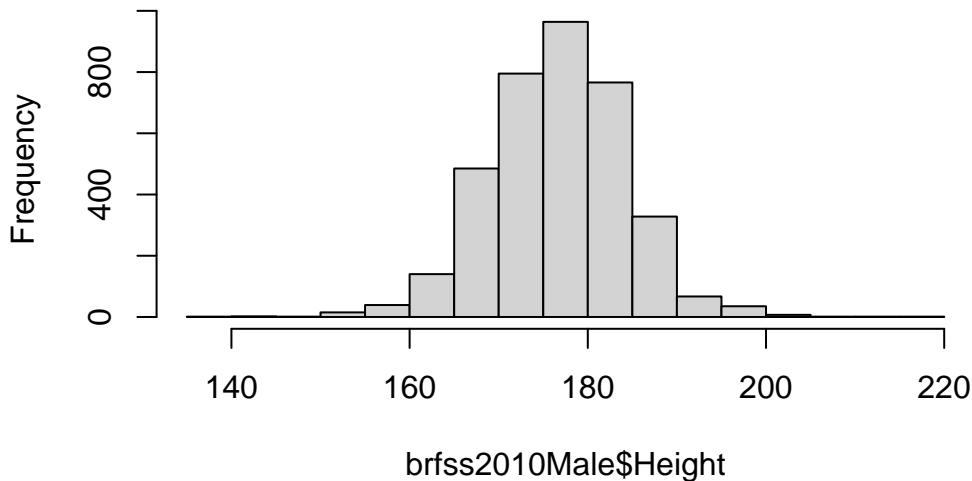
13. Case Study: Behavioral Risk Factor Surveillance System

Histogram of brfss2010Male\$Weight



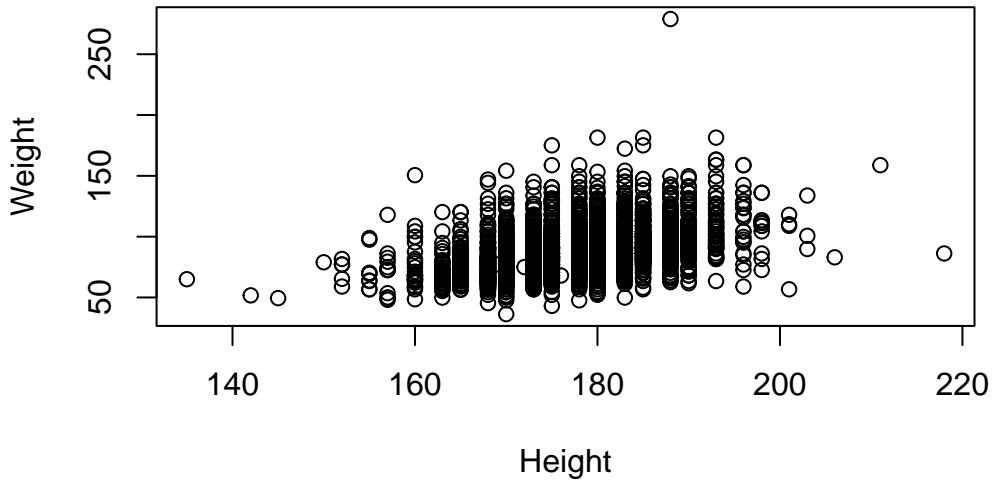
```
hist(brfss2010Male$Height)
```

Histogram of brfss2010Male\$Height



```
plot(Weight ~ Height, brfss2010Male)
```

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- Fit a linear model (regression)

```
fit <- lm(Weight ~ Height, brfss2010Male)
fit
```

```
Call:
lm(formula = Weight ~ Height, data = brfss2010Male)
```

```
Coefficients:
```

(Intercept)	Height
-86.8747	0.9873

Summarize as ANOVA table

```
anova(fit)
```

Analysis of Variance Table

Response: Weight

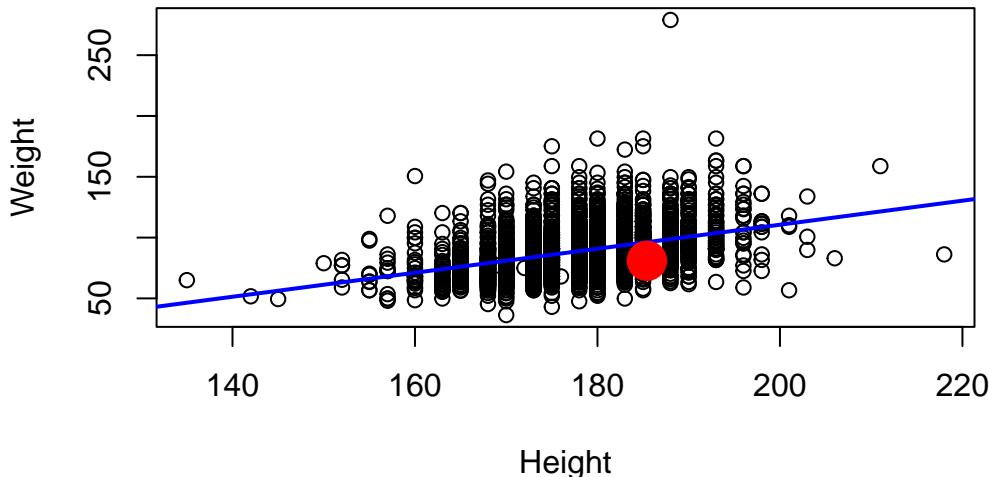
Df	Sum Sq	Mean Sq	F value	Pr(>F)
Height	1	197664	197664	693.8 < 2.2e-16 ***
Residuals	3617	1030484	285	

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

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- Plot points, superpose fitted regression line; where am I?

```
plot(Weight ~ Height, brfss2010Male)
abline(fit, col="blue", lwd=2)
# Substitute your own weight and height...
points(73 * 2.54, 178 / 2.2, col="red", cex=4, pch=20)
```



- Class and available ‘methods’

```
class(fit)          # 'noun'
methods(class=class(fit)) # 'verb'
```

- Diagnostics

```
plot(fit)
# Note that the "plot" above does not have a ".lm"
# However, R will use "plot.lm". Why?
?plot.lm
```

14. Self-Guided Data Visualization in R

Data visualization is a critical skill in the data scientist’s toolkit. It’s the bridge between raw data and human understanding. Effective visualizations can reveal patterns, trends, and outliers that might be missed in a table of numbers. In the R programming language, the `ggplot2` package stands as the gold standard for creating beautiful, flexible, and powerful graphics.

This document will guide you through the principles of effective data visualization and show you how to apply them using `ggplot2`. We’ll cover best practices, common plot types, and the “grammar of graphics” methodology that makes `ggplot2` so intuitive.

Before diving in, though, there are some truly amazing online resources that showcase what can be done with R graphics and also stimulate your imagination. Two of the best are:

- [The R Graph Gallery](#): A comprehensive collection of R graphics examples, covering a wide range of plot types and customization options.
- [From Data to Viz](#): A guide that helps you choose the right type of visualization for your data and provides examples in R.

After walking through this document, go back to these resources and explore the examples. You’ll see how the principles we discuss here are applied in real-world scenarios, and you’ll gain inspiration for your own visualizations.

14.1. Getting Started with ggplot2

To get started, we need to load the `ggplot2` package, which is part of the `tidyverse`.

```
# Load the necessary R packages for data visualization
library(ggplot2)
library(dplyr)
```

14.2. Core Principles of Effective Data Visualization

Before we start plotting, it's essential to understand what makes a visualization effective. Two key principles are maximizing the data-ink ratio and using clear labels.

14.2.1. The “Least Ink” Principle

Coined by the statistician Edward Tufte, the **data-ink ratio** is the proportion of a graphic's ink devoted to the non-redundant display of data information. The goal is to maximize this ratio. In simpler terms, **every single pixel should have a reason to be there**.

Avoid chart junk like:

- Redundant grid lines
- Unnecessary backgrounds or colors
- 3D effects on 2D plots
- Shadows and other decorative elements

Let's look at an example. The first plot has a lot of “chart junk,” while the second one is cleaner and focuses on the data.

```
# Using the built-in 'mpg' dataset
ggplot(mpg, aes(x = displ, y = hwy, color = class)) +
  geom_point() +
  theme_gray() + # A theme with a lot of non-data ink
  labs(title = "Fuel Efficiency vs. Engine Displacement",
       subtitle = "This is a very busy plot",
       x = "Engine Displacement (Liters)",
       y = "Highway Miles per Gallon",
       color = "Vehicle Class")
```

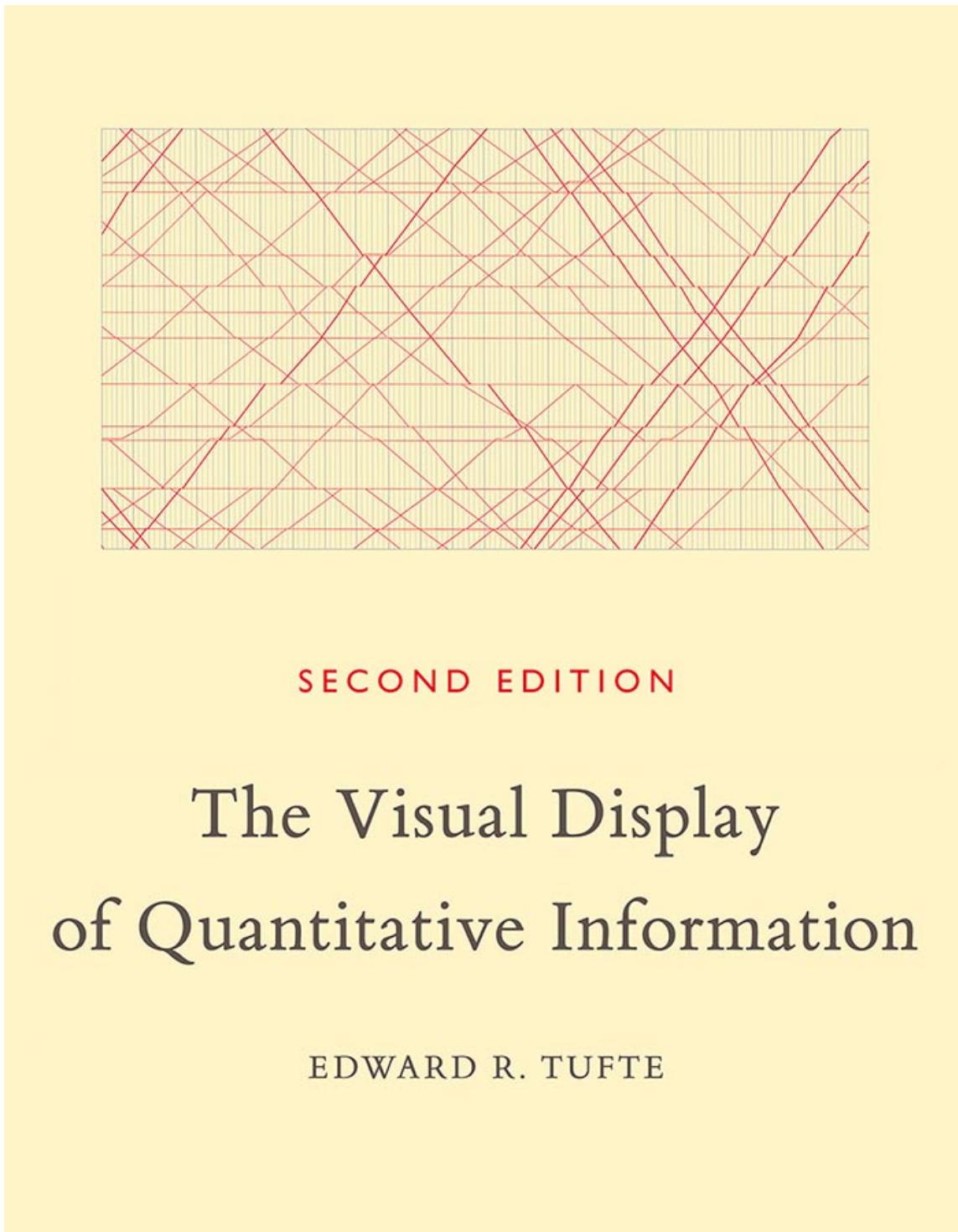


Figure 14.1.: Edward Tufte's landmark book, "The Visual Display of Quantitative Information," emphasizes the importance of maximizing the data-ink ratio.

Fuel Efficiency vs. Engine Displacement

This is a very busy plot

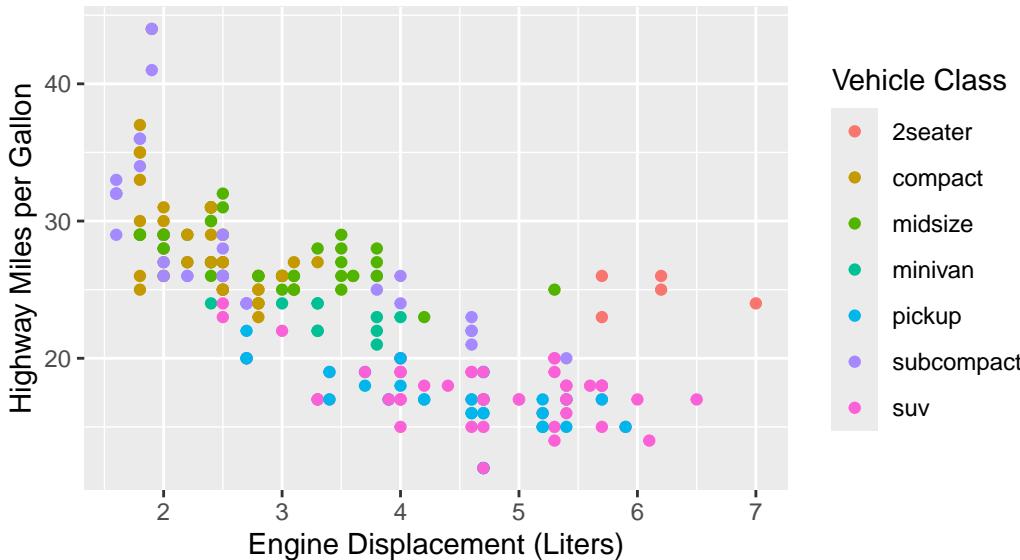


Figure 14.2.: A cluttered plot with low data-ink ratio. The gray background, heavy grid-lines, and legend title are all unnecessary.

Here's a cleaner version of the same plot that follows the “least ink” principle. Notice how it removes unnecessary elements while still conveying the same information.

```
ggplot(mpg, aes(x = displ, y = hwy, color = class)) +
  geom_point() +
  theme_minimal() # A cleaner theme
  labs(title = "Fuel Efficiency vs. Engine Displacement",
       x = "Engine Displacement (Liters)",
       y = "Highway Miles per Gallon",
       color = "Class") # Simpler legend title
```

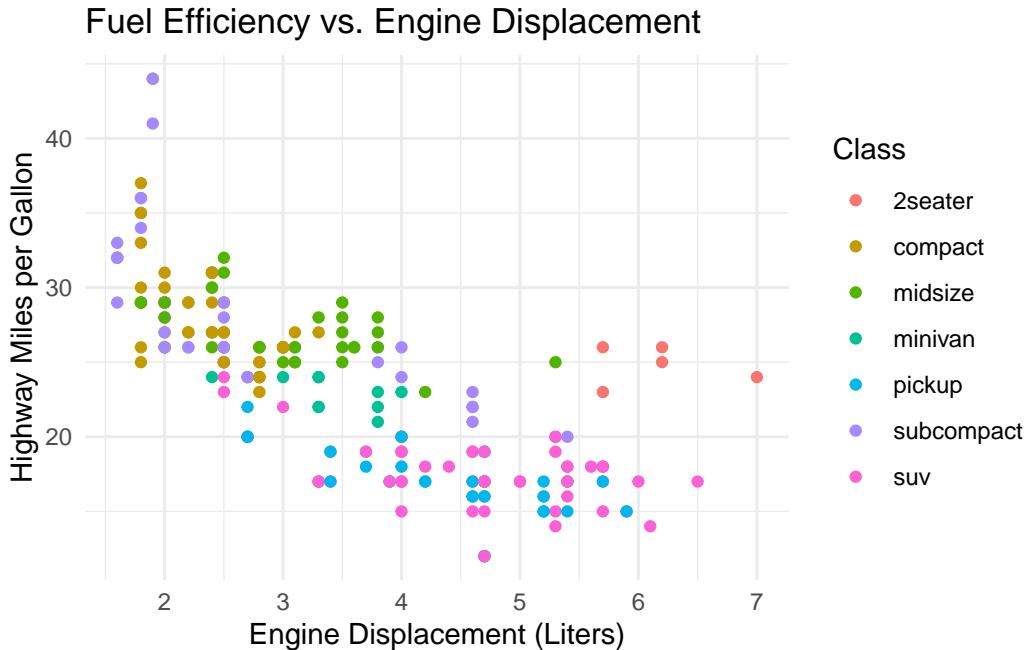


Figure 14.3.: A clean, minimalist plot that follows the ‘least ink’ principle. The focus is entirely on the relationship between the data points.

While this is a subjective topic, the goal is to make your plots as clear and informative as possible. The “least ink” principle is a guideline, not a rule, but it can help you create more effective visualizations.

14.2.2. The Importance of Clear Labeling

A plot without labels is just a picture. To be a useful piece of analysis, it needs to communicate context. Always ensure your plots have:

- A clear and descriptive title.
- Labeled axes with units (*e.g.*, “Temperature (°C”).
- An informative legend if you’re using color, shape, or size to encode data.

14.2.3. Color and Contrast

Color is a powerful tool in data visualization, but it can also be misused. R provides several built-in color palettes, and you can also use packages like `RColorBrewer` for more options.

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Think in terms of colorblind-friendly palettes, and avoid using too many colors in a single plot.

Color palettes can be roughly categorized into:

- Sequential palettes (first list of colors), which are suited to ordered data that progress from low to high (gradient).
- Qualitative palettes (second list of colors), which are best suited to represent nominal or categorical data. They do not imply magnitude differences between groups.
- Diverging palettes (third list of colors), which put equal emphasis on mid-range critical values and extremes at both ends of the data range.

```
library(RColorBrewer)  
display.brewer.all()
```

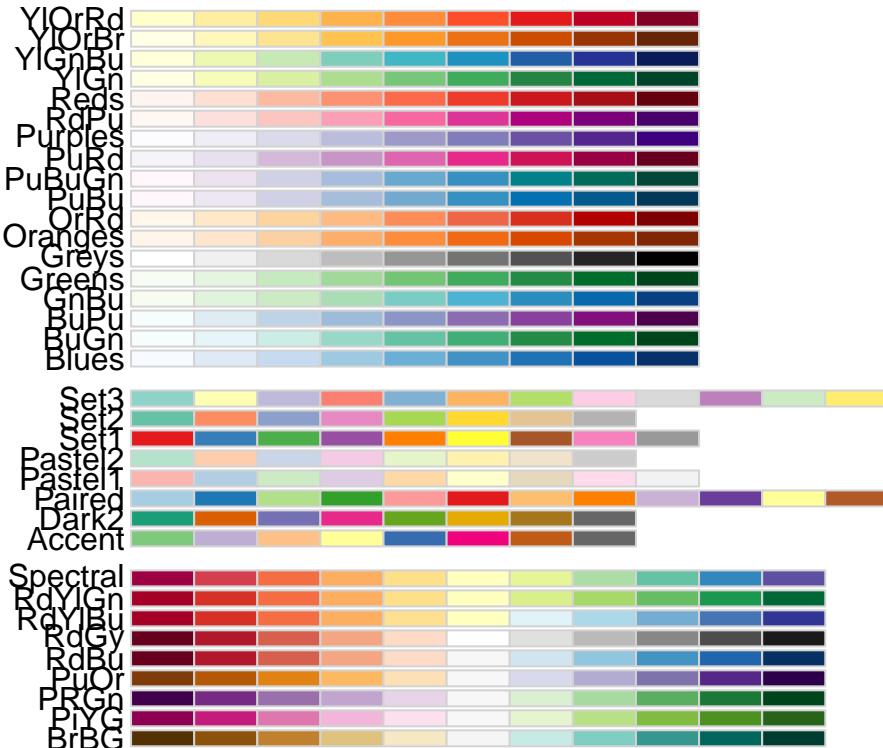


Figure 14.4.: Examples of color palettes in R. The first row shows sequential palettes, the second row shows qualitative palettes, and the third row shows diverging palettes.

14. Self-Guided Data Visualization in R

It is also important to consider colorblindness when choosing colors for your plots. The most common types of color blindness are red-green and blue-yellow. You can use tools like the `colorspace` package to check how your plots will look to people with different types of color vision deficiencies.

```
display.brewer.all(colorblindFriendly=TRUE)
```

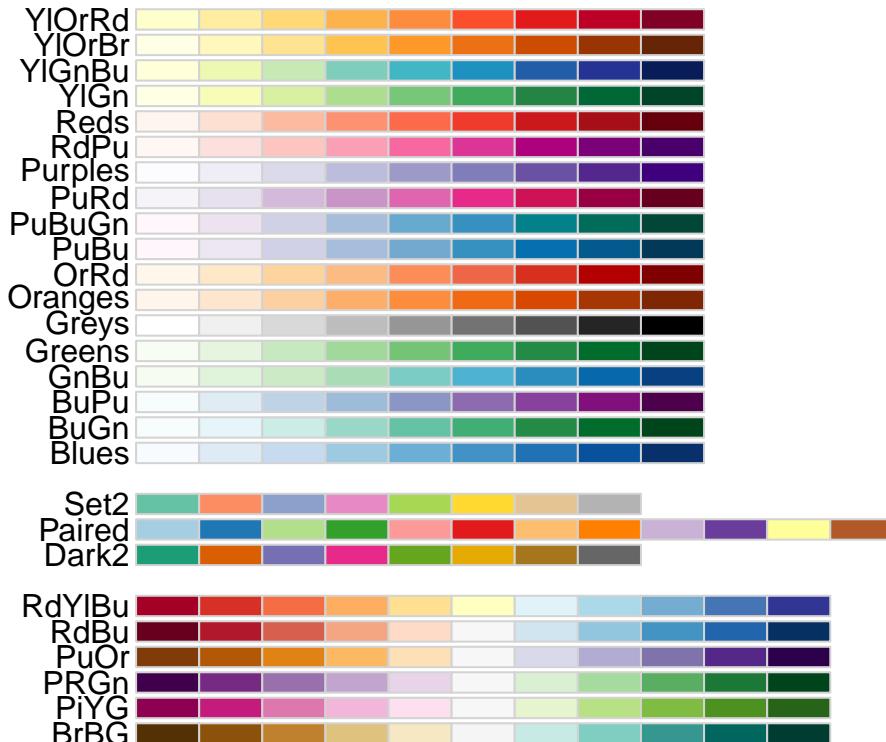


Figure 14.5.: A colorblind-friendly palette from the ‘colorspace’ package. This palette is designed to be distinguishable for people with various types of color vision deficiencies.

14.3. Introduction to `ggplot2`: The Grammar of Graphics

Rather than reproducing excellent online resources, for this section, pick any or all of the following resources to learn about the grammar of graphics and how to use `ggplot2`:

- [R for Data Science: Data Visualization](#)
- [ggplot2 documentation](#)

- Modern Data Visualization with R

14.4. Sets and Intersections: UpSet Plots

When dealing with multiple sets, visualizing their intersections can be challenging. Traditional Venn diagrams become cluttered and hard to read with more than three sets. An **UpSet plot** is a powerful alternative for visualizing the intersections of multiple sets. It consists of two main parts: a matrix that shows which sets are part of an intersection, and a bar chart that shows the size of each intersection. This makes it far more scalable and easier to interpret than a complex Venn diagram.

To create an UpSet plot, we use the `UpSetR` package. It takes a specific input format where 0s and 1s indicate the absence or presence of an element in a set.

```
# install.packages("UpSetR")
library(UpSetR)
movies <- read.csv(system.file("extdata", "movies.csv", package = "UpSetR"),
  header = T, sep = ";")

# Use the 'movies' dataset that comes with UpSetR
# This dataset is already in the correct binary format
upset(movies,
  nsets = 5, # Show the 5 most frequent genres
  order.by = "freq",
  mainbar.y.label = "Intersection Size",
  sets.x.label = "Total Movies in Genre")
```

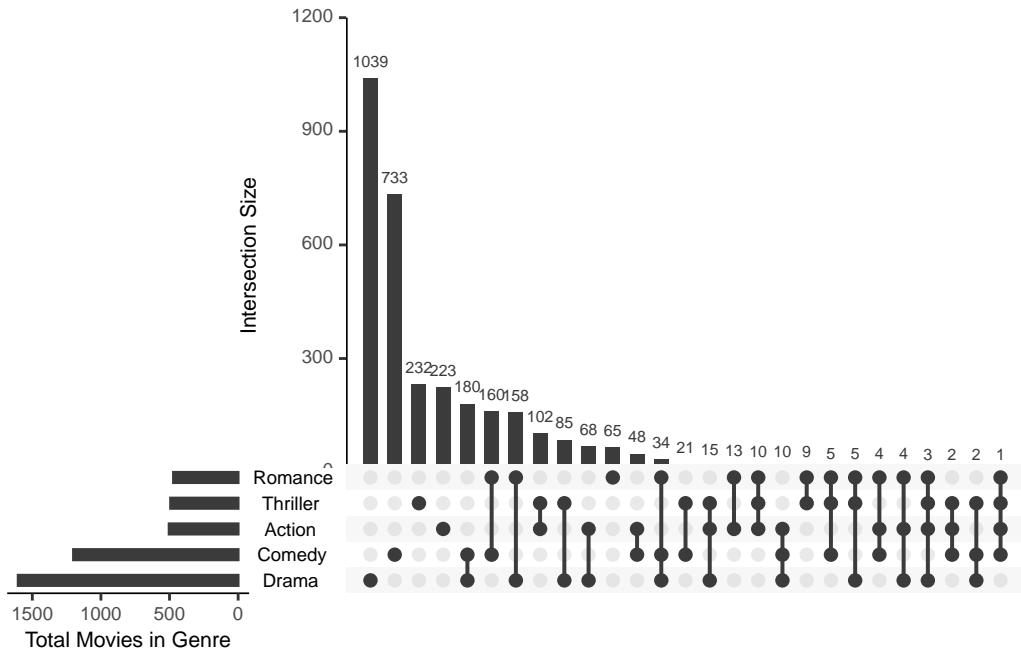


Figure 14.6.: An UpSet plot visualizing movie genres. The main bar chart shows the size of intersections (e.g., how many movies are both ‘Comedy’ and ‘Romance’). The bottom-left matrix indicates which genres are part of each intersection. This is much clearer than a 5-set Venn diagram.

The UpSet plot clearly shows us, for instance, the number of movies that are exclusively “Drama” versus those that are a combination of “Drama,” “Comedy,” and “Romance.” This level of detail is difficult to achieve with a Venn diagram.

14.5. Complex Heatmaps

Heatmaps are a powerful way to visualize complex data matrices, especially when dealing with large datasets. They allow you to see patterns and relationships in the data at a glance.

What is a heatmap? It’s a graphical representation of data where individual values are represented as colors. The color intensity indicates the magnitude of the value, making it easy to spot trends and outliers. The underlying data is typically a matrix of numbers.

i Note

A matrix is a two-dimensional array of numbers, where each element is identified by its row and column indices. Matrices can include only ONE data type.

There are many ways to create heatmaps in R including the base R `heatmap()` function, the `ggplot2` package, and specialized packages like `ComplexHeatmap`.

Feel free to explore the following resources for some of the most popular heatmap packages in R:

- [ggplot2 Heatmaps](#) allows you to create basic heatmaps using the `geom_tile()` function. This is a good starting point for simple heatmaps.
- [The heatmap\(\) function](#) in base R is a simple way to create heatmaps. It automatically scales the data and provides options for clustering rows and columns.
- [The pheatmap package](#) is a popular package for creating heatmaps with more customization options. It allows you to add annotations, customize colors, and control clustering.
- [Complex Heatmaps](#) is a powerful R package for creating complex heatmaps. It allows you to visualize data matrices with multiple annotations, making it ideal for genomic data analysis.
- [Interactive Complex Heatmaps](#) is an extension of the Complex Heatmaps package that allows you to create interactive heatmaps. This can be useful for exploring large datasets and identifying patterns.

14.6. Genome and Genomic Data Visualization

The [Gviz package](#) is a powerful tool for visualizing genomic data in R. It allows you to create publication-quality plots of genomic features, such as gene annotations, sequence alignments, and expression data.

The [GenomicDistributions package](#) is another useful package for visualizing genomic data. It provides functions for creating distribution plots of genomic features, such as coverage, chip-seq or atac-seq distributions relative to genomic features, etc.

14.7. Conclusion

This document has provided a comprehensive foundation for creating effective data visualizations in R with `ggplot2`. We've covered the core principles of good design, explored

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a wide range of common plot types including heatmaps, and seen how `ggplot2`'s layered grammar allows for the creation of complex, insightful graphics by mapping multiple data dimensions to aesthetics. We also discussed why certain plots like Venn diagrams can be problematic and introduced powerful alternatives like UpSet plots.

The key to mastering data visualization is practice. Experiment with different datasets, try new `geoms`, and always think critically about the story your plot is telling and the best way to tell it.

Part IV.

statistics

15. Working with distribution functions

Which values do pnorm, dnorm, qnorm, and rnorm return? How do I remember the difference between these?

I find it helpful to have visual representations of distributions as pictures. It is difficult for me to think of distributions, or differences between probability, density, and quantiles without visualizing the shape of the distribution. So I figured it would be helpful to have a visual guide to pnorm, dnorm, qnorm, and rnorm.

Table 15.1.: Table 1.1: Functions for the normal distribution

Function	Input	Output
pnorm	x	$P(X < x)$
dnorm	x	$f(x)$, or the height of the density curve at x
qnorm	q, a quantile from 0 to 1	x such that $P(X < x) = q$
rnorm	n	n random samples from the distribution

What is the relationship between these functions? The pnorm function gives the area under the curve to the left of a given point, while dnorm gives the height of the curve at that point. The qnorm function is the inverse of pnorm, returning the x value for a given probability. Finally, rnorm generates random samples from the normal distribution.

15.1. pnorm

This function gives the probability function for a normal distribution. If you do not specify the mean and standard deviation, R defaults to standard normal. Figure 15.1

```
pnorm(q, mean = 0, sd = 1, lower.tail = TRUE, log.p = FALSE)
```

The R help file for pnorm provides the template above. The value you input for q is a value on the x-axis, and the returned value is the area under the distribution curve to the left of that point.

15. Working with distribution functions

```
Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.  
i Please use `linewidth` instead.
```

This function gives the probability function for a normal distribution. If you do not specify the mean and standard deviation, R defaults to standard normal.

`pnorm(q, mean = 0, sd = 1, lower.tail = TRUE, log.p = FALSE)` The R help file for `pnorm` provides the template above. The value you input for `q` is a value on the x-axis, and the returned value is the area under the distribution curve to the left of that point.

The option `lower.tail = TRUE` tells R to use the area to the left of the given point. This is the default, so will remain true even without entering it. In order to compute the area to the right of the given point, you can either switch to `lower.tail = FALSE`, or simply calculate `1-pnorm()` instead. This is demonstrated below.

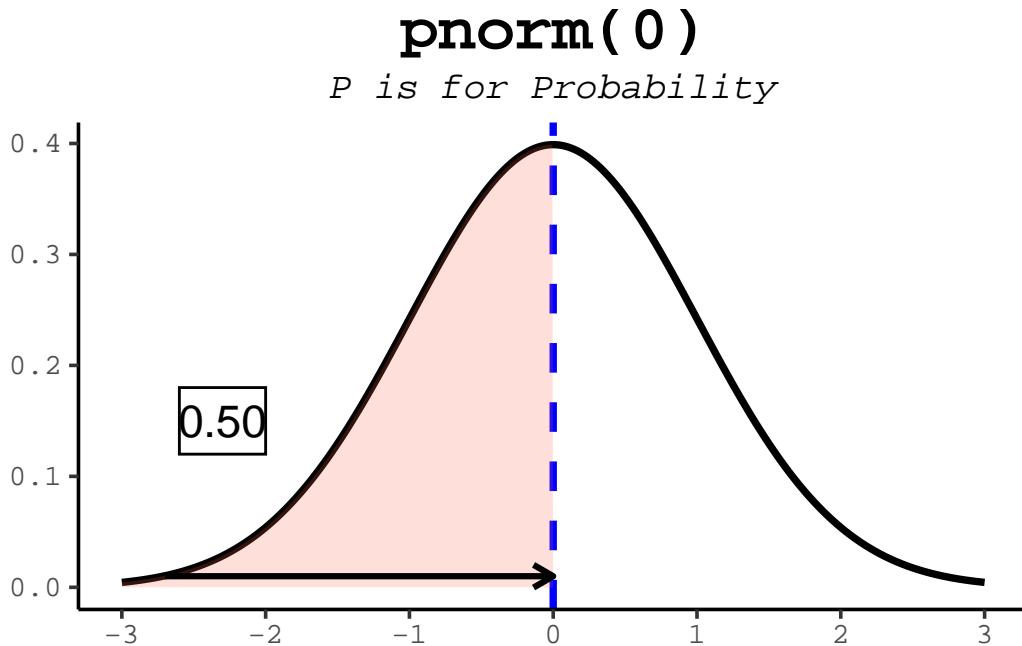


Figure 15.1.: The `pnorm` function takes a quantile (value on the x-axis) and returns the area under the curve to the left of that value.

The option `lower.tail = TRUE` tells R to use the area to the left of the given point. This is the default, so will remain true even without entering it. In order to compute the area to the right of the given point, you can either switch to `lower.tail = FALSE`, or simply calculate `1-pnorm()` instead.

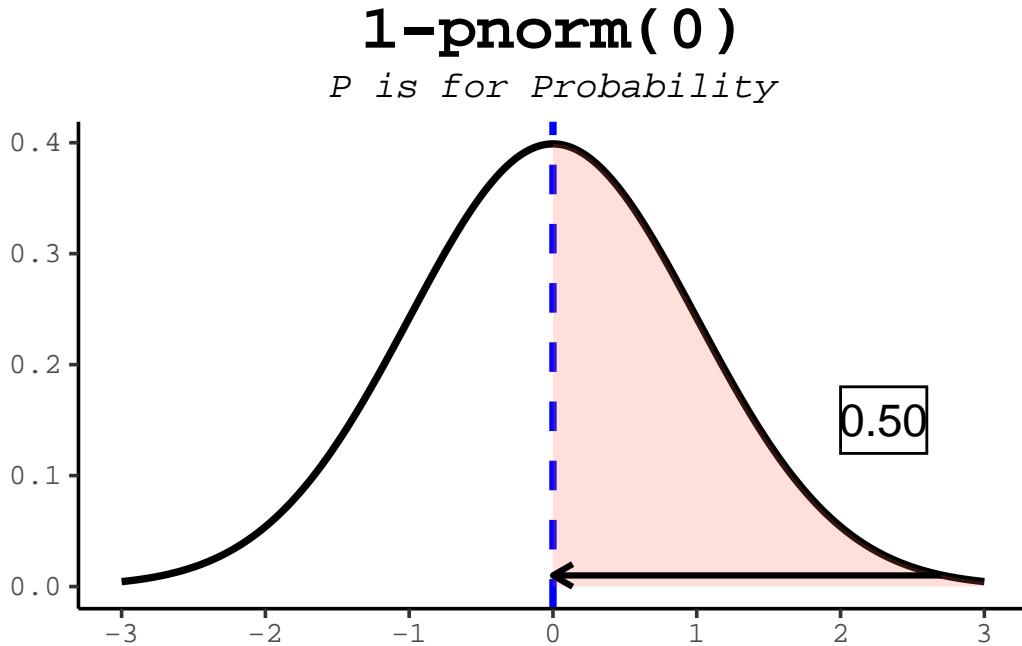


Figure 15.2.: The `pnorm` function takes a quantile (value on the x-axis) and returns the area under the curve to the left of that value.

15.2. `dnorm`

This function calculates the probability density function (PDF) for the normal distribution. It gives the probability density (height of the curve) at a specified value (x).

15.3. `qnorm`

This function calculates the quantiles of the normal distribution. It returns the value (x) corresponding to a specified probability (p). It is the inverse of the `pnorm` function.

15.4. `rnorm`

```
print(r1)
```

15. Working with distribution functions

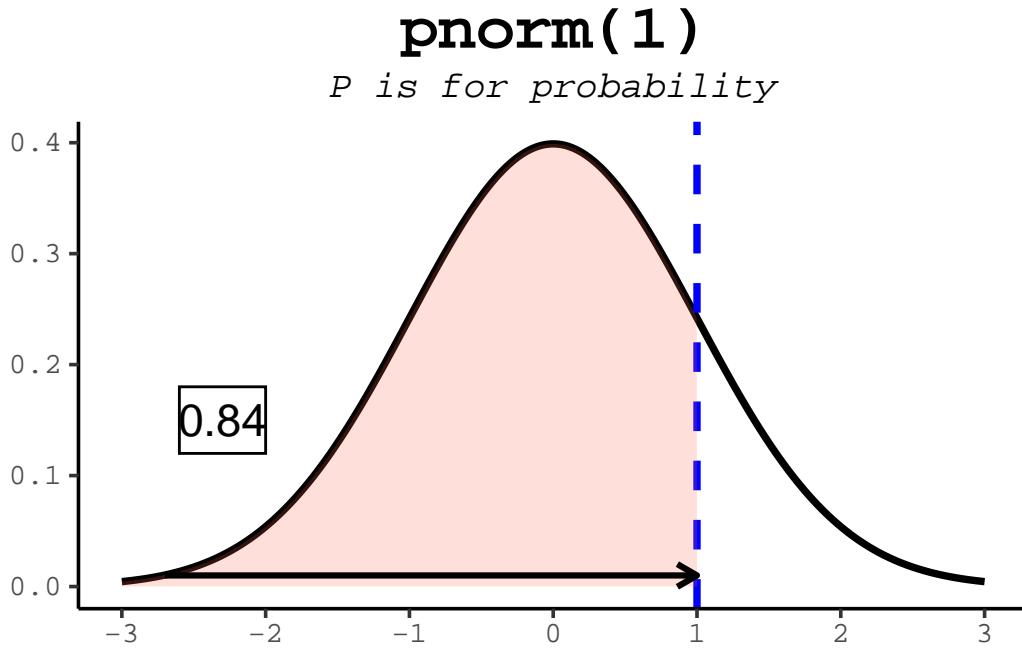


Figure 15.3.: The pnorm function takes a quantile (value on the x-axis) and returns the area under the curve to the left of that value.

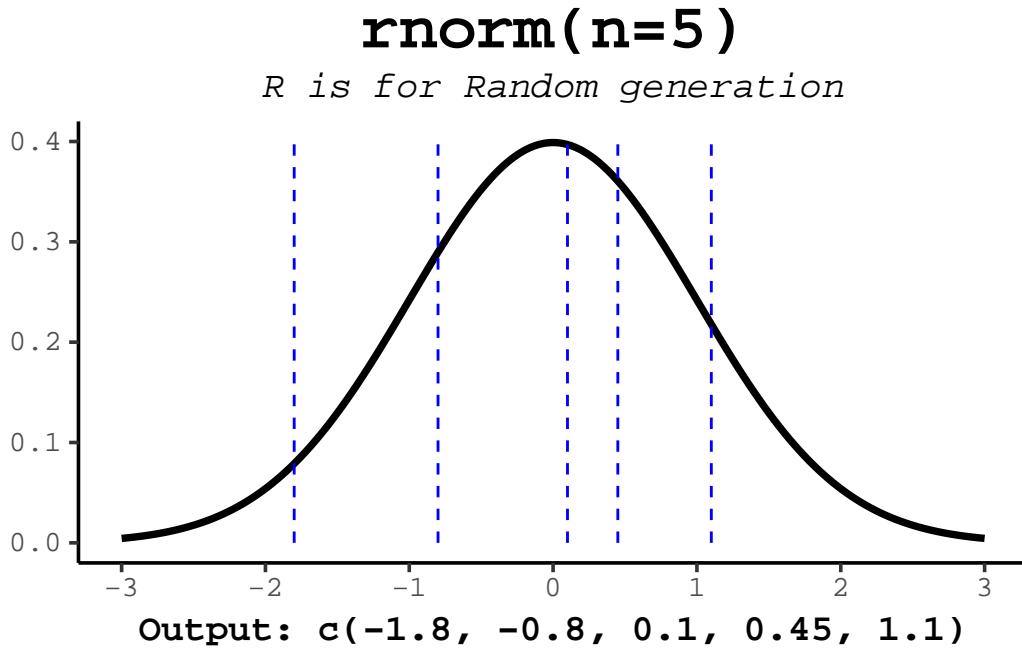


Figure 15.13.: The rnorm function takes a number of samples and returns a vector of random numbers from the normal distribution (with mean=0, sd=1 as defaults)

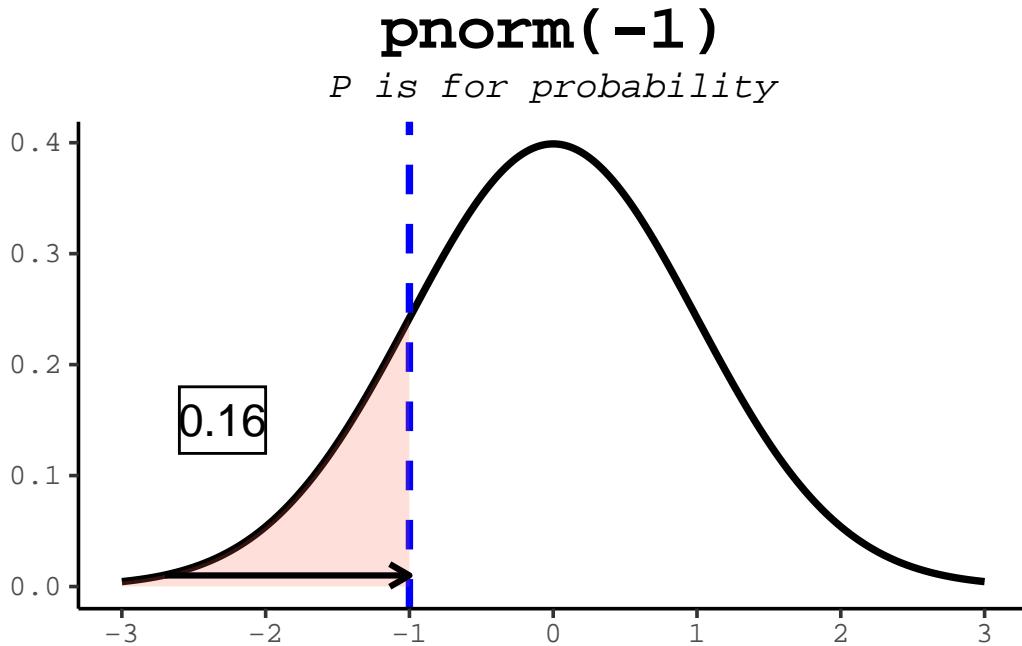


Figure 15.4.: The `pnorm` function takes a quantile (value on the x-axis) and returns the area under the curve to the left of that value.

15.5. IQ scores

Normal Distribution and its Application with IQ

The normal distribution, also known as the Gaussian distribution, is a continuous probability distribution characterized by its bell-shaped curve. It is defined by two parameters: the mean (μ) and the standard deviation (σ). The mean represents the central tendency of the distribution, while the standard deviation represents the dispersion or spread of the data.

The IQ scores are an excellent example of the normal distribution, as they are designed to follow this distribution pattern. The mean IQ score is set at 100, and the standard deviation is set at 15. This means that the majority of the population (about 68%) have an IQ score between 85 and 115, while 95% of the population have an IQ score between 70 and 130.

- What is the probability of having an IQ score between 85 and 115?

```
pnorm(115, mean = 100, sd = 15) - pnorm(85, mean = 100, sd = 15)
```

- What is the 90th percentile of the IQ scores?

15. Working with distribution functions

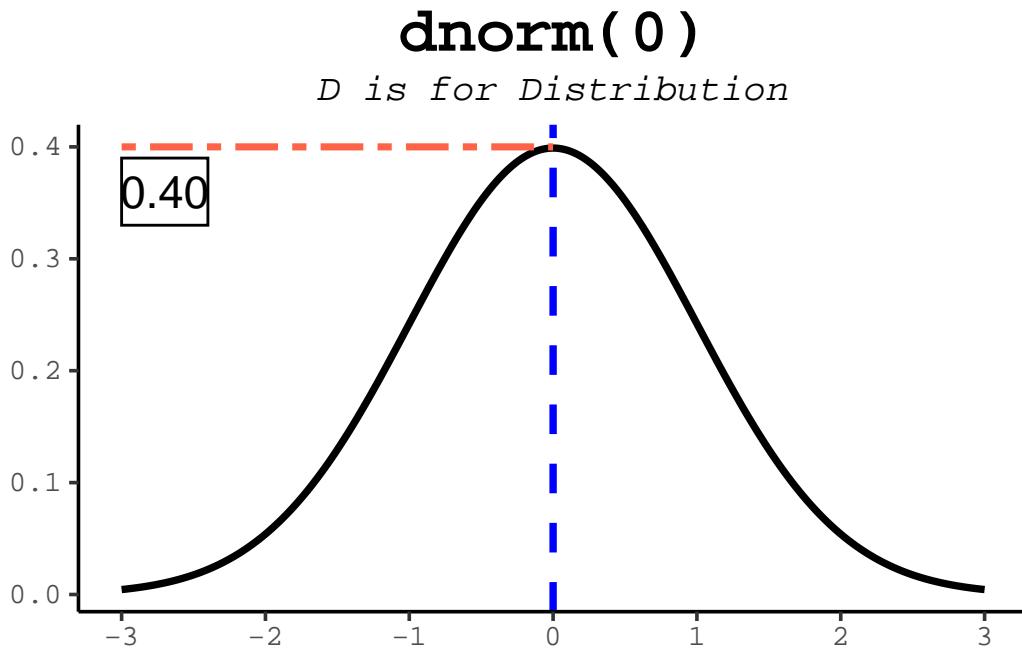


Figure 15.5.: The `dnorm` function returns the height of the normal distribution at a given point.

```
qnorm(0.9, mean = 100, sd = 15)
```

- What is the probability of having an IQ score above 130?

```
1 - pnorm(130, mean = 100, sd = 15)
```

- What is the probability of having an IQ score below 70?

```
pnorm(70, mean = 100, sd = 15)
```

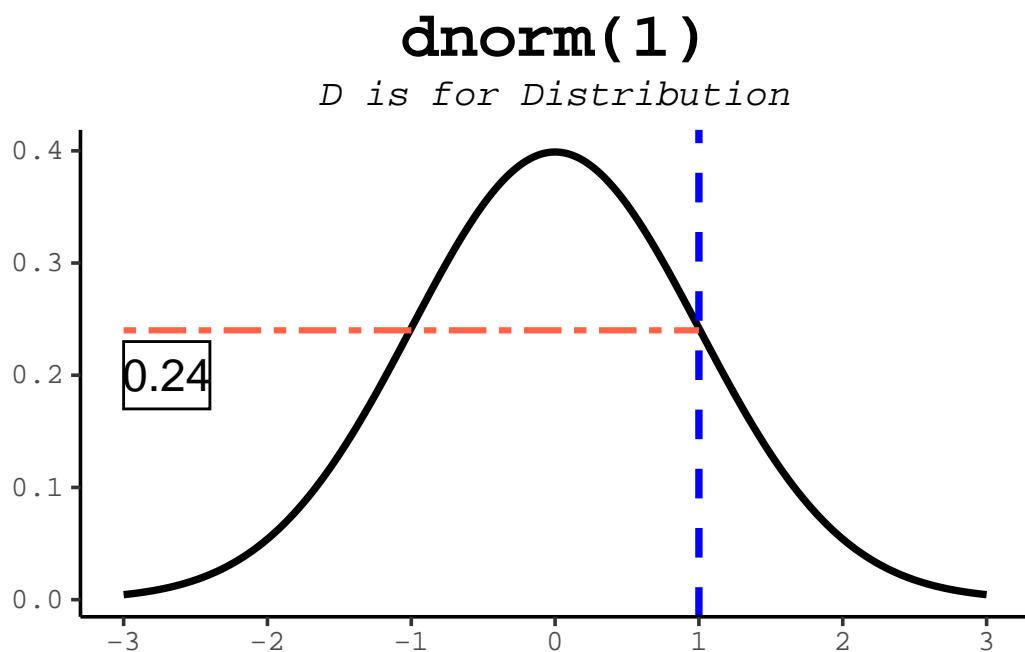


Figure 15.6.: The `dnorm` function returns the height of the normal distribution at a given point.

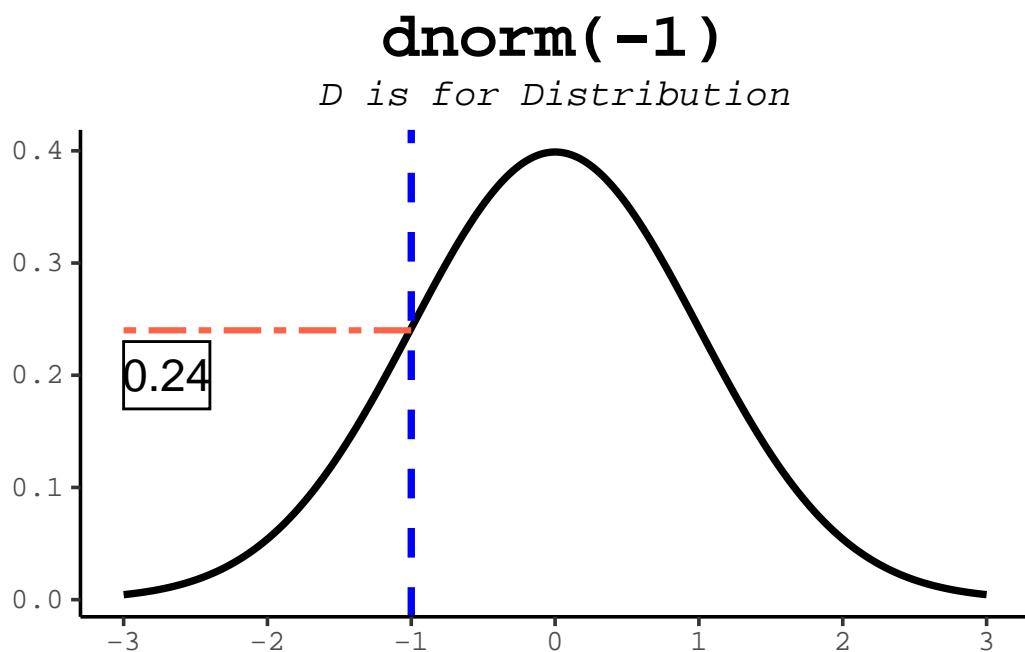


Figure 15.7.: The `dnorm` function returns the height of the normal distribution at a given point.

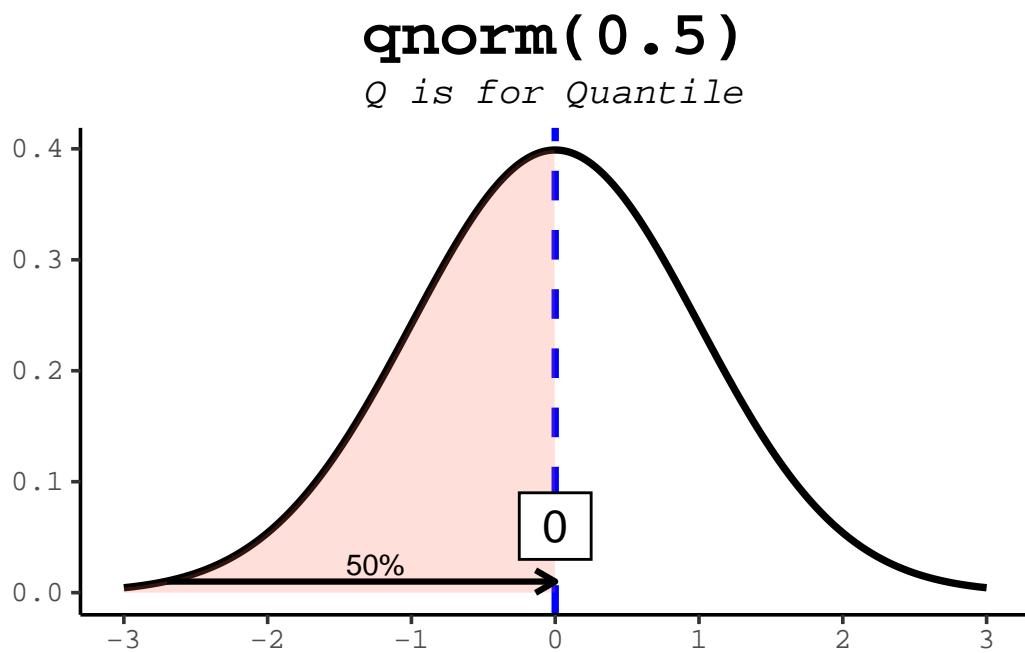


Figure 15.8.: The qnorm function is the inverse of the pnorm function in that it takes a probability and gives the quantile.

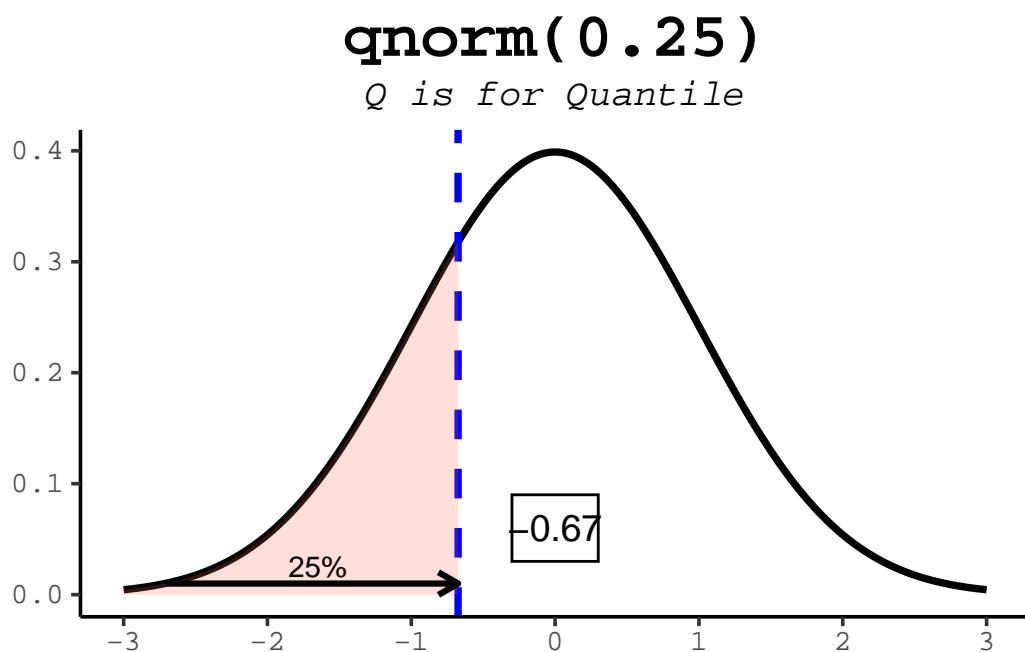


Figure 15.9.: The qnorm function is the inverse of the pnorm function in that it takes a probability and gives the quantile.

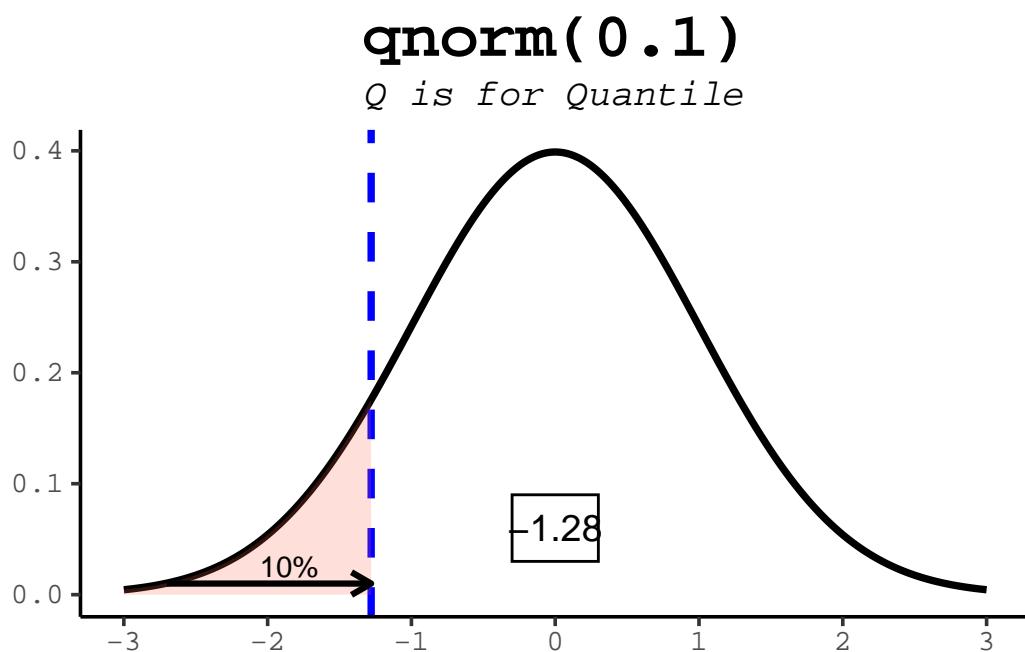


Figure 15.10.: The qnorm function is the inverse of the pnorm function in that it takes a probability and gives the quantile.

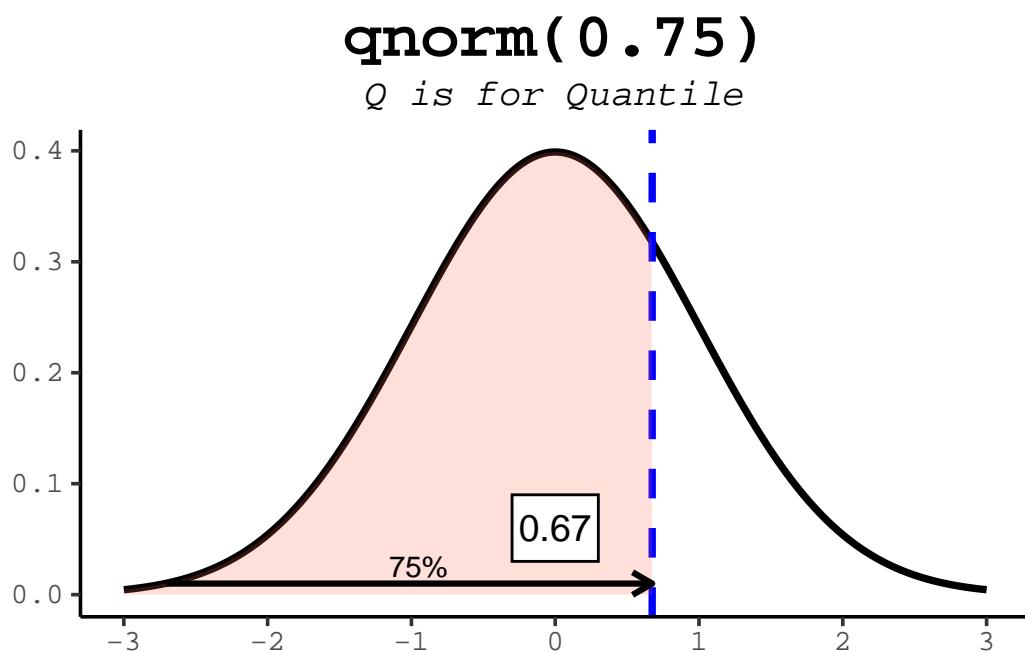


Figure 15.11.: The qnorm function is the inverse of the pnorm function in that it takes a probability and gives the quantile.

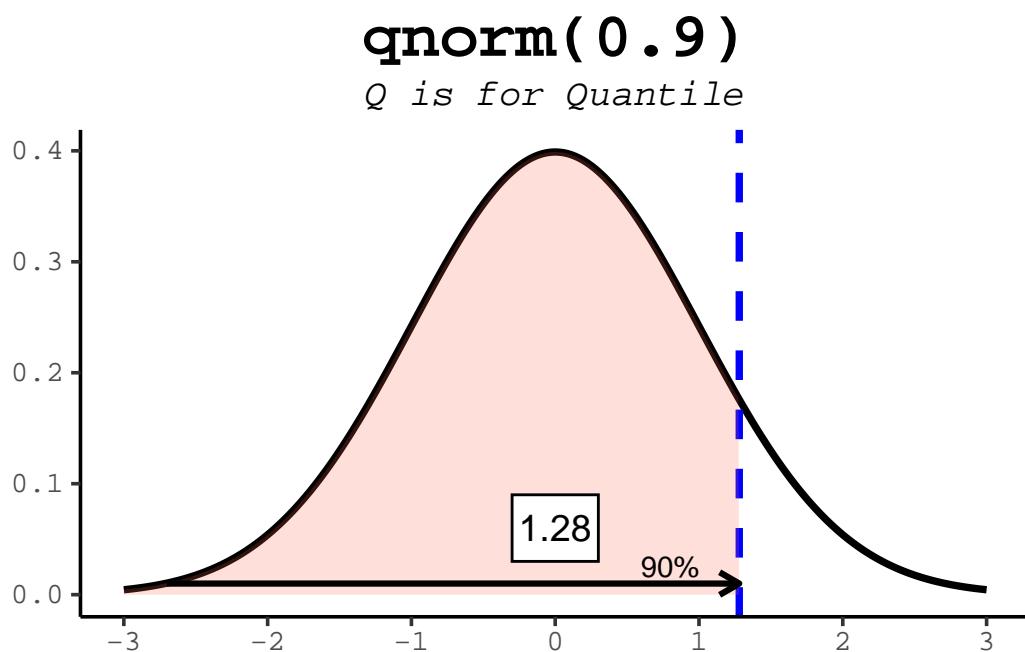


Figure 15.12.: The qnorm function is the inverse of the pnorm function in that it takes a probability and gives the quantile.

16. The t-statistic and t-distribution

16.1. Background

The t-test is a [statistical hypothesis test](#) that is commonly used when the data are normally distributed (follow a normal distribution) if the value of the population standard deviation were known. When the population standard deviation is not known and is replaced by an estimate based on the data, the test statistic follows a Student's t distribution.

T-tests are handy hypothesis tests in statistics when you want to compare means. You can compare a sample mean to a hypothesized or target value using a one-sample t-test. You can compare the means of two groups with a two-sample t-test. If you have two groups with paired observations (e.g., before and after measurements), use the paired t-test.

A t-test looks at the t-statistic, the t-distribution values, and the degrees of freedom to determine the statistical significance. To conduct a test with three or more means, we would use an analysis of variance.

The distribution that the t-statistic follows was described in a famous paper (Student 1908) by “Student”, a pseudonym for [William Sealy Gosset](#).

16.2. The Z-score and probability

Before talking about the t-distribution and t-scores, let's review the Z-score, its relation to the normal distribution, and probability.

The Z-score is defined as:

$$Z = \frac{x - \mu}{\sigma} \quad (16.1)$$

where μ is the population mean from which x is drawn and σ is the population standard deviation (taken as known, not estimated from the data).

The probability of observing a Z score of z or greater can be calculated by $pnorm(z, \mu, \sigma)$.

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For example, let's assume that our "population" is known and it truly has a mean 0 and standard deviation 1. If we have observations drawn from that population, we can assign a probability of seeing that observation by random chance *under the assumption that the null hypothesis is TRUE*.

```
zscore = seq(-5, 5, 1)
```

For each value of zscore, let's calculate the p-value and put the results in a `data.frame`.

```
df = data.frame(  
  zscore = zscore,  
  pval   = pnorm(zscore, 0, 1)  
)  
df
```

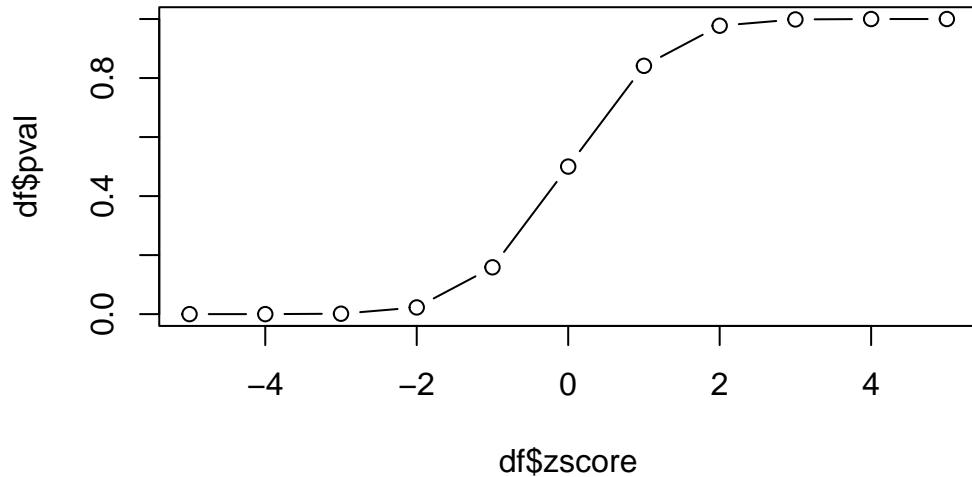
	zscore	pval
1	-5	2.866516e-07
2	-4	3.167124e-05
3	-3	1.349898e-03
4	-2	2.275013e-02
5	-1	1.586553e-01
6	0	5.000000e-01
7	1	8.413447e-01
8	2	9.772499e-01
9	3	9.986501e-01
10	4	9.999683e-01
11	5	9.999997e-01

Why is the p-value of something 5 population standard deviations away from the mean ($zscore=5$) nearly 1 in this calculation? What is the default for `pnorm` with respect to being one-sided or two-sided?

Let's plot the values of probability vs z-score:

```
plot(df$zscore, df$pval, type='b')
```

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This plot is the *empirical* cumulative density function (cdf) for our data. How can we use it? If we know the z-score, we can look up the probability of observing that value. Since we have constructed our experiment to follow the standard normal distribution, this cdf also represents the cdf of the standard normal distribution.

16.2.1. Small diversion: two-sided `pnorm` function

The `pnorm` function returns the “one-sided” probability of having a value at least as extreme as the observed x and uses the “lower” tail by default. Let’s create a function that computes two-sided p-values.

1. Take the absolute value of x
2. Compute `pnorm` with `lower.tail=FALSE` so we get lower p-values with larger values of x .
3. Since we want to include both tails, we need to multiply the area (probability) returned by `pnorm` by 2.

```
twosidedpnorm = function(x, mu=0, sd=1) {  
  2*pnorm(abs(x), mu, sd, lower.tail=FALSE)  
}
```

And we can test this to see how likely it is to be 2 or 3 standard deviations from the mean:

```
twosidedpnorm(2)
```

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```
[1] 0.04550026
```

```
twosidedpnorm(3)
```

```
[1] 0.002699796
```

16.3. The t-distribution

We spent time above working with z-scores and probability. An important aspect of working with the normal distribution is that we MUST assume that we know the standard deviation. Remember that the Z-score is defined as:

$$Z = \frac{x - \mu}{\sigma}$$

The formula for the *population* standard deviation is:

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (xi - \mu)^2} \quad (16.2)$$

In general, the population standard deviation is taken as “known” as we did above.

If we do not but only have a *sample* from the population, instead of using the Z-score, we use the t-score defined as:

$$t = \frac{x - \bar{x}}{s} \quad (16.3)$$

This looks quite similar to the formula for Z-score, but here we have to *estimate* the standard deviation, s from the data. The formula for s is:

$$s = \sqrt{\frac{1}{N-1} \sum_{i=1}^N (x_i - \bar{x})^2} \quad (16.4)$$

Since we are estimating the standard deviation from the data, this leads to extra variability that shows up as “fatter tails” for smaller sample sizes than for larger sample sizes. We can see this by comparing the *t-distribution* for various numbers of degrees of freedom (sample sizes).

16. The t-statistic and t-distribution

We can look at the effect of sample size on the distributions graphically by looking at the densities for 3, 5, 10, 20 degrees of freedom and the normal distribution:

```
library(dplyr)
library(ggplot2)
t_values = seq(-6,6,0.01)
df = data.frame(
  value = t_values,
  t_3   = dt(t_values,3),
  t_6   = dt(t_values,6),
  t_10  = dt(t_values,10),
  t_20  = dt(t_values,20),
  Normal= dnorm(t_values)
) |>
  tidyr::gather("Distribution", "density", -value)
ggplot(df, aes(x=value, y=density, color=Distribution)) +
  geom_line()
```

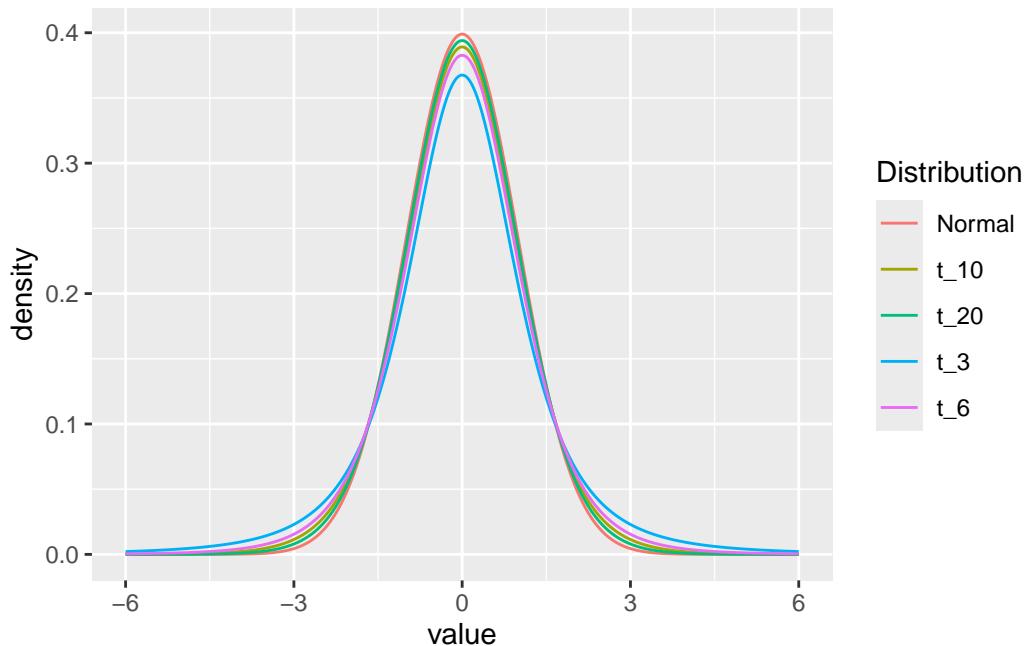
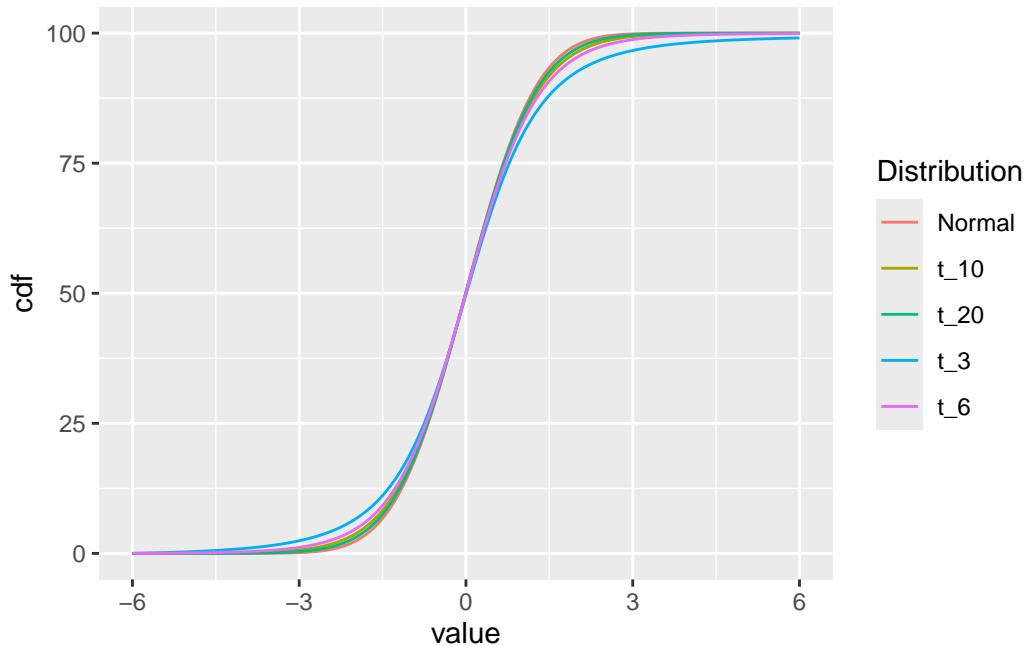


Figure 16.1.: t-distributions for various degrees of freedom. Note that the tails are fatter for smaller degrees of freedom, which is a result of estimating the standard deviation from the data.

16. The t-statistic and t-distribution

The `dt` and `dnorm` functions give the density of the distributions for each point.

```
df2 = df |>
  group_by(Distribution) |>
  arrange(value) |>
  mutate(cdf=cumsum(density))
ggplot(df2, aes(x=value, y=cdf, color=Distribution)) +
  geom_line()
```



16.3.1. p-values based on Z vs t

When we have a “sample” of data and want to compute the statistical significance of the difference of the mean from the population mean, we calculate the standard deviation of the sample means (standard error).

$$z = \frac{x - \mu}{\sigma / \sqrt{n}}$$

Let’s look at the relationship between the p-values of Z (from the normal distribution) vs t for a **sample** of data.

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```
set.seed(5432)
samp = rnorm(5,mean = 0.5)
z = sqrt(length(samp)) * mean(samp) #simplifying assumption (sigma=1, mu=0)
```

And the p-value if we assume we know the standard deviation:

```
pnorm(z, lower.tail = FALSE)
```

```
[1] 0.02428316
```

In reality, we don't know the standard deviation, so we have to estimate it from the data. We can do this by calculating the sample standard deviation:

```
ts = sqrt(length(samp)) * mean(samp) / sd(samp)
pnorm(ts, lower.tail = FALSE)
```

```
[1] 0.0167297
```

```
pt(ts,df = length(samp)-1, lower.tail = FALSE)
```

```
[1] 0.0503001
```

16.3.2. Experiment

When sampling from a normal distribution, we often calculate p-values to test hypotheses or determine the statistical significance of our results. The p-value represents the probability of obtaining a test statistic as extreme or more extreme than the one observed, under the null hypothesis.

In a typical scenario, we assume that the population mean and standard deviation are known. However, in many real-life situations, we don't know the true population standard deviation, and we have to estimate it using the sample standard deviation (Equation 16.4). This estimation introduces some uncertainty into our calculations, which affects the p-values. When we include an estimate of the standard deviation, we switch from using the standard normal (z) distribution to the t-distribution for calculating p-values.

What would happen if we used the normal distribution to calculate p-values when we use the sample standard deviation? Let's find out!

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1. Simulate a bunch of samples of size n from the standard normal distribution
2. Calculate the p-value distribution for those samples based on the normal.
3. Calculate the p-value distribution for those samples based on the normal, but with the *estimated* standard deviation.
4. Calculate the p-value distribution for those samples based on the t-distribution.

Create a function that draws a sample of size n from the standard normal distribution.

```
zf = function(n) {  
  samp = rnorm(n)  
  z = sqrt(length(samp)) * mean(samp) / 1 #simplifying assumption (sigma=1, mu=0)  
  z  
}
```

And give it a try:

```
zf(5)
```

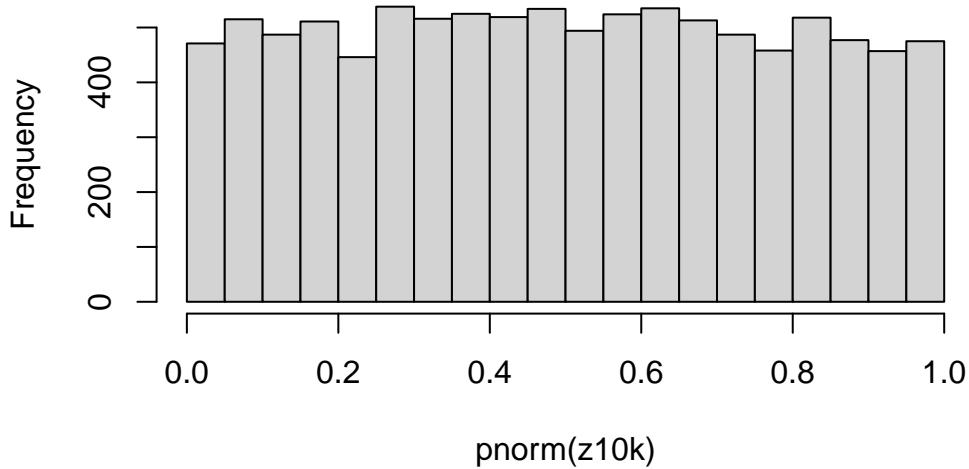
```
[1] 0.7406094
```

Perform 10000 replicates of our sampling and z-scoring. We are using the assumption that we know the population standard deviation; in this case, we do know since we are sampling from the standard normal distribution.

```
z10k = replicate(10000,zf(5))  
hist(pnorm(z10k))
```

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Histogram of pnorm(z10k)



And do the same, but now creating a t-score function. We are using the assumption that we *don't* know the population standard deviation; in this case, we must estimate it from the data. Note the difference in the calculation of the t-score (`ts`) as compared to the z-score (`z`).

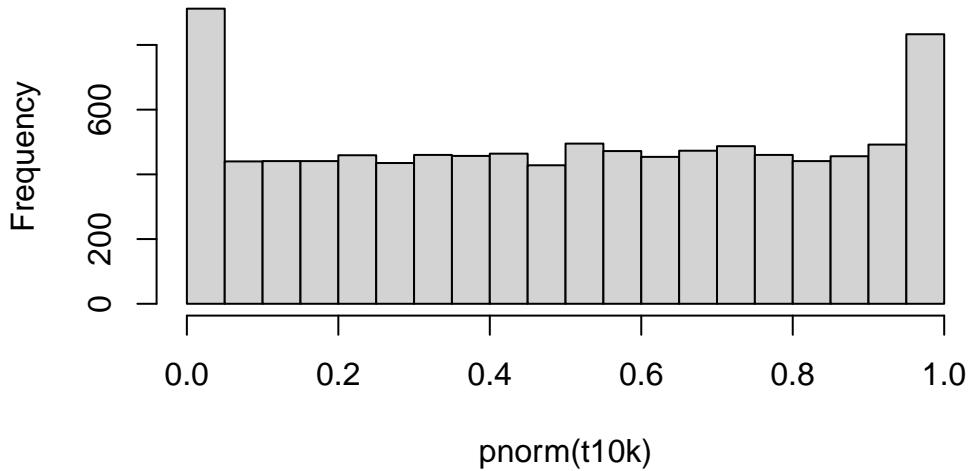
```
tf = function(n) {
  samp = rnorm(n)
  # now, using the sample standard deviation since we
  # "don't know" the population standard deviation
  ts = sqrt(length(samp)) * mean(samp) / sd(samp)
  ts
}
```

If we use those t-scores and calculate the p-values based on the normal distribution, the histogram of those p-values looks like:

```
t10k = replicate(10000,tf(5))
hist(pnorm(t10k))
```

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Histogram of $\text{pnorm}(\text{t10k})$

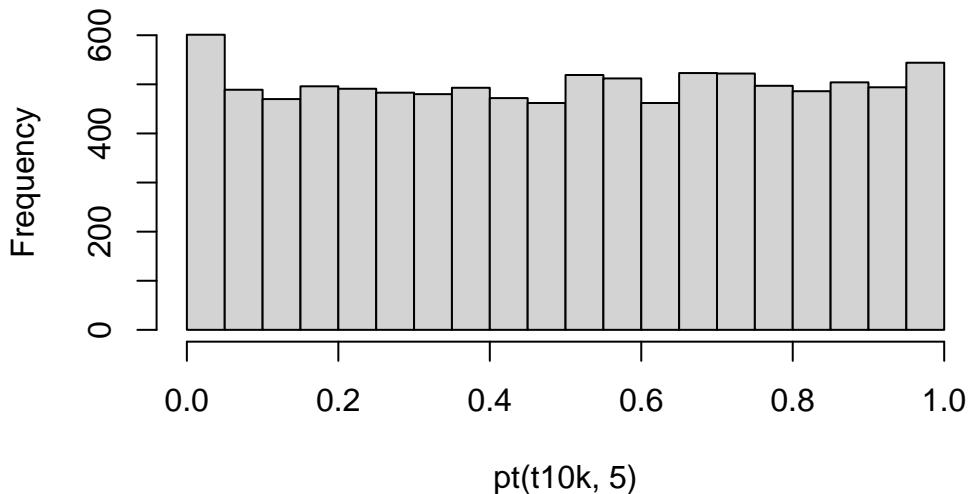


Since we are using the normal distribution to calculate the p-values, we are, in effect, assuming that we know the population standard deviation. This assumption is incorrect, and we can see that the p-values are not uniformly distributed between 0 and 1.

If we use those t-scores and calculate the p-values based on the t -distribution, the histogram of those p-values looks like:

```
hist(pt(t10k, 5))
```

Histogram of $\text{pt}(\text{t10k}, 5)$

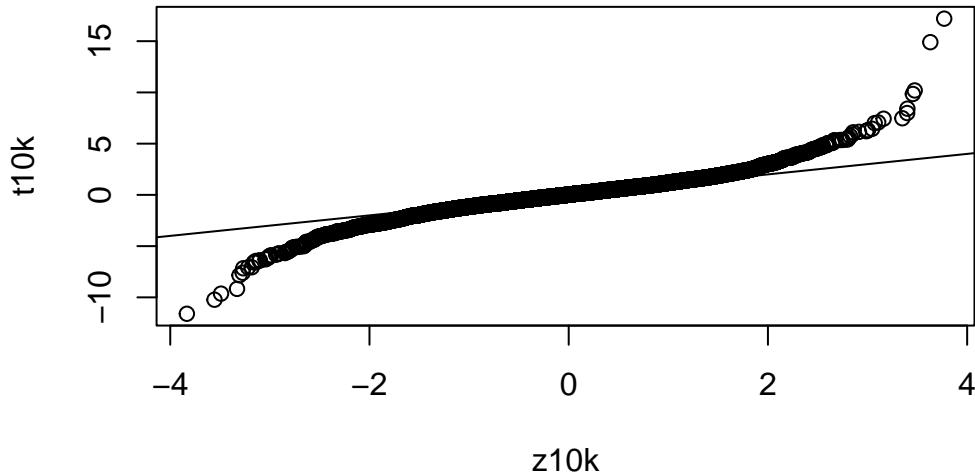


16. The t-statistic and t-distribution

Now, the p-values are uniformly distributed between 0 and 1, as expected.

What is a qqplot and how do we use it? A qqplot is a plot of the quantiles of two distributions against each other. If the two distributions are identical, the points will fall on a straight line. If the two distributions are different, the points will deviate from the straight line. We can use a qqplot to compare the t-distribution to the normal distribution. If the t-distribution is identical to the normal distribution, the points will fall on a straight line. If the t-distribution is different from the normal distribution, the points will deviate from the straight line. In this case, we can see that the t-distribution is different from the normal distribution, as the points deviate from the straight line. What would happen if we increased the sample size? The t-distribution would approach the normal distribution, and the points would fall closer and closer to the straight line.

```
qqplot(z10k,t10k)
abline(0,1)
```



16.4. Summary of t-distribution vs normal distribution

The t-distribution is a family of probability distributions that depends on a parameter called degrees of freedom, which is related to the sample size. The t-distribution approaches the standard normal distribution as the sample size increases but has heavier tails for smaller sample sizes. This means that the t-distribution is more conservative in calculating p-values for small samples, making it harder to reject the null hypothesis. Including an estimate of the standard deviation changes the way we calculate p-values by switching from the standard normal distribution to the t-distribution, which accounts for

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the uncertainty introduced by estimating the population standard deviation from the sample. This adjustment is particularly important for small sample sizes, as it provides a more accurate assessment of the statistical significance of our results.

16.5. `t.test`

16.5.1. One-sample

We are going to use the `t.test` function to perform a one-sample t-test. The `t.test` function takes a vector of values as input that represents the sample values. In this case, we'll simulate our sample using the `rnorm` function and presume that our “effect-size” is 1.

```
x = rnorm(20,1)
# small sample
# Just use the first 5 values of the sample
t.test(x[1:5])
```

One Sample t-test

```
data: x[1:5]
t = 0.97599, df = 4, p-value = 0.3843
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
-1.029600 2.145843
sample estimates:
mean of x
0.5581214
```

In this case, we set up the experiment so that the null hypothesis is true (the true mean is not zero, but actually 1). However, we only have a small sample size that leads to a modest p-value.

Increasing the sample size allows us to see the effect more clearly.

```
t.test(x[1:20])
```

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One Sample t-test

```
data: x[1:20]
t = 3.8245, df = 19, p-value = 0.001144
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
0.3541055 1.2101894
sample estimates:
mean of x
0.7821474
```

16.5.2. two-sample

```
x = rnorm(10,0.5)
y = rnorm(10,-0.5)
t.test(x,y)
```

Welch Two Sample t-test

```
data: x and y
t = 3.4296, df = 17.926, p-value = 0.003003
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
0.5811367 2.4204048
sample estimates:
mean of x mean of y
0.7039205 -0.7968502
```

16.5.3. from a data.frame

In some situations, you may have data and groups as columns in a data.frame. See the following data.frame, for example

```
df = data.frame(value=c(x,y),group=as.factor(rep(c('g1','g2'),each=10)))
df
```

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	value	group
1	1.12896674	g1
2	-1.26838101	g1
3	1.04577597	g1
4	1.69075585	g1
5	0.18672204	g1
6	1.99715092	g1
7	1.15424947	g1
8	0.37671442	g1
9	-0.09565723	g1
10	0.82290783	g1
11	-1.48530261	g2
12	-1.29200440	g2
13	-0.18778362	g2
14	0.59205742	g2
15	-2.10065248	g2
16	-0.29961560	g2
17	-0.38985115	g2
18	-2.47126235	g2
19	-0.63654380	g2
20	0.30245611	g2

R allows us to perform a t-test using the `formula` notation.

```
t.test(value ~ group, data=df)
```

```
Welch Two Sample t-test

data: value by group
t = 3.4296, df = 17.926, p-value = 0.003003
alternative hypothesis: true difference in means between group g1 and group g2 is not equal
95 percent confidence interval:
 0.5811367 2.4204048
sample estimates:
mean in group g1 mean in group g2
 0.7039205      -0.7968502
```

You read that as **value is a function of group**. In practice, this will do a t-test between the **values** in g1 vs g2.

16.5.4. Equivalence to linear model

```
t.test(value ~ group, data=df, var.equal=TRUE)
```

Two Sample t-test

```
data: value by group
t = 3.4296, df = 18, p-value = 0.002989
alternative hypothesis: true difference in means between group g1 and group g2 is not equal
95 percent confidence interval:
0.5814078 2.4201337
sample estimates:
mean in group g1 mean in group g2
0.7039205      -0.7968502
```

This is *equivalent* to:

```
res = lm(value ~ group, data=df)
summary(res)
```

```
Call:
lm(formula = value ~ group, data = df)

Residuals:
    Min      1Q  Median      3Q     Max 
-1.9723 -0.5600  0.2511  0.5252  1.3889 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept)  0.7039     0.3094   2.275  0.03538 *  
groupg2     -1.5008     0.4376  -3.430  0.00299 ** 
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.9785 on 18 degrees of freedom
Multiple R-squared:  0.3952,    Adjusted R-squared:  0.3616 
F-statistic: 11.76 on 1 and 18 DF,  p-value: 0.002989
```

16.6. Power calculations

The power of a statistical test is the probability that the test will reject the null hypothesis when the alternative hypothesis is true. In other words, the power of a statistical test is the probability of not making a Type II error. The power of a statistical test depends on the significance level (alpha), the sample size, and the effect size.

The `power.t.test` function can be used to calculate the power of a one-sample t-test.

Looking at `help("power.t.test")`, we see that the function takes the following arguments:

- `n` - sample size
- `delta` - effect size
- `sd` - standard deviation of the sample
- `sig.level` - significance level
- `power` - power

We need to supply four of these arguments to calculate the fifth. For example, if we want to calculate the power of a one-sample t-test with a sample size of 5, a standard deviation of 1, and an effect size of 1, we can use the following command:

```
power.t.test(n = 5, delta = 1, sd = 1, sig.level = 0.05)
```

Two-sample t test power calculation

```

n = 5
delta = 1
sd = 1
sig.level = 0.05
power = 0.2859276
alternative = two.sided
```

NOTE: n is number in *each* group

This gives a nice summary of the power calculation. We can also extract the power value from the result:

16. The *t*-statistic and *t*-distribution

```
power.t.test(n = 5, delta = 1, sd = 1,  
             sig.level = 0.05, type='one.sample')$power
```

```
[1] 0.4013203
```

Tip

When getting results from a function that don't look "computable" such as those from `power.t.test`, you can use the `$` operator to extract the value you want. In this case, we want the `power` value from the result of `power.t.test`.

How would you know what to extract? You can use the `names` function or the `str` function to see the structure of the result. For example:

```
names(power.t.test(n = 5, delta = 1, sd = 1,  
                   sig.level = 0.05, type='one.sample'))  
  
[1] "n"           "delta"        "sd"          "sig.level"    "power"  
[6] "alternative" "note"         "method"
```

```
# or  
str(power.t.test(n = 5, delta = 1, sd = 1,  
                  sig.level = 0.05, type='one.sample'))
```

```
List of 8  
 $ n           : num 5  
 $ delta       : num 1  
 $ sd          : num 1  
 $ sig.level   : num 0.05  
 $ power       : num 0.401  
 $ alternative: chr "two.sided"  
 $ note        : NULL  
 $ method      : chr "One-sample t test power calculation"  
 - attr(*, "class")= chr "power.htest"
```

Alternatively, we may know a lot about our experimental system and want to calculate the sample size needed to achieve a certain power. For example, if we want to achieve a power of 0.8 with a standard deviation of 1 and an effect size of 1, we can use the following command:

16. The t-statistic and t-distribution

```
power.t.test(delta = 1, sd = 1, sig.level = 0.05, power = 0.8, type = "one.sample")
```

```
One-sample t test power calculation

n = 9.937864
delta = 1
sd = 1
sig.level = 0.05
power = 0.8
alternative = two.sided
```

The `power.t.test` function is convenient and quite fast. As we've seen before, though, sometimes the distribution of the test statistics is now easily calculated. In those cases, we can use simulation to calculate the power of a statistical test. For example, if we want to calculate the power of a one-sample t-test with a sample size of 5, a standard deviation of 1, and an effect size of 1, we can use the following command:

```
sim_t_test_pval <- function(n = 5, delta = 1, sd = 1, sig.level = 0.05) {
  x = rnorm(n, delta, sd)
  t.test(x)$p.value <= sig.level
}
pow = mean(replicate(1000, sim_t_test_pval()))
pow
```

```
[1] 0.405
```

Let's break this down. First, we define a function called `sim_t_test_pval` that takes the same arguments as the `power.t.test` function. Inside the function, we simulate a sample of size `n` from a normal distribution with mean `delta` and standard deviation `sd`. Then, we perform a one-sample t-test on the sample and return a logical value indicating whether the p-value is less than the significance level. Next, we use the `replicate` function to repeat the simulation 1000 times. Finally, we calculate the proportion of simulations in which the p-value was less than the significance level. This proportion is an estimate of the power of the one-sample t-test.

Let's compare the results of the `power.t.test` function and our simulation-based approach:

16. The t-statistic and t-distribution

```
power.t.test(n = 5, delta = 1, sd = 1, sig.level = 0.05, type='one.sample')$power  
  
[1] 0.4013203  
  
mean(replicate(1000, sim_t_test_pval(n = 5, delta = 1, sd = 1, sig.level = 0.05)))  
  
[1] 0.414
```

16.7. Resources

See the [pwr package](#) for more information on power calculations.

17. K-means clustering

17.1. History of the k-means algorithm

The k-means clustering algorithm was first proposed by Stuart Lloyd in 1957 as a technique for pulse-code modulation. However, it was not published until 1982. In 1965, Edward W. Forgy published an essentially identical method, which became widely known as the k-means algorithm. Since then, k-means clustering has become one of the most popular unsupervised learning techniques in data analysis and machine learning.

K-means clustering is a method for finding patterns or groups in a dataset. It is an unsupervised learning technique, meaning that it doesn't rely on previously labeled data for training. Instead, it identifies structures or patterns directly from the data based on the similarity between data points (see Figure 17.1).

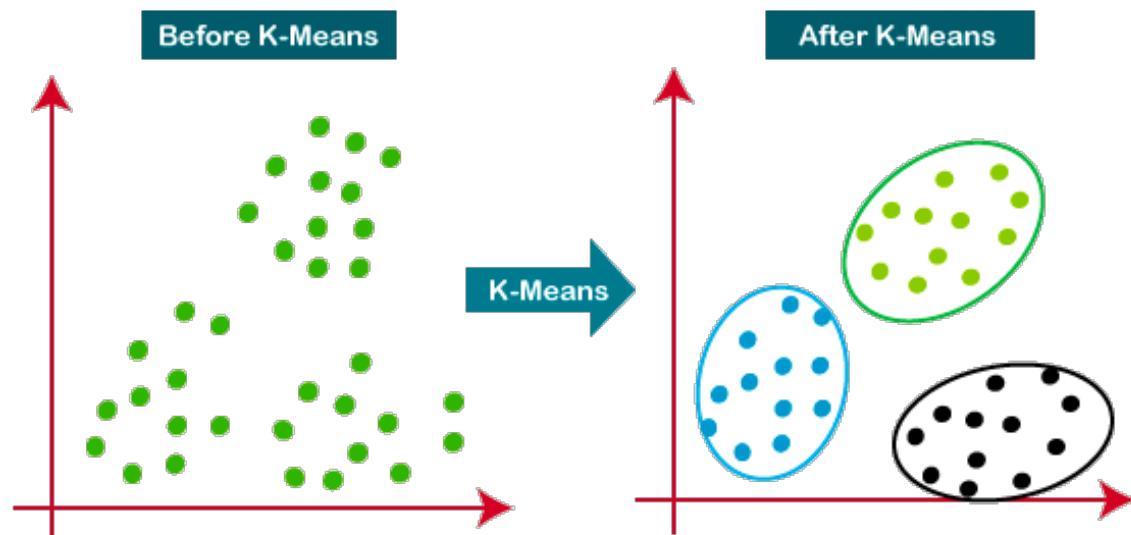


Figure 17.1.: K-means clustering takes a dataset and divides it into k clusters.

In simple terms, k-means clustering aims to divide a dataset into k distinct groups or clusters, where each data point belongs to the cluster with the nearest mean (average).

17. K-means clustering

The goal is to minimize the variability within each cluster while maximizing the differences between clusters. This helps to reveal hidden patterns or relationships in the data that might not be apparent otherwise.

17.2. The k-means algorithm

The k-means algorithm follows these general steps:

1. Choose the number of clusters k .
2. Initialize the cluster centroids randomly by selecting k data points from the dataset.
3. Assign each data point to the nearest centroid.
4. Update the centroids by computing the mean of all the data points assigned to each centroid.
5. Repeat steps 3 and 4 until the centroids no longer change or a certain stopping criterion is met (e.g., a maximum number of iterations).

The algorithm converges when the centroids stabilize or no longer change significantly. The final clusters represent the underlying patterns or structures in the data. Advantages and disadvantages of k-means clustering

17.3. Pros and cons of k-means clustering

Compared to other clustering algorithms, k-means has several advantages:

- **Simplicity and ease of implementation** The k-means algorithm is relatively straightforward and can be easily implemented, even for large datasets.
- **Scalability** The algorithm can be adapted for large datasets using various optimization techniques or parallel processing.
- **Speed** K-means is generally faster than other clustering algorithms, especially when the number of clusters k is small.
- **Interpretability** The results of k-means clustering are easy to understand, as the algorithm assigns each data point to a specific cluster based on its similarity to the cluster's centroid.

However, k-means clustering has several disadvantages as well:

17. K-means clustering

- **Choice of k** Selecting the appropriate number of clusters can be challenging and often requires domain knowledge or experimentation. A poor choice of k may yield poor results.
- **Sensitivity to initial conditions** The algorithm's results can vary depending on the initial placement of centroids. To overcome this issue, the algorithm can be run multiple times with different initializations and the best solution can be chosen based on a criterion (e.g., minimizing within-cluster variation).
- **Assumes spherical clusters** K-means assumes that clusters are spherical and evenly sized, which may not always be the case in real-world datasets. This can lead to poor performance if the underlying clusters have different shapes or densities.
- **Sensitivity to outliers** The algorithm is sensitive to outliers, which can heavily influence the position of centroids and the final clustering result. Preprocessing the data to remove or mitigate the impact of outliers can help improve the performance of k-means clustering.

Despite limitations, k-means clustering remains a popular and widely used method for exploring and analyzing data, particularly in biological data analysis, where identifying patterns and relationships can provide valuable insights into complex systems and processes.

17.4. An example of k-means clustering

17.4.1. The data and experimental background

The data we are going to use are from DeRisi, Iyer, and Brown (1997). From their abstract:

DNA microarrays containing virtually every gene of *Saccharomyces cerevisiae* were used to carry out a comprehensive investigation of the temporal program of gene expression accompanying the metabolic shift from fermentation to respiration. The expression profiles observed for genes with known metabolic functions pointed to features of the metabolic reprogramming that occur during the diauxic shift, and the expression patterns of many previously uncharacterized genes provided clues to their possible functions.

These data are available from NCBI GEO as [GSE28](#).

In the case of the baker's or brewer's yeast *Saccharomyces cerevisiae* growing on glucose with plenty of aeration, the diauxic growth pattern is commonly observed in batch culture.

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During the first growth phase, when there is plenty of glucose and oxygen available, the yeast cells prefer glucose fermentation to aerobic respiration even though aerobic respiration is the more efficient pathway to grow on glucose. This experiment profiles gene expression for 6400 genes over a time course during which the cells are undergoing a [diauxic shift](#).

The data in deRisi et al. have no replicates and are time course data. Sometimes, seeing how groups of genes behave can give biological insight into the experimental system or the function of individual genes. We can use clustering to group genes that have a similar expression pattern over time and then potentially look at the genes that do so.

Our goal, then, is to use `kmeans` clustering to divide highly variable (informative) genes into groups and then to visualize those groups.

17.5. Getting data

These data were deposited at NCBI GEO back in 2002. GEOquery can pull them out easily.

```
library(GEOquery)
gse = getGEO("GSE28")[[1]]
class(gse)
```

```
[1] "ExpressionSet"
attr(,"package")
[1] "Biobase"
```

GEOquery is a little dated and was written before the `SummarizedExperiment` existed. However, Bioconductor makes a conversion from the old `ExpressionSet` that `GEOquery` uses to the `SummarizedExperiment` that we see so commonly used now.

```
library(SummarizedExperiment)
gse = as(gse, "SummarizedExperiment")
gse
```

```
class: SummarizedExperiment
dim: 6400 7
metadata(3): experimentData annotation protocolData
assays(1): exprs
rownames(6400): 1 2 ... 6399 6400
```

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```
rowData names(20): ID ORF ... FAILED IS_CONTAMINATED
colnames(7): GSM887 GSM888 ... GSM892 GSM893
colData names(33): title geo_accession ... supplementary_file
  data_row_count
```

Taking a quick look at the `colData()`, it might be that we want to reorder the columns a bit.

```
colData(gse)$title
```

```
[1] "diauxic shift timecourse: 15.5 hr" "diauxic shift timecourse: 0 hr"
[3] "diauxic shift timecourse: 18.5 hr" "diauxic shift timecourse: 9.5 hr"
[5] "diauxic shift timecourse: 11.5 hr" "diauxic shift timecourse: 13.5 hr"
[7] "diauxic shift timecourse: 20.5 hr"
```

So, we can reorder by hand to get the time course correct:

```
gse = gse[, c(2,4,5,6,1,3,7)]
```

17.6. Preprocessing

In gene expression data analysis, the primary objective is often to identify genes that exhibit significant differences in expression levels across various conditions, such as diseased vs. healthy samples or different time points in a time-course experiment. However, gene expression datasets are typically large, noisy, and contain numerous genes that do not exhibit substantial changes in expression levels. Analyzing all genes in the dataset can be computationally intensive and may introduce noise or false positives in the results.

One common approach to reduce the complexity of the dataset and focus on the most informative genes is to subset the genes based on their standard deviation in expression levels across the samples. The standard deviation is a measure of dispersion or variability in the data, and genes with high standard deviations have more variation in their expression levels across the samples.

By selecting genes with high standard deviations, we focus on genes that show relatively large changes in expression levels across different conditions. These genes are more likely to be biologically relevant and involved in the underlying processes or pathways of interest. In contrast, genes with low standard deviations exhibit little or no change in expression levels and are less likely to be informative for the analysis. It turns out that applying

17. K-means clustering

filtering based on criteria such as standard deviation can also increase power and reduce false positives in the analysis (Bourgon, Gentleman, and Huber 2010).

To subset the genes for analysis based on their standard deviation, the following steps can be followed: Calculate the standard deviation of each gene's expression levels across all samples. Set a threshold for the standard deviation, which can be determined based on domain knowledge, data distribution, or a specific percentile of the standard deviation values (e.g., selecting the top 10% or 25% of genes with the highest standard deviations). Retain only the genes with a standard deviation above the chosen threshold for further analysis.

By subsetting the genes based on their standard deviation, we can reduce the complexity of the dataset, speed up the subsequent analysis, and increase the likelihood of detecting biologically meaningful patterns and relationships in the gene expression data. The threshold for the standard deviation cutoff is rather arbitrary, so it may be beneficial to try a few to check for sensitivity of findings.

```
sds = apply(assays(gse)[[1]], 1, sd)
hist(sds)
```

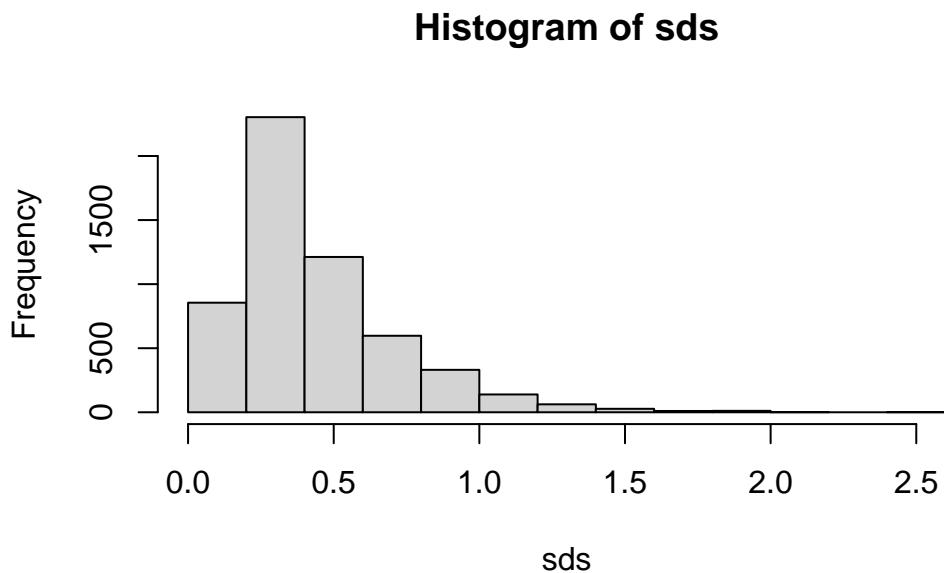


Figure 17.2.: Histogram of standard deviations for all genes in the deRisi dataset.

Examining the plot, we can see that the most highly variable genes have an $sd > 0.8$ or so (arbitrary). We can, for convenience, create a new `SummarizedExperiment` that contains only our most highly variable genes.

```
idx = sds>0.8 & !is.na(sds)
gse_sub = gse[idx,]
```

17.7. Clustering

Now, `gse_sub` contains a subset of our data.

The `kmeans` function takes a matrix and the number of clusters as arguments.

```
k = 4
km = kmeans(assays(gse_sub)[[1]], 4)
```

The `km` `kmeans` result contains a vector, `km$cluster`, which gives the cluster associated with each gene. We can plot the genes for each cluster to see how these different genes behave.

```
expression_values = assays(gse_sub)[[1]]
par(mfrow=c(2,2), mar=c(3,4,1,2)) # this allows multiple plots per page
for(i in 1:k) {
  matplot(t(expression_values[km$cluster==i, ]), type='l', ylim=c(-3,3),
          ylab = paste("cluster", i))
}
```

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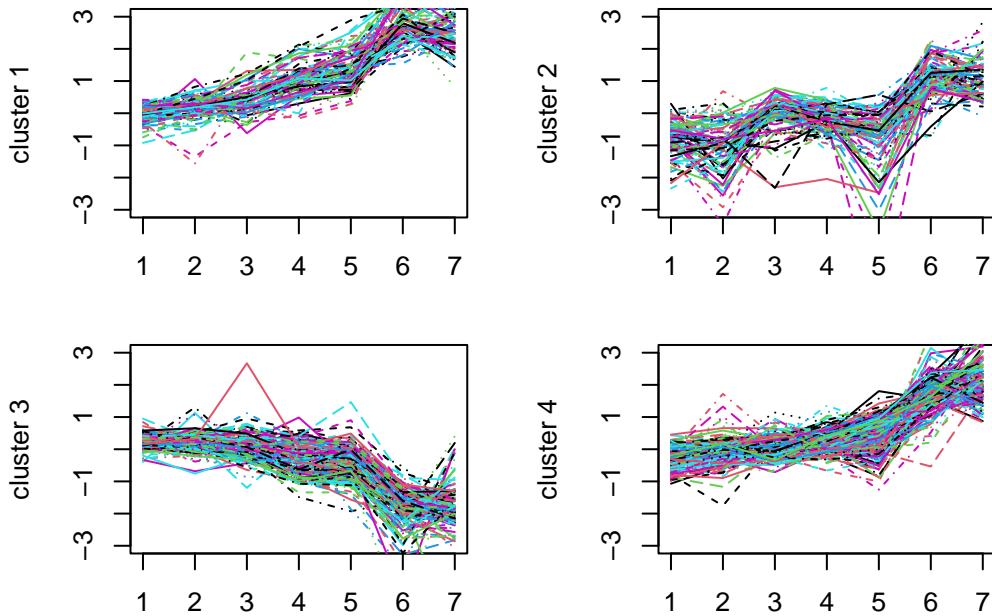


Figure 17.3.: Gene expression profiles for the four clusters identified by k-means clustering.
Each line represents a gene in the cluster, and each column represents a time point in the experiment. Each cluster shows a distinct trend where the genes in the cluster are potentially co-regulated.

Try this with different size k . Perhaps go back to choose more genes (using a smaller cutoff for sd).

17.8. Summary

In this lesson, we have learned how to use k-means clustering to identify groups of genes that behave similarly over time. We have also learned how to subset our data to focus on the most informative genes.

Part V.

Machine Learning

18. Introduction

Machine learning represents a fundamental shift in how we approach problem-solving with computers. Rather than explicitly programming every rule and decision path, machine learning allows algorithms to discover patterns in data and make predictions or decisions based on these learned patterns. This approach has proven particularly powerful for complex problems where traditional rule-based programming becomes unwieldy or where the underlying patterns are too subtle for humans to easily codify.

At its core, machine learning is about generalization. We want to build models that can take what they've learned from historical data and apply that knowledge to new, previously unseen situations. This capability makes machine learning invaluable across diverse fields, from predicting stock prices and diagnosing diseases to recognizing speech and recommending movies.

Machine learning in biology is a really broad topic. Greener et al. (2022) present a nice overview of the different types of machine learning methods that are used in biology. Libbrecht and Noble (2015) also present an early review of machine learning in genetics and genomics.

18.1. Types of Machine Learning

The field of machine learning encompasses several distinct approaches, each suited to different types of problems and data structures. Understanding these categories helps practitioners choose appropriate methods and set realistic expectations for their projects.

Supervised learning forms the foundation of most practical machine learning applications. In supervised learning, we have access to both input features and the correct answers (labels or targets) for our training examples. The algorithm learns to map inputs to outputs by studying these example pairs. Classification problems, where we predict discrete categories, and regression problems, where we predict continuous numerical values, both fall under supervised learning. For instance, predicting whether an email is spam (classification) or forecasting house prices (regression) are classic supervised learning tasks.

Unsupervised learning tackles scenarios where we have input data but no predetermined correct answers. Instead of learning to predict specific outputs, unsupervised algorithms

18. Introduction

seek to discover hidden structures or patterns within the data itself. Clustering algorithms group similar data points together, while dimensionality reduction techniques identify the most important underlying factors that explain variation in the data. These methods often serve as exploratory tools, helping analysts understand their data better before applying supervised techniques.

Reinforcement learning takes a different approach entirely, focusing on learning through interaction with an environment. Rather than learning from fixed examples, reinforcement learning agents take actions and receive rewards or penalties, gradually improving their decision-making through trial and error. This approach has achieved remarkable success in game-playing scenarios and robotics, though it requires specialized techniques and considerable computational resources.

Learning Type	Data Requirements	Goal	Common Applications
Supervised	Input-output pairs	Predict labels/values	Classification, regression
Unsupervised	Input data only	Discover patterns	Clustering, dimensionality reduction
Reinforcement	Environment interaction	Optimize decisions	Game playing, robotics

When thinking about machine learning, it can help to have a simple framework in mind. In Figure 18.1, we present a simple view of machine learning according to the [scikit-learn](#) package.

Terminology and Concepts

- **Data** Data is the foundation of machine learning and can be structured (tabular) or unstructured (text, images, audio). It is usually divided into training, validation, and testing sets for model development and evaluation.
- **Features** Features are the variables or attributes used to describe the data points. Feature engineering and selection are crucial steps in machine learning to improve model performance and interpretability.
- **Models and Algorithms** Models are mathematical representations of the relationship between features and the target variable(s). Algorithms are the methods used to train models, such as linear regression, decision trees, and neural networks.

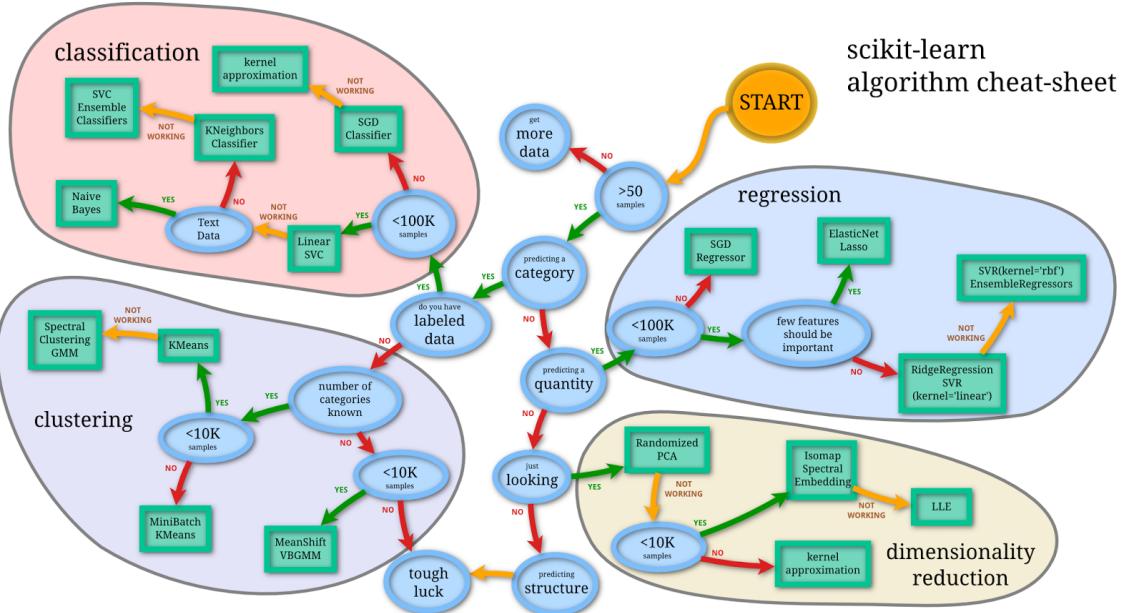


Figure 18.1.: A simple view of machine learning according the sklearn.

- **Hyperparameters and Tuning** Hyperparameters are adjustable parameters that control the learning process of an algorithm. Tuning involves finding the optimal set of hyperparameters to improve model performance.
- **Evaluation Metrics** Evaluation metrics quantify the performance of a model, such as accuracy, precision, recall, F1-score (for classification), and mean squared error, R-squared (for regression).

18.2. The Machine Learning Workflow

Successful machine learning projects follow a structured workflow that ensures robust, reliable results. This process begins long before any algorithms are trained and extends well beyond initial model development.

The Machine Learning Workflow

In a nutshell, the machine learning workflow consists of the following steps:

1. **Problem Definition:** Clearly define the problem and determine if machine learning is the right approach.
2. **Data Collection and Preparation:** Gather relevant data and preprocess it to make it suitable for modeling.
3. **Data Splitting:** Divide the data into training, validation, and test sets to ensure unbiased evaluation.
4. **Model Selection:** Choose the appropriate machine learning algorithm and configure its hyperparameters.
5. **Training:** Fit the model to the training data, allowing it to learn patterns and relationships.
6. **Evaluation:** Assess model performance using validation data and appropriate metrics.
7. **Deployment:** Integrate the model into production systems for real-world use.

The journey starts with problem definition, where practitioners must clearly articulate what they're trying to achieve and whether machine learning is the appropriate solution. Not every problem requires machine learning; sometimes simpler statistical methods or rule-based systems provide better solutions with less complexity and maintenance overhead.

Data collection and preparation typically consume the majority of time in real-world projects. Raw data rarely arrives in a format suitable for machine learning algorithms. Common preprocessing steps include handling missing values, encoding categorical variables, scaling numerical features, and addressing outliers. The quality of this preprocessing often determines the success or failure of the entire project.

Data splitting deserves special attention because it directly impacts the reliability of your results. The training set teaches the algorithm, but if we evaluate performance on the same data used for training, we get an overly optimistic view of how well our model will perform on new data. This is analogous to letting students see exam questions while studying and then using the same questions for the actual exam.

The Critical Importance of Data Splitting

One of the most crucial steps in the machine learning workflow is properly splitting your data into separate sets for training, validation, and testing. This separation serves as the foundation for honest evaluation and prevents overfitting.

- **Training data** is used to fit the model parameters.

- **Validation data** helps select the best model architecture and hyperparameters.
- **Test data** provides a final, unbiased estimate of model performance on new data.

The golden rule: never use test data for any decision-making during model development. Reserve it exclusively for final evaluation.

A common approach involves splitting data into 80% for training and 20% for testing. For more complex projects, a three-way split might use 60% for training, 20% for validation (model selection), and 20% for final testing. Cross-validation provides an alternative approach where the training data is repeatedly split into smaller training and validation sets, providing more robust estimates of model performance while still preserving an untouched test set.

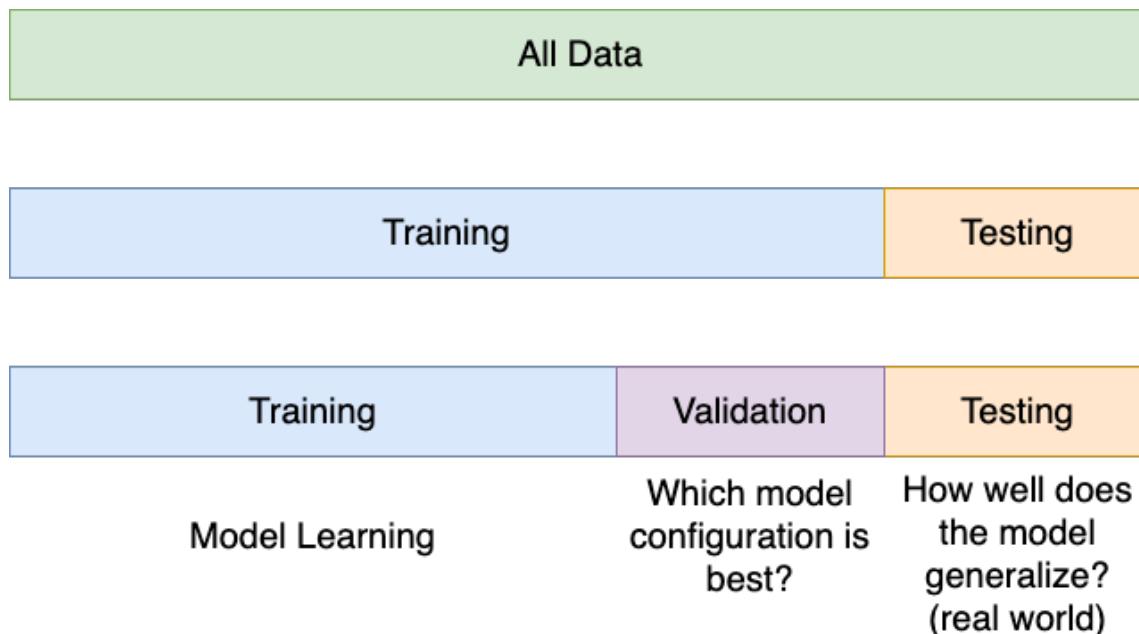


Figure 18.2.: Data splitting and train/validate/test paradigm. For models without “hyperparameters”, only the training/testing sets are necessary. For models that require learning model *structure* (such as the k in k-nearest-neighbor) as well as model parameters (like betas in linear regression), a separate validation set is essential.

Model selection involves choosing both the type of algorithm and its specific configuration. Different algorithms make different assumptions about the data and excel in different scenarios. Linear models work well when relationships are approximately linear and

18. Introduction

interpretability is important. Tree-based methods handle nonlinear relationships and interactions naturally but may overfit with limited data. Neural networks can model complex patterns but require large datasets and careful tuning. Hyperparameters are the parameters that describe the details of the model such as the depth of a decision tree, the choice of k in k -nearest neighbors, or the learning rate in gradient descent. Hyperparameter tuning is the process of finding the best values for these parameters, often using techniques like grid search or random search combined with cross-validation.

Training is where the algorithm actually learns from the data. During this phase, the model adjusts its internal parameters to minimize prediction errors on the training set. However, the goal isn't to achieve perfect performance on training data. Models that fit training data too closely often fail to generalize to new examples, a problem known as overfitting.

Evaluation determines whether our model is ready for deployment. This involves multiple metrics beyond simple accuracy, including precision, recall, F1-score for classification, or mean squared error and R-squared for regression. We also examine model behavior across different subgroups in our data to ensure fair and consistent performance.

18.3. Understanding Overfitting and Underfitting

Recall that the goal of machine learning is to build models that generalize well to new, unseen data. Any model that is complex enough can perfectly model data given to it. However, achieving this balance between fitting the training data and maintaining good performance on *new examples* (ie., generalization) is the goal, not just performing well on the training data.

The concept of overfitting represents one of the central challenges in machine learning. When a model overfits, it learns the training data too well, memorizing specific examples rather than generalizing patterns. This results in excellent performance on training data but poor performance on new, unseen data.

Imagine teaching someone to recognize cats by showing them 100 photos. An overfitted learner might memorize every pixel of those specific photos rather than learning general features like whiskers, pointed ears, and fur patterns. When shown new cat photos, they would struggle because they focused on irrelevant details specific to the training images.

Underfitting represents the opposite problem. An underfitted model is too simple to capture the underlying patterns in the data. It performs poorly on both training and test data because it lacks the complexity needed to model the relationships present in the data. Continuing our cat recognition analogy, an underfitted model might only look at image brightness and miss all the important visual features that distinguish cats from other animals.

```

set.seed(123)
sinsim <- function(n,sd=0.1) {
  x <- seq(0,1,length.out=n)
  y <- sin(2*pi*x) + rnorm(n,0,sd)
  return(data.frame(x=x,y=y))
}
dat <- sinsim(100,0.25)
library(ggplot2)
library(patchwork)
p_base <- ggplot(dat,aes(x=x,y=y)) +
  geom_point(alpha=0.7) +
  theme_bw()
p_lm <- p_base +
  geom_smooth(method="lm", se=FALSE, alpha=0.6, formula = y ~ x)
p_lmsin <- p_base +
  geom_smooth(method="lm",formula=y~sin(2*pi*x), se=FALSE, alpha=0.6)
p_loess_wide <- p_base +
  geom_smooth(method="loess",span=0.5, se=FALSE, alpha=0.6, formula = y ~ x)
p_loess_narrow <- p_base +
  geom_smooth(method="loess",span=0.05, se=FALSE, alpha=0.6, formula = y ~ x)
p_lm + p_lmsin + p_loess_wide + p_loess_narrow + plot_layout(ncol=2) +
  plot_annotation(tag_levels = 'A') &
  theme(plot.tag = element_text(size = 8))

```

Warning in simpleLoess(y, x, w, span, degree = degree, parametric = parametric, : k-d tree limited by memory. ncmax= 200

Warning in sqrt(sum.squares/one.delta): NaNs produced

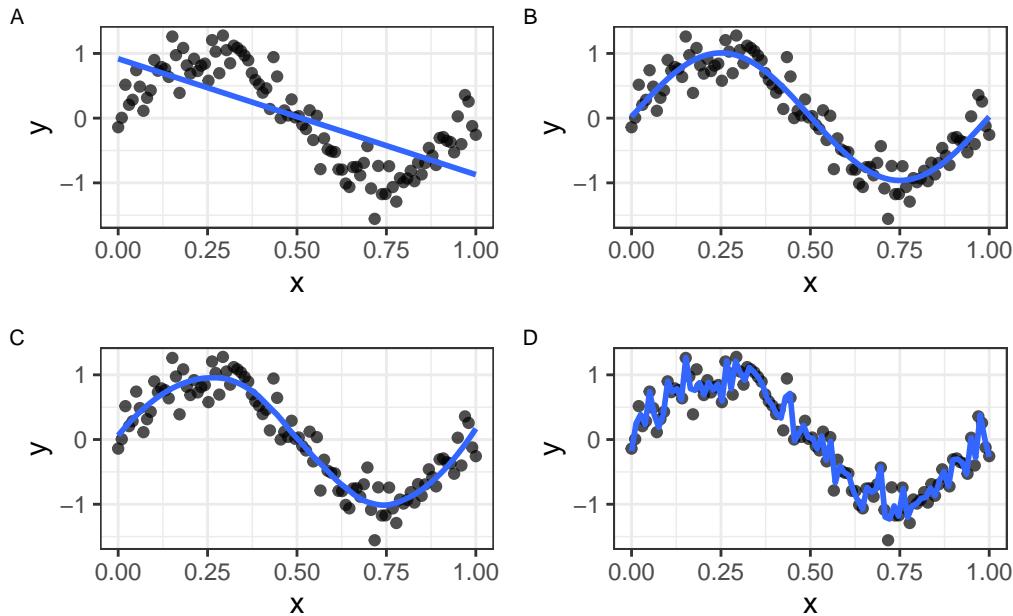


Figure 18.3.: Data simulated according to the function $f(x) = \sin(2\pi x) + N(0, 0.25)$ fitted with four different models. A) A simple linear model demonstrates *underfitting*. B) A linear model with a sin function ($y = \sin(2\pi x)$) and C) a loess model with a wide span (0.5) demonstrate *good fits*. D) A loess model with a narrow span (0.05) is a good example of *overfitting*.

In Figure 18.3, we simulate data according to the function $f(x) = \sin(2\pi x) + N(0, 0.25)$ and fit four different models. Choosing a model that is too simple (A) will result in *underfitting* the data, while choosing a model that is too complex (D) will result in *overfitting* the data. For model (D), the loess model with a narrow span, the fitted line follows the noise in the data too closely, capturing random fluctuations rather than the underlying trend. In contrast, models (B) and (C) demonstrate good fits, capturing the essential pattern without being overly complex.

The relationship between model complexity and performance often follows a characteristic U-shaped curve. Very simple models underperform due to underfitting. As complexity increases, performance improves as the model captures more relevant patterns. However, beyond an optimal point, additional complexity leads to overfitting and degraded performance on new data.

Detecting Overfitting

Overfitting reveals itself through a growing gap between training and validation performance. If your model achieves 95% accuracy on training data but only 70% on validation data, you're likely overfitting.

Monitor both training and validation metrics throughout model development. The best models show similar performance on both sets, indicating good generalization.

Several strategies help combat overfitting. Regularization techniques add penalties for model complexity, encouraging simpler solutions. Cross-validation provides more robust estimates of model performance by training and validating on multiple data splits. Early stopping halts training when validation performance begins to degrade, even if training performance continues improving. Feature selection reduces the number of input variables, focusing the model on the most relevant information.

The bias-variance tradeoff provides a theoretical framework for understanding these phenomena. Bias refers to systematic errors due to overly simple models, while variance refers to sensitivity to small changes in training data. High-bias models underfit, while high-variance models overfit. The optimal model balances these competing sources of error.

18.4. Cross-Validation and Model Selection

Cross-validation addresses a fundamental challenge in machine learning: how do we reliably estimate model performance when we have limited data? Simple train-test splits can be misleading, especially with small datasets, because performance estimates depend heavily on which specific examples end up in each set.

K-fold cross-validation provides a more robust solution. The training data is divided into k equal-sized subsets (folds). The model is trained k times, each time using $k-1$ folds for training and the remaining fold for validation. This process yields k performance estimates, which can be averaged to get a more stable assessment of model quality.

Five-fold and ten-fold cross-validation are common choices, providing good balance between computational efficiency and reliable estimates. Leave-one-out cross-validation represents an extreme case where k equals the number of training examples. While this maximizes the use of training data, it can be computationally expensive and may provide overly optimistic estimates for some types of models.

Stratified cross-validation ensures that each fold maintains the same proportion of examples from each class, which is particularly important for classification problems with imbalanced datasets. Time series data requires special consideration, as temporal order matters. Time

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series cross-validation uses only past data to predict future values, respecting the temporal structure.

Cross-validation serves multiple purposes in the model development process. It helps select the best algorithm from a set of candidates, tune hyperparameters within a chosen algorithm, and provide realistic estimates of expected performance on new data. However, it's crucial to remember that cross-validation results still come from the training data. Final model evaluation should always use a completely separate test set.

19. Supervised Learning

In the previous chapter, we introduced the three main paradigms of machine learning: supervised, unsupervised, and reinforcement learning. We also highlighted the importance of a structured workflow, particularly the critical step of data splitting to prevent overfitting. Now, we'll dive deeper into the world of **supervised learning**, the most common and widely applied category of machine learning.

This chapter provides a practical framework for understanding how different supervised learning algorithms work. Instead of viewing each algorithm as a completely separate entity, we'll see that they all share a common conceptual structure. By grasping this structure, you can more easily understand, compare, and select the right algorithm for your problem. We will then use this framework to explore some of the most fundamental and popular algorithms for both regression and classification tasks.

19.1. A Framework for Understanding Supervised Algorithms

At a high level, every supervised learning algorithm can be understood as having three core components: the **hypothesis space**, the **objective function**, and the **learning algorithm**. Thinking about new algorithms in terms of these three parts can demystify how they operate and highlight their key differences.

The Three Pillars of a Supervised Algorithm

1. **Hypothesis Space (The Model Family):** This is the set of all possible models the algorithm is allowed to consider. For example, in linear regression, the hypothesis space is the set of all possible straight lines. For a decision tree, it's the set of all possible branching rules. The choice of hypothesis space imposes a certain structure or *bias* on the solution.
2. **Objective Function (The Goal):** This function defines what a “good” model looks like. It measures how well a particular model from the hypothesis space fits the training data. For instance, in regression, a common objective function is the *Mean Squared Error (MSE)*, which penalizes models for making large

prediction errors. The goal of learning is to find the model that minimizes this objective function.

3. **Learning Algorithm (The Optimizer):** This is the computational procedure used to search through the hypothesis space and find the model that best minimizes the objective function. This could be a straightforward mathematical formula (as in simple linear regression) or a complex iterative process (as in training neural networks).

By framing algorithms in this way, we can see, for example, that Ridge and Lasso regression share the same hypothesis space and learning algorithm as linear regression but differ in their objective function, which includes a penalty for complexity. This small change in the objective function has profound effects on the final model, helping to prevent overfitting.

19.2. Supervised Learning

19.2.1. Linear regression

In [statistics](#), **linear regression** is a [linear](#) approach for modelling the relationship between a [scalar](#) response and one or more explanatory variables (also known as [dependent](#) and [independent variables](#)). The case of one explanatory variable is called [*simple linear regression*](#); for more than one, the process is called **multiple linear regression**. This term is distinct from [*multivariate linear regression*](#), where multiple [correlated](#) dependent variables are predicted, rather than a single scalar variable.

In linear regression, the relationships are modeled using [linear predictor functions](#) whose unknown model [parameters](#) are [estimated](#) from the [data](#). Such models are called [linear models](#). Most commonly, the [conditional mean](#) of the response given the values of the explanatory variables (or predictors) is assumed to be an [affine function](#) of those values; less commonly, the conditional [median](#) or some other [quantile](#) is used. Like all forms of [regression analysis](#), linear regression focuses on the [conditional probability distribution](#) of the response given the values of the predictors, rather than on the [joint probability distribution](#) of all of these variables, which is the domain of [multivariate analysis](#).

Linear regression was the first type of regression analysis to be studied rigorously, and to be used extensively in practical applications. This is because models which depend linearly on their unknown parameters are easier to fit than models which are non-linearly related to their parameters and because the statistical properties of the resulting estimators are easier to determine.

19.2.2. K-nearest Neighbor

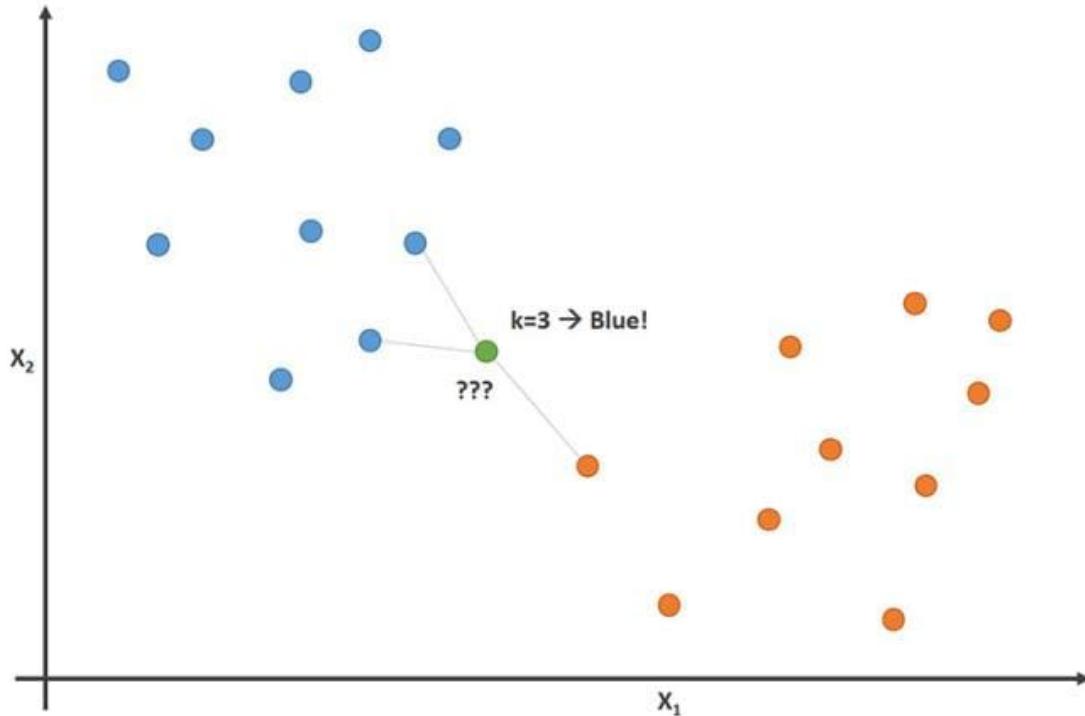


Figure 19.1.: **Figure.** The k-nearest neighbor algorithm can be used for regression or classification.

The **k-nearest neighbors algorithm (k-NN)** is a [non-parametric supervised learning](#) method first developed by [Evelyn Fix](#) and [Joseph Hodges](#) in 1951, and later expanded by [Thomas Cover](#). It is used for [classification](#) and [regression](#). In both cases, the input consists of the k closest training examples in a [data set](#).

The k-nearest neighbor (k-NN) algorithm is a simple, yet powerful, supervised machine learning method used for classification and regression tasks. It is an instance-based, non-parametric learning method that stores the entire training dataset and makes predictions based on the similarity between data points. The underlying principle of the k-NN algorithm is that similar data points (those that are close to each other in multidimensional space) are likely to have similar outcomes or belong to the same class.

Here's a description of how the k-NN algorithm works:

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1. Determine the value of k: The first step is to choose the number of nearest neighbors (k) to consider when making predictions. The value of k is a user-defined hyperparameter and can significantly impact the algorithm's performance. A small value of k can lead to overfitting, while a large value may result in underfitting.
2. Compute distance: Calculate the distance between the new data point (query point) and each data point in the training dataset. The most common distance metrics used are Euclidean, Manhattan, and Minkowski distance. The choice of distance metric depends on the problem and the nature of the data.
3. Find k -nearest neighbors: Identify the k data points in the training dataset that are closest to the query point, based on the chosen distance metric.
4. Make predictions: Once the k -nearest neighbors are identified, the final step is to make predictions. The prediction for the query point can be made in two ways:
 - a. For classification, determine the class labels of the k -nearest neighbors and assign the class label with the highest frequency (majority vote) to the query point. In case of a tie, one can choose the class with the smallest average distance to the query point or randomly select one among the tied classes.
 - b. For regression tasks, the k -NN algorithm follows a similar process, but instead of majority voting, it calculates the mean (or median) of the target values of the k -nearest neighbors and assigns it as the prediction for the query point.

The k -NN algorithm is known for its simplicity, ease of implementation, and ability to handle multi-class problems. However, it has some drawbacks, such as high computational cost (especially for large datasets), sensitivity to the choice of k and distance metric, and poor performance with high-dimensional or noisy data. Scaling and preprocessing the data, as well as using dimensionality reduction techniques, can help mitigate some of these issues.

- In *k -NN classification*, the output is a class membership. An object is classified by a plurality vote of its neighbors, with the object being assigned to the class most common among its k nearest neighbors (k is a positive [integer](#), typically small). If $k = 1$, then the object is simply assigned to the class of that single nearest neighbor.
- In *k -NN regression*, the output is the property value for the object. This value is the average of the values of k nearest neighbors.

k -NN is a type of [classification](#) where the function is only approximated locally and all computation is deferred until function evaluation. Since this algorithm relies on distance for classification, if the features represent different physical units or come in vastly different scales then [normalizing](#) the training data can improve its accuracy dramatically.

Both for classification and regression, a useful technique can be to assign weights to the contributions of the neighbors, so that the nearer neighbors contribute more to the average

than the more distant ones. For example, a common weighting scheme consists in giving each neighbor a weight of $1/d$, where d is the distance to the neighbor.

The neighbors are taken from a set of objects for which the class (for k -NN classification) or the object property value (for k -NN regression) is known. This can be thought of as the training set for the algorithm, though no explicit training step is required.

19.3. Penalized regression

Adapted from <http://www.sthda.com/english/articles/37-model-selection-essentials-in-r/153-penalized-regression-essentials-ridge-lasso-elastic-net/>.

Penalized regression is a type of regression analysis that introduces a penalty term to the loss function in order to prevent overfitting and improve the model's ability to generalize. Remember that in regression, the *loss* function is the sum of squares Equation 19.1.

$$L = \sum_{i=0}^n (\hat{y}_i - y_i)^2 \quad (19.1)$$

In Equation 19.1, \hat{y}_i is the predicted output, y_i is the actual output, and n is the number of observations. The goal of regression is to minimize the loss function by finding the optimal values of the model parameters or coefficients. The model parameters are estimated using the training data. The model is then evaluated using the test data. If the model performs well on the training data but poorly on the test data, it is said to be overfit. Overfitting occurs when the model learns the training data too well, including the noise, and is not able to generalize well to new data. This is a common problem in machine learning, particularly when there are a large number of predictors compared to the number of observations, and can be addressed by penalized regression.

The two most common types of penalized regression are Ridge Regression (L2 penalty) and LASSO Regression (L1 penalty). Both Ridge and LASSO help to reduce model complexity and prevent over-fitting which may result from simple linear regression. However, the choice between Ridge and LASSO depends on the situation and the dataset at hand. If feature selection is important for the interpretation of the model, LASSO might be preferred. If the goal is prediction accuracy and the model needs to retain all features, Ridge might be the better choice.

19.3.1. Ridge regression

Ridge regression shrinks the regression coefficients, so that variables, with minor contribution to the outcome, have their coefficients close to zero. The shrinkage of the coefficients is achieved by penalizing the regression model with a penalty term called L2-norm, which is the sum of the squared coefficients. The amount of the penalty can be fine-tuned using a constant called lambda (λ). Selecting a good value for λ is critical. When $\lambda=0$, the penalty term has no effect, and ridge regression will produce the classical least square coefficients. However, as λ increases to infinite, the impact of the shrinkage penalty grows, and the ridge regression coefficients will get close zero. The loss function for Ridge Regression is:

$$L = \sum_{i=0}^n (\hat{y}_i - y_i)^2 + \lambda \sum_{j=0}^k \beta_j^2 \quad (19.2)$$

Here, \hat{y}_i is the predicted output, y_i is the actual output, β_j represents the model parameters or coefficients, and λ is the regularization parameter. The second term, $\sum_j \beta_j^2$, is the penalty term where all parameters are squared and summed. Ridge regression tends to shrink the coefficients but doesn't necessarily zero them.

Note that, in contrast to the ordinary least square regression, ridge regression is highly affected by the scale of the predictors. Therefore, it is better to standardize (i.e., scale) the predictors before applying the ridge regression (James et al. 2014), so that all the predictors are on the same scale. The standardization of a predictor x , can be achieved using the formula $x' = \frac{x}{sd(x)}$, where $sd(x)$ is the standard deviation of x . The consequence of this is that, all standardized predictors will have a standard deviation of one allowing the final fit to not depend on the scale on which the predictors are measured.

One important advantage of the ridge regression, is that it still performs well, compared to the ordinary least square method (see Equation 19.1), in a situation where you have a large multivariate data with the number of predictors (p) larger than the number of observations (n). One disadvantage of the ridge regression is that, it will include all the predictors in the final model, unlike the stepwise regression methods, which will generally select models that involve a reduced set of variables. Ridge regression shrinks the coefficients towards zero, but it will not set any of them exactly to zero. The LASSO regression is an alternative that overcomes this drawback.

19.3.2. LASSO regression

LASSO stands for *Least Absolute Shrinkage and Selection Operator*. It shrinks the regression coefficients toward zero by penalizing the regression model with a penalty term called

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L1-norm, which is the sum of the absolute coefficients. In the case of LASSO regression, the penalty has the effect of forcing some of the coefficient estimates, with a minor contribution to the model, to be exactly equal to zero. This means that, LASSO can be also seen as an alternative to the subset selection methods for performing variable selection in order to reduce the complexity of the model. As in ridge regression, selecting a good value of λ for the LASSO is critical. The loss function for LASSO Regression is:

$$L = \sum_{i=0}^n (\hat{y}_i - y_i)^2 + \lambda \sum_{j=0}^k |\beta_j| \quad (19.3)$$

Similar to Ridge, \hat{y}_i is the predicted output, y_i is the actual output, j represents the model parameters or coefficients, and λ is the regularization parameter. The second term, $|\beta_j|$, is the penalty term where the absolute values of all parameters are summed. LASSO regression tends to shrink the coefficients and can zero out some of them, effectively performing variable selection.

One obvious advantage of LASSO regression over ridge regression, is that it produces simpler and more interpretable models that incorporate only a reduced set of the predictors. However, neither ridge regression nor the LASSO will universally dominate the other. Generally, LASSO might perform better in a situation where some of the predictors have large coefficients, and the remaining predictors have very small coefficients. Ridge regression will perform better when the outcome is a function of many predictors, all with coefficients of roughly equal size (James et al. 2014).

Cross-validation methods can be used for identifying which of these two techniques is better on a particular data set.

19.3.3. Elastic Net

Elastic Net produces a regression model that is penalized with both the L1-norm and L2-norm. The consequence of this is to effectively shrink coefficients (like in ridge regression) and to set some coefficients to zero (as in LASSO).

19.3.4. Classification and Regression Trees (CART)

[Decision Tree Learning](#) is supervised learning approach used in statistics, data mining and machine learning. In this formalism, a classification or regression decision tree is used as a predictive model to draw conclusions about a set of observations. Decision trees are a popular machine learning method used for both classification and regression tasks. They are hierarchical, tree-like structures that model the relationship between features and the

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target variable by recursively splitting the data into subsets based on the feature values. Each internal node in the tree represents a decision or test on a feature, and each branch represents the outcome of that test. The leaf nodes contain the final prediction, which is the majority class for classification tasks or the mean/median of the target values for regression tasks.

Here's an overview of the decision tree learning process:

- Select the best feature and split value: Start at the root node and choose the feature and split value that results in the maximum reduction of impurity (or increase in information gain) in the child nodes. For classification tasks, impurity measures like Gini index or entropy are commonly used, while for regression tasks, mean squared error (MSE) or mean absolute error (MAE) can be used.
- Split the data: Partition the dataset into subsets based on the chosen feature and split value.
- Recursion: Repeat steps 1 and 2 for each subset until a stopping criterion is met. Stopping criteria can include reaching a maximum tree depth, a minimum number of samples per leaf, or no further improvement in impurity.
- Prune the tree (optional): To reduce overfitting, decision trees can be pruned by removing branches that do not significantly improve the model's performance on the validation dataset. This can be done using techniques like reduced error pruning or cost-complexity pruning.

Decision trees have several advantages, such as:

- **Interpretability** They are easy to understand, visualize, and explain, even for non-experts.
- **Minimal data preprocessing** Decision trees can handle both numerical and categorical data, and they are robust to outliers and missing values.
- **Non-linear relationships** They can capture complex non-linear relationships between features and the target variable.

However, decision trees also have some drawbacks:

- **Overfitting** They are prone to overfitting, especially when the tree is deep or has few samples per leaf. Pruning and setting stopping criteria can help mitigate this issue.
- **Instability** Small changes in the data can lead to different tree structures. This can be addressed by using ensemble methods like random forests or gradient boosting machines (GBMs).

Survival of passengers on the Titanic

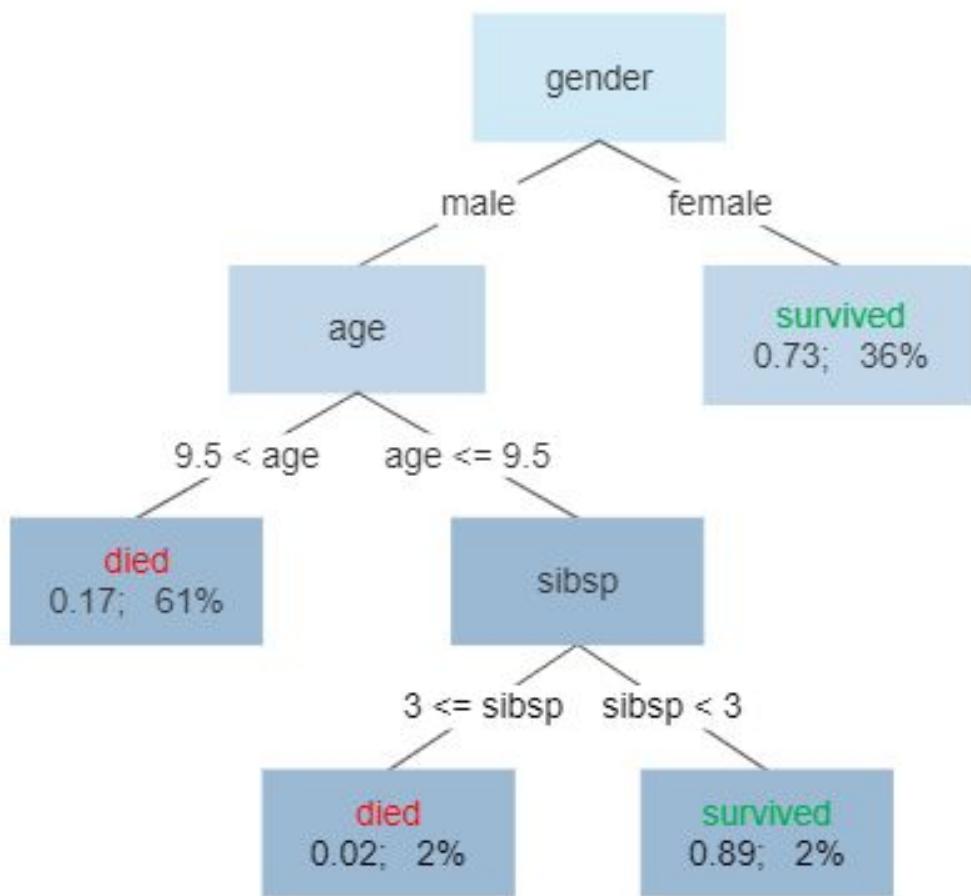


Figure 19.2.: Graphical representation of a decision tree.

19. Supervised Learning

- **Greedy learning** Decision tree algorithms use a greedy approach, meaning they make locally optimal choices at each node. This may not always result in a globally optimal tree.

Despite these limitations, decision trees are widely used in various applications due to their simplicity, interpretability, and ability to handle diverse data types.

19.3.5. RandomForest

Random forests or **random decision forests** is an [ensemble learning](#) method for [classification](#), [regression](#) and other tasks that operates by constructing a multitude of [decision trees](#) at training time. For classification tasks, the output of the random forest is the class selected by most trees. For regression tasks, the mean or average prediction of the individual trees is returned. Random decision forests correct for decision trees' habit of [overfitting](#) to their [training set](#). Random forests generally outperform [decision trees](#), but their accuracy is lower than gradient boosted trees [[citation needed](#)]. However, data characteristics can affect their performance.

The first algorithm for random decision forests was created in 1995 by [Tin Kam Ho](#) using the [random subspace method](#), which, in Ho's formulation, is a way to implement the "stochastic discrimination" approach to classification proposed by Eugene Kleinberg.

An extension of the algorithm was developed by [Leo Breiman](#) and [Adele Cutler](#), who registered "Random Forests" as a [trademark](#) in 2006 (as of 2019[[update](#)], owned by [Minitab, Inc.](#)). The extension combines Breiman's "bagging" idea and random selection of features, introduced first by Ho and later independently by Amit and [Geman](#) in order to construct a collection of decision trees with controlled variance.

Random forests are frequently used as "blackbox" models in businesses, as they generate reasonable predictions across a wide range of data while requiring little configuration.

Random Forest Simplified

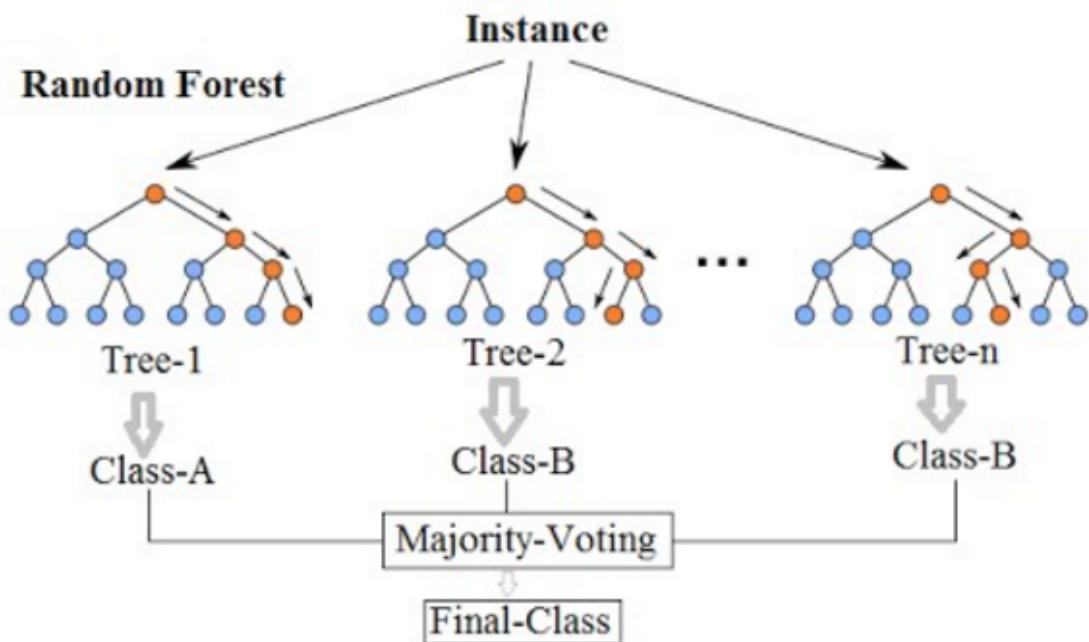


Figure 19.3.: Graphical representation of random forests.

20. The mlr3verse

The R ecosystem offers numerous packages for machine learning, each with its own interface, conventions, and capabilities. While this diversity provides flexibility, it also creates challenges for practitioners who must learn different APIs for different algorithms and spend time on repetitive data preparation tasks. The mlr3verse addresses these challenges by providing a unified, consistent framework for machine learning in R.

20.1. The Philosophy of mlr3verse

The mlr3verse follows a modular design philosophy that separates different aspects of the machine learning workflow into distinct, interchangeable components. This separation of concerns makes it easier to experiment with different combinations of preprocessing steps, algorithms, and evaluation strategies without rewriting code.

Rather than monolithic functions that handle everything from data preprocessing to model evaluation, mlr3verse provides specialized objects for each component of the machine learning pipeline. Tasks define the problem and data, learners implement algorithms, measures specify evaluation metrics, and resamplings control validation strategies. This modular approach promotes code reusability and makes it easier to understand and maintain complex machine learning workflows.

The framework emphasizes object-oriented design, leveraging R6 classes to provide consistent interfaces across different components. This design ensures that similar operations work the same way regardless of which specific algorithm or evaluation metric you're using. Once you learn the basic patterns, you can easily work with new algorithms and techniques.

Reproducibility receives special attention in mlr3verse. All random operations can be controlled through seed settings, and the framework provides tools to track and reproduce experimental results. This focus on reproducibility is essential for scientific applications and helps practitioners debug and iterate on their models.

20.2. The *mlr3verse* Ecosystem

The *mlr3verse* consists of several interconnected packages, each focused on specific aspects of machine learning. Understanding these components helps practitioners choose the right tools for their projects and leverage the full power of the ecosystem.

Package	Purpose	Key Features
<code>mlr3</code>	Core framework	Tasks, learners, measures, resampling
<code>mlr3learners</code>	Extended algorithms	Additional ML algorithms beyond base <code>mlr3</code>
<code>mlr3pipelines</code>	Preprocessing & pipelines	Feature engineering, model stacking
<code>mlr3tuning</code>	Hyperparameter optimization	Grid search, random search, Bayesian optimization
<code>mlr3measures</code>	Additional metrics	Extended evaluation measures
<code>mlr3viz</code>	Visualization	Plotting utilities for models and results
<code>mlr3filters</code>	Feature selection	Filter-based feature selection methods

The core `mlr3` package provides the foundation, implementing basic tasks, learners, and evaluation procedures. It includes common algorithms like linear regression, logistic regression, and decision trees, along with fundamental evaluation metrics and resampling strategies.

`mlr3learners` extends the available algorithms significantly, providing interfaces to popular R packages like `randomForest`, `glmnet`, and `xgboost`. This extension allows practitioners to access state-of-the-art algorithms while maintaining the consistent `mlr3` interface.

`mlr3pipelines` introduces powerful preprocessing and model composition capabilities. It allows users to chain together multiple preprocessing steps, combine different algorithms, and create complex model architectures. This package particularly shines in scenarios requiring sophisticated feature engineering or ensemble methods.

`mlr3tuning` automates the search for optimal hyperparameters, implementing various optimization strategies from simple grid search to sophisticated Bayesian optimization. Hyperparameter tuning can dramatically improve model performance, but it requires careful validation to avoid overfitting.

20.3. Core mlr3 Concepts and Objects

The mlr3 framework organizes machine learning workflows around four fundamental object types:

- **Tasks** provide the data and problem definition.
- **Learners** implement the algorithms.
- **Measures** evaluate performance.
- **Resamplings** ensure robust validation.

Understanding these objects and how they interact forms the foundation for effective use of the mlr3verse. The goal is to provide a consistent, reusable interface for machine learning tasks, allowing practitioners to focus on solving problems rather than learning different APIs.

Tasks encapsulate the machine learning problem, combining data with metadata about the prediction target and feature types. Classification tasks specify categorical targets, while regression tasks involve continuous targets. Tasks handle many routine data management operations automatically, such as identifying feature types and managing factor levels. They also provide methods for data manipulation, including filtering rows, selecting features, and creating subsets.

```
Loading required package: mlr3
```

```
# Create a classification task with Palmer Penguins data
task <- as_task_classif(penguins, target = "species")

# Examine task properties
task$nrow # Number of observations
```

```
[1] 333
```

```
task$ncol # Number of features
```

```
[1] 8
```

```
task$feature_names # Names of predictor variables
```

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```
[1] "bill_depth_mm"      "bill_length_mm"      "body_mass_g"  
[4] "flipper_length_mm"  "island"              "sex"  
[7] "year"
```

```
task$target_names # Name of target variable
```

```
[1] "species"
```

Learners implement machine learning algorithms, providing a consistent interface regardless of the underlying implementation. Each learner specifies its capabilities, including which task types it supports, whether it can handle missing values, and what hyperparameters are available for tuning. Learners maintain information about their training state and can generate predictions on new data.

The learner registry provides a convenient way to discover available algorithms. You can query the registry to find learners for specific task types or search for algorithms with particular capabilities.

```
# Explore available classification learners  
classif_learners <- mlr_learners$keys("classif")  
head(classif_learners, 10)
```

```
[1] "classif.cv_glmnet"    "classif.debug"        "classif.featureless"  
[4] "classif.glmnet"       "classif.kknn"         "classif.lda"  
[7] "classif.log_reg"      "classif.multinom"     "classif.naive_bayes"  
[10] "classif.nnet"
```

```
# Examine a specific learner  
rpart_learner <- lrn("classif.rpart")  
rpart_learner$param_set$ids() # Available hyperparameters
```

```
[1] "cp"                  "keep_model"        "maxcompete"      "maxdepth"  
[5] "maxsurrogate"        "minbucket"        "minsplit"        "surrogatestyle"  
[9] "usesurrogate"        "xval"
```

Learner Naming Convention

mlr3 uses a consistent naming scheme for learners: `[task_type].[algorithm]`. For example, `classif.rpart` implements decision trees for classification, while `regr.lm` provides linear regression. This naming makes it easy to find appropriate algorithms for your task type.

Measures define evaluation metrics for assessing model performance. Different measures emphasize different aspects of model quality, and the choice of measure can significantly impact model selection and hyperparameter tuning. Classification measures include accuracy, precision, recall, and F1-score, while regression measures encompass mean squared error, mean absolute error, and R-squared.

```
# Common classification measures
acc_measure <- msr("classif.acc") # Accuracy
ce_measure <- msr("classif.ce") # Classification error
auc_measure <- msr("classif.auc") # Area under ROC curve
```

Resamplings control how data is split for training and validation. They implement various strategies including simple holdout splits, k-fold cross-validation, and bootstrap sampling. The choice of resampling strategy affects both the reliability of performance estimates and computational requirements.

```
# Different resampling strategies
holdout <- rsmp("holdout", ratio = 0.8) # 80/20 split
cv5 <- rsmp("cv", folds = 5) # 5-fold cross-validation
bootstrap <- rsmp("bootstrap", repeats = 30) # Bootstrap sampling

# Examine resampling properties
cv5$param_set
```

	<code>id</code>	<code>class</code>	<code>lower</code>	<code>upper</code>	<code>nlevels</code>	<code>default</code>	<code>value</code>
	<code><char></code>	<code><char></code>	<code><int></code>	<code><num></code>	<code><num></code>	<code><list></code>	<code><list></code>
1:	<code>folds</code>	<code>ParamInt</code>	2	<code>Inf</code>	<code>Inf</code>	<code><NoDefault[0]></code>	5

These four object types work together to create complete machine learning workflows. Tasks provide the data and problem definition, learners implement the algorithms, measures evaluate performance, and resamplings ensure robust validation. This modular design

20. The mlr3verse

allows practitioners to mix and match components easily, experimenting with different combinations to find optimal solutions for their specific problems.

The interaction between these objects follows predictable patterns. Learners train on tasks, producing fitted models that can generate predictions. These predictions are evaluated using measures, with resampling strategies ensuring that evaluation results generalize beyond the specific training data used. Understanding these interactions enables practitioners to build sophisticated machine learning pipelines while maintaining clear, readable code.

! Key Advantages of mlr3verse

The mlr3verse provides several crucial advantages for machine learning practitioners:

Consistency: All algorithms use the same interface, reducing learning overhead and making code more maintainable.

Flexibility: Modular design allows easy experimentation with different combinations of preprocessing, algorithms, and evaluation strategies.

Reproducibility: Built-in support for controlling randomness and tracking experimental results.

Extensibility: Easy to add new algorithms, measures, and preprocessing steps while maintaining compatibility with existing code.

Best Practices: Framework encourages proper practices like train/test splitting and cross-validation through its core design.

This foundation in mlr3verse concepts prepares practitioners to tackle real machine learning problems with confidence. The consistent interfaces and modular design reduce the cognitive load associated with learning new algorithms, allowing focus on the more important aspects of problem-solving: understanding the data, choosing appropriate methods, and interpreting results. In the hands-on sections that follow, these concepts will come together to demonstrate how mlr3verse facilitates efficient, robust machine learning workflows.

21. Examples

21.1. Overview

In this chapter, we focus on practical aspects of machine learning. The goal is to provide a hands-on introduction to the application of machine learning techniques to real-world data. While the theoretical foundations of machine learning are important, the ability to apply these techniques to solve practical problems is equally crucial. In this chapter, we will use the `mlr3` package in R to build and evaluate machine learning models for classification and regression tasks.

We will use three examples to illustrate the machine learning workflow:

1. **Cancer types classification:** We will classify different types of cancer based on gene expression data.
2. **Age prediction from DNA methylation:** We will predict the chronological age of individuals based on DNA methylation patterns.
3. **Gene expression prediction:** We will predict gene expression levels based on histone modification data.

We'll be applying knn, decision trees, and random forests, linear regression, and penalized regression models to these datasets.

The `mlr3` R package is a modern, object-oriented machine learning framework in R that builds on the success of its predecessor, the `mlr` package. It provides a flexible and extensible platform for handling common machine learning tasks such as data preprocessing, model training, hyperparameter tuning, and model evaluation Figure 21.1. The package is designed to guide and standardize the process of using complex machine learning pipelines.

21.1.1. Key features of `mlr3`

- **Task abstraction** `mlr3` encapsulates different types of learning problems like classification, regression, and survival analysis into “Task” objects, making it easier to

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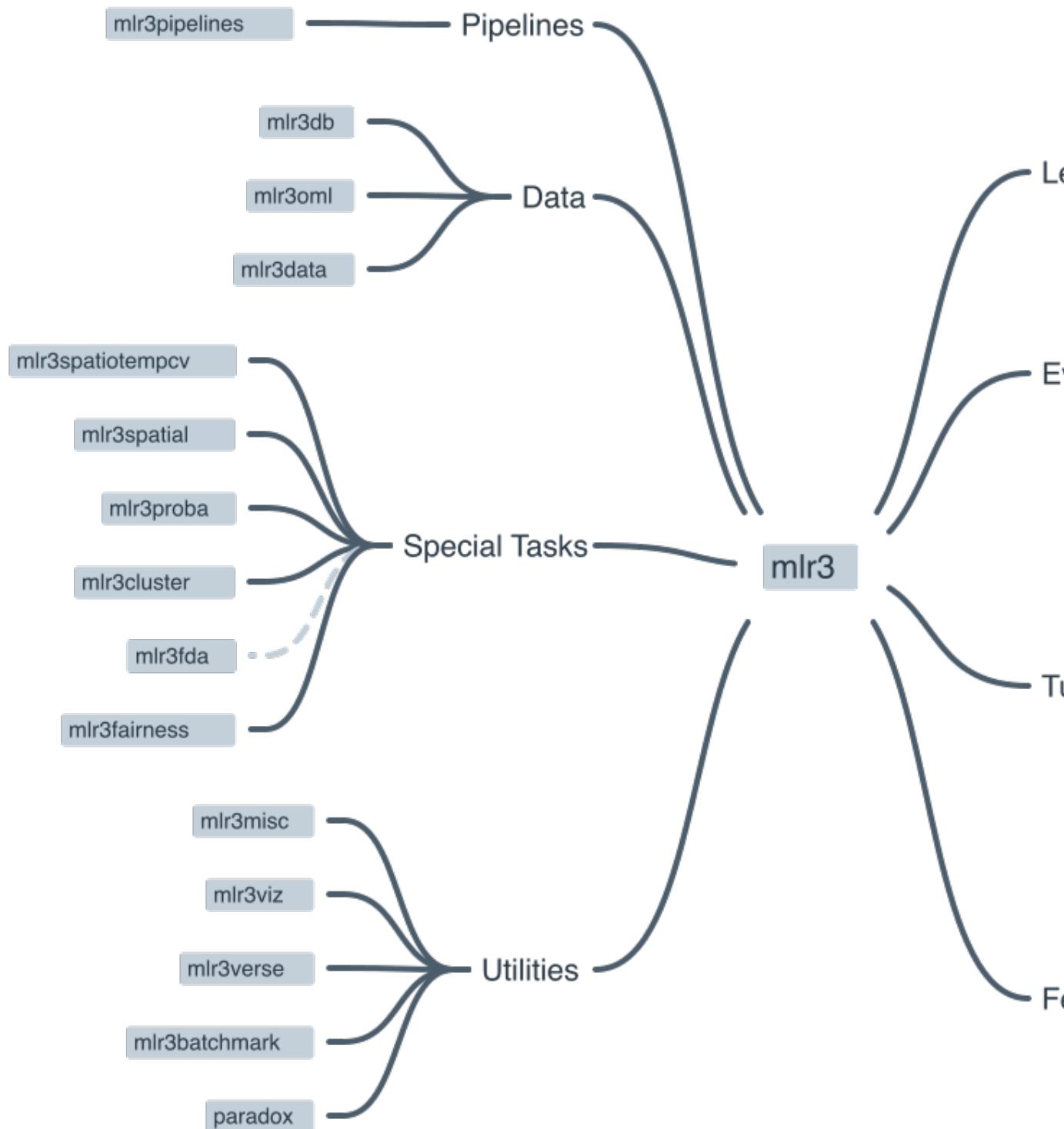


Figure 21.1.: The mlr3 ecosystem.

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handle various learning scenarios. Examples of tasks include classification tasks, regression tasks, and survival tasks.

- **Modular design** The package follows a modular design, allowing users to quickly swap out different components such as learners (algorithms), measures (performance metrics), and resampling strategies. Examples of learners include linear regression, logistic regression, and random forests. Examples of measures include accuracy, precision, recall, and F1 score. Examples of resampling strategies include cross-validation, bootstrapping, and holdout validation.
- **Extensibility** Users can extend the functionality of mlr3 by adding custom components like learners, measures, and preprocessing steps via the R6 object-oriented system.
- **Preprocessing** mlr3 provides a flexible way to preprocess data using “PipeOps” (pipeline operations), allowing users to create reusable preprocessing pipelines.
- **Tuning and model selection** mlr3 supports hyperparameter tuning and model selection using various search strategies like grid search, random search, and Bayesian optimization.
- **Parallelization** The package allows for parallelization of model training and evaluation, making it suitable for large-scale machine learning tasks.
- **Benchmarking** mlr3 facilitates benchmarking of multiple algorithms on multiple tasks, simplifying the process of comparing and selecting the best models.

You can find more information, including tutorials and examples, on the official mlr3 GitHub repository¹ and the mlr3 book².

21.2. The mlr3 workflow

The mlr3 package is designed to simplify the process of creating and deploying complex machine learning pipelines. The package follows a modular design, which means that users can quickly swap out different components such as learners (algorithms), measures (performance metrics), and resampling strategies. The package also supports parallelization of model training and evaluation, making it suitable for large-scale machine learning tasks.

The following sections describe each of these steps in detail.

¹<https://github.com/mlr-org/mlr3>

²<https://mlr3book.mlro.org/>

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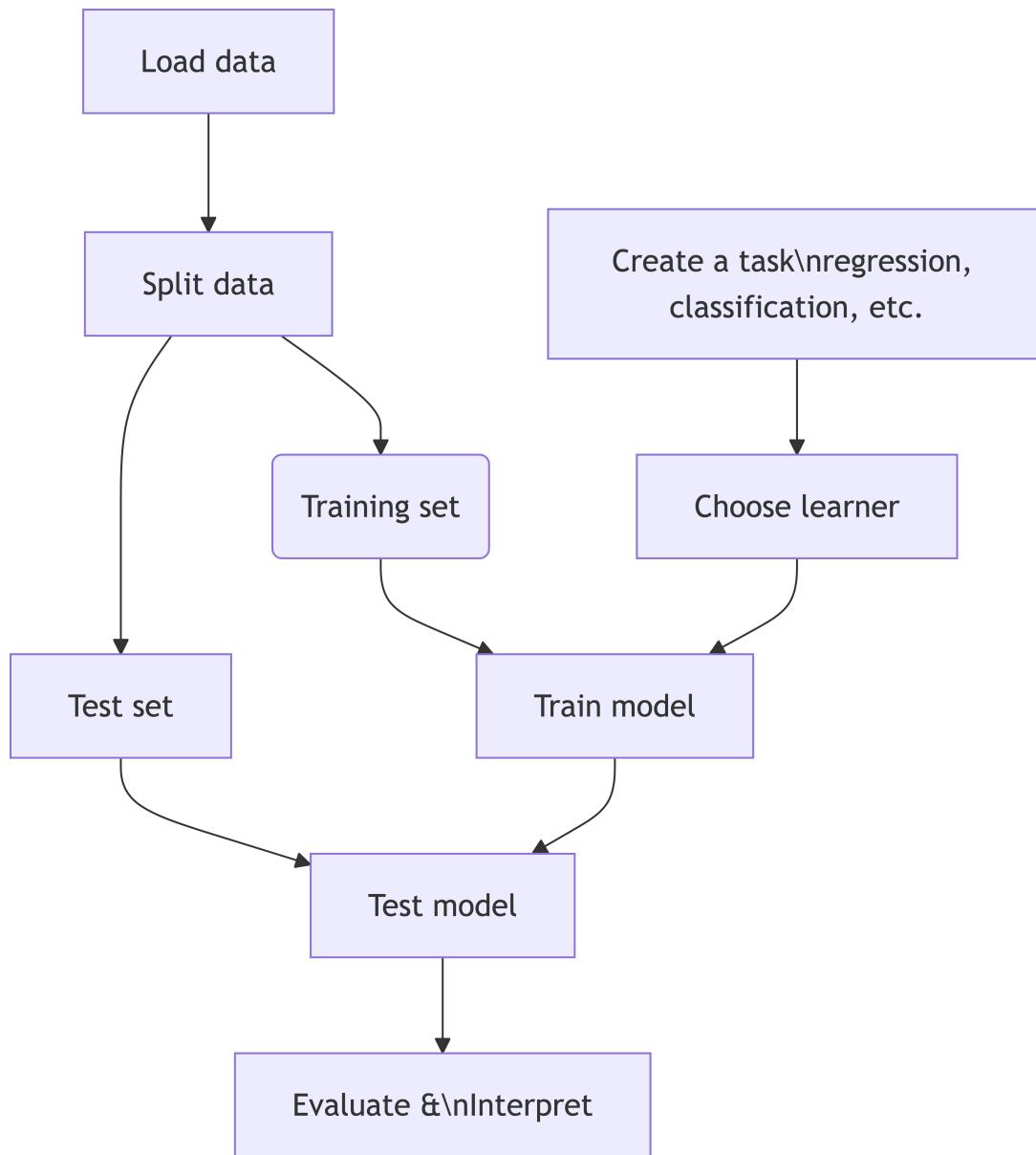


Figure 21.2.: The simplified workflow of a machine learning pipeline using mlr3.

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21.2.1. The machine learning Task

Imagine you want to teach a computer how to make predictions or decisions, similar to how you might teach a student. To do this, you need to clearly define what you want the computer to learn and work on. This is called defining a “task.” Let’s break down what this involves and why it’s important.

21.2.1.1. Step 1: Understand the Problem

First, think about what problem you want to solve or what question you want the computer to answer. For example: - Do you want to predict the weather for tomorrow? - Are you trying to figure out if an email is spam or not? - Do you want to know how much a house might sell for?

These questions define your **task type**. In machine learning, there are several common task types:

- **Classification:** Deciding which category something belongs to (e.g., spam or not spam).
- **Regression:** Predicting a number (e.g., the price of a house).
- **Clustering:** Grouping similar items together (e.g., customer segmentation).

21.2.1.2. Step 2: Choose Your Data

Next, you need data that is related to your problem. Think of data as the information or examples you’ll use to teach the computer. For instance, if your task is to predict house prices, your data might include:

- The size of the house
- The number of bedrooms
- The location of the house
- The age of the house

These pieces of information are called **features**. Features are the input that the computer uses to make predictions.

21.2.1.3. Step 3: Define the Target

Along with features, you need to define the **target**. The target is what you want to predict or decide. In the house price example, the target would be the actual price of the house.

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21.2.1.4. Step 4: Create the Task

Now that you have your problem, data, and target, you can create the task. In mlr3, a task brings together the type of problem (task type), the features (input data), and the target (what you want to predict).

Here's a simple summary:

1. **Task Type:** What kind of problem are you solving? (e.g., classification, regression)
2. **Features:** What information do you have to make the prediction? (e.g., size, location)
3. **Target:** What are you trying to predict? (e.g., house price)

By clearly defining these elements, you set a solid foundation for the machine learning process. This helps ensure that the computer can learn effectively and make accurate predictions.

21.2.1.5. mlr3 and Tasks

The mlr3 package uses the concept of “Tasks” to encapsulate different types of learning problems like classification, regression, and survival analysis. A Task contains the data (features and target variable) and additional metadata to define the machine learning problem. For example, in a classification task, the target variable is a label (stored as a character or factor), while in a regression task, the target variable is a numeric quantity (stored as an integer or numeric).

There are a number of [Task Types](#) that are supported by mlr3. To create a task from a `data.frame()`, `data.table()` or `Matrix()`, you first need to select the right task type:

- **Classification Task:** The target is a label (stored as `character` or `factor`) with only relatively few distinct values → [TaskClassif](#).
- **Regression Task:** The target is a numeric quantity (stored as `integer` or `numeric`) → [TaskRegr](#).
- **Survival Task:** The target is the (right-censored) time to an event. More censoring types are currently in development → [mlr3proba::TaskSurv](#) in add-on package `mlr3proba`.
- **Density Task:** An unsupervised task to estimate the density → [mlr3proba::TaskDens](#) in add-on package `mlr3proba`.

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- **Cluster Task:** An unsupervised task type; there is no target and the aim is to identify similar groups within the feature space → `mlr3cluster::TaskClust` in add-on package `mlr3cluster`.
- **Spatial Task:** Observations in the task have spatio-temporal information (e.g. coordinates) → `mlr3spatiotempcv::TaskRegrST` or `mlr3spatiotempcv::TaskClassifST` in add-on package `mlr3spatiotempcv`.
- **Ordinal Regression Task:** The target is ordinal → `TaskOrdinal` in add-on package `mlr3ordinal` (still in development).

21.2.2. The “Learner” in Machine Learning

After you’ve defined your task, the next step in teaching a computer to make predictions or decisions is to choose a “learner.” Let’s explore what a learner is and how it fits into the `mlr3` package.

21.2.2.1. What is a “Learner”?

Think of a learner as the method or tool that the computer uses to learn from the data. Another common name for a “learner” is a “model.” It’s similar to choosing a tutor or a teacher for a student. Different learners have different ways of understanding and processing information. For example:

- Some learners might be great at recognizing patterns in data, like a tutor who is excellent at spotting trends.
- Others might be good at making decisions based on rules, like a tutor who uses step-by-step logic.

In machine learning, there are many types of learners, each with its own strengths and weaknesses. Here are a few examples:

- **Decision Trees:** These learners make decisions by asking a series of questions, like “Is the house larger than 1000 square feet?” and “Does it have more than 3 bedrooms?”
- **k-Nearest Neighbors:** These learners make predictions based on the similarity of new data points to existing data points.
- **Linear Regression:** This learner tries to fit a straight line through the data points to make predictions about numbers.
- **Random Forests:** These are like a group of decision trees working together to make more accurate predictions.

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- **Support Vector Machines:** These learners find the best boundary that separates different categories in the data.

21.2.2.2. Choosing the Right Learner

Selecting the right learner is crucial because different learners work better for different types of tasks and data. For example:

- If your task is to classify emails as spam or not spam, a decision tree or a support vector machine might work well.
- If you're predicting house prices, linear regression or random forests could be good choices.

The goal is to find a learner that can understand the patterns in your data and make accurate predictions. This is where the `mlr3` package comes in handy. It provides a wide range of learners that you can choose from, making it easier to experiment and find the best learner for your task.

21.2.2.3. Learners in `mlr3`

In the `mlr3` package, learners are pre-built tools that you can easily use for your tasks. Here's how it works:

1. **Select a Learner:** `mlr3` provides a variety of learners to choose from, like decision trees, linear regression, and more.
2. **Train the Learner:** Once you've selected a learner, you provide it with your task (the problem, data, and target). The learner uses this information to learn and make predictions.
3. **Evaluate and Improve:** After training, you can test how well the learner performs and make adjustments if needed, such as trying a different learner or fine-tuning the current one.

21.2.2.4. `mlr3` and Learners

Objects of class `Learner` provide a unified interface to many popular machine learning algorithms in R. They consist of methods to train and predict a model for a `Task` and provide meta-information about the learners, such as the hyperparameters (which control the behavior of the learner) you can set.

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The base class of each learner is `Learner`, specialized for regression as `LearnerRegr` and for classification as `LearnerClassif`. Other types of learners, provided by extension packages, also inherit from the `Learner` base class, e.g. `mlr3proba::LearnerSurv` or `mlr3cluster::LearnerClust`.

All Learners work in a two-stage procedure:

- **Training stage:** The training data (features and target) is passed to the Learner’s `$train()` function which trains and stores a model, i.e. the relationship of the target and features.
- **Predict stage:** The new data, usually a different slice of the original data than used for training, is passed to the `$predict()` method of the Learner. The model trained in the first step is used to predict the missing target, e.g. labels for classification problems or the numerical value for regression problems.

There are a number of [predefined learners](#). The `mlr3` package ships with the following set of classification and regression learners. We deliberately keep this small to avoid unnecessary dependencies:

- `classif.featureless`: Simple baseline classification learner. The default is to always predict the label that is most frequent in the training set. While this is not very useful by itself, it can be used as a “[fallback learner](#)” to make predictions in case another, more sophisticated, learner failed for some reason.
- `regr.featureless`: Simple baseline regression learner. The default is to always predict the mean of the target in training set. Similar to `mlr_learners_classif.featureless`, it makes for a good “[fallback learner](#)”
- `classif.rpart`: Single classification tree from package `rpart`.
- `regr.rpart`: Single regression tree from package `rpart`.

This set of baseline learners is usually insufficient for a real data analysis. Thus, we have cherry-picked implementations of the most popular machine learning method and collected them in the `mlr3learners` package:

- Linear (`regr.lm`) and logistic (`classif.log_reg`) regression
- Penalized Generalized Linear Models (`regr.glmnet`, `classif.glmnet`), possibly with built-in optimization of the penalization parameter (`regr.cv_glmnet`, `classif.cv_glmnet`)
- (Kernelized) k-Nearest Neighbors regression (`regr.kknn`) and classification (`classif.kknn`).
- Kriging / Gaussian Process Regression (`regr.km`)
- Linear (`classif.lda`) and Quadratic (`classif.qda`) Discriminant Analysis
- Naive Bayes Classification (`classif.naive_bayes`)
- Support-Vector machines (`regr.svm`, `classif.svm`)
- Gradient Boosting (`regr.xgboost`, `classif.xgboost`)

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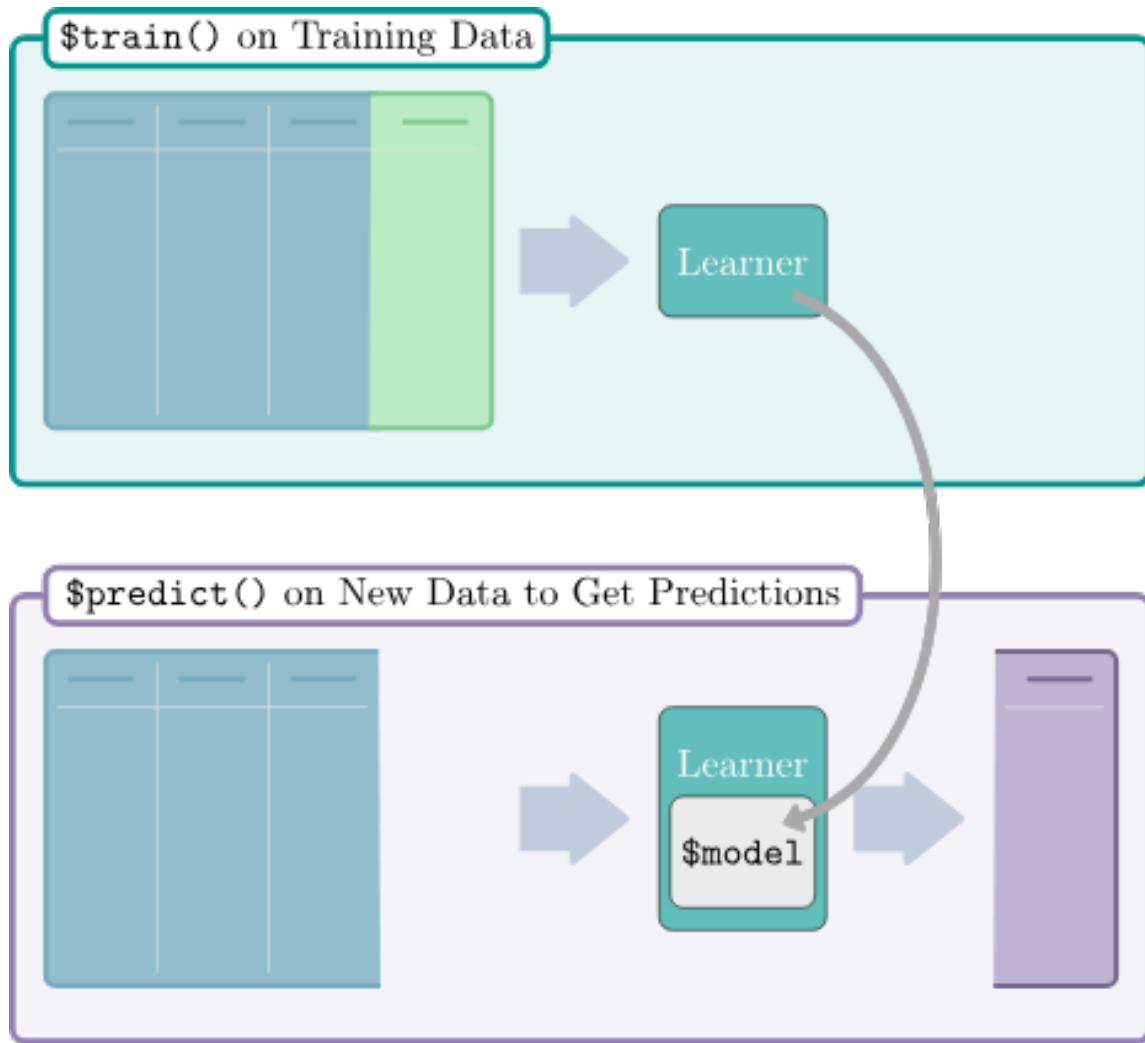


Figure 21.3.: Two stages of a learner. Top: data (features and a target) are passed to an (untrained) learner. Bottom: new data are passed to the trained model which makes predictions for the ‘missing’ target column.

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- Random Forests for regression and classification (`regr.ranger`, `classif.ranger`)

More machine learning methods and alternative implementations are collected in the [mlr3extralearners repository](#).

21.3. Setup

```
library(mlr3verse)
library(GEOquery)
library(mlr3learners) # for knn
library(ranger) # for randomforest
set.seed(789)
```

21.4. Example: Cancer types

In this exercise, we will be classifying cancer types based on gene expression data. The data we are going to access are from Brouwer-Visser et al. (2018).

The data are from the Gene Expression Omnibus (GEO) database, a public repository of functional genomics data. The data are from a study that aimed to identify gene expression signatures that can distinguish between different types of cancer. The data include gene expression profiles from patients with different types of cancer. The goal is to build a machine learning model that can predict the cancer type based on the gene expression data.

21.4.1. Understanding the Problem

Before we start building a machine learning model, it's important to understand the problem we are trying to solve. Here are some key questions to consider:

- What are the features?
- What is the target variable?
- What type of machine learning task is this (classification, regression, clustering)?
- What is the goal of the analysis?

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21.4.2. Data Preparation

Use the [GEOquery](#) package to fetch data about [GSE103512](#).

```
library(GEOquery)
gse = getGEO("GSE103512")[[1]]
```

The first step, a detail, is to convert from the older Bioconductor data structure (GEOquery was written in 2007), the `ExpressionSet`, to the newer `SummarizedExperiment`.

```
library(SummarizedExperiment)
se = as(gse, "SummarizedExperiment")
```

Examine two variables of interest, cancer type and tumor/normal status.

```
with(colData(se), table(`cancer.type.ch1`, `normal.ch1`))
```

```
normal.ch1
cancer.type.ch1 no yes
      BC    65   10
      CRC    57   12
      NSCLC  60    9
      PCA    60    7
```

Before embarking on a machine learning analysis, we need to make sure that we understand the data. Things like missing values, outliers, and other problems can cause problems for machine learning algorithms.

In R, plotting, summaries, and other exploratory data analysis tools are available. PCA analysis, clustering, and other methods can also be used to understand the data. It is worth spending time on this step, as it can save time later.

21.4.3. Feature selection and data cleaning

While we could use all genes in the analysis, we will select the most informative genes using the variance of gene expression across samples. Other methods for feature selection are available, including those based on correlation with the outcome variable.

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! Feature selection

Feature selection should be done on the training data only, not the test data to avoid overfitting. The test data should be used only for evaluation. In other words, the test data should be “unseen” by the model until the final evaluation.

Remember that the `apply` function applies a function to each row or column of a matrix. Here, we apply the `sd` function to each row of the expression matrix to get a vector of stan

```
sds = apply(assay(se, 'exprs'), 1, sd)
## filter out normal tissues
se_small = se[order(sds, decreasing = TRUE)[1:200],
              colData(se)$characteristics_ch1.1=='normal: no']
# remove genes with no gene symbol
se_small = se_small[rowData(se_small)$Gene.Symbol!='', ]
```

To make the data easier to work with, we will use the opportunity to use one of the `rowData` columns as the rownames of the data frame. The `make.names` function is used to make sure that the rownames are valid R variable names and unique.

```
## convert to matrix for later use
dat = assay(se_small, 'exprs')
rownames(dat) = make.names(rowData(se_small)$Gene.Symbol)
```

We also need to transpose the data so that the rows are the samples and the columns are the features in order to use the data with `mlr3`.

```
feat_dat = t(dat)
tumor = data.frame(tumor_type = colData(se_small)$cancer.type.ch1, feat_dat)
```

This is another good time to check the data. Make sure that the data is in the format that you expect. Check the dimensions, the column names, and the data types.

21.4.4. Creating the “task”

The first step in using `mlr3` is to create a `task`. A task is a data set with a target variable. In this case, the target variable is the cancer type. The `mlr3` package provides a function

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to convert a data frame into a task. These tasks can be used with any machine learning algorithm in mlr3.

This is a classification task, so we will use the `as_task_classif` function to create the task. The classification task requires a target variable that is categorical.

```
library(mlr3)
tumor$tumor_type = as.factor(tumor$tumor_type)
task = as_task_classif(tumor,target='tumor_type')
```

21.4.5. Splitting the data

Here, we randomly divide the data into 2/3 training data and 1/3 test data. This is a common split, but other splits can be used. The training data is used to train the model, and the test data is used to evaluate the trained model.

```
set.seed(7)
train_set = sample(task$row_ids, 0.67 * task$nrow)
test_set = setdiff(task$row_ids, train_set)
```

! Important

Training and testing on the same data is a common mistake. We want to test the model on data that it has not seen before. This is the only way to know if the model is overfitting and to get an accurate estimate of the model's performance.

In the next sections, we will train and evaluate three different models on the data: k-nearest-neighbor, classification tree, and random forest. Remember that the goal is to predict the cancer type based on the gene expression data. The mlr3 package uses the concept of “learners” to encapsulate different machine learning algorithms.

21.4.6. Example learners

21.4.6.1. K-nearest-neighbor

The first model we will use is the k-nearest-neighbor model. This model is based on the idea that similar samples have similar outcomes. The number of neighbors to use is a parameter that can be tuned. We'll use the default value of 7, but you can try other values to see how they affect the results. In fact, mlr3 provides the ability to tune parameters automatically, but we won't cover that here.

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21.4.6.1.1. Create the learner

In mlr3, the machine learning algorithms are called learners. To create a learner, we use the `lrn` function. The `lrn` function takes the name of the learner as an argument. The `lrn` function also takes other arguments that are specific to the learner. In this case, we will use the default values for the arguments.

```
library(mlr3learners)
learner = lrn("classif.kknn")
```

You can get a list of all the learners available in mlr3 by using the `lrn()` function without any arguments.

```
lrn()
```

```
<DictionaryLearner> with 51 stored values
Keys: classif.cv_glmnet, classif.debug, classif.featureless,
       classif.glmnet, classif.kknn, classif.lda, classif.log_reg,
       classif.multinom, classif.naive_bayes, classif.nnet, classif.qda,
       classif.ranger, classif.rpart, classif.svm, classif.xgboost,
       clust.agnes, clust.ap, clust.bico, clust.birch, clust.cmeans,
       clust.cobweb, clust.dbscan, clust.dbscan_fpc, clust.diana, clust.em,
       clust.fanny, clust.featureless, clust.ff, clust.hclust,
       clust.hdbscan, clust.kkmeans, clust.kmeans, clust.MBatchKMeans,
       clust.mclust, clust.meanshift, clust.optics, clust.pam,
       clust.SimpleKMeans, clust.xmeans, regr.cv_glmnet, regr.debug,
       regr.featureless, regr.glmnet, regr.kknn, regr.km, regr.lm,
       regr.nnet, regr.ranger, regr.rpart, regr.svm, regr.xgboost
```

21.4.6.1.2. Train

To train the model, we use the `train` function. The `train` function takes the task and the row ids of the training data as arguments.

```
learner$train(task, row_ids = train_set)
```

Here, we can look at the trained model:

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```
# output is large, so do this on your own  
learner$model
```

21.4.6.1.3. Predict

Lets use our trained model works to predict the classes of the **training** data. Of course, we already know the classes of the training data, but this is a good way to check that the model is working as expected. It also gives us a measure of performance on the training data that we can compare to the test data to look for overfitting.

```
pred_train = learner$predict(task, row_ids=train_set)
```

And check on the test data:

```
pred_test = learner$predict(task, row_ids=test_set)
```

21.4.6.1.4. Assess

In this section, we can look at the accuracy and performance of our model on the training data and the test data. We can also look at the confusion matrix to see which classes are being confused with each other.

```
pred_train$confusion
```

	truth			
response	BC	CRC	NSCLC	PCA
BC	42	0	0	0
CRC	0	40	0	0
NSCLC	1	0	44	0
PCA	0	0	0	35

This is a multi-class confusion matrix. The rows are the true classes and the columns are the predicted classes. The diagonal shows the number of samples that were correctly classified. The off-diagonal elements show the number of samples that were misclassified.

We can also look at the accuracy of the model on the training data and the test data. The accuracy is the number of correctly classified samples divided by the total number of samples.

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```
measures = msrs(c('classif.acc'))
pred_train$score(measures)
```

```
classif.acc
0.9938272
```

```
pred_test$confusion
```

		truth			
response		BC	CRC	NSCLC	PCA
BC		22	0	0	0
CRC		0	17	1	0
NSCLC		0	0	15	0
PCA		0	0	0	25

```
pred_test$score(measures)
```

```
classif.acc
0.9875
```

Compare the accuracy on the training data to the accuracy on the test data. Do you see any evidence of overfitting?

21.4.6.2. Classification tree

We are going to use a classification tree to classify the data. A classification tree is a series of yes/no questions that are used to classify the data. The questions are based on the features in the data. The classification tree is built by finding the feature that best separates the data into the different classes. Then, the data is split based on the value of that feature. The process is repeated until the data is completely separated into the different classes.

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21.4.6.2.1. Train

```
# in this case, we want to keep the model  
# so we can look at it later  
learner = lrn("classif.rpart", keep_model = TRUE)  
  
learner$train(task, row_ids = train_set)
```

We can take a look at the model.

```
learner$model  
  
n= 162  
  
node), split, n, loss, yval, (yprob)  
* denotes terminal node  
  
1) root 162 118 NSCLC (0.26543210 0.24691358 0.27160494 0.21604938)  
2) CDHR5>=5.101625 40 0 CRC (0.00000000 1.00000000 0.00000000 0.00000000) *  
3) CDHR5< 5.101625 122 78 NSCLC (0.35245902 0.00000000 0.36065574 0.28688525)  
6) ACPP< 6.088431 87 43 NSCLC (0.49425287 0.00000000 0.50574713 0.00000000)  
12) GATA3>=4.697803 41 1 BC (0.97560976 0.00000000 0.02439024 0.00000000) *  
13) GATA3< 4.697803 46 3 NSCLC (0.06521739 0.00000000 0.93478261 0.00000000) *  
7) ACPP>=6.088431 35 0 PCA (0.00000000 0.00000000 0.00000000 1.00000000) *
```

Decision trees are easy to visualize if they are small. Here, we can see that the tree is very simple, with only two splits.

```
library(mlr3viz)  
library(ggparty)
```

Loading required package: ggplot2

Loading required package: partykit

Loading required package: grid

Loading required package: libcoin

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```
Loading required package: mvtnorm
```

```
Attaching package: 'partykit'
```

```
The following object is masked from 'package:SummarizedExperiment':
```

```
width
```

```
The following object is masked from 'package:GenomicRanges':
```

```
width
```

```
The following object is masked from 'package:IRanges':
```

```
width
```

```
The following object is masked from 'package:S4Vectors':
```

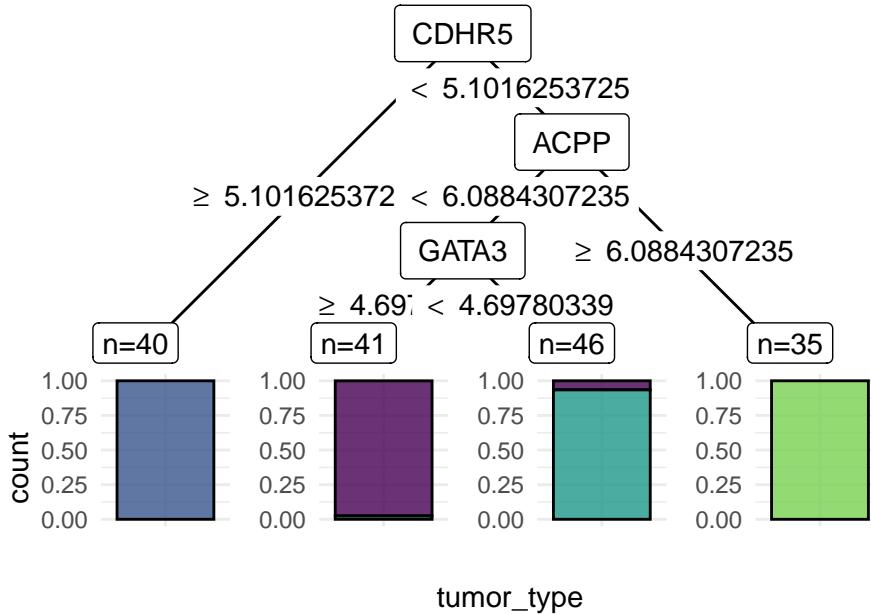
```
width
```

```
The following object is masked from 'package:BiocGenerics':
```

```
width
```

```
autoplot(learner, type='ggparty')
```

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21.4.6.2.2. Predict

Now that we have trained the model on the *training* data, we can use it to predict the classes of the training data and the test data. The `$predict` method takes a `task` and produces a prediction based on the *trained* model, in this case, called `learner`.

```
pred_train = learner$predict(task, row_ids=train_set)
```

Remember that we split the data into training and test sets. We can use the trained model to predict the classes of the test data. Since the *test* data was not used to train the model, it is not “cheating” like what we just did where we did the prediction on the *training* data.

```
pred_test = learner$predict(task, row_ids=test_set)
```

21.4.6.2.3. Assess

For classification tasks, we often look at a confusion matrix of the *truth* vs the *predicted* classes for the samples.

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! Important

Assessing the performance of a model should **always** be **reported** from assessment on an independent test set.

```
pred_train$confusion
```

```
    truth
response BC  CRC  NSCLC PCA
      BC    40    0     1    0
      CRC    0   40     0    0
      NSCLC  3    0    43    0
      PCA    0    0     0   35
```

- What does this confusion matrix tell you?

We can also ask for several “measures” of the performance of the model. Here, we ask for the accuracy of the model. To get a complete list of measures, use `msr()`.

```
measures = msrs(c('classif.acc'))
pred_train$score(measures)
```

```
classif.acc
0.9753086
```

- How does the accuracy compare to the confusion matrix?
- How does this accuracy compare to the accuracy of the k-nearest-neighbor model?
- How about the decision tree model?

```
pred_test$confusion
```

```
    truth
response BC  CRC  NSCLC PCA
      BC    20    0     1    0
      CRC    0   17     3    0
      NSCLC  2    0    12    0
      PCA    0    0     0   25
```

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```
pred_test$score(measures)
```

```
classif.acc  
0.925
```

- What does the confusion matrix in the *test* set tell you?
- How do the assessments of the *test* and *training* sets differ?

💡 Overfitting

When the assessment of the test set is worse than the evaluation of the training set, the model may be *overfit*. How to address overfitting varies by model type, but it is a sign that you should pay attention to model selection and parameters.

21.4.6.3. RandomForest

```
learner = lrn("classif.ranger", importance = "impurity")
```

21.4.6.3.1. Train

```
learner$train(task, row_ids = train_set)
```

Again, you can look at the model that was trained.

```
learner$model
```

Ranger result

Call:

```
ranger::ranger(dependent.variable.name = task$target_names, data = task$data(), proba
```

Type:	Classification
Number of trees:	500
Sample size:	162
Number of independent variables:	192
Mtry:	13

21. Examples

```
Target node size:           1
Variable importance mode:  impurity
Splitrule:                  gini
OOB prediction error:     0.62 %
```

For more details, the mlr3 random forest approach is based on the ranger package. You can look at the ranger documentation.

- What is the OOB error in the output?

Random forests are a collection of decision trees. Since predictors enter the trees in a random order, the trees are different from each other. The random forest procedure gives us a measure of the “importance” of each variable.

```
head(learner$importance(), 15)
```

```
CDHR5   TRPS1.1    FABP1    EPS8L3    KRT20    EFHD1    LGALS4    TRPS1
4.791870 3.918063 3.692649 3.651422 3.340382 3.314491 2.952969 2.926175
SFTPB   SFTPB.1    GATA3    GATA3.1   TMPRSS2    MUC12    POF1B
2.805811 2.681004 2.344603 2.271845 2.248734 2.207347 1.806906
```

More “important” variables are those that are more often used in the trees. Are the most important variables the same as the ones that were important in the decision tree?

If you are interested, look up a few of the important variables in the model to see if they make biological sense.

21.4.6.3.2. Predict

Again, we can use the trained model to predict the classes of the training data and the test data.

```
pred_train = learner$predict(task, row_ids=train_set)
```

```
pred_test = learner$predict(task, row_ids=test_set)
```

21.4.6.3.3. Assess

21. Examples

```
pred_train$confusion
```

```
    truth
response BC CRC NSCLC PCA
  BC     43    0    0    0
  CRC     0   40    0    0
  NSCLC    0    0   44    0
  PCA     0    0    0   35
```

```
measures = msrs(c('classif.acc'))
pred_train$score(measures)
```

```
classif.acc
      1
```

```
pred_test$confusion
```

```
    truth
response BC CRC NSCLC PCA
  BC     22    0    0    0
  CRC     0   17    0    0
  NSCLC    0    0   16    0
  PCA     0    0    0   25
```

```
pred_test$score(measures)
```

```
classif.acc
      1
```

21.5. Example Predicting age from DNA methylation

We will be building a regression model for chronological age prediction, based on DNA methylation. This is based on the work of [Jana Naue et al. 2017](#), in which biomarkers are examined to predict the chronological age of humans by analyzing the DNA methylation patterns. Different machine learning algorithms are used in this study to make an age prediction.

21. Examples

It has been recognized that within each individual, the level of **DNA methylation** changes with age. This knowledge is used to select useful biomarkers from DNA methylation datasets. The **CpG sites** with the highest correlation to age are selected as the biomarkers (and therefore features for building a regression model). In this tutorial, specific biomarkers are analyzed by machine learning algorithms to create an age prediction model.

The data are taken from [this tutorial](#).

```
library(data.table)
meth_age = rbind(
  fread('https://zenodo.org/record/2545213/files/test_rows_labels.csv'),
  fread('https://zenodo.org/record/2545213/files/train_rows.csv')
)
```

Let's take a quick look at the data.

```
head(meth_age)
```

```
RPA2_3 ZYG11A_4 F5_2 HOXC4_1 NKIRAS2_2 MEIS1_1 SAMD10_2 GRM2_9 TRIM59_5
<num> <num> <num> <num> <num> <num> <num> <num> <num>
1: 65.96 18.08 41.57 55.46 30.69 63.42 40.86 68.88 44.32
2: 66.83 20.27 40.55 49.67 29.53 30.47 37.73 53.30 50.09
3: 50.30 11.74 40.17 33.85 23.39 58.83 38.84 35.08 35.90
4: 65.54 15.56 33.56 36.79 20.23 56.39 41.75 50.37 41.46
5: 59.01 14.38 41.95 30.30 24.99 54.40 37.38 30.35 31.28
6: 81.30 14.68 35.91 50.20 26.57 32.37 32.30 55.19 42.21
LDB2_3 ELOVL2_6 DDO_1 KLF14_2 Age
<num> <num> <num> <num> <int>
1: 56.17 62.29 40.99 2.30 40
2: 58.40 61.10 49.73 1.07 44
3: 58.81 50.38 63.03 0.95 28
4: 58.05 50.58 62.13 1.99 37
5: 65.80 48.74 41.88 0.90 24
6: 70.15 61.36 33.62 1.87 43
```

As before, we create the `task` object, but this time we use `as_task_regr()` to create a regression task.

- Why is this a regression task?

21. Examples

```
task = as_task_regr(meth_age,target = 'Age')

set.seed(7)
train_set = sample(task$row_ids, 0.67 * task$nrow)
test_set = setdiff(task$row_ids, train_set)
```

21.5.1. Example learners

21.5.1.1. Linear regression

We will start with a simple linear regression model.

```
learner = lrn("regr.lm")
```

21.5.1.1.1. Train

```
learner$train(task, row_ids = train_set)
```

When you train a linear regression model, we can evaluate some of the diagnostic plots to see if the model is appropriate (Figure 21.4).

```
par(mfrow=c(2,2))
plot(learner$model)
```

21. Examples

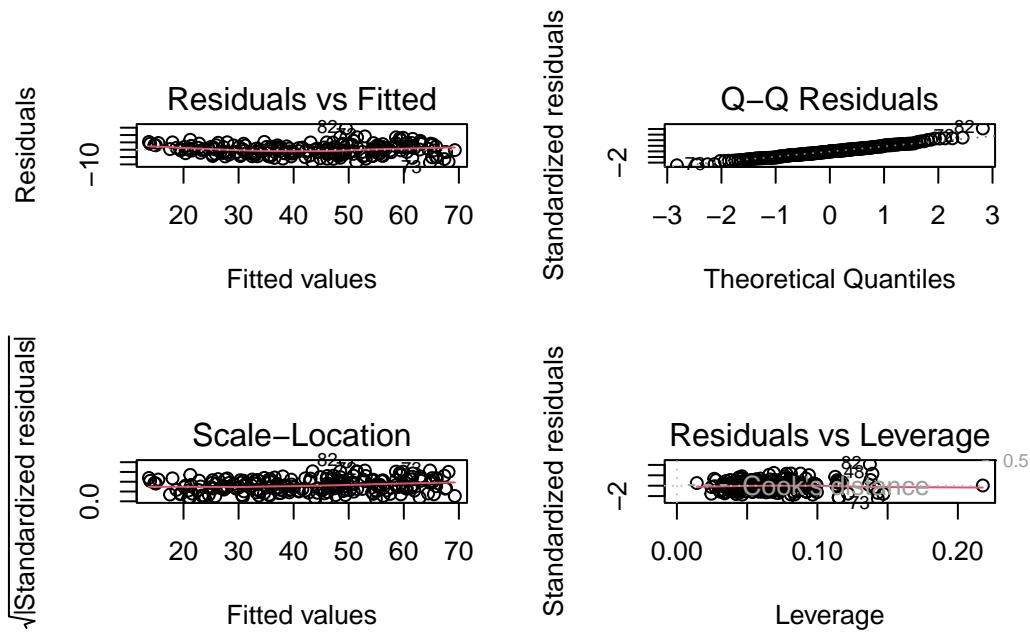


Figure 21.4.: Regression diagnostic plots. The top left plot shows the residuals vs. fitted values. The top right plot shows the normal Q-Q plot. The bottom left plot shows the scale-location plot. The bottom right plot shows the residuals vs. leverage.

21.5.1.1.2. Predict

```
pred_train = learner$predict(task, row_ids=train_set)
```

```
pred_test = learner$predict(task, row_ids=test_set)
```

21.5.1.1.3. Assess

```
pred_train
```

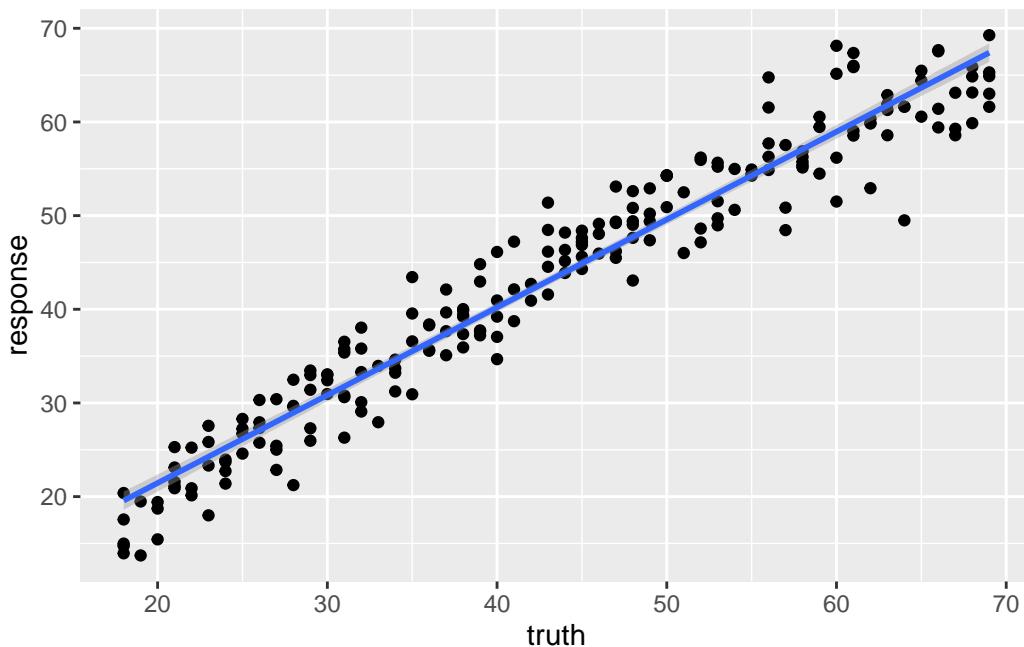
```
<PredictionRegr> for 209 observations:
  row_ids  truth  response
    298     29  31.40565
    103     58  56.26019
    194     53  48.96480
```

21. Examples

```
---  ---  ---  
312  48  52.61195  
246  66  67.66312  
238  38  39.38414
```

We can plot the relationship between the `truth` and `response`, or predicted value to see visually how our model performs.

```
library(ggplot2)  
ggplot(pred_train,aes(x=truth, y=response)) +  
  geom_point() +  
  geom_smooth(method='lm')  
  
'geom_smooth()' using formula = 'y ~ x'
```



We can use the r-squared of the fit to roughly compare two models.

```
measures = msrs(c('regr.rsq'))  
pred_train$score(measures)
```

21. Examples

```
rsq  
0.9376672
```

```
pred_test
```

```
<PredictionRegr> for 103 observations:  
  row_ids truth response  
    4      37 37.64301  
    5      24 28.34777  
    7      34 33.22419  
    ---  ---  ---  
   306     42 41.65864  
   307     63 58.68486  
   309     68 70.41987
```

```
pred_test$score(measures)
```

```
rsq  
0.9363526
```

21.5.1.2. Regression tree

```
learner = lrn("regr.rpart", keep_model = TRUE)
```

21.5.1.2.1. Train

```
learner$train(task, row_ids = train_set)
```

```
learner$model
```

```
n= 209
```

```
node), split, n, deviance, yval  
  * denotes terminal node
```

```
1) root 209 45441.4500 43.27273
```

21. Examples

```
2) ELOVL2_6< 56.675 98 5512.1220 30.24490
   4) ELOVL2_6< 47.24 47 866.4255 24.23404
      8) GRM2_9< 31.3 34 289.0588 22.29412 *
      9) GRM2_9>=31.3 13 114.7692 29.30769 *
   5) ELOVL2_6>=47.24 51 1382.6270 35.78431
   10) F5_2>=39.295 35 473.1429 33.28571 *
    11) F5_2< 39.295 16 213.0000 41.25000 *
3) ELOVL2_6>=56.675 111 8611.3690 54.77477
   6) ELOVL2_6< 65.365 63 3101.2700 49.41270
      12) KLF14_2< 3.415 37 1059.0270 46.16216 *
      13) KLF14_2>=3.415 26 1094.9620 54.03846 *
   7) ELOVL2_6>=65.365 48 1321.3120 61.81250 *
```

What is odd about using a regression tree here is that we end up with only a few discrete estimates of age. Each “leaf” has a value.

21.5.1.2.2. Predict

```
pred_train = learner$predict(task, row_ids=train_set)

pred_test = learner$predict(task, row_ids=test_set)
```

21.5.1.2.3. Assess

```
pred_train
```

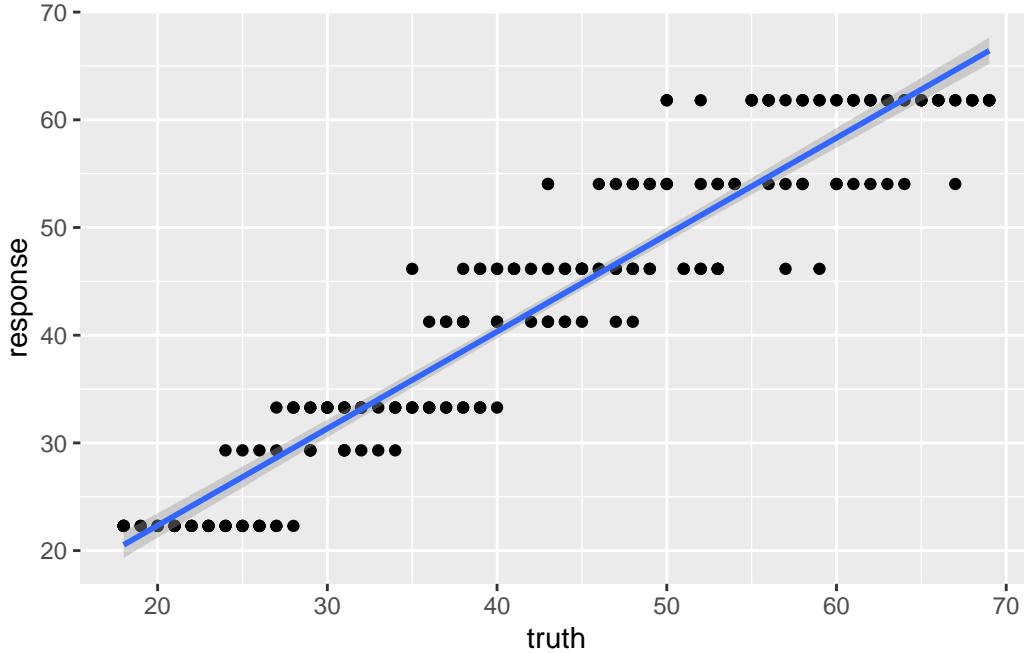
```
<PredictionRegr> for 209 observations:
  row_ids truth response
    298     29 33.28571
    103     58 61.81250
    194     53 46.16216
    ---     ---     ---
    312     48 54.03846
    246     66 61.81250
    238     38 41.25000
```

We can see the effect of the discrete values much more clearly here.

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```
library(ggplot2)
ggplot(pred_train,aes(x=truth, y=response)) +
  geom_point() +
  geom_smooth(method='lm')

`geom_smooth()` using formula = 'y ~ x'
```



And the r-squared values for this model prediction shows quite a bit of difference from the linear regression above.

```
measures = msrs(c('regr.rsq'))
pred_train$score(measures)
```

```
rsq
0.8995351
```

```
pred_test
```

21. Examples

```
<PredictionRegr> for 103 observations:  
  row_ids truth response  
    4      37 41.25000  
    5      24 33.28571  
    7      34 33.28571  
    ---  ----  ---  
   306     42 46.16216  
   307     63 61.81250  
   309     68 61.81250
```

```
pred_test$score(measures)
```

```
rsq  
0.8545402
```

21.5.1.3. RandomForest

Randomforest is also tree-based, but unlike the single regression tree above, randomforest is a “forest” of trees which will eliminate the discrete nature of a single tree.

```
learner = lrn("regr.ranger", mtry=2, min.node.size=20)
```

21.5.1.3.1. Train

```
learner$train(task, row_ids = train_set)
```

```
learner$model
```

Ranger result

Call:

```
ranger::ranger(dependent.variable.name = task$target_names, data = task$data(), min.n
```

Type: Regression
Number of trees: 500
Sample size: 209
Number of independent variables: 13

21. Examples

```
Mtry:                      2
Target node size:          20
Variable importance mode: none
Splitrule:                 variance
OOB prediction error (MSE): 18.85364
R squared (OOB):           0.9137009
```

21.5.1.3.2. Predict

```
pred_train = learner$predict(task, row_ids=train_set)

pred_test = learner$predict(task, row_ids=test_set)
```

21.5.1.3.3. Assess

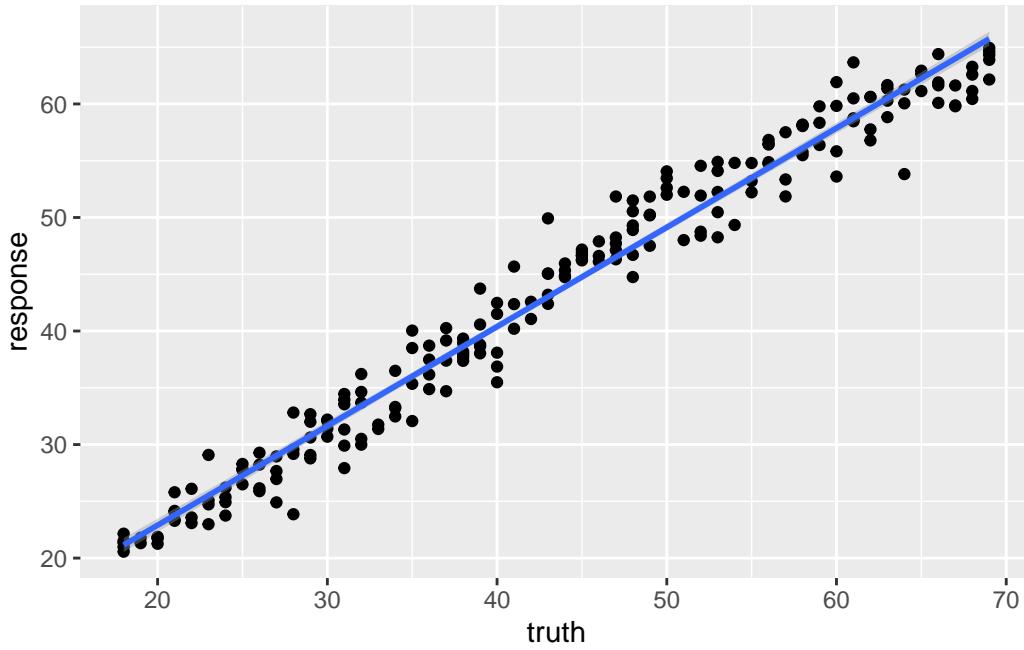
```
pred_train

<PredictionRegr> for 209 observations:
  row_ids truth response
    298     29 30.62154
    103     58 58.05445
    194     53 48.25661
    ---     ---    ---
    312     48 51.49846
    246     66 64.39315
    238     38 38.18038

ggplot(pred_train,aes(x=truth, y=response)) +
  geom_point() +
  geom_smooth(method='lm')

`geom_smooth()` using formula = 'y ~ x'
```

21. Examples



```
measures = msrs(c('regr.rsq'))
pred_train$score(measures)
```

```
rsq
0.960961
```

```
pred_test
```

```
<PredictionRegr> for 103 observations:
  row_ids   truth   response
        4     37 37.79631
        5     24 29.18371
        7     34 33.26780
    ---
  306     42 40.29101
  307     63 58.26534
  309     68 63.15481
```

```
pred_test$score(measures)
```

```
rsq
0.9208394
```

21. Examples

21.6. Example: Expression prediction from histone modification data

In this little set of exercises, you will be using histone marks near a gene to predict its expression (Figure 21.5).

$$y \sim h1 + h2 + h3 + \dots \quad (21.1)$$

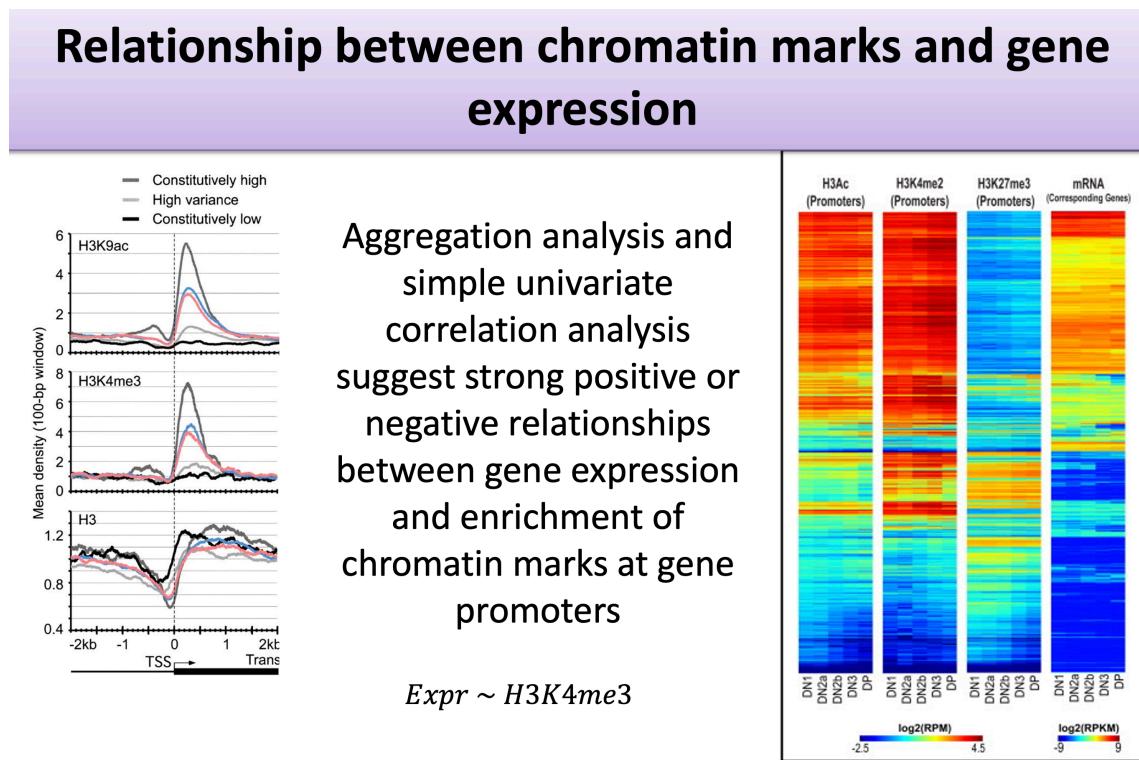


Figure 21.5.: What is the combined effect of histone marks on gene expression?

The data are from a study that aimed to predict gene expression from histone modification data. The data include gene expression levels and histone modification data for a set of genes. The goal is to build a machine learning model that can predict gene expression levels based on the histone modification data. The histone modification data are simply summaries of the histone marks within the promoter, defined as the region 2kb upstream of the transcription start site for this exercise.

We will try a couple of different approaches:

21. Examples

1. Penalized regression
2. RandomForest

21.6.1. The Data

The data in this exercise were developed by Anshul Kundaje. We are not going to focus on the details of the data collection, etc. Instead, this is

```
fullFeatureSet <- read.table("http://seandavi.github.io/ITR/expression-prediction/features.
```

What are the column names of the predictor variables?

```
colnames(fullFeatureSet)
```

```
[1] "Control"    "Dnase"      "H2az"       "H3k27ac"    "H3k27me3"  "H3k36me3"  
[7] "H3k4me1"   "H3k4me2"   "H3k4me3"   "H3k79me2"   "H3k9ac"    "H3k9me1"  
[13] "H3k9me3"  "H4k20me1"
```

These are going to be predictors combined into a model. Some of our learners will rely on predictors being on a similar scale. Are our data already there?

To perform centering and scaling by column, we can convert to a matrix and then use `scale`.

```
par(mfrow=c(1,2))  
scaled_features <- scale(as.matrix(fullFeatureSet))  
boxplot(fullFeatureSet, title='Original data')  
boxplot(scaled_features, title='Centered and scaled data')
```

21. Examples

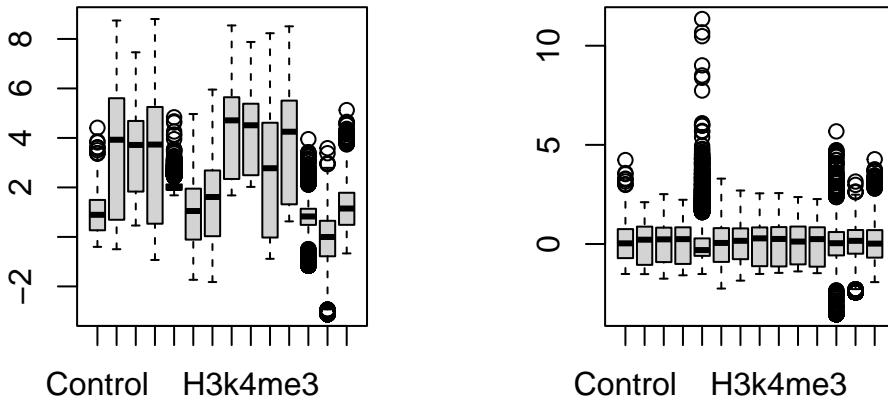


Figure 21.6.: Boxplots of original and scaled data.

There is a row for each gene and a column for each histone mark and we can see that the data are centered and scaled by column. We can also see some patterns in the data (see Figure 21.7).

```
sampled_features <- fullFeatureSet[sample(nrow(scaled_features), 500),]
library(ComplexHeatmap)
```

```
=====
ComplexHeatmap version 2.22.0
Bioconductor page: http://bioconductor.org/packages/ComplexHeatmap/
Github page: https://github.com/jokergoo/ComplexHeatmap
Documentation: http://jokergoo.github.io/ComplexHeatmap-reference

If you use it in published research, please cite either one:
- Gu, Z. Complex Heatmap Visualization. iMeta 2022.
- Gu, Z. Complex heatmaps reveal patterns and correlations in multidimensional genomic data. Bioinformatics 2016.
```

The new `InteractiveComplexHeatmap` package can directly export static complex heatmaps into an interactive Shiny app with zero effort. Have a try!

This message can be suppressed by:
`suppressPackageStartupMessages(library(ComplexHeatmap))`

21. Examples

```
Heatmap(sampled_features, name='histone marks', show_row_names=FALSE)
```

Warning: The input is a data frame-like object, convert it to a matrix.

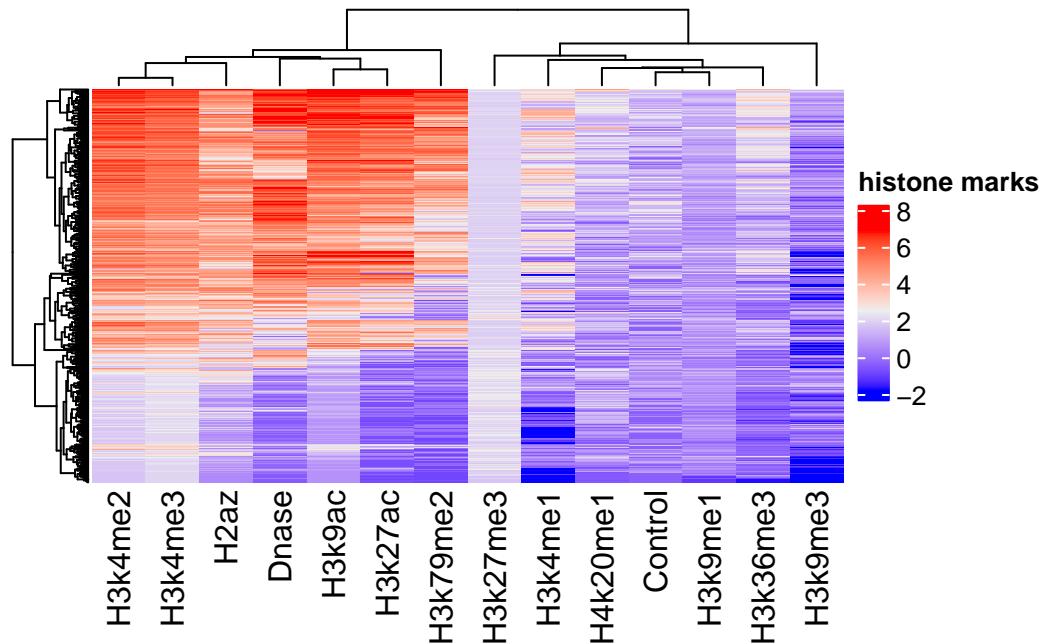


Figure 21.7.: Heatmap of 500 randomly sampled rows of the data. Columns are histone marks and there is a row for each gene.

Now, we can read in the associated gene expression measures that will become our “target” for prediction.

```
target <- scan(url("http://seandavi.github.io/ITR/expression-prediction/target.txt"), skip=1)
# make into a data frame
exp_pred_data <- data.frame(gene_expression=target, scaled_features)
```

And the first few rows of the target data frame using:

```
head(exp_pred_data, 3)
```

21. Examples

	gene_expression	Control	Dnase	H2az
ENSG00000000419.7.49575069	6.082343	0.7452926	0.7575546	1.0728432
ENSG00000000457.8.169863093	2.989145	1.9509786	1.0216546	0.3702787
ENSG00000000938.7.27961645	-5.058894	-0.3505542	-1.4482958	-1.0390775
	H3k27ac	H3k27me3	H3k36me3	H3k4me1
ENSG00000000419.7.49575069	1.0950440	-0.5125312	1.1334793	0.4127984
ENSG00000000457.8.169863093	0.7142157	-0.4079244	0.8739005	1.1649282
ENSG00000000938.7.27961645	-1.0173283	1.4117293	-0.5157582	-0.5017450
	H3k4me2	H3k4me3	H3k79me2	H3k9ac
ENSG00000000419.7.49575069	1.2136176	1.1202901	1.5155803	1.2468256
ENSG00000000457.8.169863093	0.6456572	0.6508561	0.7976487	0.5792891
ENSG00000000938.7.27961645	-0.1878255	-0.6560973	-1.3803974	-1.0067972
	H3k9me1	H3k9me3	H4k20me1	
ENSG00000000419.7.49575069	0.1426980	1.185622	1.9599992	
ENSG00000000457.8.169863093	0.3630902	1.014923	-0.2695111	
ENSG00000000938.7.27961645	0.6564520	-1.370871	-1.8773178	

21.6.2. Create task

```
exp_pred_task = as_task_regr(exp_pred_data, target='gene_expression')
```

Partition the data into test and training sets. We will use $\frac{1}{3}$ and $\frac{2}{3}$ of the data for testing.

```
split = partition(exp_pred_task)
```

21.6.3. Example learners

21.6.3.1. Linear regression

```
learner = lrn("regr.lm")
```

21.6.3.1.1. Train

```
learner$train(exp_pred_task, split$train)
```

21. Examples

21.6.3.1.2. Predict

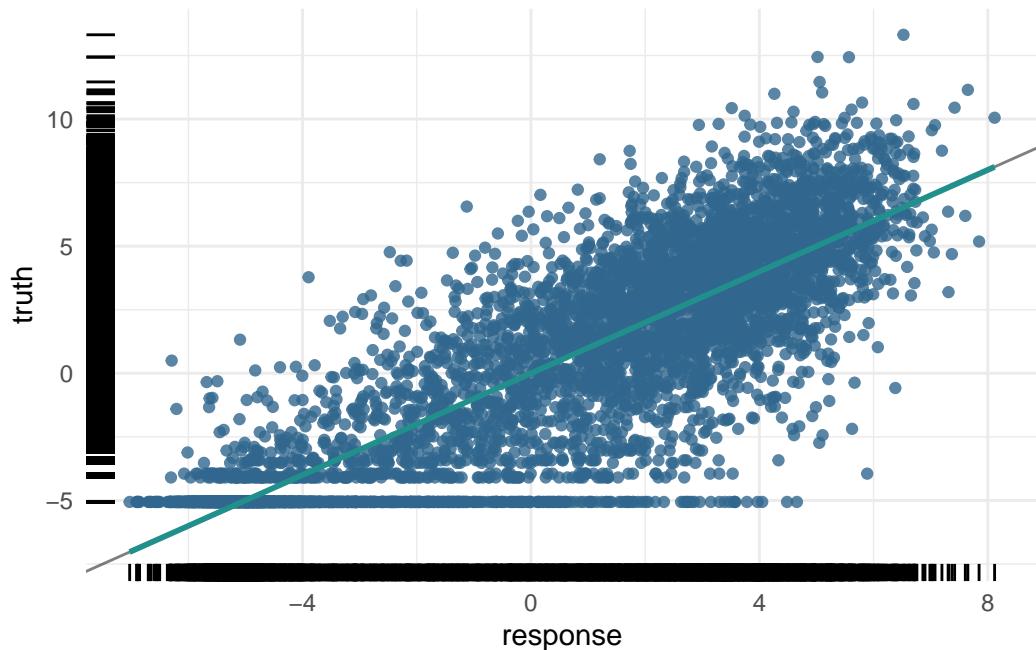
```
pred_train = learner$predict(exp_pred_task, split$train)
pred_test = learner$predict(exp_pred_task, split$test)
```

21.6.3.1.3. Assess

```
pred_train
```

```
<PredictionRegr> for 5789 observations:
  row_ids      truth   response
    1  6.082343  5.182373
    2  2.989145  2.970278
    3 -5.058894 -5.283509
    ...
  8637 -5.058894 -3.955237
  8638  6.089159  4.809801
  8640 -3.114148 -4.723061
```

```
plot(pred_train)
```



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For the training data:

```
measures = msrs(c('regr.rsq'))
pred_train$score(measures)
```

```
rsq
0.7505366
```

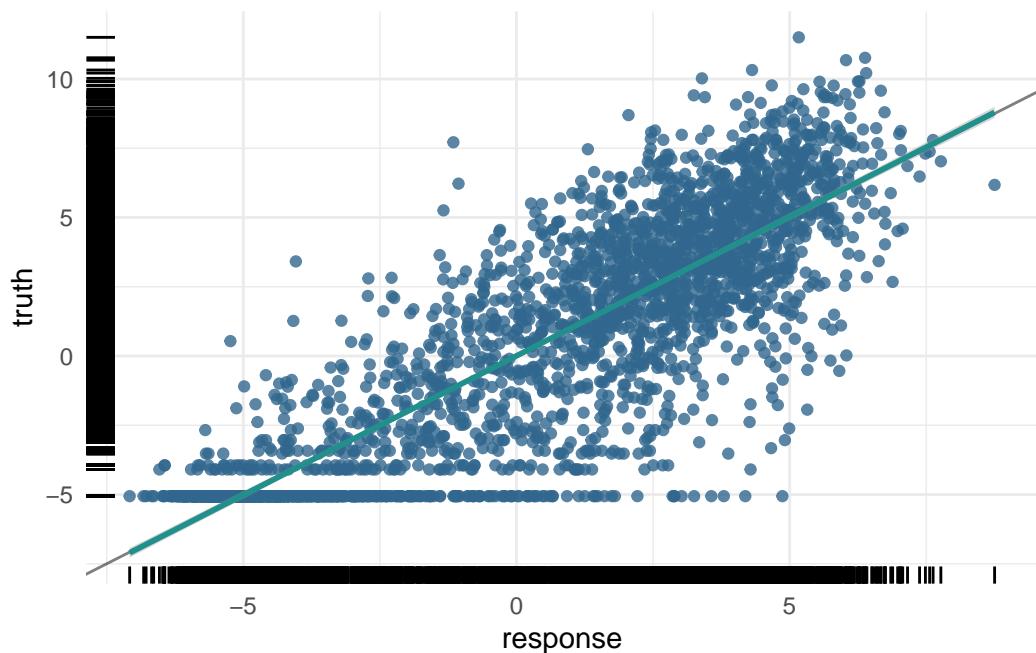
And the test data:

```
pred_test$score(measures)
```

```
rsq
0.7510334
```

And the plot of the test data predictions:

```
plot(pred_test)
```



21. Examples

21.6.3.2. Penalized regression

Imagine you want to teach a computer to predict house prices based on various features like size, number of bedrooms, and location. You decide to use **regression**, which finds a relationship between these features and the house prices. But what if your model becomes too complicated? This is where **penalized regression** comes in.

21.6.3.2.1. The Problem with Overfitting

Sometimes, the model tries too hard to fit every single data point perfectly. This can make the model very complex, like trying to draw a perfect line through a very bumpy path. This problem is called **overfitting**. An overfitted model works well on the data it has seen (training data) but performs poorly on new, unseen data (testing data).

21.6.3.2.2. Introducing Penalized Regression

Penalized regression helps prevent overfitting by adding a “penalty” to the model for being too complex. Think of it as a way to encourage the model to be simpler and more general. There are three common types of penalized regression:

1. Ridge Regression (L2 Penalty):

- Adds a penalty based on the size of the coefficients. It tries to keep all coefficients small.
- If the model’s equation looks too complicated, Ridge Regression will push it towards a simpler form by shrinking the coefficients.
- Imagine you have a rubber band that pulls the coefficients towards zero, making the model less likely to overfit.

2. Lasso Regression (L1 Penalty):

- Adds a penalty that can shrink some coefficients all the way to zero.
- This means Lasso Regression can completely remove some features from the model, making it simpler.
- Imagine you have a pair of scissors that can cut off the least important features, leaving only the most important ones.

3. Elastic Net:

- Combines both Ridge and Lasso penalties. It adds penalties for both the size and the number of coefficients.
- This method balances between shrinking coefficients and eliminating some altogether, offering the benefits of both Ridge and Lasso.

21. Examples

- Think of Elastic Net as using both the rubber band (Ridge) and scissors (Lasso) to simplify the model.

With our data, the number of predictors is not huge, but we might be interested in 1) reducing overfitting, 2) improving interpretability, or 3) both by minimizing the number of predictors in our model without drastically affecting our prediction accuracy. Without penalized regression, the model might come up with a very complex equation. With Ridge, Lasso, or Elastic Net, the model simplifies this equation by either shrinking the coefficients (Ridge), removing some of them (Lasso), or balancing both (Elastic Net).

Here's a simple summary:

- **Ridge Regression:** Reduces the impact of less important features by shrinking their coefficients.
- **Lasso Regression:** Can eliminate some features entirely by setting their coefficients to zero.
- **Elastic Net:** Combines the effects of Ridge and Lasso, shrinking some coefficients and eliminating others.

Using penalized regression in machine learning ensures that your model:

1. **Performs Better on New Data:** By avoiding overfitting, the model can make more accurate predictions on new, unseen data.
2. **Is Easier to Interpret:** A simpler model with fewer features is easier to understand and explain.

21.6.3.3. Penalized Regression with mlr3

In the `mlr3` package, you can easily apply penalized regression methods to your tasks. Here's how:

1. **Select Penalized Regression Learners:** `mlr3` provides learners for Ridge, Lasso, and Elastic Net Regression.
2. **Train the Learner:** Use your data to train the chosen penalized regression model.
3. **Evaluate and Adjust:** Check how well the model performs and make adjustments if needed.

This description explains penalized regression, including Ridge, Lasso, and Elastic Net, in an intuitive way, highlighting their benefits and how they work, while relating them to familiar concepts and the `mlr3` package.

21. Examples

Recall that we can use penalized regression to select the most important predictors from a large set of predictors. In this case, we will use the `glmnet` package to perform penalized regression, but we will use the `m1r` interface to `glmnet` to make it easier to use.

The `nfolds` parameter is the number of folds to use in the cross-validation procedure.

What is Cross-Validation? Cross-validation is a technique used to assess how well a model will perform on unseen data. It involves splitting the data into multiple parts, training the model on some of these parts, and validating it on the remaining parts. This process is repeated several times to ensure the model's performance is consistent.

Why Use Cross-Validation? Cross-validation helps to:

- Avoid Overfitting: By testing the model on different subsets of the data, cross-validation helps ensure that the model does not memorize the training data but learns to generalize from it.
- Select the Best Model Parameters: Penalized regression models, such as those trained with `glmnet`, have parameters that control the strength of the penalty (e.g., `lambda`). Cross-validation helps find the best values for these parameters.

When using the `glmnet` package, cross-validation can be performed using the `cv.glmnet` function. Here's how the process works:

1. Split the Data: The data is divided into k folds (common choices are 5 or 10 folds). Each fold is a subset of the data.
2. Train and Validate: The model is trained k times. In each iteration, $k - 1$ folds are used for training, and the remaining fold is used for validation. This process is repeated until each fold has been used as the validation set exactly once.
3. Calculate Performance: The performance of the model (e.g., mean squared error for regression) is calculated for each fold. The average performance across all folds is computed to get an overall measure of how well the model is expected to perform on unseen data.
4. Select the Best Parameters: The `cv.glmnet` function evaluates different values of the penalty parameter (`lambda`). It selects the `lambda` value that results in the best average performance across the folds.

In this case, we will use the `cv_glmnet` learner, which will automatically select the best value of the penalization parameters. When the `alpha` parameter is set to 0, the model is a Ridge regression model. When the `alpha` parameter is set to 1, the model is a Lasso regression model.

21. Examples

```
learner = lrn("regr.cv_glmnet", nfolds=10, alpha=0)
```

21.6.3.3.1. Train

```
learner$train(exp_pred_task)

measures = msrs(c('regr.rsq', 'regr.mse', 'regr.rmse'))
pred_train$score(measures)

rsq  regr.mse regr.rmse
0.7505366 4.8335493 2.1985334
```

In the case of the penalized regression, we can also look at the coefficients of the model.

```
coef(learner$model)

15 x 1 sparse Matrix of class "dgCMatrix"
  s0
(Intercept) 0.10173828
Control      -0.07049573
Dnase        0.87495827
H2az         0.33778155
H3k27ac     0.19454755
H3k27me3    -0.26196627
H3k36me3    0.70067015
H3k4me1     -0.06753216
H3k4me2     0.15796965
H3k4me3     0.38806405
H3k79me2    0.94399114
H3k9ac       0.50694074
H3k9me1     -0.07422291
H3k9me3     -0.17013775
H4k20me1    0.11617186
```

Note that the coefficients are all zero for the histone marks that were not selected by the model. In this case, we can use the model not to predict new data, but to help us understand the data.

21. Examples

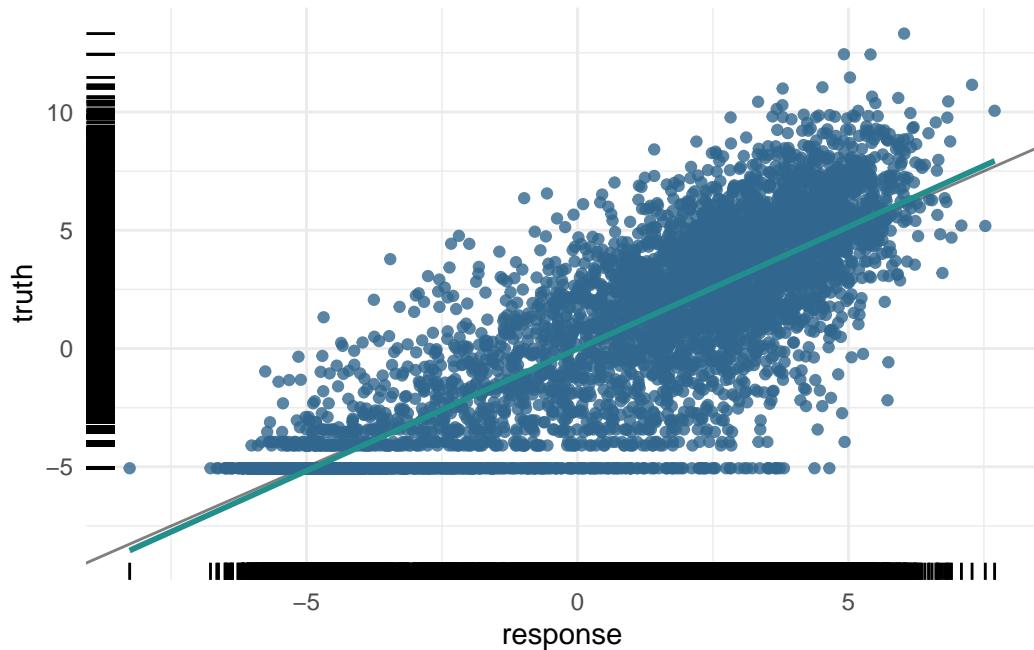
```
pred_train = learner$predict(exp_pred_task, split$train)
pred_test = learner$predict(exp_pred_task, split$test)
```

21.6.3.3.2. Assess

```
pred_train
```

```
<PredictionRegr> for 5789 observations:
  row_ids      truth   response
    1  6.082343  4.892642
    2  2.989145  2.932909
    3 -5.058894 -4.518292
    ...
  8637 -5.058894 -4.341742
  8638  6.089159  4.696146
  8640 -3.114148 -4.153795
```

```
plot(pred_train)
```



For the training data:

21. Examples

```
measures = msrs(c('regr.rsq'))
pred_train$score(measures)
```

```
rsq
0.742853
```

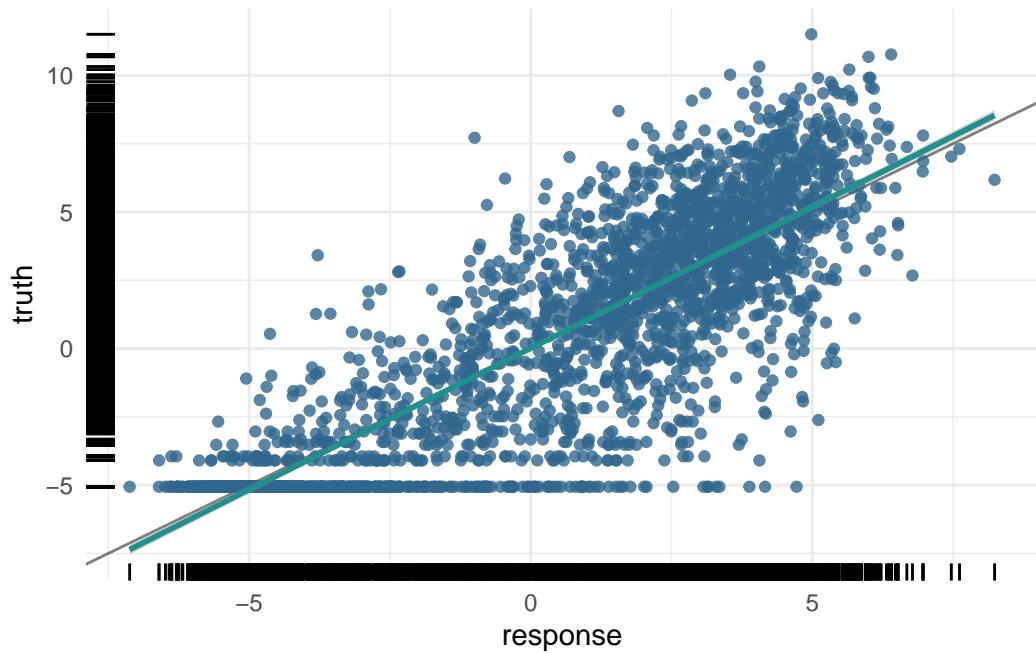
And the test data:

```
pred_test$score(measures)
```

```
rsq
0.7428019
```

And the plot of the test data predictions:

```
plot(pred_test)
```



21. Examples

```
# Calculate the R-squared value
truth <- pred_test$truth
predicted <- pred_test$response
rss <- sum((truth - predicted)^2) # Residual sum of squares
tss <- sum((truth - mean(truth))^2) # Total sum of squares
r_squared <- 1 - (rss / tss)
```

Part VI.

Bioconductor

22. Accessing and working with public omics data

22.1. Background

The data we are going to access are from [this paper](#).

Background: The tumor microenvironment is an important factor in cancer immunotherapy response. To further understand how a tumor affects the local immune system, we analyzed immune gene expression differences between matching normal and tumor tissue. Methods: We analyzed public and new gene expression data from solid cancers and isolated immune cell populations. We also determined the correlation between CD8, FoxP3 IHC, and our gene signatures. Results: We observed that regulatory T cells (Tregs) were one of the main drivers of immune gene expression differences between normal and tumor tissue. A tumor-specific CD8 signature was slightly lower in tumor tissue compared with normal of most (12 of 16) cancers, whereas a Treg signature was higher in tumor tissue of all cancers except liver. Clustering by Treg signature found two groups in colorectal cancer datasets. The high Treg cluster had more samples that were consensus molecular subtype 1/4, right-sided, and microsatellite-instable, compared with the low Treg cluster. Finally, we found that the correlation between signature and IHC was low in our small dataset, but samples in the high Treg cluster had significantly more CD8+ and FoxP3+ cells compared with the low Treg cluster. Conclusions: Treg gene expression is highly indicative of the overall tumor immune environment. Impact: In comparison with the consensus molecular subtype and microsatellite status, the Treg signature identifies more colorectal tumors with high immune activation that may benefit from cancer immunotherapy.

In this little exercise, we will:

1. Access public omics data using the GEOquery package
2. Get an opportunity to work with another SummarizedExperiment object.
3. Perform a simple unsupervised analysis to visualize these public data.

22.2. GEOquery to PCA

The first step is to install the R package [GEOquery](#). This package allows us to access data from the Gene Expression Omnibus (GEO) database. GEO is a public repository of omics data.

```
BiocManager::install("GEOquery")
```

GEOquery has only one commonly used function, `getGEO()` which takes a GEO accession number as an argument. The GEO accession number is a unique identifier for a dataset.

Use the [GEOquery](#) package to fetch data about [GSE103512](#).

```
library(GEOquery)
gse = getGEO("GSE103512")[[1]]
```

You might ask why we are using `[[1]]` at the end of the `getGEO()` function. The reason is that `getGEO()` returns a list of GSE objects. We are only interested in the first one (and in this case, the only one). We return a list of GSE objects because in the early days, it was not unusual to have a single GEO accession number represent multiple datasets. While uncommon now, we've kept the convention since lots of "older" data is still quite useful.

Again, a historically-derived detail, is to convert from the older Bioconductor data structure (GEOquery was written in 2007), the `ExpressionSet`, to the newer `SummarizedExperiment`.

```
library(SummarizedExperiment)
se = as(gse, "SummarizedExperiment")
```

Use some code to determine the answers to the following:

- What is the class of `se`?
- What are the dimensions of `se`?
- What are the dimensions of the `assay` slot of `se`?
- What are the dimensions of the `colData` slot of `se`?
- What variables are in the `colData` slot of `se`?

Examine two variables of interest, cancer type and tumor/normal status. The `with` function is a convenience to allow us to access variables in a data frame by name (rather than having to do `dataframe$variable_name`). Recalling that the `table` function is a convenient way to summarize the counts of unique values in a vector, we can use `with` to access the variables of interest and `table` to summarize the counts of unique values.

22. Accessing and working with public omics data

```
with(colData(se),table(`cancer.type.ch1`,`normal.ch1`))
```

```
normal.ch1
cancer.type.ch1 no yes
    BC     65 10
    CRC    57 12
    NSCLC 60  9
    PCA    60  7
```

- How many samples are there of each cancer type?
- How many samples are there of each tumor/normal status?

When performing unsupervised analysis, it is common to filter genes by variance to find the most informative genes. It is common practice to filter genes by standard deviation or some other measure of variability and keep the top X percent of them when performing dimensionality reduction. There is not a single right answer to what percentage to use, so try a few to see what happens. In the example code, I chose to use the top 500 genes by standard deviation, but you can play with the threshold to see what happens.

Recall that the `assay` function is used to access the data matrix of the `SummarizedExperiment` object.

Think through the code below and then run it.

```
sds = apply(assay(se, 'exprs'), 1, sd)
dat = assay(se, 'exprs')[order(sds, decreasing = TRUE)[1:500],]
```

If you don't recognize the function `apply`, it is a function that applies a function to each row or column of a matrix. In this case, we are applying the `sd` function to each row of the data matrix. The `order` function is used to sort the standard deviations in decreasing order (when `decreasing=TRUE`). And the `[1:500]` is used to subset the data matrix to the top 500 genes by standard deviation.

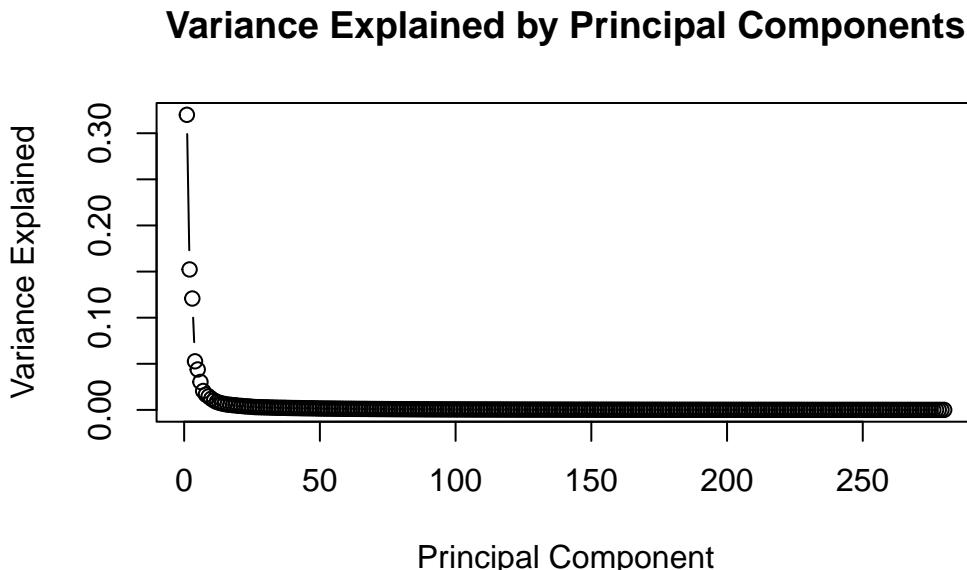
Perform PCA and prepare for plotting. We will be using `ggplot2`, so we need to make a `data.frame` before plotting.

```
pca_results <- prcomp(t(dat))
pca_df = as.data.frame(pca_results$x)
pca_df$Type=factor(colData(se)[,'cancer.type.ch1'])
pca_df$Normal = factor(colData(se)[,'normal.ch1'])
```

22. Accessing and working with public omics data

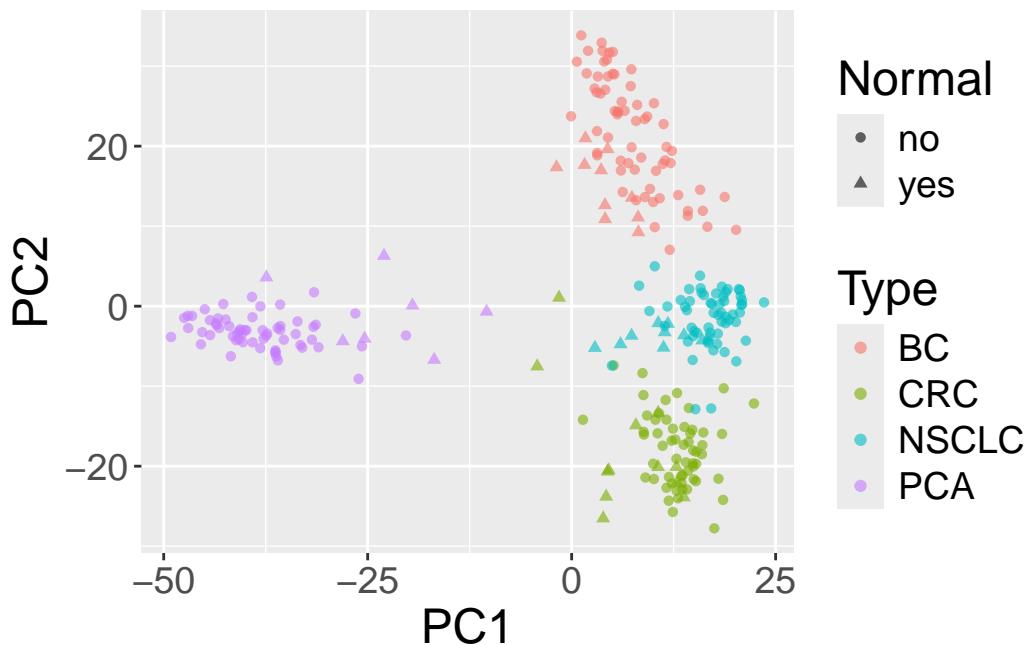
We can take a look at the variance explained by each principal component as a plot.

```
library(ggplot2)
pca_var <- pca_results$sdev^2 / sum(pca_results $sdev^2)
plot(pca_var, xlab = "Principal Component", ylab = "Variance Explained",
     main = "Variance Explained by Principal Components", type = "b")
```



Now, we are going to plot the results of the PCA, coloring the points by cancer type and using different shapes for normal and tumor samples.

```
library(ggplot2)
ggplot(pca_df, aes(x=PC1,y=PC2,shape=Normal,color=Type)) +
  geom_point( alpha=0.6) + theme(text=element_text(size = 18))
```



In this case, the x-axis is the first principal component and the y-axis is the second principal component.

- What do you see?
- What about additional principal components?
- Bonus: Try using the `GGally` package to plot principal components (using the `ggpairs` function).
- Bonus: Calculate the variance explained by each principal component and plot the results.

23. Introduction to `SummarizedExperiment`

The `SummarizedExperiment` class is used to store rectangular matrices of experimental results, which are commonly produced by sequencing and microarray experiments. Each object stores observations of one or more samples, along with additional meta-data describing both the observations (features) and samples (phenotypes).

A key aspect of the `SummarizedExperiment` class is the coordination of the meta-data and assays when subsetting. For example, if you want to exclude a given sample you can do for both the meta-data and assay in one operation, which ensures the meta-data and observed data will remain in sync. Improperly accounting for meta and observational data has resulted in a number of incorrect results and retractions so this is a very desirable property.

`SummarizedExperiment` is in many ways similar to the historical `ExpressionSet`, the main distinction being that `SummarizedExperiment` is more flexible in its row information, allowing both `GRanges` based as well as those described by arbitrary `DataFrames`. This makes it ideally suited to a variety of experiments, particularly sequencing based experiments such as RNA-Seq and ChIP-Seq.

```
BiocManager::install('airway')
BiocManager::install('SummarizedExperiment')
```

23.1. Anatomy of a `SummarizedExperiment`

The *SummarizedExperiment* package contains two classes: `SummarizedExperiment` and `RangedSummarizedExperiment`.

`SummarizedExperiment` is a matrix-like container where rows represent features of interest (e.g. genes, transcripts, exons, etc.) and columns represent samples. The objects contain one or more assays, each represented by a matrix-like object of numeric or other mode. The rows of a `SummarizedExperiment` object represent features of interest. Information about these features is stored in a `DataFrame` object, accessible using the function `rowData()`. Each row of the `DataFrame` provides information on the feature in the corresponding row

23. Introduction to `SummarizedExperiment`

of the `SummarizedExperiment` object. Columns of the `DataFrame` represent different attributes of the features of interest, e.g., gene or transcript IDs, etc.

`RangedSummarizedExperiment` is the “child” of the `SummarizedExperiment` class which means that all the methods on `SummarizedExperiment` also work on a `RangedSummarizedExperiment`.

The fundamental difference between the two classes is that the rows of a `RangedSummarizedExperiment` object represent genomic ranges of interest instead of a `DataFrame` of features. The `RangedSummarizedExperiment` ranges are described by a `GRanges` or a `GRangesList` object, accessible using the `rowRanges()` function.

Figure 23.1 displays the class geometry and highlights the vertical (column) and horizontal (row) relationships.

23.1.1. Assays

The `airway` package contains an example dataset from an RNA-Seq experiment of read counts per gene for airway smooth muscles. These data are stored in a `RangedSummarizedExperiment` object which contains 8 different experimental and assays 64,102 gene transcripts.

```
Loading required package: airway
```

```
library(SummarizedExperiment)
data(airway, package="airway")
se <- airway
se
```



```
class: RangedSummarizedExperiment
dim: 63677 8
metadata(1): ''
assays(1): counts
rownames(63677): ENSG000000000003 ENSG000000000005 ... ENSG00000273492
ENSG00000273493
rowData names(10): gene_id gene_name ... seq_coord_system symbol
colnames(8): SRR1039508 SRR1039509 ... SRR1039520 SRR1039521
colData names(9): SampleName cell ... Sample BioSample
```

To retrieve the experiment data from a `SummarizedExperiment` object one can use the `assays()` accessor. An object can have multiple assay datasets each of which can be accessed using the `$` operator. The `airway` dataset contains only one assay (`counts`). Here each row represents a gene transcript and each column one of the samples.

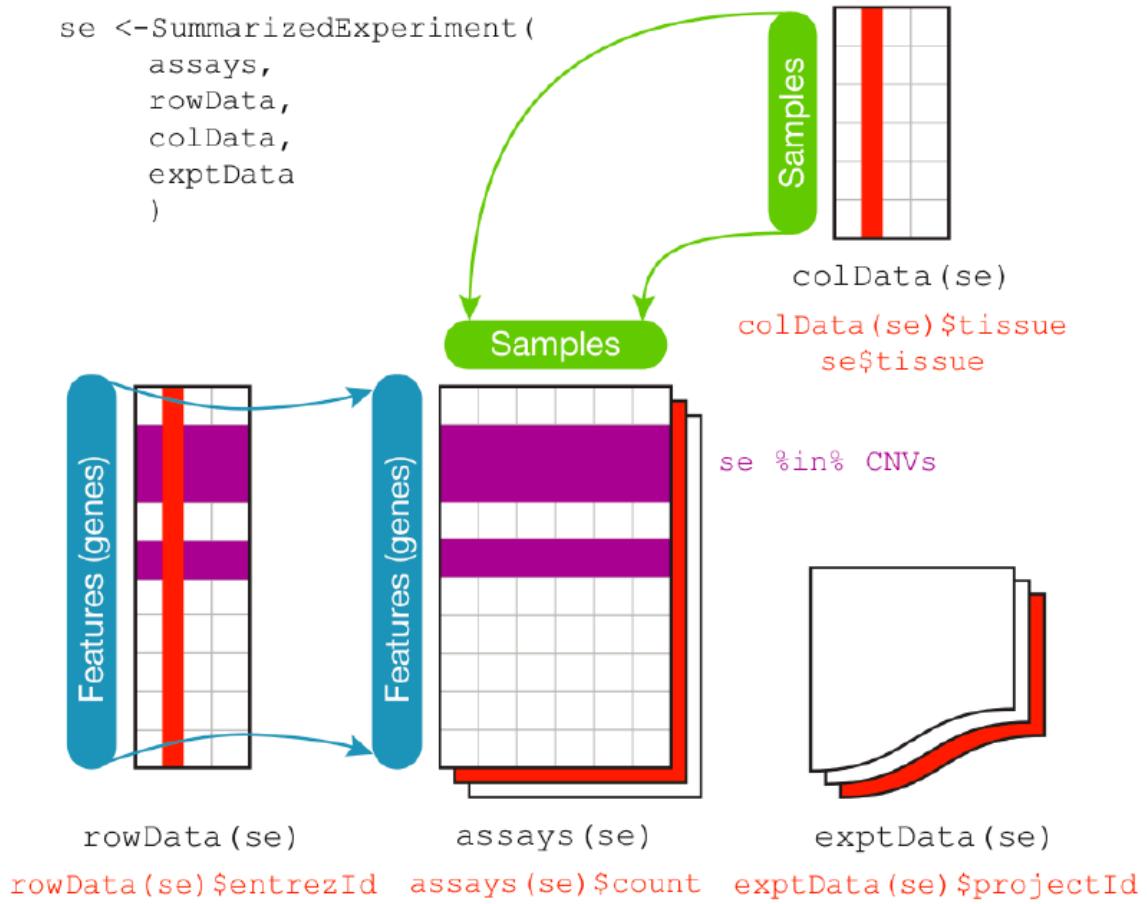


Figure 23.1.: Summarized Experiment. There are three main components, the `colData()`, the `rowData()` and the `assays()`. The accessors for the various parts of a complete `SummarizedExperiment` object match the names.

23. Introduction to *SummarizedExperiment*

```
assays(se)$counts
```

	SRR1039567	SRR1039568	SRR1039569	SRR1039570	SRR1039571	SRR1039572	SRR1039573	SRR1039574	SRR1039575	SRR1039576	SRR1039577	SRR1039578	SRR1039579	SRR1039570	SRR1039571	SRR1039572	
ENSG000000000000679	448	873	408	1138	1047	770	572	0	0	0	0	0	0	0	0	0	
ENSG0000000000050	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
ENSG0000000041467	515	621	365	587	799	417	508	211	263	164	245	331	233	229	55	40	35
ENSG000000004260	211	263	164	245	331	233	229	55	40	35	78	63	76	60	0	2	0
ENSG0000000046060	0	2	0	1	0	0	0	0	0	0	0	0	0	0	3679	6177	4252
ENSG000000009380	3679	6177	4252	6721	11027	5176	7995	1062	1733	881	1424	1439	1359	1109	1062	1733	881
ENSG0000000010333	1062	1733	881	1424	1439	1359	1109	380	595	493	820	714	696	704	380	595	493
ENSG0000000010519	380	595	493	820	714	696	704	236	464	175	658	584	360	269	236	464	175
ENSG00000000116794	236	464	175	658	584	360	269										

23.1.2. ‘Row’ (regions-of-interest) data

The `rowRanges()` accessor is used to view the range information for a `RangedSummarizedExperiment`. (Note if this were the parent `SummarizedExperiment` class we’d use `rowData()`). The data are stored in a `GRangesList` object, where each list element corresponds to one gene transcript and the ranges in each `GRanges` correspond to the exons in the transcript.

```
rowRanges(se)
```

`GRangesList` object of length 63677:

\$ENSG00000000003

`GRanges` object with 17 ranges and 2 metadata columns:

	seqnames	ranges	strand	exon_id	exon_name
	<Rle>	<IRanges>	<Rle>	<integer>	<character>
[1]	X	99883667-99884983	-	667145	ENSE00001459322
[2]	X	99885756-99885863	-	667146	ENSE00000868868
[3]	X	99887482-99887565	-	667147	ENSE00000401072
[4]	X	99887538-99887565	-	667148	ENSE00001849132
[5]	X	99888402-99888536	-	667149	ENSE00003554016
...
[13]	X	99890555-99890743	-	667156	ENSE00003512331
[14]	X	99891188-99891686	-	667158	ENSE00001886883
[15]	X	99891605-99891803	-	667159	ENSE00001855382

23. Introduction to SummarizedExperiment

```
[16]      X 99891790-99892101      - | 667160 ENSE00001863395
[17]      X 99894942-99894988      - | 667161 ENSE00001828996
-----
seqinfo: 722 sequences (1 circular) from an unspecified genome

...
<63676 more elements>
```

23.1.3. ‘Column’ (sample) data

Sample meta-data describing the samples can be accessed using `colData()`, and is a `DataFrame` that can store any number of descriptive columns for each sample row.

```
colData(se)
```

```
DataFrame with 8 rows and 9 columns
  SampleName    cell     dex   albut      Run avgLength
  <factor> <factor> <factor> <factor> <factor> <integer>
SRR1039508 GSM1275862 N61311 untrt  untrt SRR1039508      126
SRR1039509 GSM1275863 N61311 trt    untrt  SRR1039509      126
SRR1039512 GSM1275866 N052611 untrt  untrt  SRR1039512      126
SRR1039513 GSM1275867 N052611 trt    untrt  SRR1039513      87
SRR1039516 GSM1275870 N080611 untrt  untrt  SRR1039516      120
SRR1039517 GSM1275871 N080611 trt    untrt  SRR1039517      126
SRR1039520 GSM1275874 N061011 untrt  untrt  SRR1039520      101
SRR1039521 GSM1275875 N061011 trt    untrt  SRR1039521      98
  Experiment    Sample    BioSample
  <factor> <factor> <factor>
SRR1039508 SRX384345 SRS508568 SAMN02422669
SRR1039509 SRX384346 SRS508567 SAMN02422675
SRR1039512 SRX384349 SRS508571 SAMN02422678
SRR1039513 SRX384350 SRS508572 SAMN02422670
SRR1039516 SRX384353 SRS508575 SAMN02422682
SRR1039517 SRX384354 SRS508576 SAMN02422673
SRR1039520 SRX384357 SRS508579 SAMN02422683
SRR1039521 SRX384358 SRS508580 SAMN02422677
```

This sample metadata can be accessed using the `$` accessor which makes it easy to subset the entire object by a given phenotype.

23. Introduction to *SummarizedExperiment*

```
# subset for only those samples treated with dexamethasone
se[, se$dex == "trt"]

class: RangedSummarizedExperiment
dim: 63677 4
metadata(1): ''
assays(1): counts
rownames(63677): ENSG000000000003 ENSG000000000005 ... ENSG00000273492
  ENSG00000273493
rowData names(10): gene_id gene_name ... seq_coord_system symbol
colnames(4): SRR1039509 SRR1039513 SRR1039517 SRR1039521
colData names(9): SampleName cell ... Sample BioSample
```

23.1.4. Experiment-wide metadata

Meta-data describing the experimental methods and publication references can be accessed using `metadata()`.

```
metadata(se)
```

```
[[1]]
Experiment data
  Experimenter name: Himes BE
  Laboratory: NA
  Contact information:
  Title: RNA-Seq transcriptome profiling identifies CRISPLD2 as a glucocorticoid responsive
  URL: http://www.ncbi.nlm.nih.gov/pubmed/24926665
  PMIDs: 24926665

  Abstract: A 226 word abstract is available. Use 'abstract' method.
```

Note that `metadata()` is just a simple list, so it is appropriate for *any* experiment wide metadata the user wishes to save, such as storing model formulas.

```
metadata(se)$formula <- counts ~ dex + albut

metadata(se)
```

23. Introduction to *SummarizedExperiment*

```
[[1]]
Experiment data
  Experimenter name: Himes BE
  Laboratory: NA
  Contact information:
    Title: RNA-Seq transcriptome profiling identifies CRISPLD2 as a glucocorticoid responsive
    URL: http://www.ncbi.nlm.nih.gov/pubmed/24926665
    PMIDs: 24926665

  Abstract: A 226 word abstract is available. Use 'abstract' method.
```

```
$formula
counts ~ dex + albut
```

23.2. Common operations on *SummarizedExperiment*

23.2.1. Subsetting

- [Performs two dimensional subsetting, just like subsetting a matrix or data frame.

```
# subset the first five transcripts and first three samples
se[1:5, 1:3]
```

```
class: RangedSummarizedExperiment
dim: 5 3
metadata(2): '' formula
assays(1): counts
rownames(5): ENSG00000000003 ENSG00000000005 ENSG00000000419
             ENSG00000000457 ENSG00000000460
rowData names(10): gene_id gene_name ... seq_coord_system symbol
colnames(3): SRR1039508 SRR1039509 SRR1039512
colData names(9): SampleName cell ... Sample BioSample
```

- \$ operates on `colData()` columns, for easy sample extraction.

```
se[, se$cell == "N61311"]
```

```

class: RangedSummarizedExperiment
dim: 63677 2
metadata(2): '' formula
assays(1): counts
rownames(63677): ENSG000000000003 ENSG000000000005 ... ENSG00000273492
ENSG00000273493
rowData names(10): gene_id gene_name ... seq_coord_system symbol
colnames(2): SRR1039508 SRR1039509
colData names(9): SampleName cell ... Sample BioSample

```

23.2.2. Getters and setters

- `rowRanges()` / (`rowData()`, `colData()`, `metadata()`)

```

counts <- matrix(1:15, 5, 3, dimnames=list(LETTERS[1:5], LETTERS[1:3]))

dates <- SummarizedExperiment(assays=list(counts=counts),
                             rowData=DataFrame(month=month.name[1:5], day=1:5))

# Subset all January assays
dates[rowData(dates)$month == "January", ]

```

```

class: SummarizedExperiment
dim: 1 3
metadata(0):
assays(1): counts
rownames(1): A
rowData names(2): month day
colnames(3): A B C
colData names(0):

```

- `assay()` versus `assays()` There are two accessor functions for extracting the assay data from a `SummarizedExperiment` object. `assays()` operates on the entire list of assay data as a whole, while `assay()` operates on only one assay at a time. `assay(x, i)` is simply a convenience function which is equivalent to `assays(x)[[i]]`.

```
assays(se)
```

```

List of length 1
names(1): counts

```

23. Introduction to *SummarizedExperiment*

```
assays(se) [[1]] [1:5, 1:5]
```

	SRR1039508	SRR1039509	SRR1039512	SRR1039513	SRR1039516
ENSG000000000003	679	448	873	408	1138
ENSG000000000005	0	0	0	0	0
ENSG000000000419	467	515	621	365	587
ENSG000000000457	260	211	263	164	245
ENSG000000000460	60	55	40	35	78

```
# assay defaults to the first assay if no i is given  
assay(se) [1:5, 1:5]
```

	SRR1039508	SRR1039509	SRR1039512	SRR1039513	SRR1039516
ENSG000000000003	679	448	873	408	1138
ENSG000000000005	0	0	0	0	0
ENSG000000000419	467	515	621	365	587
ENSG000000000457	260	211	263	164	245
ENSG000000000460	60	55	40	35	78

```
assay(se, 1) [1:5, 1:5]
```

	SRR1039508	SRR1039509	SRR1039512	SRR1039513	SRR1039516
ENSG000000000003	679	448	873	408	1138
ENSG000000000005	0	0	0	0	0
ENSG000000000419	467	515	621	365	587
ENSG000000000457	260	211	263	164	245
ENSG000000000460	60	55	40	35	78

23.2.3. Range-based operations

- `subsetByOverlaps()` *SummarizedExperiment* objects support all of the `findOverlaps()` methods and associated functions. This includes `subsetByOverlaps()`, which makes it easy to subset a *SummarizedExperiment* object by an interval.

In the next code block, we define a region of interest (or many regions of interest) and then subset our *SummarizedExperiment* by overlaps with this region.

23. Introduction to *SummarizedExperiment*

```
# Subset for only rows which are in the interval 100,000 to 110,000 of
# chromosome 1
roi <- GRanges(seqnames="1", ranges=100000:1100000)
sub_se = subsetByOverlaps(se, roi)
sub_se

class: RangedSummarizedExperiment
dim: 74 8
metadata(2): '' formula
assays(1): counts
rownames(74): ENSG00000131591 ENSG00000177757 ... ENSG00000272512
  ENSG00000273443
rowData names(10): gene_id gene_name ... seq_coord_system symbol
colnames(8): SRR1039508 SRR1039509 ... SRR1039520 SRR1039521
colData names(9): SampleName cell ... Sample BioSample

dim(sub_se)

[1] 74 8
```

23.3. Constructing a *SummarizedExperiment*

To construct a *SummarizedExperiment* object, you need to provide the following components:

- **assays**: A list of matrices or matrix-like objects containing the data.
- **rowData**: A **DataFrame** containing information about the features (rows).
- **colData**: A **DataFrame** containing information about the samples (columns).
- +/- **metadata**: A list containing additional metadata about the experiment.

For a nearly real example, we will use the DeRisi dataset. We'll start with the original data, which is a **data.frame** with the first couple of columns containing the gene information and the rest of the columns containing the data.

```
# Load the DeRisi dataset
deRisi <- read.csv("https://raw.githubusercontent.com/seandavi/RBiocBook/refs/heads/main/d
head(deRisi)
```

23. Introduction to *SummarizedExperiment*

ORF	Name	R1	R2	R3	R4	R5	R6	R7	R1.Bkg	R2.Bkg	R3.Bkg	
1	YHR007C	ERG11	7896	7484	14679	14617	9853	7599	6490	1155	1984	1323
2	YBR218C	PYC2	12144	11177	10241	4820	4950	7047	17035	1074	1694	1243
3	YAL051W	FUN43	4478	6435	6230	6848	5111	7180	4497	1140	1950	1649
4	YAL053W		6343	8243	6743	3304	3556	4694	3849	1020	1897	1196
5	YAL054C	ACS1	1542	3044	2076	1695	1753	4806	10802	1082	1940	1504
6	YAL055W		1769	3243	2094	1367	1853	3580	1956	975	1821	1185
		R4.Bkg	R5.Bkg	R6.Bkg	R7.Bkg	G1	G2	G3	G4	G5	G6	G7
1	1171	914	2445	981	8432	7173	11736	16798	12315	16111	13931	2404
2	876	1211	2444	742	11509	10226	13372	6500	6255	9024	6904	2148
3	1183	898	2637	927	5865	5895	5345	6302	5400	7933	5026	2422
4	881	1045	2518	697	6762	7454	6323	3595	4689	5660	4145	2107
5	1108	902	2610	980	3138	3785	2419	2114	2763	3561	1897	2405
6	851	1047	2536	698	2844	4069	2583	1651	2530	3484	1550	1674
		G2.Bkg	G3.Bkg	G4.Bkg	G5.Bkg	G6.Bkg	G7.Bkg					
1	2561	1598	1506	1696	2667	1244						
2	2527	1641	1196	1553	2569	848						
3	2496	1902	1501	1644	2808	1154						
4	2663	1607	1162	1577	2544	857						
5	2528	1847	1445	1713	2767	1142						
6	2648	1591	1114	1528	2668	870						

To convert this to a `SummarizedExperiment`, we need to extract the assay data, row data, and column data. The assay data will be the numeric values in the data frame, the row data will be the gene information, and the column data will be the sample information.

23.3.1. `rowData`, or feature information

Let's start with the `rowData`, which will be a `DataFrame` containing the gene information. We can use the first two columns of the data frame for this purpose.

```
rdata <- deRisi[, 1:2]
head(rdata)
```

```
ORF  Name
1 YHR007C ERG11
2 YBR218C PYC2
3 YAL051W FUN43
4 YAL053W
```

23. Introduction to *SummarizedExperiment*

```
5 YAL054C ACS1
6 YAL055W
```

23.3.2. colData, or sample information

Next, we will create the `colData`, which will be a `DataFrame` containing the sample information. Since the sample information really isn't in the dataset, we will create a simple `DataFrame` with sample names.

```
cdata <- DataFrame(sample=paste("Sample", 0:6), timepoint = 0:6,
  hours = c(0, 9.5,11.5,13.5,15.5,18.5,20.5))
head(cdata)
```

```
DataFrame with 6 rows and 3 columns
  sample timepoint    hours
  <character> <integer> <numeric>
1   Sample 0         0      0.0
2   Sample 1         1      9.5
3   Sample 2         2     11.5
4   Sample 3         3     13.5
5   Sample 4         4     15.5
6   Sample 5         5     18.5
```

23.3.3. assays, or the data

Remember that the DeRisi dataset has four *different* assays,

assay	description
R	Red fluorescence
G	Green fluorescence
Rb	Red background fluorescence
Gb	Green background fluorescence

We will create a list of matrices, one for each assay. The matrices will be the numeric values in the data frame, excluding the first two columns.

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```
R <- as.matrix(deRisi[, 3:9])
G <- as.matrix(deRisi[, 10:16])
Rb <- as.matrix(deRisi[, 17:23])
Gb <- as.matrix(deRisi[, 24:30])
```

When we create a *SummarizedExperiment* object, the “constructor” will check to see that the colnames of the matrices in the list are the same as the *rownames* of the *colData DataFrame*, and that the rownames of the matrices in the list are the same as the *rownames* of the *rowData DataFrame*.

So, we need to fix that all up. Let’s start wit the rownames of the *rowData DataFrame*:

```
rownames(rdata) <- rdata$ORF
```

Now, let’s set the rownames of the *coldata DataFrame* to the sample names:

```
rownames(cdata) <- cdata$sample
```

Now, we can fix the rownames and colnames of the matrices for our R, G, Rb, and Gb assays:

```
rownames(R) <- rdata$ORF
rownames(G) <- rdata$ORF
rownames(Rb) <- rdata$ORF
rownames(Gb) <- rdata$ORF
colnames(R) <- cdata$sample
colnames(G) <- cdata$sample
colnames(Rb) <- cdata$sample
colnames(Gb) <- cdata$sample
```

Take a look at the matrices to make sure they look right.

23.3.4. Putting it all together

```
se <- SummarizedExperiment(assays=list(R=R, G=G, Rb=Rb, Gb=Gb), rowData=rdata, colData=cdata)
```

23.3.5. Getting logRatios

Now that we have a `SummarizedExperiment` object, we can easily compute the log ratios of the Red and Green foreground fluorescence. This is a common operation in microarray data analysis.

```
logRatios <- log2(
  (assay(se, "R") - assay(se, "Rb")) / (assay(se, "G") - assay(se, "Gb"))
)
```

Warning: NaNs produced

```
assays(se)$logRatios <- logRatios
```

Now, we've added a new assay to the `SummarizedExperiment` object called `logRatios`. This assay contains the log ratios of the Red and Green foreground fluorescence.

```
assays(se)
```

```
List of length 5
names(5): R G Rb Gb logRatios
```

And if we want to access the log ratios, we can do so using the `assay()` method:

```
head(assay(se, "logRatios"))
```

	Sample 0	Sample 1	Sample 2	Sample 3	Sample 4	Sample 5
YHR007C	-1.2204686	NaN	NaN	2.70275677	1.6545902	5.260867
YBR218C	NaN	NaN	2.9757832	2.39231742	1.9319816	3.983313
YAL051W	0.1135715	NaN	NaN	NaN	-1.3681061	2.138654
YAL053W	-1.3753298	NaN	NaN	0.05044902	1.0906497	5.215440
YAL054C	0.2706476	0.333657387	0.0000000	0.31420165	0.3165815	NaN
YAL055W	0.6209723	-0.001745548	0.2683547	0.11082813	0.4931189	NaN
	Sample 6					
YHR007C	4.8223618					
YBR218C	NaN					
YAL051W	1.2205754					
YAL053W	0.8875253					
YAL054C	NaN					
YAL055W	NaN					

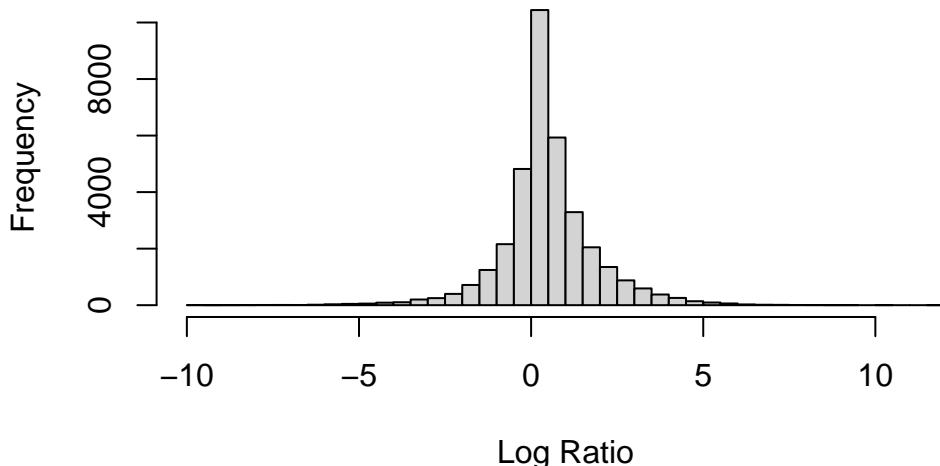
23. Introduction to SummarizedExperiment

```
## OR  
head(assays(se)$logRatios)
```

	Sample 0	Sample 1	Sample 2	Sample 3	Sample 4	Sample 5
YHR007C	-1.2204686	NaN	NaN	2.70275677	1.6545902	5.260867
YBR218C	NaN	NaN	2.9757832	2.39231742	1.9319816	3.983313
YAL051W	0.1135715	NaN	NaN	NaN	-1.3681061	2.138654
YAL053W	-1.3753298	NaN	NaN	0.05044902	1.0906497	5.215440
YAL054C	0.2706476	0.333657387	0.0000000	0.31420165	0.3165815	NaN
YAL055W	0.6209723	-0.001745548	0.2683547	0.11082813	0.4931189	NaN
	Sample 6					
YHR007C	4.8223618					
YBR218C	NaN					
YAL051W	1.2205754					
YAL053W	0.8875253					
YAL054C	NaN					
YAL055W	NaN					

```
hist(assays(se)$logRatios, breaks=50, main="Log Ratios of Red and Green Foreground Fluorescence")
```

Log Ratios of Red and Green Foreground Fluorescence



24. Genomic Ranges Introduction

24.1. Introduction

Genomic ranges are fundamental data structures in bioinformatics that represent intervals on chromosomes. They are essential for analyzing ChIP-seq peaks, gene annotations, regulatory elements, and other genomic features. In this tutorial, we'll explore the BED file format and demonstrate practical genomic range operations using R's rtracklayer package.

This tutorial will cover:

- Understanding the BED file format
- Loading genomic ranges from BED files
- Basic exploration of genomic ranges
- Accessing and manipulating genomic coordinates

24.2. The dataset

We'll use CTCF ChIP-seq peak data from the ENCODE project. CTCF (CCCTC-binding factor) is a key architectural protein that helps organize chromatin structure. The data is available in BED format, which we will load and analyze. Each peak represents the results of a ChIP-seq experiment, indicating regions where CTCF binds to DNA. The sample was sequenced, aligned, and peaks were called using standard ChIP-seq analysis pipelines. The peaks are stored in a BED file, which we will import into R for analysis.

24.3. The BED File Format

The Browser Extensible Data (BED) format is a standard way to represent genomic intervals. BED files are tab-delimited text files where each line represents a genomic feature.

24.3.1. BED Format Structure

The BED format has several required and optional fields:

Required fields (BED3):

- **chrom**: Chromosome name (e.g., chr1, chr2, chrX)
- **chromStart**: Start position (0-based, inclusive)
- **chromEnd**: End position (0-based, exclusive)

Optional fields:

- **name**: Feature name/identifier
- **score**: Score (0-1000)
- **strand**: Strand (+ or - OR '')
- **thickStart**: Start of thick drawing
- **thickEnd**: End of thick drawing
- **itemRgb**: RGB color values
- **blockCount**: Number of blocks
- **blockSizes**: Block sizes
- **blockStarts**: Block start positions

24.3.2. Key Concepts

- **0-based coordinate system**: BED uses 0-based coordinates where the first base is position 0
- **Half-open intervals**: chromStart is inclusive, chromEnd is exclusive
- **Width calculation**: Width = chromEnd - chromStart

Example BED entry:

```
chr1      1000      2000      peak1      500      +
```

This represents a feature named “peak1” on chromosome 1, from position 1000 to 1999 (width = 1000 bp).

24.4. Loading Required Libraries

```
# Load required libraries
library(rtracklayer)
library(GenomicRanges)
library(ggplot2)
library(dplyr)

# Set up plotting theme
theme_set(theme_minimal())
```

24.5. Loading CTCF ChIP-seq Data

We'll work with CTCF ChIP-seq peak data from the ENCODE project. CTCF (CCCTC-binding factor) is a key architectural protein that helps organize chromatin structure.

```
# URL for the CTCF ChIP-seq BED file
bed_url <- "https://www.encodeproject.org/files/ENCFF960ZGP/@@download/ENCFF960ZGP.bed.gz"

# Let's first load this file using readr::read_table to check its structure
ctcf_peaks_raw <- readr::read_table(bed_url, col_names=FALSE)

-- Column specification -----
cols(
  X1 = col_character(),
  X2 = col_double(),
  X3 = col_double(),
  X4 = col_character(),
  X5 = col_double(),
  X6 = col_character(),
  X7 = col_double(),
  X8 = col_double(),
  X9 = col_double(),
  X10 = col_double()
)

# Display the first few rows of the raw data
head(ctcf_peaks_raw)
```

24. Genomic Ranges Introduction

```
# A tibble: 6 x 10
  X1      X2      X3 X4      X5 X6      X7     X8     X9     X10
  <chr>    <dbl>    <dbl> <chr>    <dbl> <chr>    <dbl>    <dbl>    <dbl>
1 chr2  238305323 238305539 .     1000 .     7.70   -1  0.274   108
2 chr20 49982706  49982922 .     541  .     8.72   -1  0.466   108
3 chr15 39921015  39921231 .     672  .     9.08   -1  0.547   108
4 chr8   6708273   6708489 .     560  .     9.86   -1  0.662   108
5 chr9   136645956 136646172 .     584  .    10.2   -1  0.751   108
6 chr7   47669294  47669510 .     614  .    10.5   -1  0.807   108
```

Bioconductor's `rtracklayer` package provides a convenient way to import BED files directly into R as `GRanges` objects, which are optimized for genomic range operations. We'll use this package to load the CTCF peaks data.

```
# Load the BED file using rtracklayer
ctcf_peaks <- rtracklayer::import(bed_url, format="narrowPeak")
```

Let's take a look at the loaded CTCF peaks data. The `ctcf_peaks` object is a `GRanges` object that contains genomic ranges representing the CTCF ChIP-seq peaks.

```
ctcf_peaks
```

`GRanges` object with 43865 ranges and 6 metadata columns:

```
  seqnames      ranges strand |      name      score
  <Rle>        <IRanges>  <Rle> | <character> <numeric>
 [1] chr2 238305324-238305539 * | <NA>      1000
 [2] chr20 49982707-49982922 * | <NA>      541
 [3] chr15 39921016-39921231 * | <NA>      672
 [4] chr8  6708274-6708489  * | <NA>      560
 [5] chr9  136645957-136646172 * | <NA>      584
 ...
 [43861] ...       ...      ... | ...
 [43862] chr11 66222736-66222972 * | <NA>      1000
 [43863] chr10 75235956-75236225 * | <NA>      1000
 [43864] chr16 57649100-57649347 * | <NA>      1000
 [43865] chr17 37373596-37373838 * | <NA>      1000
 [43866] chr12 53676108-53676355 * | <NA>      1000
  signalValue     pValue     qValue      peak
  <numeric> <numeric> <numeric> <integer>
 [1]    7.70385      -1    0.27378      108
```

24. Genomic Ranges Introduction

```
[2] 8.71626      -1 0.46571      108
[3] 9.07638      -1 0.54697      108
[4] 9.86234      -1 0.66189      108
[5] 10.15488     -1 0.75082      108
...
[43861] 478.640    -1 4.87574     124
[43862] 480.183    -1 4.87574     141
[43863] 491.081    -1 4.87574     116
[43864] 491.991    -1 4.87574     127
[43865] 494.303    -1 4.87574     126
-----
seqinfo: 26 sequences from an unspecified genome; no seqlengths
```

The `ctcf_peaks` object now contains the genomic ranges of CTCF peaks, including chromosome names, start and end positions, and additional metadata such as peak scores and strand information.

24.6. Understanding GRanges Objects

To get information from a `GRanges` object, we can use various accessor functions. For example, `seqnames()` retrieves the chromosome names, `start()` and `end()` get the start and end positions, and `width()` calculates the width of each peak.

```
# Accessing chromosome names, start, end, and width
length(ctcf_peaks) # Total number of peaks

[1] 43865

seqnames(ctcf_peaks) # Chromosome names (or contig names, etc.)

factor-Rle of length 43865 with 41566 runs
Lengths: 1 1 1 1 1 ... 1 1 1 1 1
Values : chr2 chr20 chr15 chr8 chr9 ... chr11 chr10 chr16 chr17 chr12
Levels(26): chr2 chr20 chr15 ... chr1_KI270714v1_random chrUn_GL000219v1

head(start(ctcf_peaks)) # Start positions (0-based)
```

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```
[1] 238305324 49982707 39921016 6708274 136645957 47669295
```

```
head(end(ctcf_peaks)) # End positions (1-based)
```

```
[1] 238305539 49982922 39921231 6708489 136646172 47669510
```

```
head(width(ctcf_peaks)) # equivalent to end(ctcf_peaks) - start(ctcf_peaks)
```

```
[1] 216 216 216 216 216 216
```

What is the distribution of peak widths? We can visualize this using a histogram.

```
# Create a histogram of peak widths
hist(width(ctcf_peaks), breaks=50, main="CTCF Peak Widths", xlab="Width (bp)", col="lightblue")
```

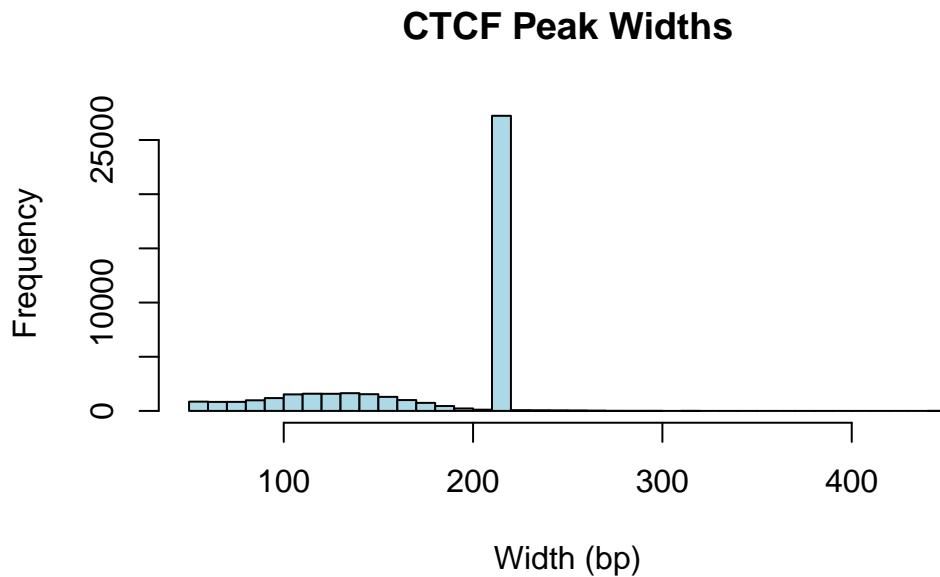


Figure 24.1.: Histogram of CTCF Peak Widths. Why is there a large peak at around 200 bp?

The “metadata” part of a `GRanges` object can be accessed using the `mcols()` function, which returns a data frame-like structure containing additional information about each genomic range.

24. Genomic Ranges Introduction

```
mcols(ctcf_peaks)
```

```
DataFrame with 43865 rows and 6 columns
  name      score signalValue     pValue     qValue     peak
  <character> <numeric>    <numeric> <numeric> <numeric> <integer>
1     NA       1000    7.70385      -1   0.27378     108
2     NA       541     8.71626      -1   0.46571     108
3     NA       672     9.07638      -1   0.54697     108
4     NA       560     9.86234      -1   0.66189     108
5     NA       584    10.15488      -1   0.75082     108
...     ...       ...       ...     ...     ...     ...
43861    NA       1000    478.640      -1   4.87574     124
43862    NA       1000    480.183      -1   4.87574     141
43863    NA       1000    491.081      -1   4.87574     116
43864    NA       1000    491.991      -1   4.87574     127
43865    NA       1000    494.303      -1   4.87574     126
```

The `mcols()` function returns a data frame-like structure containing additional information about each genomic range, such as peak scores and strand orientation. This metadata can be useful for filtering or annotating peaks.

```
mcols(ctcf_peaks)[1:5, ]
```

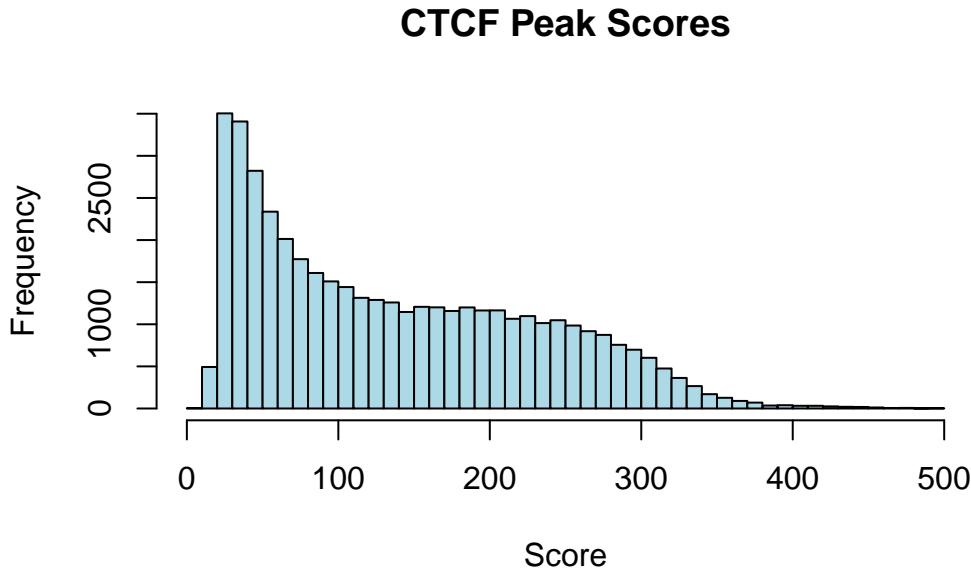
```
DataFrame with 5 rows and 6 columns
  name      score signalValue     pValue     qValue     peak
  <character> <numeric>    <numeric> <numeric> <numeric> <integer>
1     NA       1000    7.70385      -1   0.27378     108
2     NA       541     8.71626      -1   0.46571     108
3     NA       672     9.07638      -1   0.54697     108
4     NA       560     9.86234      -1   0.66189     108
5     NA       584    10.15488      -1   0.75082     108
```

```
mcols(ctcf_peaks)$signalValue[1:5] # Accessing the score column directly
```

```
[1] 7.70385 8.71626 9.07638 9.86234 10.15488
```

24. Genomic Ranges Introduction

```
hist(mcols(ctcf_peaks)$signalValue, breaks=50, main="CTCF Peak Scores", xlab="Score", col="lightblue")
```



24.7. Exploring Peak Characteristics

24.7.1. Basic Peak Statistics

How many peaks do we have? What chromosomes are represented? What is the range of peak widths? Let's calculate some basic statistics about the CTCF peaks.

```
# Calculate basic statistics
cat("==== CTCF Peak Statistics ===\n")

==== CTCF Peak Statistics ===

cat("Total number of peaks:", length(ctcf_peaks), "\n")

Total number of peaks: 43865

cat("Number of chromosomes represented:", length(unique(seqnames(ctcf_peaks))), "\n")
```

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Number of chromosomes represented: 26

```
cat("Peak width range:", min(width(ctcf_peaks)), "-", max(width(ctcf_peaks)), "bp\n")
```

Peak width range: 54 - 442 bp

```
cat("Median peak width:", median(width(ctcf_peaks)), "bp\n")
```

Median peak width: 216 bp

```
cat("Mean peak width:", round(mean(width(ctcf_peaks)), 1), "bp\n")
```

Mean peak width: 181.1 bp

```
# Show chromosome names  
cat("\nChromosomes present:\n")
```

Chromosomes present:

```
print(sort(unique(as.character(seqnames(ctcf_peaks)))))
```

```
[1] "chr1"                  "chr1_KI270714v1_random"  
[3] "chr10"                 "chr11"  
[5] "chr12"                 "chr13"  
[7] "chr14"                 "chr15"  
[9] "chr16"                 "chr17"  
[11] "chr17_GL000205v2_random" "chr18"  
[13] "chr19"                 "chr2"  
[15] "chr20"                 "chr21"  
[17] "chr22"                 "chr3"  
[19] "chr4"                  "chr5"  
[21] "chr6"                  "chr7"  
[23] "chr8"                  "chr9"  
[25] "chrUn_GL000219v1"      "chrX"
```

24.7.2. Peaks Per Chromosome

```
# Count peaks per chromosome
peaks_per_chr <- table(seqnames(ctcf_peaks))
peaks_per_chr_df <- as.data.frame(peaks_per_chr)
peaks_per_chr_df
```

	Var1	Freq
1	chr2	3332
2	chr20	1236
3	chr15	1431
4	chr8	1935
5	chr9	1820
6	chr7	2140
7	chr4	2030
8	chr12	2274
9	chr5	2355
10	chr22	873
11	chr1	4207
12	chr17	2010
13	chr3	2808
14	chr11	2417
15	chr19	1662
16	chr6	2504
17	chr13	1030
18	chrX	1460
19	chr10	2037
20	chr16	1497
21	chr14	1461
22	chr21	406
23	chr18	932
24	chr17_GL000205v2_random	4
25	chr1_KI270714v1_random	1
26	chrUn_GL000219v1	3

24.8. Accessing Peak Coordinates

24.8.1. Finding Starts and Ends

```
# Extract start and end coordinates
peak_starts <- start(ctcf_peaks)
peak_ends <- end(ctcf_peaks)
peak_centers <- start(ctcf_peaks) + (width(ctcf_peaks)/2)

head(peak_starts, 10)
```

```
[1] 238305324 49982707 39921016 6708274 136645957 47669295 136784479
[8] 139453373 122421409 102583856
```

```
head(peak_ends, 10)
```

```
[1] 238305539 49982922 39921231 6708489 136646172 47669510 136784694
[8] 139453588 122421624 102584071
```

```
head(peak_centers, 10)
```

```
[1] 238305432 49982815 39921124 6708382 136646065 47669403 136784587
[8] 139453481 122421517 102583964
```

24.9. Manipulating Peak Ranges

24.9.1. Shifting Peaks

Shifting peaks is useful for various analyses, such as creating flanking regions or adjusting peak positions.

```
# Shift peaks by different amounts
peaks_shifted_100bp <- shift(ctcf_peaks, 100) # Shift right by 100bp
peaks_shifted_neg50bp <- shift(ctcf_peaks, -50) # Shift left by 50bp

cat("==== Peak Shifting Examples ===\\n")
```

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==== Peak Shifting Examples ====

```
cat("Original peak 1:", as.character(ctcf_peaks[1]), "\n")
```

Original peak 1: chr2:238305324-238305539

```
cat("Shifted +100bp:", as.character(peaks_shifted_100bp[1]), "\n")
```

Shifted +100bp: chr2:238305424-238305639

```
cat("Shifted -50bp:", as.character(peaks_shifted_neg50bp[1]), "\n")
```

Shifted -50bp: chr2:238305274-238305489

```
# Demonstrate that width is preserved during shifting
cat("\nWidths after shifting (should be unchanged):\n")
```

Widths after shifting (should be unchanged):

```
cat("Original width:", width(ctcf_peaks[1]), "\n")
```

Original width: 216

```
cat("Shifted +100bp width:", width(peaks_shifted_100bp[1]), "\n")
```

Shifted +100bp width: 216

```
cat("Shifted -50bp width:", width(peaks_shifted_neg50bp[1]), "\n")
```

Shifted -50bp width: 216

24.9.2. Setting Peak Widths

Resizing peaks is common when standardizing peak sizes or creating fixed-width windows around peak centers.

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```
# Resize peaks to fixed width (200bp) centered on original peak center
peaks_200bp <- resize(ctcf_peaks, width = 200, fix = "center")

# Resize peaks to 500bp, keeping the start position fixed
peaks_500bp_start <- resize(ctcf_peaks, width = 500, fix = "start")

# Resize peaks to 300bp, keeping the end position fixed
peaks_300bp_end <- resize(ctcf_peaks, width = 300, fix = "end")

cat("== Peak Resizing Examples ==\n")
```

== Peak Resizing Examples ==

```
cat("Original peak 1:", as.character(ctcf_peaks[1]), "\n")
```

Original peak 1: chr2:238305324-238305539

```
cat("Resized to 200bp (center):", as.character(peaks_200bp[1]), "\n")
```

Resized to 200bp (center): chr2:238305332-238305531

```
cat("Resized to 500bp (start fixed):", as.character(peaks_500bp_start[1]), "\n")
```

Resized to 500bp (start fixed): chr2:238305324-238305823

```
cat("Resized to 300bp (end fixed):", as.character(peaks_300bp_end[1]), "\n")
```

Resized to 300bp (end fixed): chr2:238305240-238305539

```
# Verify that all peaks now have the specified width
cat("\nWidth verification:\n")
```

Width verification:

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```
cat("200bp resize - all widths 200?", all(width(peaks_200bp) == 200), "\n")  
  
200bp resize - all widths 200? TRUE  
  
cat("500bp resize - all widths 500?", all(width(peaks_500bp_start) == 500), "\n")  
  
500bp resize - all widths 500? TRUE  
  
cat("300bp resize - all widths 300?", all(width(peaks_300bp_end) == 300), "\n")  
  
300bp resize - all widths 300? TRUE
```

24.9.3. Creating Flanking Regions

```
# Create flanking regions around peaks  
upstream_1kb <- flank(ctcf_peaks, width = 1000, start = TRUE)  
downstream_1kb <- flank(ctcf_peaks, width = 1000, start = FALSE)  
  
# Create regions extending in both directions  
extended_peaks <- resize(ctcf_peaks, width = width(ctcf_peaks) + 2000, fix = "center")  
  
cat("==== Flanking Region Examples ===\n")  
  
==== Flanking Region Examples ===  
  
cat("Original peak 1:", as.character(ctcf_peaks[1]), "\n")
```

Original peak 1: chr2:238305324-238305539

```
cat("1kb upstream:", as.character(upstream_1kb[1]), "\n")
```

1kb upstream: chr2:238304324-238305323

```
cat("1kb downstream:", as.character(downstream_1kb[1]), "\n")
```

1kb downstream: chr2:238305540-238306539

```
cat("Extended ±1kb:", as.character(extended_peaks[1]), "\n")
```

Extended ±1kb: chr2:238304324-238306539

24.10. Coverage

Coverage refers to the number of times a genomic region is covered by ranges on a chromosome. A common use case is calculating coverage from ChIP-seq data, where we want to know how many reads overlap with each peak or for doing “peak calling” analysis.

We can make a toy example by simulating random reads of length 50 bp across a chromosome and then calculating coverage.

```
# Simulate random reads on chromosome 1
set.seed(42) # For reproducibility
chrom_length <- 1000000 # Length of chromosome 1
num_reads <- 100000
read_length <- 50 # Length of each read
random_starts <- sample(seq_len(chrom_length - read_length + 1), num_reads, replace = TRUE)
random_reads <- GRanges(seqnames = "chr1",
                        ranges = IRanges(start = random_starts, end = random_starts + read_length))
random_reads
```

GRanges object with 100000 ranges and 0 metadata columns:

	seqnames	ranges	strand
	<Rle>	<IRanges>	<Rle>
[1]	chr1	61413-61462	*
[2]	chr1	54425-54474	*
[3]	chr1	623844-623893	*
[4]	chr1	74362-74411	*
[5]	chr1	46208-46257	*
...
[99996]	chr1	663489-663538	*

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```
[99997] chr1 886082-886131      *
[99998] chr1 933222-933271      *
[99999] chr1 486340-486389      *
[100000] chr1 177556-177605      *
-----
seqinfo: 1 sequence from an unspecified genome; no seqlengths
```

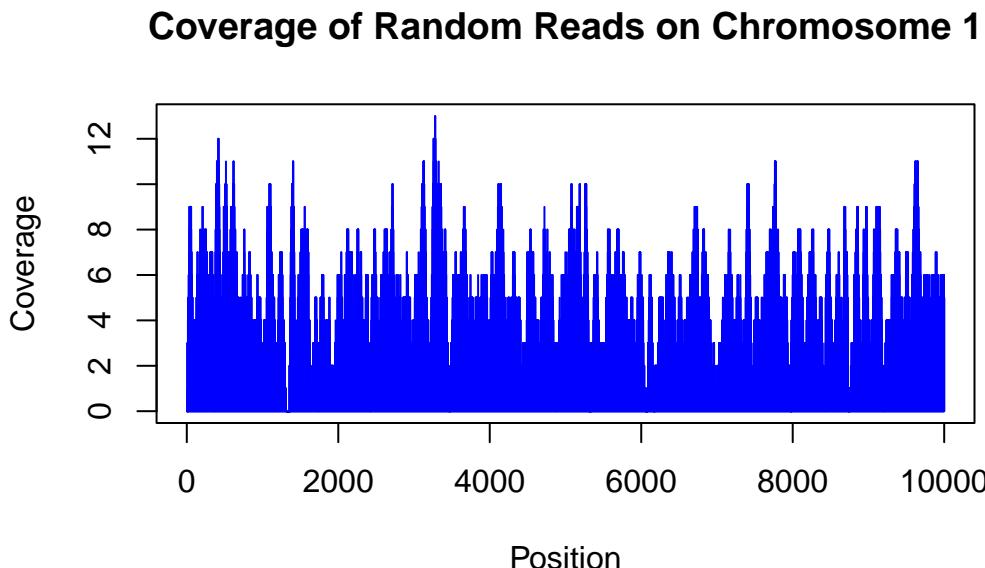
We are now ready to calculate the coverage of these random reads across the chromosome. The `coverage()` function from the `GenomicRanges` package computes the coverage of ranges in a `GRanges` object.

```
random_coverage <- coverage(random_reads, width = chrom_length)
head(random_coverage)
```

```
RleList of length 1
$chr1
integer-Rle of length 1000000 with 173047 runs
  Lengths: 7 1 6 3 8 8 1 1 22 1 4 ... 3 1 2 8 12 23 5 2 8 6
  Values : 0 1 3 4 5 6 7 8 9 8 6 ... 3 2 3 4 5 4 3 2 1 0
```

We can visualize the coverage of the random reads on chromosome 1. The `coverage()` function returns a `Rle` object, which is a run-length encoding of the coverage values.

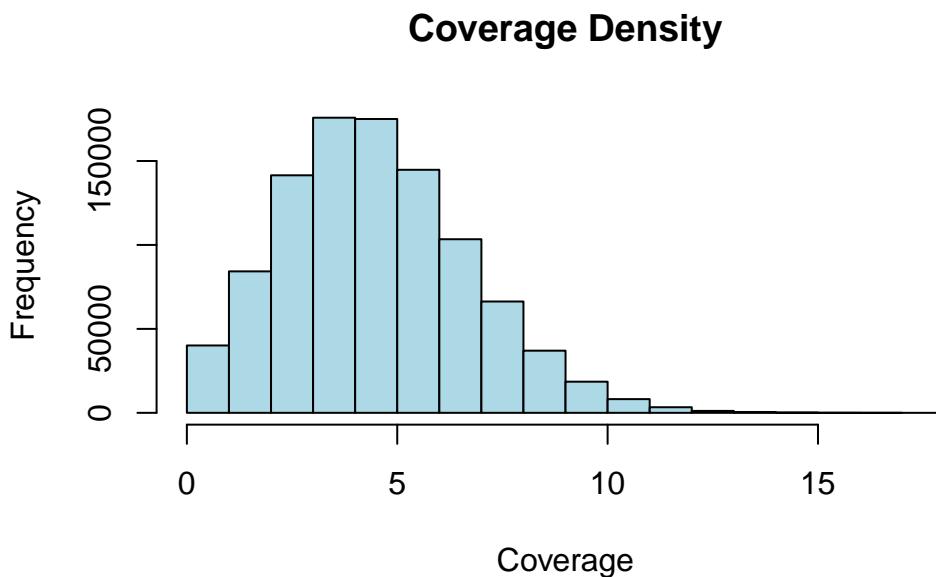
```
plot(random_coverage[[1]][1:10000], main="Coverage of Random Reads on Chromosome 1", xlab="")
```



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This plot shows the coverage of random reads across the first 10,000 bases of chromosome 1. The y-axis represents the number of reads covering each position, while the x-axis represents the genomic positions.

```
# Calculate coverage density
hist(as.numeric(random_coverage[[1]]), main="Coverage Density", xlab="Coverage", ylab="Frequency")
```



24.11. Key Takeaways

This tutorial demonstrated several important concepts:

1. **BED file format:** Understanding the structure and coordinate system of BED files
2. **Loading genomic data:** Using rtracklayer to import BED files into R
3. **Basic exploration:** Counting features, examining distributions, and summarizing data
4. **Coordinate manipulation:** Accessing starts, ends, and performing coordinate arithmetic
5. **Range operations:** Shifting, resizing, and creating flanking regions
6. **Advanced analysis:** Finding overlaps and performing grouped operations

24.11.1. Common Use Cases

- **Peak calling analysis:** Examining ChIP-seq peaks, ATAC-seq peaks, etc.
- **Annotation overlap:** Finding genes or regulatory elements near peaks
- **Comparative analysis:** Comparing peak sets between conditions or samples
- **Motif analysis:** Creating sequences around peak centers for motif discovery
- **Visualization:** Preparing data for genome browser tracks or custom plots

24.11.2. Best Practices

1. Always check coordinate systems (0-based vs 1-based)
2. Verify chromosome naming conventions match your reference genome
3. Consider peak width distributions when setting analysis parameters
4. Use appropriate genome builds for all analyses
5. Document coordinate transformations and filtering steps

This foundation in genomic ranges and BED file manipulation will serve as a basis for more advanced genomic analyses in R.

25. Genomic ranges and features

25.1. Introduction

Genomic ranges are essential components in the field of genomics, representing intervals on the genome that specify the start and end positions of DNA segments. These ranges can denote various genomic features, such as genes, exons, regulatory elements, and regions identified in genomic studies like ChIP-seq peaks. They play a pivotal role in the annotation, comparison, and interpretation of genomic features and experimental data, making them indispensable in biological data analysis.

Understanding genomic ranges begins with the concept of coordinate systems. Different databases and tools adopt different conventions for indexing genomic coordinates. For instance, the UCSC Genome Browser uses a 0-based coordinate system, while Ensembl employs a 1-based system. Moreover, genomic ranges often include strand information, indicating whether the feature is on the positive or negative DNA strand, which is crucial for correctly interpreting gene expression and other genomic functions.

Genomic ranges come in various forms, from single ranges defined by a simple start and end position (such as a single exon) to complex multi-range sets encompassing collections of ranges like all exons of a gene. Manipulating these ranges involves several fundamental operations. Intersection allows researchers to find overlapping regions between two sets of ranges, such as identifying ChIP-seq peaks that overlap with promoter regions. Union operations combine multiple ranges into a single contiguous range, while set difference identifies regions in one set that do not overlap with another set.

Several tools and libraries have been developed to facilitate the manipulation of genomic ranges. In the R programming environment, the Bioconductor project provides the GenomicRanges package, which is specifically designed for representing and manipulating genomic ranges. This package offers a variety of functions for range arithmetic and efficient overlap queries. Another useful R package is rtracklayer, which enables the import and export of genomic data in various formats, including BED and GFF files.

For those who prefer a command-line interface, BEDTools offers a suite of utilities for performing a wide range of operations on genomic intervals. This toolset is highly versatile, supporting tasks like intersecting, merging, and complementing genomic intervals. In the

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Python ecosystem, PyRanges provides a fast and flexible library for manipulating genomic intervals, offering similar functionality to Bioconductor's GenomicRanges.

The applications of genomic ranges are diverse and far-reaching. In gene annotation, for instance, RNA-seq reads are mapped to known gene models to quantify gene expression levels. Variant annotation involves mapping variants identified from sequencing data to their genomic context, predicting functional consequences based on their location within genes or intergenic regions. Comparative genomics leverages genomic ranges to compare intervals between species, identifying conserved regions that might indicate essential functional elements. Epigenomic studies utilize genomic ranges to intersect DNA methylation data or histone modification peaks with genomic features, providing insights into regulatory mechanisms.

Despite their utility, working with genomic ranges presents several challenges. Converting coordinates between different reference genomes or different versions of the same genome can be complex and prone to errors. Integrating diverse types of genomic data, such as DNA sequences, epigenetic marks, and RNA-seq data, requires meticulous handling of genomic coordinates and ranges to ensure accurate analyses. Moreover, the sheer scale of genomic data necessitates optimized algorithms and data structures to handle large datasets efficiently.

Interpreting genomic ranges within their biological context is crucial for drawing meaningful conclusions. For instance, a range within a gene's promoter region might indicate potential regulatory activity. Understanding the functional implications of genomic ranges often involves overlapping these ranges with known functional elements, such as enhancers or silencers, to infer gene regulation mechanisms and their phenotypic consequences. Tools like the UCSC Genome Browser and the Integrative Genomics Viewer (IGV) are invaluable for visualizing genomic ranges alongside other genomic annotations, aiding in the interpretation and exploration of genomic data.

25.2. Bioconductor and GenomicRanges

```
library(GenomicRanges)
```

The Bioconductor [GenomicRanges](#) package is a comprehensive toolkit designed to handle and manipulate genomic intervals and variables systematized on these intervals (Lawrence et al. 2013a). Developed by Bioconductor, this package simplifies the complexity of managing genomic data, facilitating the efficient exploration, manipulation, and visualization of such data. GenomicRanges aids in dealing with the challenges of genomic data, including its massive size, intricate relationships, and high dimensionality.

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The GenomicRanges package in Bioconductor covers a wide range of use cases related to the management and analysis of genomic data. Here are some key examples:

- **Genomic Feature Manipulation** The GenomicRanges and GRanges classes can be used to represent and manipulate various genomic features such as genes, transcripts, exons, or single-nucleotide polymorphisms (SNPs). Users can query, subset, resize, shift, or sort these features based on their genomic coordinates.
- **Genomic Interval Operations** The GenomicRanges package provides functions for performing operations on genomic intervals, such as finding overlaps, nearest neighbors, or disjoint intervals. These operations are fundamental to many types of genomic data analyses, such as identifying genes that overlap with ChIP-seq peaks, or finding variants that are in close proximity to each other.
- **Alignments and Coverage** The GAlignments and GAlignmentPairs classes can be used to represent alignments of sequencing reads to a reference genome, such as those produced by a read aligner. Users can then compute coverage of these alignments over genomic ranges of interest, which is a common task in RNA-seq or ChIP-seq analysis.
- **Annotation and Metadata Handling** The metadata column of a GRanges object can be used to store various types of annotation data associated with genomic ranges, such as gene names, gene biotypes, or experimental scores. This makes it easy to perform analyses that integrate genomic coordinates with other types of biological information.
- **Genome Arithmetic** The GenomicRanges package supports a version of “genome arithmetic”, which includes set operations (union, intersection, set difference) as well as other operations (like coverage, complement, or reduction) that are adapted to the specificities of genomic data.
- **Efficient Data Handling** The CompressedGRangesList class provides a space-efficient way to represent a large list of GRanges objects, which is particularly useful when working with large genomic datasets, such as whole-genome sequencing data.

The GenomicRanges package in Bioconductor uses the S4 class system (see Table 25.1), which is a part of the methods package in R. The S4 system is a more rigorous and formal approach to object-oriented programming in R, providing enhanced capabilities for object design and function dispatch.

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Table 25.1.: Classes within the GenomicRanges package. Each class has a slightly different use case.

Class Name	Description	Potential Use
GRanges	Represents a collection of genomic ranges and associated variables.	ChipSeq peaks, CpG islands, etc.
GRangesList	Represents a list of GenomicRanges objects.	transcript models (exons, introns)
RangesList	Represents a list of Ranges objects.	
IRanges	Represents a collection of integer ranges.	used mainly to <i>build</i> GRanges, etc.
GPos	Represents genomic positions.	SNPs or other single nucleotide locations
GAlignments	Represents alignments against a reference genome.	Sequence read locations from a BAM file
GAlignmentPairs	Represents pairs of alignments, typically representing a single fragment of DNA.	Paired-end sequence alignments

In the context of the GenomicRanges package, the S4 class system allows for the creation of complex, structured data objects that can effectively encapsulate genomic intervals and associated data. This system enables the package to handle the complexity and intricacy of genomic data.

For example, the GenomicRanges class in the package is an S4 class that combines several basic data types into a composite object. It includes slots for sequence names (seqnames), ranges (start and end positions), strand information, and metadata. Each slot in the S4 class corresponds to a specific component of the genomic data, and methods (see Table 25.2 and Table 25.3) can be defined to interact with these slots in a structured and predictable way.

Table 25.2.: Methods for accessing, manipulating single objects

Method	Description
length	Returns the number of ranges in the GRanges object.
seqnames	Retrieves the sequence names of the ranges.
ranges	Retrieves the start and end positions of the ranges.
strand	Retrieves the strand information of the ranges.

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Method	Description
elementMetadata	Retrieves the metadata associated with the ranges.
seqlevels	Returns the levels of the factor that the seqnames slot is derived from.
seqinfo	Retrieves the Seqinfo (sequence information) object associated with the GRanges object.
start, end, width	Retrieve or set the start or end positions, or the width of the ranges.
resize	Resizes the ranges.
subset, [, [[, \$	Subset or extract elements from the GRanges object.
sort	Sorts the GRanges object.
shift	Shifts the ranges by a certain number of base pairs.

The S4 class system also supports inheritance, which allows for the creation of specialized subclasses that share certain characteristics with a parent class but have additional features or behaviors.

The S4 system's formalism and rigor make it well-suited to the complexities of bioinformatics and genomic data analysis. It allows for the creation of robust, reliable code that can handle complex data structures and operations, making it a key part of the GenomicRanges package and other Bioconductor packages.

Table 25.3.: Methods for comparing and combining multiple GenomicRanges-class objects

Method	Description
findOverlaps	Finds overlaps between different sets of ranges.
countOverlaps	Counts overlaps between different sets of ranges.
subsetByOverlaps	Subsets the ranges based on overlaps.
distanceToNearest	Computes the distance to the nearest range in another set of ranges.

To get going, we can construct a GRanges object by hand as an example.

The GRanges class represents a collection of genomic ranges that each have a single start and end location on the genome. It can be used to store the location of genomic features such as contiguous binding sites, transcripts, and exons. These objects can be created by using the GRanges constructor function. The following code just creates a GRanges object from scratch.

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```
gr <- GRanges(
  seqnames = Rle(c("chr1", "chr2", "chr1", "chr3"), c(1, 3, 2, 4)),
  ranges = IRanges(101:110, end = 111:120, names = head(letters, 10)),
  strand = Rle(strand(c("-", "+", "*", "+", "-")), c(1, 2, 2, 3, 2)),
  score = 1:10,
  GC = seq(1, 0, length=10))
gr
```

GRanges object with 10 ranges and 2 metadata columns:

	seqnames	ranges	strand		score	GC
	<Rle>	<IRanges>	<Rle>		<integer>	<numeric>
a	chr1	101-111	-		1	1.000000
b	chr2	102-112	+		2	0.888889
c	chr2	103-113	+		3	0.777778
d	chr2	104-114	*		4	0.666667
e	chr1	105-115	*		5	0.555556
f	chr1	106-116	+		6	0.444444
g	chr3	107-117	+		7	0.333333
h	chr3	108-118	+		8	0.222222
i	chr3	109-119	-		9	0.111111
j	chr3	110-120	-		10	0.000000

seqinfo: 3 sequences from an unspecified genome; no seqlengths						

This creates a `GRanges` object with 10 genomic ranges. The output of the `GRanges show()` method separates the information into a left and right hand region that are separated by `|` symbols (see Figure 25.1). The genomic coordinates (seqnames, ranges, and strand) are located on the left-hand side and the metadata columns are located on the right. For this example, the metadata is comprised of score and GC information, but almost anything can be stored in the metadata portion of a `GRanges` object.

The components of the genomic coordinates within a `GRanges` object can be extracted using the `seqnames`, `ranges`, and `strand` accessor functions.

```
seqnames(gr)
```

```
factor-Rle of length 10 with 4 runs
Lengths: 1 3 2 4
Values : chr1 chr2 chr1 chr3
Levels(3): chr1 chr2 chr3
```

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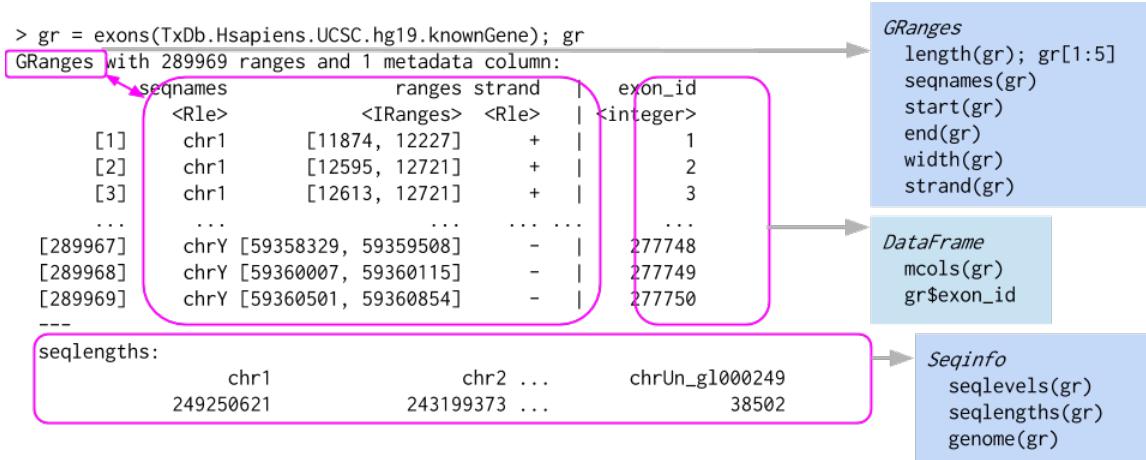


Figure 25.1.: The structure of a `GRanges` object, which behaves a bit like a vector of ranges, although the analogy is not perfect. A `GRanges` object is composed of the “Ranges” part (the lefthand box), the “metadata” columns (the righthand box), and a “seqinfo” part that describes the names and lengths of associated sequences. Only the “Ranges” part is required. The figure also shows a few of the “accessors” and approaches to subsetting a `GRanges` object.

`ranges(gr)`

IRanges object with 10 ranges and 0 metadata columns:

	start	end	width
	<integer>	<integer>	<integer>
a	101	111	11
b	102	112	11
c	103	113	11
d	104	114	11
e	105	115	11
f	106	116	11
g	107	117	11
h	108	118	11
i	109	119	11
j	110	120	11

`strand(gr)`

factor-Rle of length 10 with 5 runs

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```
Lengths: 1 2 2 3 2
Values : - + * + -
Levels(3): + - *
```

Note that the `GRanges` object has information to the “left” side of the `|` that has special accessors. The information to the right side of the `|`, when it is present, is the metadata and is accessed using `mcols()`, for “metadata columns”.

```
class(mcols(gr))
```

```
[1] "DFrame"
attr(",package")
[1] "S4Vectors"
```

```
mcols(gr)
```

```
DataFrame with 10 rows and 2 columns
  score      GC
  <integer> <numeric>
a      1 1.000000
b      2 0.888889
c      3 0.777778
d      4 0.666667
e      5 0.555556
f      6 0.444444
g      7 0.333333
h      8 0.222222
i      9 0.111111
j     10 0.000000
```

Since the `class` of `mcols(gr)` is `DFrame`, we can use our `DataFrame` approaches to work with the data.

```
mcols(gr)$score
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

We can even assign a new column.

25. Genomic ranges and features

```
  mcols(gr)$AT = 1-mcols(gr)$GC
  gr
```

GRanges object with 10 ranges and 3 metadata columns:

	seqnames	ranges	strand	score	GC	AT
	<Rle>	<IRanges>	<Rle>	<integer>	<numeric>	<numeric>
a	chr1	101-111	-	1	1.000000	0.000000
b	chr2	102-112	+	2	0.888889	0.111111
c	chr2	103-113	+	3	0.777778	0.222222
d	chr2	104-114	*	4	0.666667	0.333333
e	chr1	105-115	*	5	0.555556	0.444444
f	chr1	106-116	+	6	0.444444	0.555556
g	chr3	107-117	+	7	0.333333	0.666667
h	chr3	108-118	+	8	0.222222	0.777778
i	chr3	109-119	-	9	0.111111	0.888889
j	chr3	110-120	-	10	0.000000	1.000000

seqinfo: 3 sequences from an unspecified genome; no seqlengths

Another common way to create a GRanges object is to start with a `data.frame`, perhaps created by hand like below or read in using `read.csv` or `read.table`. We can convert from a `data.frame`, when columns are named appropriately, to a GRanges object.

```
df_regions = data.frame(chromosome = rep("chr1",10),
                        start=seq(1000,10000,1000),
                        end=seq(1100, 10100, 1000))
as(df_regions,'GRanges') # note that names have to match with GRanges slots
```

GRanges object with 10 ranges and 0 metadata columns:

	seqnames	ranges	strand
	<Rle>	<IRanges>	<Rle>
[1]	chr1	1000-1100	*
[2]	chr1	2000-2100	*
[3]	chr1	3000-3100	*
[4]	chr1	4000-4100	*
[5]	chr1	5000-5100	*
[6]	chr1	6000-6100	*
[7]	chr1	7000-7100	*
[8]	chr1	8000-8100	*

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```
[9] chr1 9000-9100 *
[10] chr1 10000-10100 *
-----
seqinfo: 1 sequence from an unspecified genome; no seqlengths
```

```
## fix column name
colnames(df_regions)[1] = 'seqnames'
gr2 = as(df_regions, 'GRanges')
gr2
```

GRanges object with 10 ranges and 0 metadata columns:

	seqnames	ranges	strand
	<Rle>	<IRanges>	<Rle>
[1]	chr1	1000-1100	*
[2]	chr1	2000-2100	*
[3]	chr1	3000-3100	*
[4]	chr1	4000-4100	*
[5]	chr1	5000-5100	*
[6]	chr1	6000-6100	*
[7]	chr1	7000-7100	*
[8]	chr1	8000-8100	*
[9]	chr1	9000-9100	*
[10]	chr1	10000-10100	*

```
-----
seqinfo: 1 sequence from an unspecified genome; no seqlengths
```

GRanges have one-dimensional-like behavior. For instance, we can check the `length` and even give GRanges names.

```
names(gr)
```

```
[1] "a" "b" "c" "d" "e" "f" "g" "h" "i" "j"
```

```
length(gr)
```

```
[1] 10
```

25.2.1. Subsetting GRanges objects

While `GRanges` objects look a bit like a `data.frame`, they can be thought of as vectors with associated ranges. Subsetting, then, works very similarly to vectors. To subset a `GRanges` object to include only second and third regions:

```
gr[2:3]
```

```
GRanges object with 2 ranges and 3 metadata columns:
  seqnames      ranges strand |      score        GC        AT
  <Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
  b      chr2    102-112     + |       2  0.888889  0.111111
  c      chr2    103-113     + |       3  0.777778  0.222222
  -----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

That said, if the `GRanges` object has metadata columns, we can also treat it like a two-dimensional object kind of like a `data.frame`. Note that the information to the left of the `|` is not like a `data.frame`, so we *cannot* do something like `gr$seqnames`. Here is an example of subsetting with the subset of one metadata column.

```
gr[2:3, "GC"]
```

```
GRanges object with 2 ranges and 1 metadata column:
  seqnames      ranges strand |      GC
  <Rle> <IRanges> <Rle> | <numeric>
  b      chr2    102-112     + |  0.888889
  c      chr2    103-113     + |  0.777778
  -----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

The usual `head()` and `tail()` also work just fine.

```
head(gr, n=2)
```

```
GRanges object with 2 ranges and 3 metadata columns:
  seqnames      ranges strand |      score        GC        AT
  <Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
```

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```
a      chr1  101-111      - |          1  1.000000  0.000000
b      chr2  102-112      + |          2  0.888889  0.111111
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

```
tail(gr,n=2)
```

GRanges object with 2 ranges and 3 metadata columns:

```
  seqnames     ranges strand |   score       GC       AT
    <Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
i      chr3  109-119      - |       9  0.111111  0.888889
j      chr3  110-120      - |      10  0.000000  1.000000
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

25.2.2. Interval operations on one GRanges object

25.2.2.1. Intra-range methods

The methods described in this section work *one-region-at-a-time* and are, therefore, called “intra-region” methods. Methods that work across all regions are described below in the [Inter-range methods](#) section.

The `GRanges` class has accessors for the “ranges” part of the data. For example:

```
## Make a smaller GRanges subset
g <- gr[1:3]
start(g) # to get start locations
```

```
[1] 101 102 103
```

```
end(g) # to get end locations
```

```
[1] 111 112 113
```

```
width(g) # to get the "widths" of each range
```

```
[1] 11 11 11
```

25. Genomic ranges and features

```
range(g) # to get the "range" for each sequence (min(start) through max(end))

GRanges object with 2 ranges and 0 metadata columns:
  seqnames      ranges strand
  <Rle> <IRanges> <Rle>
[1]   chr1    101-111     -
[2]   chr2    102-113     +
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

The GRanges class also has many methods for manipulating the ranges. The methods can be classified as intra-range methods, inter-range methods, and between-range methods. Intra-range methods operate on each element of a GRanges object independent of the other ranges in the object. For example, the flank method can be used to recover regions flanking the set of ranges represented by the GRanges object. So to get a GRanges object containing the ranges that include the 10 bases *upstream* of the ranges:

```
flank(g, 10)
```

```
GRanges object with 3 ranges and 3 metadata columns:
  seqnames      ranges strand |   score      GC      AT
  <Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
  a     chr1    112-121     - |       1  1.000000  0.000000
  b     chr2    92-101      + |       2  0.888889  0.111111
  c     chr2    93-102      + |       3  0.777778  0.222222
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

Note how `flank` pays attention to “strand”. To get the flanking regions *downstream* of the ranges, we can do:

```
flank(g, 10, start=FALSE)
```

```
GRanges object with 3 ranges and 3 metadata columns:
  seqnames      ranges strand |   score      GC      AT
  <Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
  a     chr1    91-100     - |       1  1.000000  0.000000
  b     chr2    113-122     + |       2  0.888889  0.111111
```

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```
c      chr2  114-123      + |      3  0.777778  0.222222
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

Other examples of intra-range methods include `resize` and `shift`. The `shift` method will move the ranges by a specific number of base pairs, and the `resize` method will extend the ranges by a specified width.

```
shift(g, 5)
```

GRanges object with 3 ranges and 3 metadata columns:

```
seqnames      ranges strand |      score        GC        AT
<Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
a      chr1    106-116     - |      1  1.000000  0.000000
b      chr2    107-117     + |      2  0.888889  0.111111
c      chr2    108-118     + |      3  0.777778  0.222222
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

```
resize(g, 30)
```

GRanges object with 3 ranges and 3 metadata columns:

```
seqnames      ranges strand |      score        GC        AT
<Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
a      chr1    82-111      - |      1  1.000000  0.000000
b      chr2    102-131     + |      2  0.888889  0.111111
c      chr2    103-132     + |      3  0.777778  0.222222
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

The [GenomicRanges](#) help page `?"intra-range-methods"` summarizes these methods.

25.2.2.2. Inter-range methods

Inter-range methods involve comparisons between ranges in a single GRanges object. For instance, the `reduce` method will align the ranges and merge overlapping ranges to produce a simplified set.

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```
reduce(g)
```

```
GRanges object with 2 ranges and 0 metadata columns:
  seqnames      ranges strand
  <Rle> <IRanges> <Rle>
[1]   chr1    101-111     -
[2]   chr2    102-113     +
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

The reduce method could, for example, be used to collapse individual overlapping coding exons into a single set of coding regions.

Sometimes one is interested in the gaps or the qualities of the gaps between the ranges represented by your GRanges object. The gaps method provides this information:

```
gaps(g)
```

```
GRanges object with 2 ranges and 0 metadata columns:
  seqnames      ranges strand
  <Rle> <IRanges> <Rle>
[1]   chr1      1-100     -
[2]   chr2      1-101     +
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

In this case, we have not specified the lengths of the chromosomes, so Bioconductor is making the assumption (incorrectly) that the chromosomes end at the largest location on each chromosome. We can correct this by setting the `seqlengths` correctly, but we can ignore that detail for now.

The disjoin method represents a GRanges object as a collection of non-overlapping ranges:

```
disjoin(g)
```

```
GRanges object with 4 ranges and 0 metadata columns:
  seqnames      ranges strand
  <Rle> <IRanges> <Rle>
[1]   chr1    101-111     -
```

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```
[2] chr2      102      +
[3] chr2    103-112      +
[4] chr2      113      +
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

The `coverage` method quantifies the degree of overlap for all the ranges in a GRanges object.

```
coverage(g)
```

```
RleList of length 3
$chr1
integer-Rle of length 111 with 2 runs
  Lengths: 100 11
  Values : 0   1

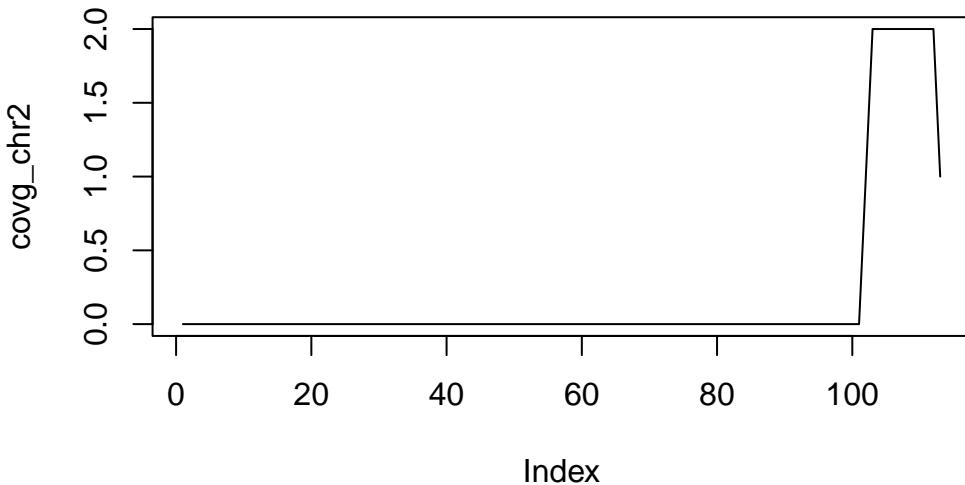
$chr2
integer-Rle of length 113 with 4 runs
  Lengths: 101   1   10   1
  Values : 0     1     2     1

$chr3
integer-Rle of length 0 with 0 runs
  Lengths:
  Values :
```

The coverage is summarized as a list of coverages, one for each chromosome. The `Rle` class is used to store the values. Sometimes, one must convert these values to `numeric` using `as.numeric`. In many cases, this will happen automatically, though.

```
covg = coverage(g)
covg_chr2 = covg[['chr2']]
plot(covg_chr2, type='l')
```

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See the [GenomicRanges](#) help page `?"intra-range-methods"` for more details.

25.2.3. Set operations for GRanges objects

Between-range methods calculate relationships between different GRanges objects. Of central importance are `findOverlaps` and related operations; these are discussed below. Additional operations treat GRanges as mathematical sets of coordinates; `union(g, g2)` is the union of the coordinates in `g` and `g2`. Here are examples for calculating the union, the intersect and the asymmetric difference (using `setdiff`).

```
g2 <- head(gr, n=2)
GenomicRanges::union(g, g2)
```

```
GRanges object with 2 ranges and 0 metadata columns:
  seqnames      ranges strand
  <Rle> <IRanges>  <Rle>
[1]   chr1    101-111    -
[2]   chr2    102-113    +
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

```
GenomicRanges::intersect(g, g2)
```

```
GRanges object with 2 ranges and 0 metadata columns:
  seqnames      ranges strand
  <Rle> <IRanges>  <Rle>
```

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```
<Rle> <IRanges> <Rle>
[1] chr1 101-111 -
[2] chr2 102-112 +
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths

GenomicRanges::setdiff(g, g2)
```

```
GRanges object with 1 range and 0 metadata columns:
  seqnames      ranges strand
  <Rle> <IRanges> <Rle>
[1] chr2        113      +
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

There is extensive additional help available or by looking at the vignettes in at the [GenomicRanges](#) pages.

```
?GRanges
```

There are also many possible `methods` that work with `GRanges` objects. To see a complete list (long), try:

```
methods(class="GRanges")
```

25.3. GRangesList

Some important genomic features, such as spliced transcripts that are comprised of exons, are inherently compound structures. Such a feature makes much more sense when expressed as a compound object such as a `GRangesList`. If we think of each transcript as a set of exons, each transcript would be summarized as a `GRanges` object. However, if we have multiple transcripts, we want to somehow keep them separate, with each transcript having its own exons. The `GRangesList` is then a list of `GRanges` objects that. Continuing with the transcripts thought, a `GRangesList` can contain all the transcripts and their exons; each transcript is an element in the list.

Whenever genomic features consist of multiple ranges that are grouped by a parent feature, they can be represented as a `GRangesList` object. Consider the simple example of the two transcript `GRangesList` below created using the `GRangesList` constructor.

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```
> grl = exonsBy(TxDb.Hsapiens.UCSC.hg19.knownGene, "tx", use.names=TRUE); grl
GRangesList of length 82960:
$uc001aaa.3
GRanges with 3 ranges and 3 metadata columns:
  seqnames      ranges strand | exon_id exon_name exon_rank
  <Rle>      <IRanges> <Rle> | <integer> <character> <integer>
[1] chr1 [11874, 12227]    + |     1    <NA>      1
[2] chr1 [12613, 12721]    + |     3    <NA>      2
[3] chr1 [13221, 14409]    + |     5    <NA>      3
```

GRangesList
(list of GRanges)
length(grl)
grl[1:3]
shift(grl, 1)
range(grl)


```
$uc010nxq.1
GRanges with 3 ranges and 3 metadata columns:
  seqnames      ranges strand | exon_id exon_name exon_rank
  <Rle>      <IRanges> <Rle> | <integer> <character> <integer>
[1] chr1 [11874, 12227]    + |     1    <NA>      1
[2] chr1 [12595, 12721]    + |     2    <NA>      2
[3] chr1 [13403, 14409]    + |     6    <NA>      3
```

GRanges
grl[[2]]
grl[["uc010nxq.1"]]


```
$uc010nrxr.1
GRanges with 3 ranges and 3 metadata columns:
  seqnames      ranges strand | exon_id exon_name exon_rank
  <Rle>      <IRanges> <Rle> | <integer> <character> <integer>
[1] chr1 [11874, 12227]    + |     1    <NA>      1
[2] chr1 [12646, 12697]    + |     4    <NA>      2
[3] chr1 [13221, 14409]    + |     5    <NA>      3
...
<82957 more elements>
---
seqinfo: 93 sequences (1 circular) from hg19 genome
```

Two kinds of fun!
introns =
psetdiff(range(grl), grl)

grr = unlist(grl)
transform grr, then...
grl = relist(grr, grl)

'flesh' 'skeleton'

Figure 25.2.: The structure of a GRangesList, which is a `list` of GRanges objects. While the analogy is not perfect, a GRangesList behaves a bit like a list. Each element in the GRangesList is a Granges object. A common use case for a GRangesList is to store a list of transcripts, each of which have exons as the regions in the GRanges.

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```
gr1 <- GRanges(
  seqnames = "chr1",
  ranges = IRanges(103, 106),
  strand = "+",
  score = 5L, GC = 0.45)
gr2 <- GRanges(
  seqnames = c("chr1", "chr1"),
  ranges = IRanges(c(107, 113), width = 3),
  strand = c("+", "-"),
  score = 3:4, GC = c(0.3, 0.5))
```

The `gr1` and `gr2` are each `GRanges` objects. We can combine them into a “named” `GRangesList` like so:

```
grl <- GRangesList("txA" = gr1, "txB" = gr2)
grl
```

```
GRangesList object of length 2:
$txA
GRanges object with 1 range and 2 metadata columns:
  seqnames      ranges strand |      score      GC
  <Rle> <IRanges> <Rle> | <integer> <numeric>
[1]     chr1    103-106     + |       5      0.45
-----
seqinfo: 1 sequence from an unspecified genome; no seqlengths

$txB
GRanges object with 2 ranges and 2 metadata columns:
  seqnames      ranges strand |      score      GC
  <Rle> <IRanges> <Rle> | <integer> <numeric>
[1]     chr1    107-109     + |       3      0.3
[2]     chr1    113-115     - |       4      0.5
-----
seqinfo: 1 sequence from an unspecified genome; no seqlengths
```

The `show` method for a `GRangesList` object displays it as a named list of `GRanges` objects, where the names of this list are considered to be the names of the grouping feature. In the example above, the groups of individual exon ranges are represented as separate `GRanges` objects which are further organized into a list structure where each element name is a

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transcript name. Many other combinations of grouped and labeled `GRanges` objects are possible of course, but this example is a common arrangement.

In some cases, `GRangesLists` behave quite similarly to `GRanges` objects.

25.3.1. Basic `GRangesList` accessors

Just as with `GRanges` object, the components of the genomic coordinates within a `GRangesList` object can be extracted using simple accessor methods. Not surprisingly, the `GRangesList` objects have many of the same accessors as `GRanges` objects. The difference is that many of these methods return a list since the input is now essentially a list of `GRanges` objects. Here are a few examples:

```
seqnames(grl)
```

```
RleList of length 2
$txA
factor-Rle of length 1 with 1 run
  Lengths: 1
  Values : chr1
Levels(1): chr1

$txB
factor-Rle of length 2 with 1 run
  Lengths: 2
  Values : chr1
Levels(1): chr1
```

```
ranges(grl)
```

```
IRangesList object of length 2:
$txA
IRanges object with 1 range and 0 metadata columns:
      start     end     width
      <integer> <integer> <integer>
[1]       103       106        4

$txB
IRanges object with 2 ranges and 0 metadata columns:
```

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```
      start      end      width
<integer> <integer> <integer>
[1]      107      109       3
[2]      113      115       3
```

```
strand(grl)
```

```
RleList of length 2
$txA
factor-Rle of length 1 with 1 run
  Lengths: 1
  Values : +
Levels(3): + - *

$txB
factor-Rle of length 2 with 2 runs
  Lengths: 1 1
  Values : + -
Levels(3): + - *
```

The length and names methods will return the length or names of the list and the seqlengths method will return the set of sequence lengths.

```
length(grl)
```

```
[1] 2
```

```
names(grl)
```

```
[1] "txA" "txB"
```

```
seqlengths(grl)
```

```
chr1
NA
```

25.4. Relationships between region sets

One of the more powerful approaches to genomic data integration is to ask about the relationship between sets of genomic ranges. The key features of this process are to look at overlaps and distances to the nearest feature. These functionalities, combined with the operations like `flank` and `resize`, for instance, allow pretty useful analyses with relatively little code. In general, these operations are *very* fast, even on thousands to millions of regions.

25.4.1. Overlaps

The `findOverlaps` method in the `GenomicRanges` package is a very useful function that allows users to identify overlaps between two sets of genomic ranges.

Here's how it works:

- **Inputs** The function requires two `GRanges` objects, referred to as query and subject.
- **Processing** The function then compares every range in the query object with every range in the subject object, looking for overlaps. An overlap is defined as any instance where the range in the query object intersects with a range in the subject object.
- **Output** The function returns a `Hits` (see `?Hits`) object, which is a compact representation of the matrix of overlaps. Each entry in the `Hits` object corresponds to a pair of overlapping ranges, with the query index and the subject index.

Here is an example of how you might use the `findOverlaps` function:

```
# Create two GRanges objects
gr1 <- gr[1:4]
gr2 <- gr[3:8]
gr1
```

```
GRanges object with 4 ranges and 3 metadata columns:
  seqnames      ranges strand |   score       GC       AT
  <Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
  a     chr1    101-111    - |        1  1.000000  0.000000
  b     chr2    102-112    + |        2  0.888889  0.111111
  c     chr2    103-113    + |        3  0.777778  0.222222
  d     chr2    104-114    * |        4  0.666667  0.333333
```

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```
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths

gr2

GRanges object with 6 ranges and 3 metadata columns:
  seqnames      ranges strand |      score        GC        AT
  <Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
  c     chr2    103-113    + |      3  0.777778  0.222222
  d     chr2    104-114    * |      4  0.666667  0.333333
  e     chr1    105-115    * |      5  0.555556  0.444444
  f     chr1    106-116    + |      6  0.444444  0.555556
  g     chr3    107-117    + |      7  0.333333  0.666667
  h     chr3    108-118    + |      8  0.222222  0.777778
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths

# Find overlaps
overlaps <- findOverlaps(query = gr1, subject = gr2)
overlaps
```

Hits object with 7 hits and 0 metadata columns:

queryHits	subjectHits
<integer>	<integer>

```
  [1]      1      3
  [2]      2      1
  [3]      2      2
  [4]      3      1
  [5]      3      2
  [6]      4      1
  [7]      4      2
-----
queryLength: 4 / subjectLength: 6
```

In the resulting overlaps object, each row corresponds to an overlapping pair of ranges, with the first column giving the index of the range in gr1 and the second column giving the index of the overlapping range in gr2.

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If you are interested in only the `queryHits` or the `subjectHits`, there are accessors for those (ie., `queryHits(overlaps)`). To get the actual ranges that overlap, you can use the `subjectHits` or `queryHits` as an index into the original `GRanges` object.

Spend some time looking at these results. Note how the strand comes into play when determining overlaps.

```
gr1[queryHits(overlaps)]
```

```
GRanges object with 7 ranges and 3 metadata columns:
  seqnames      ranges strand |      score        GC        AT
  <Rle> <IRanges>  <Rle> | <integer> <numeric> <numeric>
  a     chr1    101-111     - |      1  1.000000  0.000000
  b     chr2    102-112     + |      2  0.888889  0.111111
  b     chr2    102-112     + |      2  0.888889  0.111111
  c     chr2    103-113     + |      3  0.777778  0.222222
  c     chr2    103-113     + |      3  0.777778  0.222222
  d     chr2    104-114     * |      4  0.666667  0.333333
  d     chr2    104-114     * |      4  0.666667  0.333333
  -----
  seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

```
gr2[subjectHits(overlaps)]
```

```
GRanges object with 7 ranges and 3 metadata columns:
  seqnames      ranges strand |      score        GC        AT
  <Rle> <IRanges>  <Rle> | <integer> <numeric> <numeric>
  e     chr1    105-115     * |      5  0.555556  0.444444
  c     chr2    103-113     + |      3  0.777778  0.222222
  d     chr2    104-114     * |      4  0.666667  0.333333
  c     chr2    103-113     + |      3  0.777778  0.222222
  d     chr2    104-114     * |      4  0.666667  0.333333
  c     chr2    103-113     + |      3  0.777778  0.222222
  d     chr2    104-114     * |      4  0.666667  0.333333
  -----
  seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

As you might expect, the `countOverlaps` method counts the regions in the second `GRanges` that overlap with those that overlap with each element of the first.

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```
countOverlaps(gr1, gr2)
```

```
a b c d  
1 2 2 2
```

The `subsetByOverlaps` method simply subsets the query `GRanges` object to include *only* those that overlap the subject.

```
subsetByOverlaps(gr1, gr2)
```

`GRanges` object with 4 ranges and 3 metadata columns:

seqnames	ranges	strand		score	GC	AT	
<Rle>	<IRanges>	<Rle>		<integer>	<numeric>	<numeric>	
a	chr1	101-111	-		1	1.000000	0.000000
b	chr2	102-112	+		2	0.888889	0.111111
c	chr2	103-113	+		3	0.777778	0.222222
d	chr2	104-114	*		4	0.666667	0.333333

seqinfo: 3 sequences from an unspecified genome; no seqlengths

In some cases, you may be interested in only one hit when doing overlaps. Note the `select` parameter. See the help for `findOverlaps`

```
findOverlaps(gr1, gr2, select="first")
```

```
[1] 3 1 1 1
```

```
findOverlaps(gr1, gr2, select="first")
```

```
[1] 3 1 1 1
```

The `%over%` logical operator allows us to do similar things to `findOverlaps` and `subsetByOverlaps`.

```
gr2 %over% gr1
```

```
[1] TRUE TRUE TRUE FALSE FALSE FALSE
```

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```
gr1[gr1 %over% gr2]
```

```
GRanges object with 4 ranges and 3 metadata columns:
  seqnames      ranges strand |      score        GC        AT
  <Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
  a     chr1    101-111     - |       1  1.000000  0.000000
  b     chr2    102-112     + |       2  0.888889  0.111111
  c     chr2    103-113     + |       3  0.777778  0.222222
  d     chr2    104-114     * |       4  0.666667  0.333333
  -----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

25.4.2. Nearest feature

There are a number of useful methods that find the nearest feature (region) in a second set for each element in the first set.

We can review our two `GRanges` toy objects:

```
g
```

```
GRanges object with 3 ranges and 3 metadata columns:
  seqnames      ranges strand |      score        GC        AT
  <Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
  a     chr1    101-111     - |       1  1.000000  0.000000
  b     chr2    102-112     + |       2  0.888889  0.111111
  c     chr2    103-113     + |       3  0.777778  0.222222
  -----
seqinfo: 3 sequences from an unspecified genome; no seqlengths
```

```
gr
```

```
GRanges object with 10 ranges and 3 metadata columns:
  seqnames      ranges strand |      score        GC        AT
  <Rle> <IRanges> <Rle> | <integer> <numeric> <numeric>
  a     chr1    101-111     - |       1  1.000000  0.000000
  b     chr2    102-112     + |       2  0.888889  0.111111
  c     chr2    103-113     + |       3  0.777778  0.222222
```

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```

d    chr2  104-114      * |      4  0.666667  0.333333
e    chr1  105-115      * |      5  0.555556  0.444444
f    chr1  106-116      + |      6  0.444444  0.555556
g    chr3  107-117      + |      7  0.333333  0.666667
h    chr3  108-118      + |      8  0.222222  0.777778
i    chr3  109-119      - |      9  0.111111  0.888889
j    chr3  110-120      - |     10  0.000000  1.000000
-----
seqinfo: 3 sequences from an unspecified genome; no seqlengths

```

- nearest: Performs conventional nearest neighbor finding. Returns an integer vector containing the index of the nearest neighbor range in subject for each range in x. If there is no nearest neighbor NA is returned. For details of the algorithm see the man page in the IRanges package (?nearest).
- precede: For each range in x, precede returns the index of the range in subject that is directly preceded by the range in x. Overlapping ranges are excluded. NA is returned when there are no qualifying ranges in subject.
- follow: The opposite of precede, follow returns the index of the range in subject that is directly followed by the range in x. Overlapping ranges are excluded. NA is returned when there are no qualifying ranges in subject.

Orientation and strand for precede and follow: Orientation is 5' to 3', consistent with the direction of translation. Because positional numbering along a chromosome is from left to right and transcription takes place from 5' to 3', precede and follow can appear to have 'opposite' behavior on the + and - strand. Using positions 5 and 6 as an example, 5 precedes 6 on the + strand but follows 6 on the - strand.

The table below outlines the orientation when ranges on different strands are compared. In general, a feature on * is considered to belong to both strands. The single exception is when both x and subject are * in which case both are treated as +.

	x		subject		orientation
a)	+		+		--->
b)	+		-		NA
c)	+		*		--->
d)	-		+		NA
e)	-		-		<---
f)	-		*		<---
g)	*		+		--->

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```
h)      * | -          | <---  
i)      * | *          | ---> (the only situation where * arbitrarily means +)
```

```
res = nearest(g, gr)  
res
```

```
[1] 5 4 4
```

While `nearest` and friends give the index of the nearest feature, the distance to the nearest is sometimes also useful to have. The `distanceToNearest` method calculates the nearest feature as well as reporting the distance.

```
res = distanceToNearest(g, gr)  
res
```

```
Hits object with 3 hits and 1 metadata column:  
  queryHits subjectHits | distance  
  <integer>   <integer> | <integer>  
 [1]         1           5 |       0  
 [2]         2           4 |       0  
 [3]         3           4 |       0  
-----  
queryLength: 3 / subjectLength: 10
```

25.5. Gene models

The `TxDb` package provides a convenient interface to gene models from a variety of sources. The `TxDb.Hsapiens.UCSC.hg38.knownGene` package provides access to the UCSC known-Gene gene model for the hg19 build of the human genome.

```
library(TxDb.Hsapiens.UCSC.hg38.knownGene)  
txdb <- TxDb.Hsapiens.UCSC.hg38.knownGene
```

The `transcripts` function returns a `GRanges` object with the transcripts for all genes in the database.

25. Genomic ranges and features

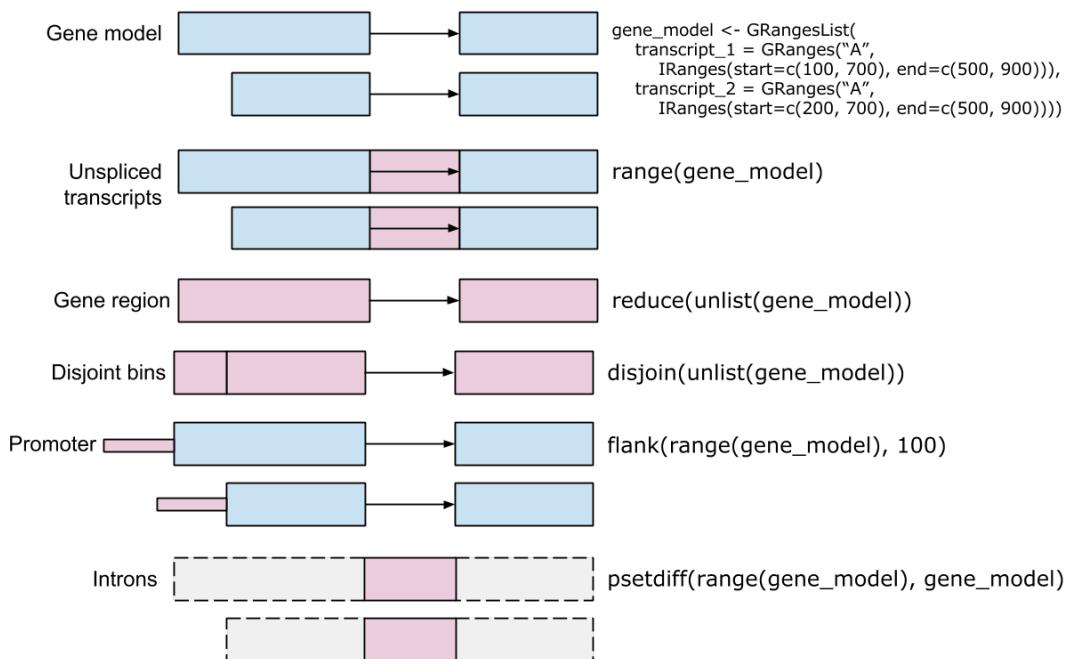


Figure 25.3.: A graphical representation of range operations demonstrated on a gene model.

25. Genomic ranges and features

```
tx <- transcripts(txdb)
```

The `exons` function returns a `GRanges` object with the exons.

```
ex <- exons(txdb)
```

The `genes` function returns a `GRanges` object with the genes.

```
gn <- genes(txdb)
```

26. Ranges Exercises

In the following exercises, we will use the `GenomicRanges` package to explore range operations. We will use the `AnnotationHub` package to load DNase hypersensitivity data from the ENCODE project. In practice, the ENCODE project published datasets like these as bed files. `AnnotationHub` has packaged these into `GRanges` objects that we can load and use directly. However, if you have a bed file of your own (peak calls, enhancer regions, etc.), you can load them into `GRanges` objects using `rtracklayer::import`.

26.1. Exercise 1

In this exercise, we will use DNase hypersensitivity data to practice working with a `GRanges` object.

- Use the `AnnotationHub` package to find the `goldenpath/hg19/encodeDCC/wgEncodeUwDnase/wgEncodeUwDnaseK562PkRep1.narrowPeak.g` `GRanges` object. Load that into R as the variable `dnase`.

```
library(AnnotationHub)
ah = AnnotationHub()
query(ah, "goldenpath/hg19/encodeDCC/wgEncodeUwDnase/wgEncodeUwDnaseK562PkRep1.narrowPeak.g"
# the thing above should have only one record, so we can
# just grab it
dnase = query(ah, "goldenpath/hg19/encodeDCC/wgEncodeUwDnase/wgEncodeUwDnaseK562PkRep1.narr
```

- What type of object is `dnase`?

```
dnase
class(dnase)
```

- What metadata is stored in `dnase`?

```
mcols(dnase)
• How many peaks are on each chromosome?
```

26. Ranges Exercises

```
library(GenomicFeatures)
table(seqnames(dnase))
```

- What are the mean, min, max, and median widths of the peaks?

```
summary(width(dnase))
```

- What are the sequences that were used in the analysis? Do the names have “chr” or not? Experiment with changing the `seqlevelsStyle` to adjust the sequence names.

```
seqlevels(dnase)
seqlevelsStyle(dnase)
seqlevelsStyle(dnase) = 'ensembl'
seqlevelsStyle(dnase)
seqlevels(dnase)
```

- What is the total amount of “landscape” covered by the peaks? Assume that the peaks do not overlap. What portion of the genome does this represent?

```
sum(width(dnase))
sum(seqlengths(dnase))
sum(width(dnase))/sum(seqlengths(dnase))
```

26.2. Exercise 2

In this exercise, we are going to load the second DNase hypersensitivity replicate to investigate overlaps with the first replicate.

- Use the AnnotationHub to find the second replicate, `goldenpath/hg19/encodeDCC/wgEncodeUwDnase/wgEncodeUwDnaseK562PkRep2.narrowPeak.g`. Load that as `dnase2`.

```
query(ah, "goldenpath/hg19/encodeDCC/wgEncodeUwDnase/wgEncodeUwDnaseK562PkRep2.narrowPeak.g"
# the thing above should have only one record, so we can
# just grab it
dnase2 = query(ah, "goldenpath/hg19/encodeDCC/wgEncodeUwDnase/wgEncodeUwDnaseK562PkRep2.nar
```

- How many peaks are there in `dnase` and `dnase2`? Are there are similar number?

26. Ranges Exercises

```
length(dnase)
length(dnase2)
```

- What are the peak sizes for `dnase2`?

```
summary(width(dnase2))
```

- What proportion of the genome does `dnase2` cover?

```
sum(width(dnase))/sum(seqLengths(dnase))
```

- Count the number of peaks from `dnase` that overlap with `dnase2`.

```
sum(dnase %over% dnase2)
```

- Assume that your peak-caller was “too specific” and that you want to expand your peaks by 50 bp on each end (so make them 100 bp larger). Use a combination of `resize` (and pay attention to the `fix` argument) and `width` to do this expansion to `dnase` and call the new `GRanges` object “`dnase_wide`”.

```
w = width(dnase)
dnase_wide = resize(dnase, width=w+100, fix='center') #make a copy
width(dnase_wide)
```

26.3. Exercise 3

In this exercise, we are going to look at the overlap of DNAse sites relative to genes. To get started, install and load the `TxDb.Hsapiens.UCSC.hg19.knownGene` txdb object.

```
BiocManager::install("TxDb.Hsapiens.UCSC.hg19.knownGene")
library("TxDb.Hsapiens.UCSC.hg19.knownGene")
kg = TxDb.Hsapiens.UCSC.hg19.knownGene
```

- Load the transcripts from the `knownGene` txdb into a variable. What is the class of this object?

26. Ranges Exercises

```
library("TxDb.Hsapiens.UCSC.hg19.knownGene")
kg = TxDb.Hsapiens.UCSC.hg19.knownGene
gx = genes(kg)
class(gx)
length(gx)
```

- Read about the `flank` method for GRanges objects. How could you use that to get the “promoter” regions of the transcripts? Let’s assume that the promoter region is 2kb upstream of the gene.

```
flank(gx, 2000)
```

- Instead of using `flank`, could you do the same thing with the `TxDb` object? (See `?promoters`).

```
proms = promoters(kg)
```

- Do any of the regions in the promoters overlap with each other?

```
summary(countOverlaps(proms))
```

- To find overlap of our DNase sites with promoters, let’s collapse overlapping “promoters” to just keep the contiguous regions by using `reduce`.

```
# reduce takes all overlapping regions and collapses them
# into a single region that spans all of the overlapping regions
prom_regions = reduce(proms)

# now we can check for overlaps
summary(countOverlaps(prom_regions))
```

- Count the number of DNase sites that overlap with our promoter regions.

```
sum(dnase %over% prom_regions)
# if you notice no overlap, check the seqlevels
# and seqlevelsStyle
seqlevelsStyle(dnase) = "UCSC"
sum(dnase %over% prom_regions)
sum(dnase2 %over% prom_regions)
```

26. Ranges Exercises

- Is this surprising? If we were to assume that the promoter and dnase regions are “independent” of each other, what number of overlaps would we expect?

```
prop_proms = sum(width(prom_regions))/sum(seqlengths(prom_regions))
prop_dnase = sum(width(dnase))/sum(seqlengths(prom_regions))
# Iff the dnase and promoter regions are
# not related, then we would expect this number
# of DNase overlaps with promoters.
prop_proms * prop_dnase * length(dnase)
```

26.4. Exercise 4

We'll be using data from histone modification ChIP-seq experiments in human cells to illustrate the concepts of genomic ranges and features. The data consists of genomic intervals representing regions of the genome where specific histone modifications are enriched. These intervals are typically identified using ChIP-seq, a technique that maps protein-DNA interactions across the genome.

The ChIP-seq data is stored in a BED file format, which is a tab-delimited text file format commonly used to represent genomic intervals. Each line in the BED file corresponds to a genomic interval and contains information about the chromosome, start and end positions, and strand orientation of the interval. Additional columns may include metadata such as the signal strength or significance of the interval.

The AnnotationHub package in Bioconductor provides access to a wide range of genomic datasets, including ChIP-seq data. We can use this package to retrieve the ChIP-seq data for histone modifications in human cells and convert it into a GenomicRanges object for further analysis.

<https://www.encodeproject.org/chip-seq/histone/>

Let's start by loading the AnnotationHub package and retrieving the ChIP-seq data for histone modifications in human cells. You can read more about the AnnotationHub package and how to use it in the Bioconductor documentation.

```
library(AnnotationHub)
ah <- AnnotationHub()
```

There are multiple ways to search the AnnotationHub database. We've done that for you and here are the GRanges objects for each of four histone marks, and one histone mark replicate.

26. Ranges Exercises

```
h3k4me1 <- ah[['AH25832']]
h3k4me3 <- ah[['AH25833']]
h3k9ac <- ah[['AH25834']]
h3k27me3 <- ah[['AH25835']]
h3k4me3_2 <- ah[['AH27284']]
```

Each of these variables now represents the peak calls after a chip-seq experiment pulling down the histone mark of interest. In the encode project these records were `bed` files. The `bed` files have been converted to `GRanges` objects to allow computation within R.

```
# Grab cpg islands as well
cpg = query(ah, c('cpg', 'UCSC', 'hg19'))[[1]]
```

Let's say that we don't know the behavior of the histone methylation marks with respect to CpG islands. We could ask the question, "What is the overlap of the histone peaks with CpG islands?"

```
sum(h3k4me1 %over% cpg)
```

We might want to actually count the number of bases of overlap between the methyl mark and CpG islands.

```
# The intersection of two peak sets results in the
# overlapping regions as a new set of regions
# The width of each peak is the number of overlapping bases
# And the sum of the widths is the total bases overlapping
sum(width(intersect(h3k4me1, cpg)))
```

But some methyl marks are known to have very broad signals, meaning that there is a higher chance of overlapping CpG islands just because there are more methylated bases. We can adjust for this by "normalizing" for all possible bases covered by either set of peaks, using `union`. We might think of this as a sort of "enrichment score" of one set in another set.

```
sum(width(union(h3k4me1, cpg)))
# and now "normalize"
sum(width(intersect(h3k4me1, cpg)))/sum(width(union(h3k4me1, cpg)))
```

Let's write a small function to calculate our little enrichment score.

26. Ranges Exercises

```
range_enrichment_score <- function(r1, r2) {  
  i = sum(width(intersect(r1, r2)))  
  u = sum(width(union(r1,r2)))  
  return(i/u)  
}
```

And give it a try:

```
range_enrichment_score(h3k4me1, cpg)
```

27. Genomic ranges and ATAC-Seq

R / Bioconductor packages used

- *Rsamtools*
- *GenomicRanges*
- *GenomicFeatures*
- *GenomicAlignments*
- *rtracklayer*
- *heatmaps*

27.1. Background

Chromatin accessibility assays measure the extent to which DNA is open and accessible. Such assays now use high throughput sequencing as a quantitative readout. DNase assays, first using microarrays(Crawford, Davis, et al. 2006) and then DNase-Seq (Crawford, Holt, et al. 2006), requires a larger amount of DNA and is labor-indensive and has been largely supplanted by ATAC-Seq (Buenrostro et al. 2013).

The Assay for Transposase Accessible Chromatin with high-throughput sequencing (ATAC-seq) method maps chromatin accessibility genome-wide. This method quantifies DNA accessibility with a hyperactive Tn5 transposase that cuts and inserts sequencing adapters into regions of chromatin that are accessible. High throughput sequencing of fragments produced by the process map to regions of increased accessibility, transcription factor binding sites, and nucleosome positioning. The method is both fast and sensitive and can be used as a replacement for DNase and MNase.

An early review of chromatin accessibility assays (Tsompana and Buck 2014) compares the use cases, pros and cons, and expected signals from each of the most common approaches (Figure @ref(fig:chromatinAssays)).

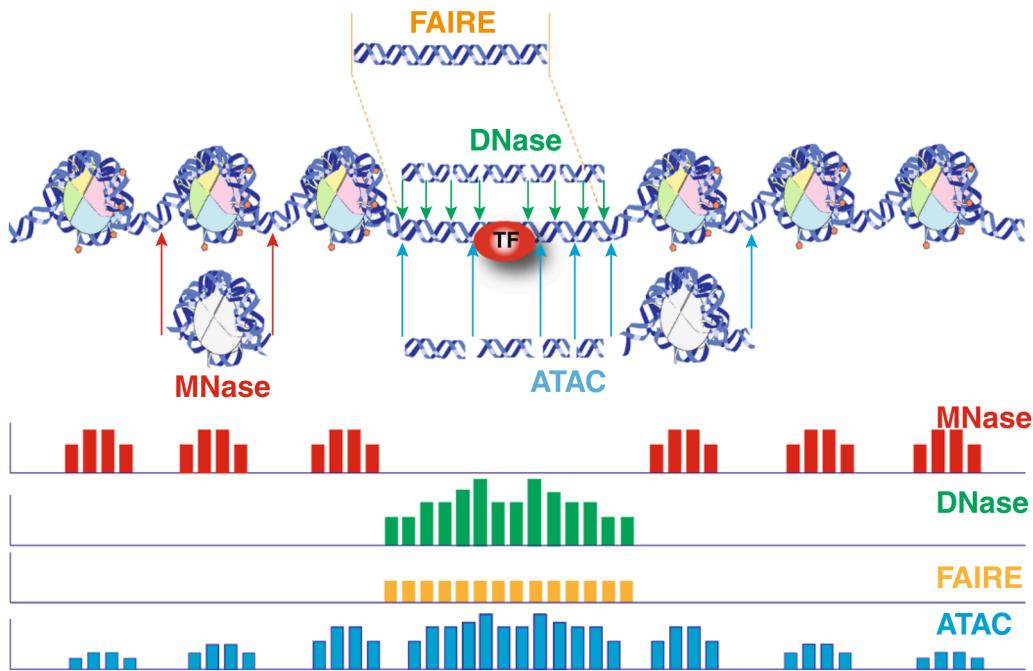


Figure 27.1.: Chromatin accessibility methods, compared. Representative DNA fragments generated by each assay are shown, with end locations within chromatin defined by colored arrows. Bar diagrams represent data signal obtained from each assay across the entire region. The footprint created by a transcription factor (TF) is shown for ATAC-seq and DNase-seq experiments.

The first manuscript describing ATAC-Seq protocol and findings outlined how ATAC-Seq data “line up” with other datatypes such as ChIP-seq and DNase-seq (Figure @ref(fig:greenleaf)). They also highlight how fragment length correlates with specific genomic regions and characteristics (Buenrostro et al. 2013, fig. 3).

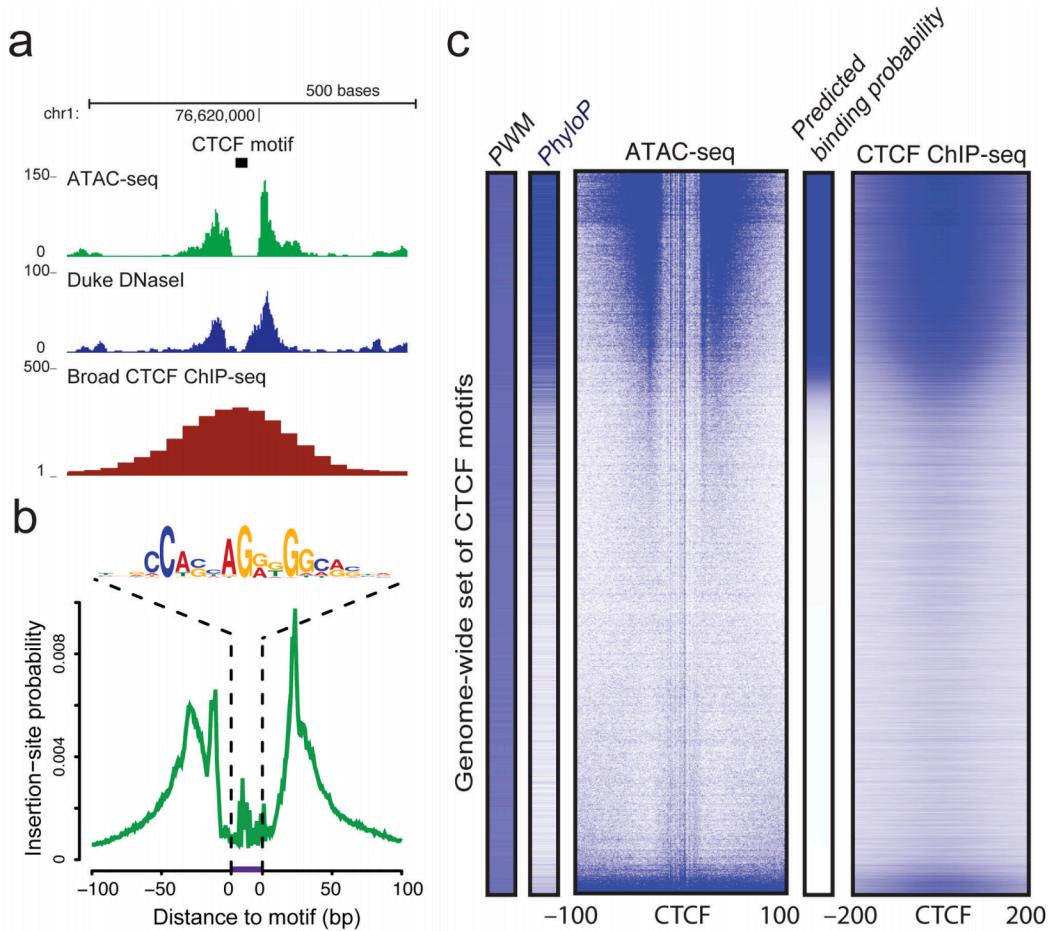


Figure 27.2.: Multimodal chromatin comparisons. From (Buenrostro et al. 2013), Figure 4.
 (a) CTCF footprints observed in ATAC-seq and DNase-seq data, at a specific locus on chr1. (b) Aggregate ATAC-seq footprint for CTCF (motif shown) generated over binding sites within the genome (c) CTCF predicted binding probability inferred from ATAC-seq data, position weight matrix (PWM) scores for the CTCF motif, and evolutionary conservation (PhyloP). Right-most column is the CTCF ChIP-seq data (ENCODE) for this GM12878 cell line, demonstrating high concordance with predicted binding probability.

Buenrostro et al. provide a detailed protocol for performing ATAC-Seq and quality control of results (Buenrostro et al. 2015). Updated and modified protocols that improve on signal-to-noise and reduce input DNA requirements have been described.

27.2. Informatics overview

ATAC-Seq protocols typically utilize paired-end sequencing protocols. The reads are aligned to the respective *genome* using `bowtie2`, `BWA`, or other short-read aligner. The result, after appropriate manipulation, often using `samtools`, results in a BAM file. Among other details, the BAM format includes columns for:

```
knitr:::include_graphics('imgs/bam_shot.png')
```

```
NCI-02069526-ML:extdata sdavis2$ samtools view Sorted_ATAC_21_22.bam | head -10
SRR891269.3150012    99   chr21  9411377 40      50M   =      9411438 111   CTCTGTTCTTGCTGACCTC
TTTGTCTATCCTTTGCTGAGAGGTC CCCFFDFHHHHHJJJJJJJJJJGJIIFHIJIIJJJJJJJJJJGHH HI:i:1 NH:i:1 NM:i
SRR891269.6181501    99   chr21  9411377 40      50M   =      9411438 111   CTCTGTTCTTGCTGACCTC
TTTGTCTATCCTTTGCTGAGAGGTC CCCFFFFHHHHHJJJJJJJJJJJJJJJJJJJJJJJJJJFIIJJHH HI:i:1 NH:i:1 NM:i
SRR891269.13803406   73   chr21  9411423 0       46M4S  *      0       0       GGTCTGCTTAACCTCCCTTT
AGGTAGCTCGATTATGCTAAATCT ?81B;D>DFF<+C@E+2AAC<33<CHB<9<+9B##### HI:i:1 NH:i:1 NM:i
SRR891269.3150012    147  chr21  9411438 20     50M   =      9411377 -111   CTTTTAGTCAGGTAGCTCCA
ATGCTAAGCTTCTTAGTTGCTCACCT JJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJ HI:i:1 NH:i:1 NM:i
SRR891269.6181501    147  chr21  9411438 20     50M   =      9411377 -111   CTTTTAGTCAGGTAGCTCCA
ATGCTAAGCTTCTTAGTTGCTCACCT JJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJ HI:i:1 NH:i:1 NM:i
SRR891269.52466482    81   chr21  9411533 0       8S42M  =      9411534 59    AAGAGACAGAAATTGCATTG
TACCGGCCCTTATCAAGCCCTGGCC JJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJ HI:i:1 NH:i:1 NM:i
SRR891269.52466482    161  chr21  9411534 0       41M9S  =      9411533 -59    AAATTGCATTGTCTACCG
TTTATCAAGCCCTGGCCCTGTCTCTT @BCFFFFFFHHHHHJJJJJJJJJJJJJJJJJJJJJJJJ HI:i:1 NH:i:1 NM:i
SRR891269.8220653    163  chr21  9411566 13     50M   =      9411639 123    GCCCTGGCCACCATGATACT
AATTCCAATTGTGTCTATGCAGGCC CCCFFFFHHHHHJJJJJJJJJJJJJJJJJJJJJJJJJJ HI:i:1 NH:i:1 NM:i
SRR891269.8220653    83   chr21  9411639 20     50M   =      9411566 -123   GCTACCATTTCCTTCTAGC
TGCTCAGCAAATGTATCAAATGAAA EJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJJ HI:i:1 NH:i:1 NM:i
```

Figure 27.3.: A BAM file in text form. The output of `samtools view` is the text format of the BAM file (called SAM format). Bioconductor and many other tools use BAM files for input. Note that BAM files also often include an index `.bai` file that enables random access into the file; one can read just a genomic region without having to read the entire file.

- sequence name (`chr1`)
- start position (integer)
- a *CIGAR* string that describes the alignment in a compact form
- the sequence to which the pair aligns
- the position to which the pair aligns
- a bit flag field that describes multiple characteristics of the alignment
- the sequence and quality string of the read
- additional tags that tend to be aligner-specific

Duplicate fragments (those with the *same* start and end position of other reads) are marked and likely discarded. Reads that fail to align “properly” are also often excluded from analysis. It is worth noting that most software packages allow simple “marking” of such reads and that there is usually no need to create a special BAM file before proceeding with downstream work.

After alignment and BAM processing, the workflow can switch to *Bioconductor*.

27.3. Working with sequencing data in Bioconductor

The *Bioconductor* project includes several infrastructure packages for dealing with ranges (sequence name, start, end, +/- strand) on sequences (Lawrence et al. 2013b) as well as capabilities with working with Fastq files directly (Morgan et al. 2016).

Table 27.1.: Commonly used Bioconductor and their high-level use cases.

Package	Use cases
<i>Rsamtools</i>	low level access to FASTQ, VCF, SAM, BAM, BCF formats
<i>GenomicRanges</i>	Container and methods for handling genomic regions
<i>GenomicFeatures</i>	Work with transcript databases, gff, gtf and BED formats
<i>GenomicAlignments</i>	Reader for BAM format
<i>rtracklayer</i>	import and export multiple UCSC file formats including BigWig and Bed

As noted in the previous section, the output of an ATAC-Seq experiment is a BAM file. As paired-end sequencing is a commonly-applied approach for ATAC-Seq, the `readGAlignmentPairs` function is the appropriate method to use.

28. Data import and quality control

```
library(GenomicAlignments)
```

Reading a paired-end BAM file looks a bit complicated, but the following code will:

1. Read the included BAM file.
2. Include read pairs only (`isPaired = TRUE`)
3. Include properly paired reads (`isProperPair = TRUE`)
4. Include reads with mapping quality ≥ 1
5. Add a couple of additional fields, `mapq` (mapping quality) and `isize` (insert size) to the default fields.

```
greenleaf <- readGAlignmentPairs(  
  "https://github.com/seandavi/RBiocBook/raw/main/atac-seq/extdata/Sorted_ATAC_21_22.bam"  
  param = ScanBamParam(  
    mapqFilter = 1,  
    flag = scanBamFlag(  
      isPaired = TRUE,  
      isProperPair = TRUE  
    ),  
    what = c("mapq", " isize")  
  )  
)
```

Exercise: What is the class of `greenleaf`? *Exercise:* Use the `GenomicAlignments::first()` accessor to get the first read of the pair as a `GAlignments` object. Save the result as a variable called `gl_first_read`. Use the `mcols` accessor to find the “metadata columns” of `gl_first_read`. *Exercise:* How many read pairs map to each chromosome?

We can make plot of the number of reads mapping to each chromosome.

28. Data import and quality control

```
library(ggplot2)
library(dplyr)
chromCounts <- table(seqnames(greenleaf)) %>%
  data.frame() %>%
  dplyr::rename(chromosome = Var1, count = Freq)
```

To keep things small, the example BAM file includes only chromosomes 21 and 22.

```
ggplot(chromCounts, aes(x = chromosome, y = count)) +
  geom_bar(stat = "identity") +
  theme(axis.text.x = element_text(angle = 45, hjust = 1))
```

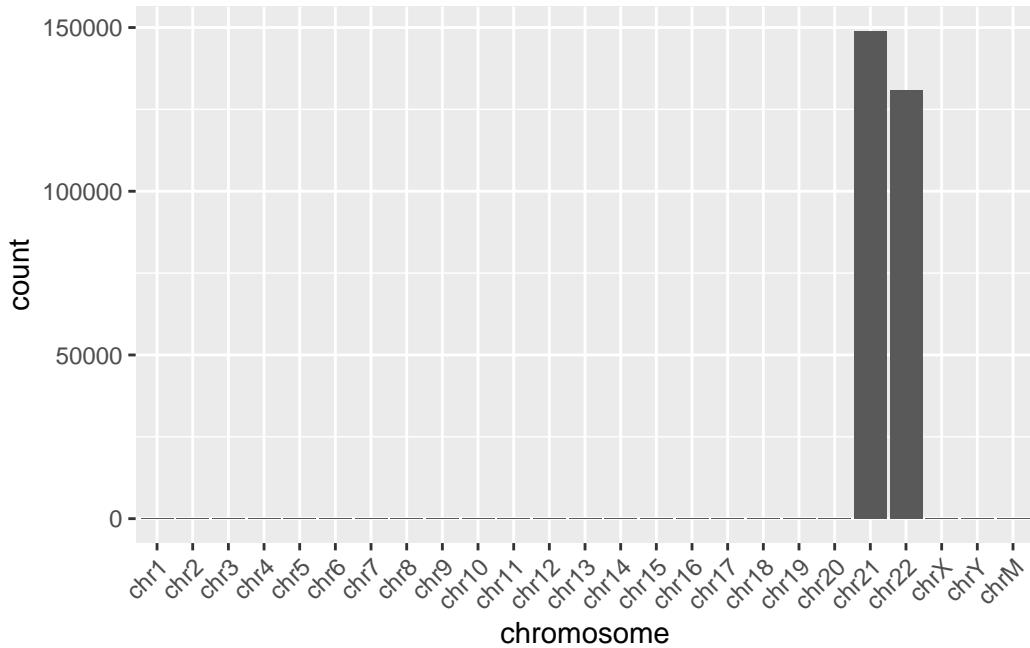


Figure 28.1.: Reads per chromosome. In our example data, we are using only chromosomes 21 and 22.

Normalizing by the chromosome length can yield the reads per megabase which should crudely be similar across all chromosomes.

```
chromCounts <- chromCounts %>%
  dplyr::mutate(readsPerMb = (count / (seqlengths(greenleaf) / 1e6)))
```

28. Data import and quality control

And show a plot. For two chromosomes, this is a little underwhelming.

```
ggplot(chromCounts, aes(x = chromosome, y = readsPerMb)) +  
  geom_bar(stat = "identity") +  
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +  
  theme_bw()
```

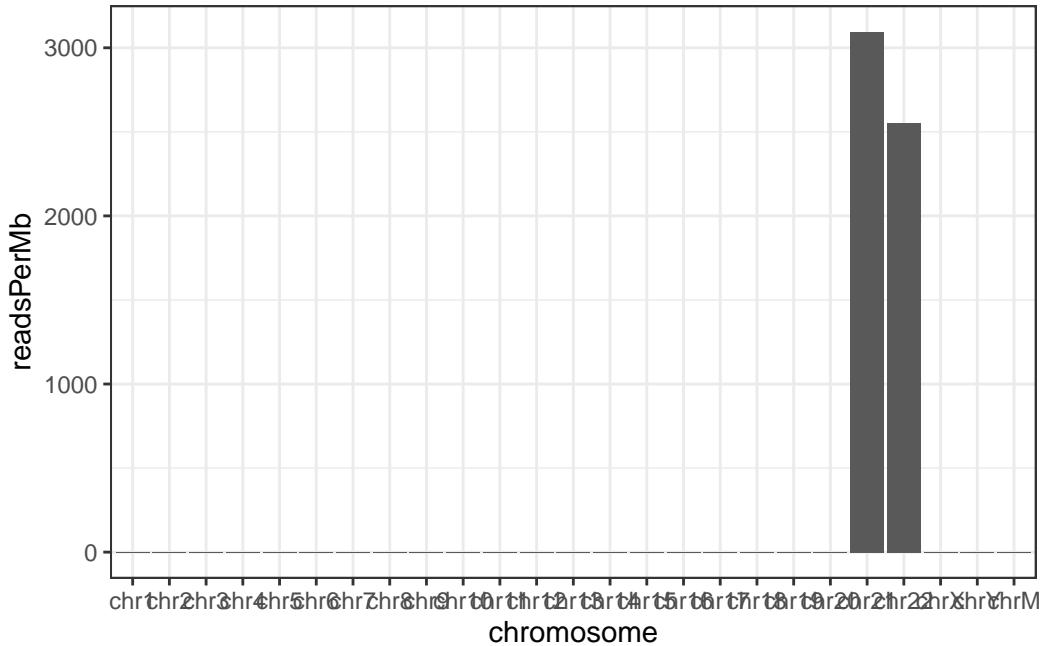


Figure 28.2.: Read counts normalized by chromosome length. This is not a particularly important plot, but it can be useful to see the relative contribution of each chromosome given its length.

28.1. Coverage

The `coverage` method for genomic ranges calculates, for each base, the number of overlapping features. In the case of a BAM file from ATAC-Seq converted to a GAlignmentPairs object, the coverage gives us an idea of the extent to which reads pile up to form peaks.

```
cvg <- coverage(greenleaf)  
class(cvg)
```

28. Data import and quality control

```
[1] "SimpleRleList"
attr(,"package")
[1] "IRanges"
```

The coverage is returned as a `SimpleRleList` object. Using `names` can get us the names of the elements of the list.

```
names(cvg)
```

```
[1] "chr1"  "chr2"  "chr3"  "chr4"  "chr5"  "chr6"  "chr7"  "chr8"  "chr9"
[10] "chr10" "chr11" "chr12" "chr13" "chr14" "chr15" "chr16" "chr17" "chr18"
[19] "chr19" "chr20" "chr21" "chr22" "chrX"  "chrY"  "chrM"
```

There is a name for each chromosome. Looking at the `chr21` entry:

```
cvg$chr21
```

```
integer-Rle of length 48129895 with 397462 runs
Lengths: 9411376      50       11      50 ...
Values :      0        2        0        2 ...      1        2        1        0
```

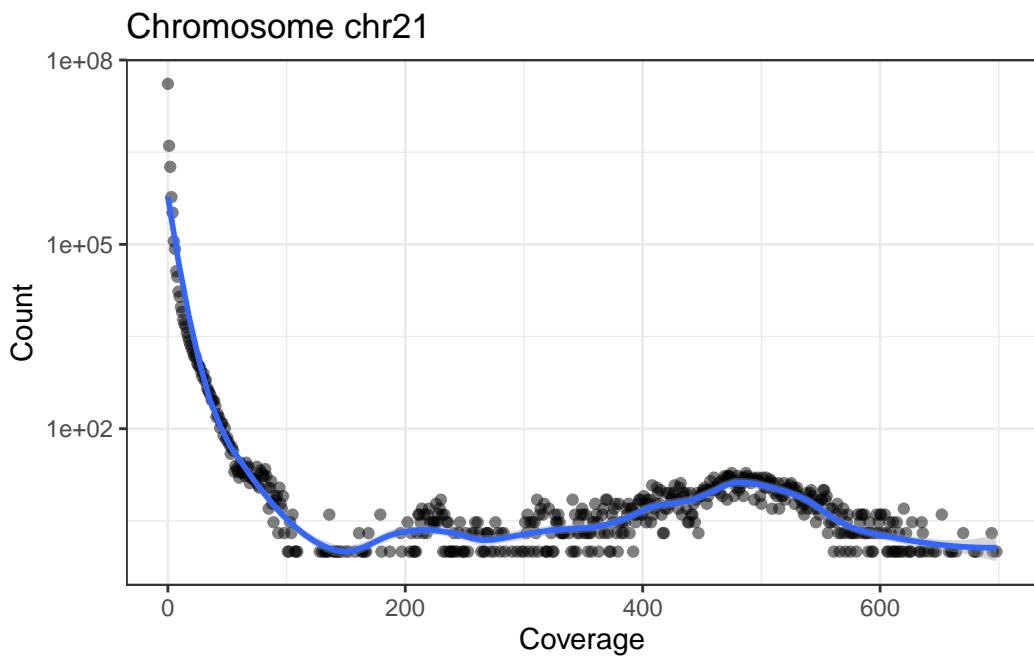
we see that each chromosome is represented as an `Rle`, short for run-length-encoding. Simply put, since along the chromosome there are many repeated values, we can recode the long vector as a set of (length: value) pairs. For example, if the first 9,410,000 base pairs have 0 coverage, we encode that as (9,410,000: 0). Doing that across the chromosome can very significantly reduce the memory use for genomic coverage.

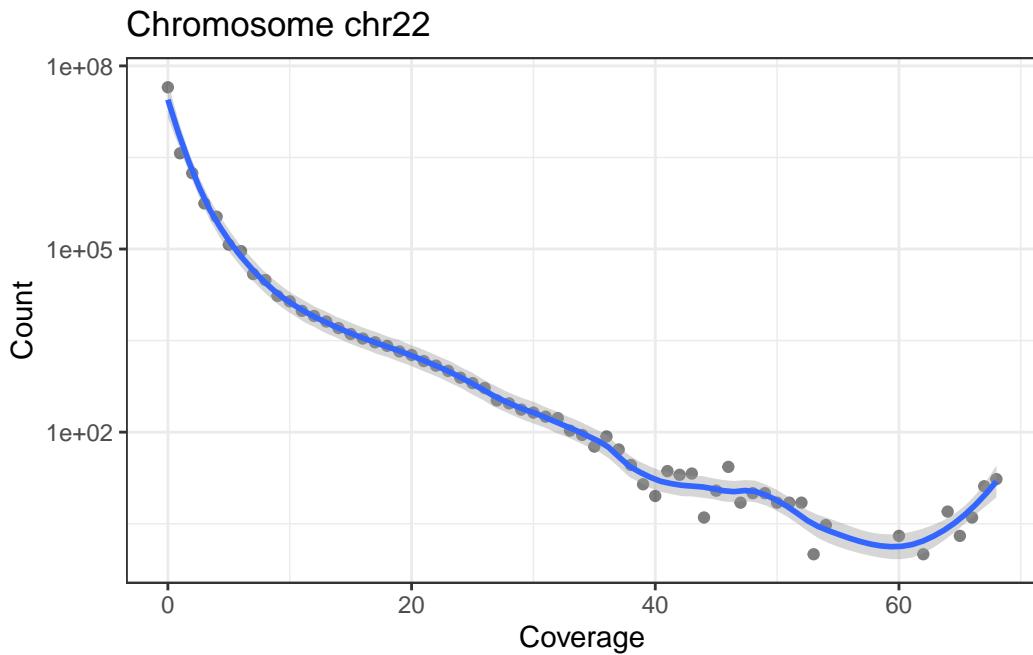
The following little function, `plotCvgHistByChrom` can plot a histogram of the coverage for a chromosome.

```
plotCvgHistByChrom <- function(cvg, chromosome) {
  library(ggplot2)
  cvgcounts <- as.data.frame(table(cvg[[chromosome]]))
  cvgcounts[, 1] <- as.numeric(as.character(cvgcounts[, 1]))
  colnames(cvgcounts) <- c("Coverage", "Count")
  ggplot(cvgcounts, aes(x = Coverage, y = Count)) +
    ggttitle(paste("Chromosome", chromosome)) +
    geom_point(alpha = 0.5) +
    geom_smooth(span = 0.2) +
```

28. Data import and quality control

```
    scale_y_log10() +  
    theme_bw()  
}  
for (i in c("chr21", "chr22")) {  
  print(plotCvgHistByChrom(cvg, i))  
}
```





28.2. Fragment Lengths

The first ATAC-Seq manuscript (Buenrostro et al. 2013) highlighted the relationship between fragment length and nucleosomes (see Figure @ref{fig:flgreenleaf}).

```
knitr::include_graphics("https://cdn.ncbi.nlm.nih.gov/pmc/blobs/0ad9/3959825/fde39a9fb288/m
```

28. Data import and quality control

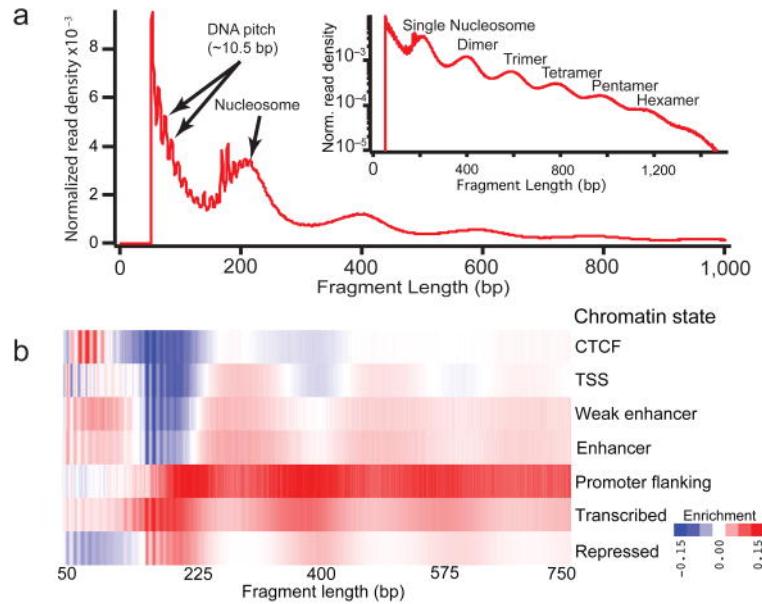


Figure 28.3.: Relationship between fragment length and nucleosome number.

Remember that we loaded the example BAM file with insert sizes (`isize`). We can use that “column” to examine the fragment lengths (another name for insert size). Also, note that the insert size for the `first` read and the `second` are the same (absolute value). Here, we will use `first`.

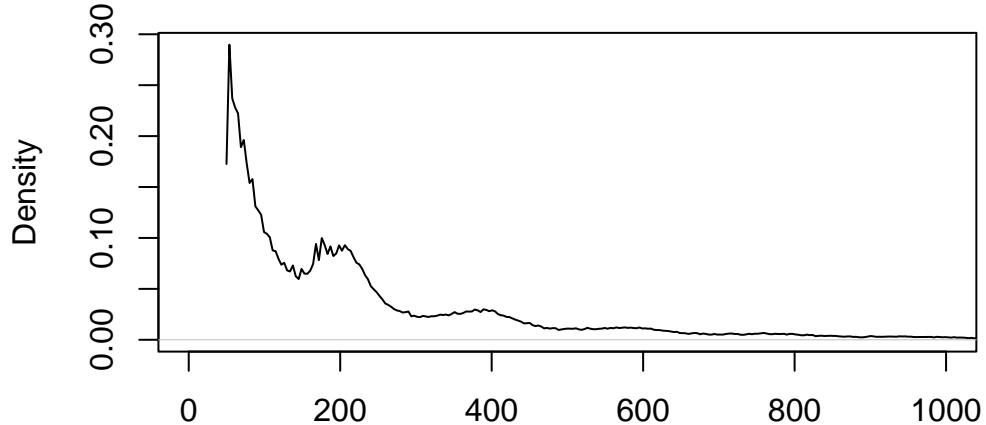
```
GenomicAlignments::first(greenleaf)
mcols(GenomicAlignments::first(greenleaf))
class(mcols(GenomicAlignments::first(greenleaf)))
head(mcols(GenomicAlignments::first(greenleaf))$isize)
fraglengths <- abs(mcols(GenomicAlignments::first(greenleaf))$isize)
```

We can plot the fragment length density (histogram) using the `density` function.

```
plot(density(fraglengths, bw = 0.05), xlim = c(0, 1000))
```

28. Data import and quality control

density(x = fraglengths, bw = 0.05)



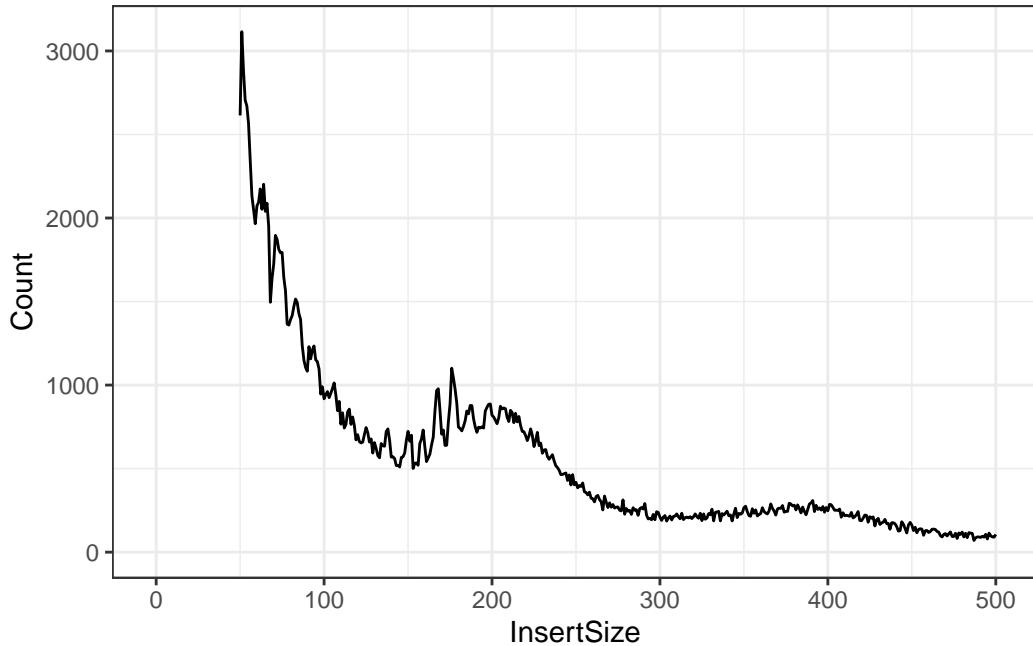
N = 279884 Bandwidth = 0.05

Figure 28.4.: Fragment length histogram.

And for fun, the ggplot2 version:

```
library(dplyr)
library(ggplot2)
fragLenPlot <- table(fraglengths) %>%
  data.frame() |>
  rename(
    InsertSize = fraglengths,
    Count = Freq
  ) |>
  mutate(
    InsertSize = as.numeric(as.vector(InsertSize)),
    Count = as.numeric(as.vector(Count))
  ) |>
  ggplot(aes(x = InsertSize, y = Count)) +
  geom_line()
print(fragLenPlot + theme_bw() + lims(x = c(-1, 500)))
```

28. Data import and quality control



Knowing that the nucleosome-free regions will have insert sizes shorter than one nucleosome, we can isolate the read pairs that have that characteristic.

```
gl_nf <- greenleaf[mcols(GenomicAlignments::first(greenleaf))$isize < 147]
```

And the mononucleosome reads will be between 147 and 294 base pairs for insert size/fragment length.

```
gl_mn <- greenleaf[mcols(GenomicAlignments::first(greenleaf))$isize > 147 &
  mcols(GenomicAlignments::first(greenleaf))$isize < 294]
```

Finally, we expect nucleosome-free reads to be enriched near the TSS while mononucleosome reads should not be. We will use the *heatmaps* package to take a look at these two sets of reads with respect to the tss of the human genome.

```
library(TxDb.Hsapiens.UCSC.hg19.knownGene)
proms <- promoters(TxDb.Hsapiens.UCSC.hg19.knownGene, 250, 250)
seqs <- c("chr21", "chr22")
seqlevels(proms, pruning.mode = "coarse") <- seqs # only chromosome 21 and 22
```

Take a look at the *heatmaps* package vignette to learn more about the heatmaps package capabilities.

28. Data import and quality control

```
library(heatmaps)
gl_nf_hm <- CoverageHeatmap(proms, coverage(gl_nf), coords = c(-250, 250))
label(gl_nf_hm) <- "NucFree"
scale(gl_nf_hm) <- c(0, 10)

gl_mn_hm <- CoverageHeatmap(proms, coverage(gl_mn), coords = c(-250, 250))
label(gl_mn_hm) <- "MonoNuc"
scale(gl_mn_hm) <- c(0, 10)
plotHeatmapMeta(list(gl_nf_hm, gl_mn_hm))
```

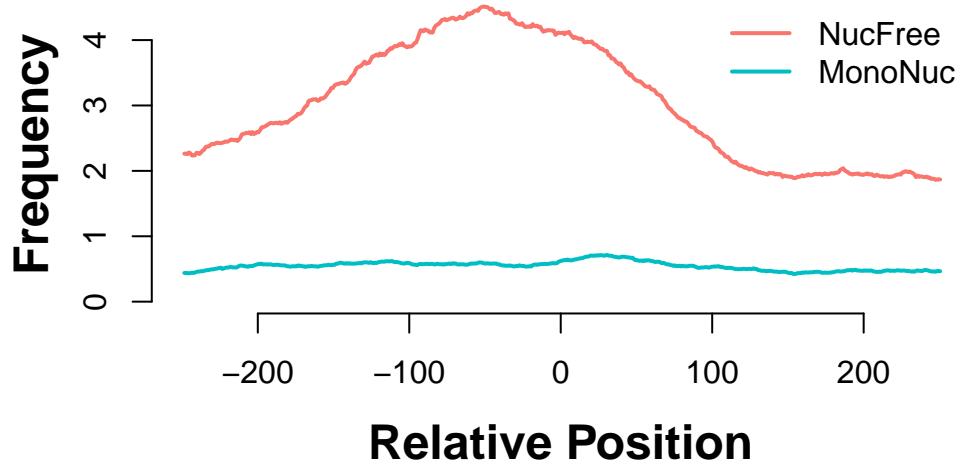


Figure 28.5.: Enrichment of nucleosome-free reads and depletion of mononucleosome reads around the TSS.

```
plotHeatmapList(list(gl_mn_hm, gl_nf_hm))
```

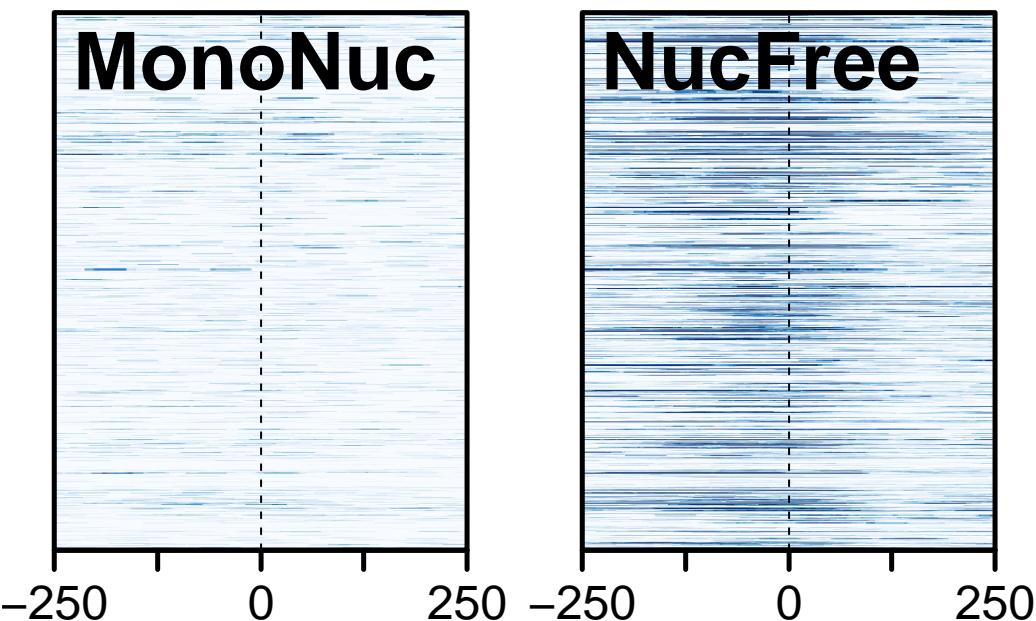


Figure 28.6.: Comparison of signals at TSS. Mononucleosome data on the left, nucleosome-free on the right. Both plots are scaled to the same range.

28.3. Viewing data in IGV

Install IGV from [here](#).

We export the greenleaf data as a BigWig file.

```
library(rtracklayer)
export.bw(coverage(greenleaf), "greenleaf.bw")
```

- *Exercise:* In IGV, choose hg19. Then, load the greenleaf.bw file and explore chromosomes 21 and 22.
- *Exercise:* Export the nucleosome-free portion of the data as a BigWig file and examine that in IGV. Where do you expect to see the strongest signals?

28.4. Additional work

For those working extensively on ATAC-Seq, there is a great workflow/tutorial available from Thomas Carroll:

MACS2

- https://rockefelleruniversity.github.io/RU_ATAC_Workshop.html

Feel free to work through it. In addition to the work above, there is also the *ATACseqQC* package vignette that offers more than just QC. At least a couple more packages are available in *Bioconductor*.

MACS2

The MACS2 package is a commonly-used package for calling peaks. Installation and other details are available¹.

```
pip install macs2
```

¹<https://github.com/taoliu/MACS>

29. Single Cell RNA-seq Analysis

29.1. Introduction

Single-cell RNA sequencing (scRNA-seq) is a powerful technique that allows us to measure gene expression in individual cells rather than bulk tissue samples. This capability has revolutionized our understanding of cellular heterogeneity, developmental processes, and disease mechanisms. Unlike traditional bulk RNA-seq, which provides an average expression profile across all cells in a sample, scRNA-seq reveals the unique molecular signatures of individual cells, enabling identification of distinct cell types, states, and trajectories.

This tutorial will walk through a typical scRNA-seq analysis workflow using R and the Bioconductor ecosystem. We'll cover data loading, quality control, normalization, dimensionality reduction, clustering, and visualization - the fundamental steps that transform raw sequencing data into biological insights.

29.2. Setup and Data Loading

29.2.1. Loading Essential Libraries

```
# Load essential libraries for single-cell RNA-seq analysis
library(scRNAseq)
library(scran)
library(scater)
```

We start by loading three essential R packages for single-cell analysis:

- **scRNAseq**: Provides access to curated single-cell RNA-seq datasets, making it easy to practice analysis techniques on real data. At the time of writing, it includes more than 50 datasets covering various tissues, organisms, and experimental conditions. See Risso and Cole (2024)

- **scran**: Contains methods for normalization, feature selection, and clustering specifically designed for single-cell data. See Lun, McCarthy, and Marioni (2016).
- **scater**: Offers tools for quality control, visualization, and exploratory data analysis. See McCarthy et al. (2017).

Single-cell data has unique characteristics (sparsity, high dimensionality, technical noise) that require specialized tools. These packages form the backbone of the Bioconductor single-cell analysis ecosystem and provide methods that account for the specific challenges of single-cell data.

29.2.2. Exploring Available Datasets

We are going to use the `scRNAseq` package to access a curated collection of single-cell datasets. This package provides a convenient way to load and explore publicly available datasets that have been processed and annotated.

```
datasets <- scRNAseq::surveyDatasets()
```

The `surveyDatasets()` function queries the `scRNAseq` package database to show all available datasets. This creates a simple table of publicly available single-cell datasets that have been processed and made easily accessible.

Having access to well-curated datasets is useful for learning and benchmarking. These datasets come from published studies and represent different tissues, conditions, and experimental designs, allowing us to practice on real biological data without having to process raw sequencing files.

```
DataFrame with 10 rows and 15 columns
      name      version       path          object
      <character> <character> <character> <character>
1 aztekin-tail-2019 2023-12-14      NA single_cell_experiment
2 splicing-demonstrati.. 2023-12-20      NA single_cell_experiment
3 marques-brain-2016 2023-12-19      NA single_cell_experiment
4 grun-bone_marrow-2016 2023-12-14      NA single_cell_experiment
5 giladi-hsc-2018 2023-12-21      crispr single_cell_experiment
6 giladi-hsc-2018 2023-12-21      rna single_cell_experiment
7 macosko-retina-2015 2023-12-19      NA single_cell_experiment
8 messmer-esc-2019 2023-12-19      NA single_cell_experiment
9 ernst-spermatogenesi.. 2023-12-21    cellranger single_cell_experiment
10 ernst-spermatogenesi.. 2023-12-21 emptydrops single_cell_experiment
```

29. Single Cell RNA-seq Analysis

```

      title          description taxonomy_id   genome    rows
      <character>      <character>     <List>    <List> <integer>
1 Identification of a .. Identification of a ..        8355 Xenla9.1    31535
2 [reprocessed, subset.. [reprocessed, subset..       10090 GRCm38    54448
3 Oligodendrocyte hete.. Oligodendrocyte hete..     10090 GRCm38    23556
4 De Novo Prediction o.. De Novo Prediction o..     10090 GRCm38    23536
5 Single-cell characte.. Single-cell characte..     10090 MGSCv37     30
6 Single-cell characte.. Single-cell characte..     10090 MGSCv37    27389
7 Highly Parallel Geno.. Highly Parallel Geno..     10090 GRCm38    24658
8 Transcriptional Hete.. Transcriptional Hete..     9606 GRCh38    58302
9 Staged developmental.. Staged developmental..    10090 GRCm38    33226
10 Staged developmental.. Staged developmental..    10090 GRCm38   32105

      columns          assays           column_annotations
      <integer>      <List>           <List>
1      13199          counts sample,DevelopmentalStage,DaysPostAmputation, ...
2      2325 spliced,unspliced                         celltype
3      5069          counts source_name,age,inferred cell type, ...
4      1915          counts sample,protocol
5      24070         counts amplification.batch
6      81408         counts Amp_batch_ID,Seq_batch_ID,tier, ...
7      49300         counts cluster
8      1344          counts Source Name,phenotype,single cell quality, ...
9      53510          counts Sample,Barcode,Library, ...
10     68937         counts Sample,Barcode,Library, ...

      reduced_dimensions alternative_experiments
      <List>          <List>
1      UMAP
2
3
4
5
6
7
8      ERCC
9
10

      sources
      <SplitDataFrameList>
1      ArrayExpress:E-MTAB-7716:NA,PubMed:31097661:NA
2      GEO:GSE109033:NA,GEO:GSM2928341:NA,SRA:SRR6459157:NA
3      GEO:GSE75330:NA,PubMed:27284195:NA

```

29. Single Cell RNA-seq Analysis

```
4           GEO:GSE76983:NA,PubMed:27345837:NA
5           PubMed:29915358:NA,GEO:GSE11349:NA
6           PubMed:29915358:NA,GEO:GSE92575:NA
7 GEO:GSE63472:NA,PubMed:26000488:NA,URL:http://mccarrolllab...:2024-02-23
8           PubMed:30673604:NA,ArrayExpress:E-MTAB-6819:NA
9           ArrayExpress:E-MTAB-6946:NA,PubMed:30890697:NA
10          ArrayExpress:E-MTAB-6946:NA,PubMed:30890697:NA
```

Each row represents a different study. The ‘columns’ field shows the number of cells, while ‘rows’ shows the number of genes. This helps you choose datasets appropriate for your computational resources and analysis goals. This little lightweight database is not the richest way to explore datasets, but it is a good starting point. In this tutorial, we will use the `ZeiselBrainData` dataset, which contains single-cell RNA-seq data from mouse brain tissue (Zeisel et al. (2015)).

Abstract: Zeisel Brain Dataset

The mammalian cerebral cortex supports cognitive functions such as sensorimotor integration, memory, and social behaviors. Normal brain function relies on a diverse set of differentiated cell types, including neurons, glia, and vasculature. Here, we have used large-scale single-cell RNA sequencing (RNA-seq) to classify cells in the mouse somatosensory cortex and hippocampal CA1 region. We found 47 molecularly distinct subclasses, comprising all known major cell types in the cortex. We identified numerous marker genes, which allowed alignment with known cell types, morphology, and location. We found a layer I interneuron expressing Pax6 and a distinct postmitotic oligodendrocyte subclass marked by Itpr2. Across the diversity of cortical cell types, transcription factors formed a complex, layered regulatory code, suggesting a mechanism for the maintenance of adult cell type identity.

```
sce <- scRNAseq::ZeiselBrainData()
```

What is the `sce` object? It is a `SingleCellExperiment` object, which is a data structure specifically designed for single-cell RNA-seq data. As with other Bioconductor data structures, it is built on top of the `SummarizedExperiment` class, which allows us to store not only the count matrix but also metadata about cells and features (genes).

Printing the `sce` object gives us a summary of the dataset:

```
sce
```

29. Single Cell RNA-seq Analysis

```
class: SingleCellExperiment
dim: 20006 3005
metadata(0):
assays(1): counts
rownames(20006): Tspan12 Tshz1 ... mt-Rnr1 mt-Nd4l
rowData names(1): featureType
colnames(3005): 1772071015_C02 1772071017_G12 ... 1772066098_A12
  1772058148_F03
colData names(9): tissue group # ... level1class level2class
reducedDimNames(0):
mainExpName: gene
altExpNames(2): repeat ERCC
```

The `SingleCellExperiment` object contains:

- **Assays:** The main data matrix (counts) and any additional matrices (e.g., normalized counts).
- **Row metadata:** Information about genes (e.g., gene names, IDs).
- **Column metadata:** Information about cells (e.g., cell barcodes, tissue type, experimental conditions).

It **can** also contain additional information such as dimensionality reductions (e.g., PCA, t-SNE), clustering results, and quality control metrics.

In fact, we are going to add some of these additional information in the next steps. First, we add a new assay with the log-normalized counts, which is a common preprocessing step in single-cell RNA-seq analysis.

```
sce <- logNormCounts(sce)
```

The `logNormCounts()` function performs log-normalization of the count data. Raw count data from scRNA-seq experiments contains technical variation due to differences in sequencing depth between cells. Some cells might have been sequenced more deeply than others, leading to higher total counts that don't reflect true biological differences. Log-normalization addresses this by:

1. **Size factor normalization:** Scaling each cell's counts by a size factor that accounts for differences in sequencing dept. There are several methods to calculate size factors, but the most common is the median of ratios method, which divides each cell's counts by the median count for each gene across all cells. This helps to adjust for differences in library size.

29. Single Cell RNA-seq Analysis

2. **Log transformation:** Taking $\log(\text{count} + 1)$ to stabilize variance and make the data more normally distributed

For each gene g in cell i , the log-normalized expression becomes:

$$\log_2(\text{count}_{g_i} \times \text{sizefactor}_i + 1)$$

This log transformation is useful because the next steps in the downstream analyses (like clustering and dimensionality reduction) assume that the data is approximately normally distributed (or at least bell-shaped). Log-normalization helps achieve this by reducing the impact of outliers and making the data more suitable for PCA and visualization.

29.3. Dimensionality reduction

Single-cell datasets are extremely high-dimensional - typically containing 15,000-30,000 genes per cell. This creates several challenges: computational complexity, noise dominance, and visualization difficulties. Dimensionality reduction techniques help us identify the most informative patterns in the data while reducing noise and computational burden.

29.3.1. Feature Selection: Identifying Highly Variable Genes

Before applying dimensionality reduction, we need to identify the most informative genes. Highly variable genes (HVGs) are those that show significant variation across cells, indicating they may be biologically relevant. These genes are often more informative for downstream analyses like clustering and visualization.

Not all genes are equally informative for distinguishing cell types. Genes that show little variation across cells (like housekeeping genes) don't help us identify distinct cell populations. Highly variable genes are more likely to:

- Reflect biological differences between cell types
- Capture developmental or activation states
- Represent responses to environmental conditions

```
library(scran)
top_var_genes <- getTopHVGs(sce, n=2000)
```

29. Single Cell RNA-seq Analysis

The `getTopHVGs()` function identifies the top 2000 highly variable genes based on their variance across cells. Choosing a subset of highly variable genes reduces the dimensionality of the dataset while retaining the most informative features for downstream analyses.

The algorithm models the relationship between gene expression mean and variance, then identifies genes that show more variation than expected based on their expression level. This accounts for the fact that highly expressed genes naturally show more variance.

```
# Visualizing the highly variable genes
library(scran)
dec <- modelGeneVar(sce)

# Visualizing the fit:
fit.mv <- metadata(dec)
plot(fit.mv$mean, fit.mv$var, xlab="Mean of log-expression",
      ylab="Variance of log-expression", ylim=c(0, 4))
curve(fit.mv$trend(x), col="dodgerblue", add=TRUE, lwd=2)
points(
  fit.mv$mean[top_var_genes], fit.mv$var[top_var_genes],
  col="red", pch=16, cex=0.5
)
```

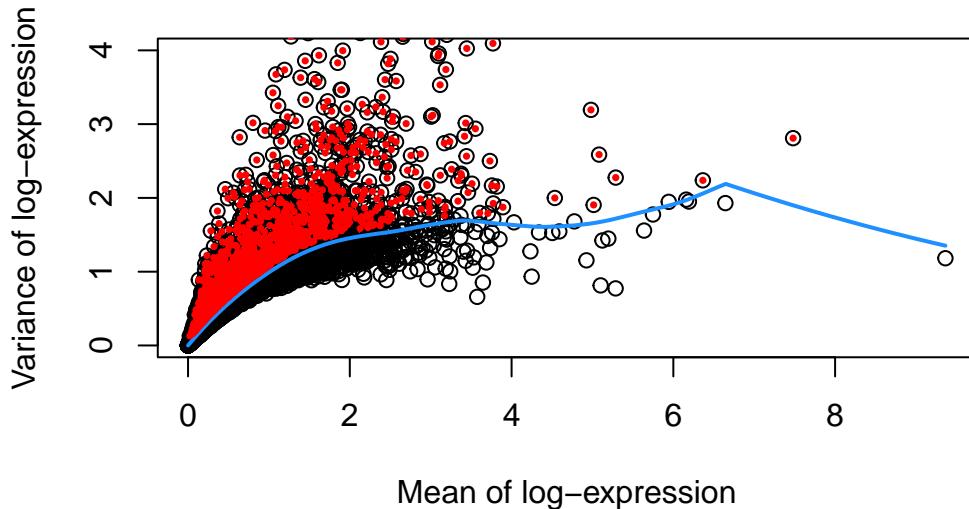


Figure 29.1.: A plot of the mean vs variance of log-expression for all the genes in the dataset, with the highly variable genes highlighted in red. Here, the x-axis represents the mean log-expression of each gene, and the y-axis represents the variance of log-expression. The blue curve represents the trend of variance as a function of mean expression, while the red points represent the highly variable genes.

Figure 29.1 shows the mean vs. variance of log-expression for all genes in the dataset, with highly variable genes highlighted in red. The blue curve represents the trend of variance as a function of mean expression, while the red points represent the highly variable genes.

We next proceed to calculating PCA using the subset of highly variable genes. PCA is a linear dimensionality reduction technique that finds the directions of maximum variance in the data. It's computationally efficient and provides a good foundation for further analysis. The first few principal components capture the most important patterns of variation in the dataset.

💡 Why PCA first?

PCA is a widely *linear* dimensionality reduction technique that:

- Reduces dimensionality while preserving variance
- Helps visualize high-dimensional data in 2D or 3D
- Serves as a preprocessing step for other methods like t-SNE or UMAP
- Is computationally efficient and easy to interpret

29. Single Cell RNA-seq Analysis

```
# Perform PCA on the highly variable genes
set.seed(100) # See below.
sce <- fixedPCA(sce, subset.row=top_var_genes)

reducedDimNames(sce)
```

[1] "PCA"

Note that we assign the output of `fixedPCA()` to the `sce` object. This function performs PCA on the highly variable genes we identified earlier, reducing the dimensionality of the dataset while retaining the most informative features. Because dimensionality reduction is a common step in single-cell RNA-seq analysis, we can store the PCA results in the `reducedDims` slot of the `SingleCellExperiment` object. This allows us to easily access and visualize the PCA coordinates later.

29.3.2. Non-linear Dimensionality Reduction with t-SNE

After PCA, we can apply non-linear dimensionality reduction techniques like t-SNE (t-distributed Stochastic Neighbor Embedding) to visualize the data in 2D or 3D. t-SNE is particularly useful for revealing local structure and separating distinct cell populations.

29.4. Why t-SNE after PCA

This is a two-step approach: 1. **PCA first:** Reduces noise and computational burden while preserving global structure 2. **t-SNE second:** Reveals local neighborhood structure and separates distinct cell populations

```
library(scater)
sce <- runTSNE(sce, dimred="PCA")
```

The `runTSNE()` function applies t-SNE to the PCA results, creating a 2D representation of the data. The `dimred="PCA"` argument specifies that we want to use the PCA coordinates as input for t-SNE.

```
nn.clusters <- clusterCells(sce, use.dimred = "TSNE")
table(nn.clusters)
```

29. Single Cell RNA-seq Analysis

```
nn.clusters
  1   2   3   4   5   6   7   8   9   10  11  12  13  14  15  16  17  18  19  20
152 126 190 286 131 191  63  87 113 328  88  97 155  45 138  40  71  42  61  92
  21  22  23  24  25  26  27  28  29  30  31  32  33  34  35  36
  54  64  35  62  58  32  27  32  20  16  12  20  28  15  18  16
```

The `clusterCells()` function uses graph-based clustering to identify groups of similar cells. Graph-based clustering was [popularized by the Seurat package](#). It builds a nearest-neighbor graph and then finds communities within this graph. The resulting clusters often correspond to distinct cell types or states. The `use.dimred = "TSNE"` argument specifies that we want to use the t-SNE coordinates for clustering. This is an important choice because t-SNE captures local structure and can reveal distinct cell populations that may not be apparent in the original high-dimensional space. There are other clustering methods available, such as k-means or hierarchical clustering, but graph-based clustering is particularly effective for single-cell data due to its ability to handle complex, non-linear relationships.

29.4.1. Visualizing Cell Types and Clusters

In this particular dataset, we have pre-defined cell type annotations that we can use to color the t-SNE plot. The `level1class` and `level2class` columns in the metadata contain these annotations. We can use these annotations to color the t-SNE plot and visualize how well the clustering aligns with known cell types.

We can cluster the cells based on their t-SNE coordinates and visualize the results. The `plotReducedDim()` function from the `scater` package allows us to create a scatter plot of the t-SNE coordinates, coloring the points by their cluster assignments or cell type annotations.

```
library(scater)
colLabels(sce) <- nn.clusters
plotReducedDim(sce, "TSNE", colour_by="level1class")
```

29. Single Cell RNA-seq Analysis

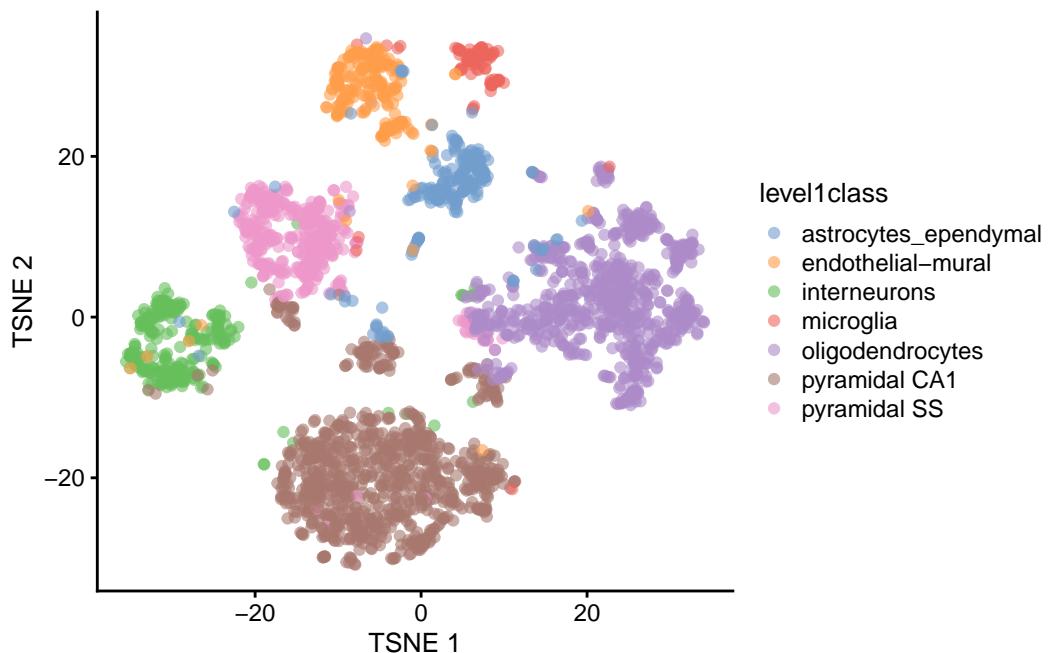


Figure 29.2.

We can also visualize the second level of cell type annotations.

```
plotReducedDim(sce, "TSNE", colour_by="level2class")
```

29. Single Cell RNA-seq Analysis

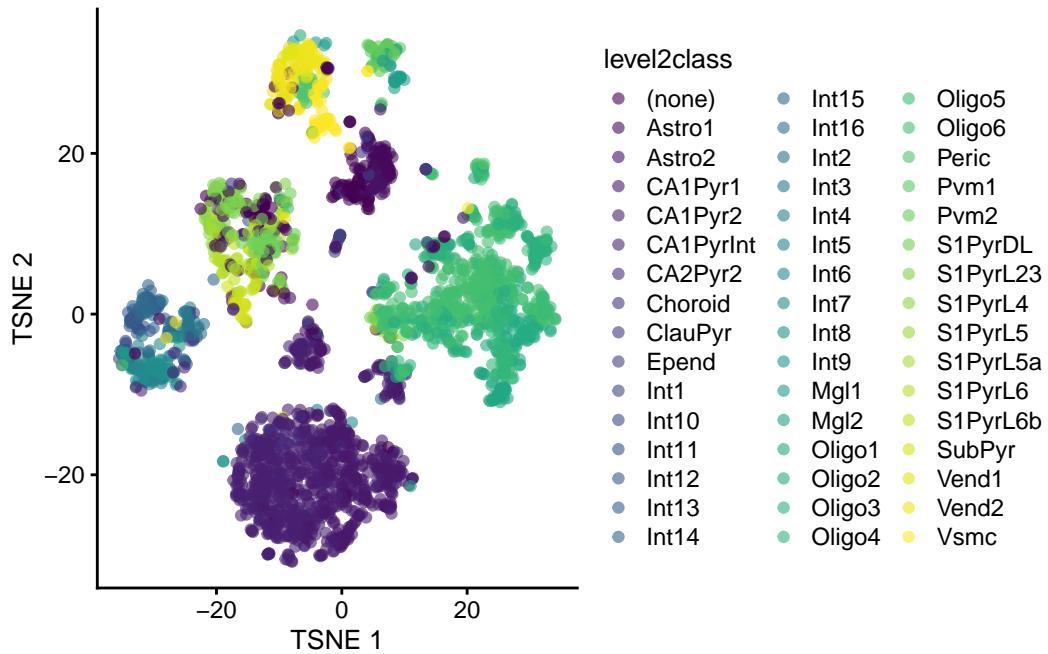


Figure 29.3.

And add additional metadata such as tissue type to the plot. The `shape_by` argument allows us to differentiate points by another categorical variable, such as tissue type.

```
plotReducedDim(sce, "TSNE", colour_by="level1class", shape_by="tissue", )
```

29. Single Cell RNA-seq Analysis

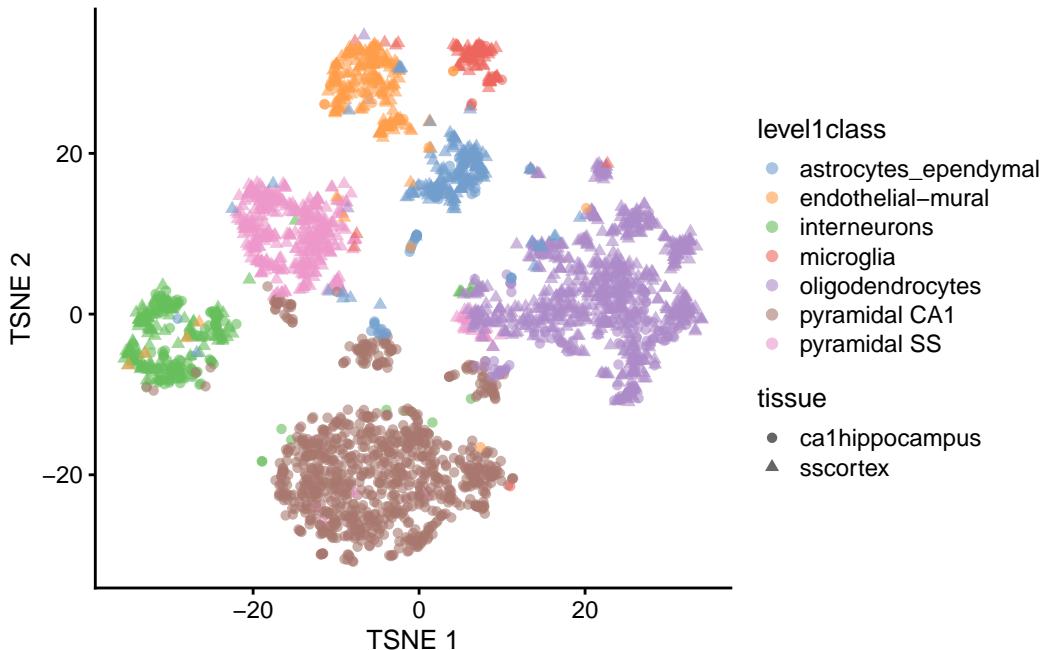


Figure 29.4.

29.5. Finding Marker Genes

Marker genes are genes that are differentially expressed in a specific cell type or cluster compared to others. Identifying marker genes helps us understand the molecular characteristics of each cell type and can provide insights into their functions.

To find marker genes, we can use the `findMarkers()` function from the `scran` package. This function performs pairwise differential expression analysis between clusters or cell types. We can specify the clusters we want to compare and the method for calculating differential expression.

```
markers <- findMarkers(sce,
  groups=as.numeric(as.factor(colData(sce)$level1class)), pval.type="all",
  direction="up", subset.row=top_var_genes, test="t")
```

The `findMarkers()` function identifies genes that are significantly upregulated in each cluster compared to all other clusters. The `pval.type="all"` argument specifies that we want to calculate p-values for all comparisons, and the `direction="up"` argument indicates that we are interested in genes that are upregulated in the specified clusters.

29. Single Cell RNA-seq Analysis

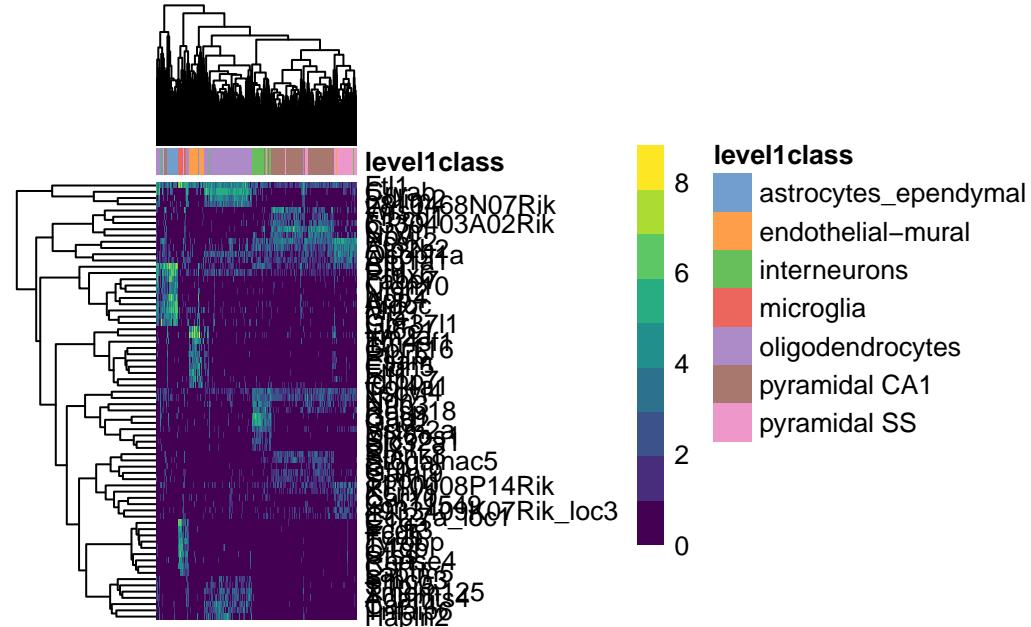
The `subset.row=top_var_genes` argument restricts the analysis to the highly variable genes we identified earlier, which are more likely to be informative for distinguishing cell types.

The resulting `markers` object is a list where each element corresponds to a cluster and contains the differential expression results for that cluster. We can visualize the top marker genes for each cluster using a heatmap.

Take my word for it that we can visualize the top marker genes for each cluster using a heatmap. This allows us to see which genes are most strongly associated with each cluster and how they differ across clusters.

```
# visualize the top marker gene for cluster 1 in a violin plot()
library(scater)
top_marker_genes_for_all_clusters = lapply(markers, function(x) {
  return(head(rownames(x), 10))
})
plotHeatmap(sce, features=unique(unlist(top_marker_genes_for_all_clusters)),
            cluster_rows=TRUE, cluster_cols=TRUE, show_colnames=FALSE,
            main="Top marker genes for cluster 1",
            color_columns_by="level1class")
```

Top marker genes for cluster 1



29.6. Bonus: Working with 10x Genomics Data

In the previous sections, we used a curated dataset from the `scRNAseq` package. However, many real-world single-cell RNA-seq datasets come from 10x Genomics platforms, which produce data in specific formats. In this section, we'll cover a hypothetical workflow for loading and processing raw 10x Genomics data using R.

29.6.1. Understanding 10x Genomics Output Formats

10x Genomics Cell Ranger produces several output formats:

1. **Matrix Market format** (.mtx files): Sparse matrix format with separate files for the matrix, gene names, and cell barcodes
2. **HDF5 format** (.h5 files): A single compressed file containing all the data
3. **Filtered vs. unfiltered**: Cell Ranger provides both versions - filtered contains only cells that pass basic quality filters

29.6.2. Loading 10x Data from Matrix Market Files

```
# Loading from standard 10x output directory
# This assumes you have a directory with:
# - matrix.mtx.gz (or matrix mtx)
# - features.tsv.gz (or genes.tsv.gz for older versions)
# - barcodes.tsv.gz

library(DropletUtils)
library(SingleCellExperiment)

# Method 1: Using DropletUtils (recommended)
sce_10x <- read10xCounts("path/to/10x/output/", col.names = TRUE)

# Method 2: Using Seurat (if you prefer the Seurat ecosystem)
# library(Seurat)
# seurat_obj <- Read10X("path/to/10x/output/")
# sce_10x <- as.SingleCellExperiment(CreateSeuratObject(seurat_obj))
```

What we're doing: The `read10xCounts()` function from `DropletUtils` reads the three files that comprise 10x output and creates a `SingleCellExperiment` object. The `col.names = TRUE` parameter ensures that cell barcodes are used as column names.

Why DropletUtils: This package is specifically designed for handling droplet-based single-cell data (like 10x Genomics). It includes specialized functions for:

- Reading 10x formats efficiently
- Distinguishing empty droplets from cells
- Handling ambient RNA contamination
- Quality control specific to droplet-based methods

29.6.3. Loading from HDF5 Files

```
# For HDF5 format files
library(rhdf5)

# Method 1: Using DropletUtils
sce_h5 <- read10xCounts("path/to/sample.h5", type = "HDF5")

# Method 2: Direct HDF5 reading (more control)
h5_file <- "path/to/sample.h5"
gene_info <- h5read(h5_file, "matrix/features")
barcodes <- h5read(h5_file, "matrix/barcodes")
matrix_data <- h5read(h5_file, "matrix/data")
# Additional processing needed to reconstruct sparse matrix
```

What we're doing: HDF5 files are more convenient as they contain all information in a single file. The `type = "HDF5"` parameter tells the function to expect this format instead of separate matrix files.

When to use H5 files:

- **Convenience:** Single file is easier to manage and transfer
- **Speed:** Often faster to read than multiple compressed files
- **Storage:** More efficient storage, especially for large datasets

29.6.4. Essential Quality Control After Loading Raw Data

```
# Add mitochondrial gene information
library(scuttle)
is.mito <- grep("MT-", rownames(sce_10x)) # Human mitochondrial genes
# For mouse data, use: is.mito <- grep("mt-", rownames(sce_10x))

# Calculate per-cell QC metrics
sce_10x <- addPerCellQC(sce_10x, subsets = list(Mito = is.mito))

# Calculate per-gene QC metrics
sce_10x <- addPerFeatureQC(sce_10x)

# View the QC metrics
colnames(colData(sce_10x))
```

What we're doing: We're calculating quality control metrics that are essential for raw 10x data:

- **Mitochondrial genes:** High mitochondrial gene expression often indicates dying cells
- **Per-cell metrics:** Total counts, number of detected genes, mitochondrial percentage
- **Per-gene metrics:** How many cells express each gene

Why QC is crucial for raw data: Unlike curated datasets, raw 10x data contains:

- **Empty droplets:** Droplets that captured ambient RNA but no cells
- **Dying cells:** Cells with compromised membranes
- **Doublets:** Droplets containing multiple cells
- **Low-quality cells:** Cells with very few detected genes

29.6.5. Filtering Low-Quality Cells and Genes

```
# Visualize QC metrics
library(scater)
plotColData(sce_10x, x = "sum", y = "detected", colour_by = "subsets_Mito_percent")

# Set filtering thresholds (these are examples - adjust based on your data)
```

29. Single Cell RNA-seq Analysis

```
# Filter cells
high_mito <- sce_10x$subsets_Mito_percent > 20 # Remove cells with >20% mitochondrial reads
low_lib_size <- sce_10x$sum < 1000 # Remove cells with <1000 total counts
low_n_features <- sce_10x$detected < 500 # Remove cells with <500 detected genes

# Filter genes (remove genes expressed in very few cells)
low_expression <- rowSums(counts(sce_10x) > 0) < 10 # Expressed in <10 cells

# Apply filters
sce_filtered <- sce_10x[!low_expression, !(high_mito | low_lib_size | low_n_features)]

# Check how many cells and genes remain
dim(sce_10x) # Before filtering
dim(sce_filtered) # After filtering
```

What we're doing: We're applying filters to remove low-quality cells and rarely expressed genes. The specific thresholds should be adjusted based on your dataset characteristics.

Understanding the filters:

- **Mitochondrial percentage:** Cells with high mitochondrial gene expression are likely dying
- **Library size:** Total number of UMIs per cell - very low values suggest poor capture
- **Number of features:** How many different genes are detected - very low values suggest poor quality
- **Gene expression frequency:** Genes expressed in very few cells are often noise

Critical considerations:

- **Thresholds are dataset-dependent:** What works for one experiment may not work for another
- **Biological vs. technical variation:** Some cell types naturally have different RNA content
- **Visualization first:** Always plot your QC metrics before setting thresholds

29.7. Further Reading and Resources

For more in-depth information on single-cell RNA-seq analysis, consider the following resources:

29. Single Cell RNA-seq Analysis

- The [Orchestrating Single-Cell RNA-seq Analysis](#) book provides a comprehensive guide to single-cell RNA-seq analysis using Bioconductor.
- The [Seurat](#) package documentation offers extensive tutorials and vignettes for single-cell analysis in the Seurat ecosystem.

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A. Appendix

A.1. Data Sets

- [BRFSS subset](#)
- [ALL clinical data](#)
- [ALL expression data](#)

A.2. Swirl

The following is from the [swirl website](#).

The swirl R package makes it fun and easy to learn R programming and data science. If you are new to R, have no fear.

To get started, we need to install a new package into R.

```
install.packages('swirl')
```

Once installed, we want to load it into the R workspace so we can use it.

```
library('swirl')
```

Finally, to get going, start swirl and follow the instructions.

```
swirl()
```

B. Git and GitHub

Git is a version control system that allows you to track changes in your code and collaborate with others. GitHub is a web-based platform that hosts Git repositories, making it easy to share and collaborate on projects. GitHub is NOT the only place to host Git repositories, but it is the most popular and has a large community of users.

You can use git by itself locally for version control. However, if you want to collaborate with others, you will need to use a remote repository, such as GitHub. This allows you to share your code with others, track changes, and collaborate on projects.

 Note

It can be confusing to understand the difference between Git and GitHub. In short, Git is the version control system that tracks changes in your code, while GitHub is a platform that hosts your Git repositories and provides additional features for collaboration.

B.1. install Git and GitHub CLI

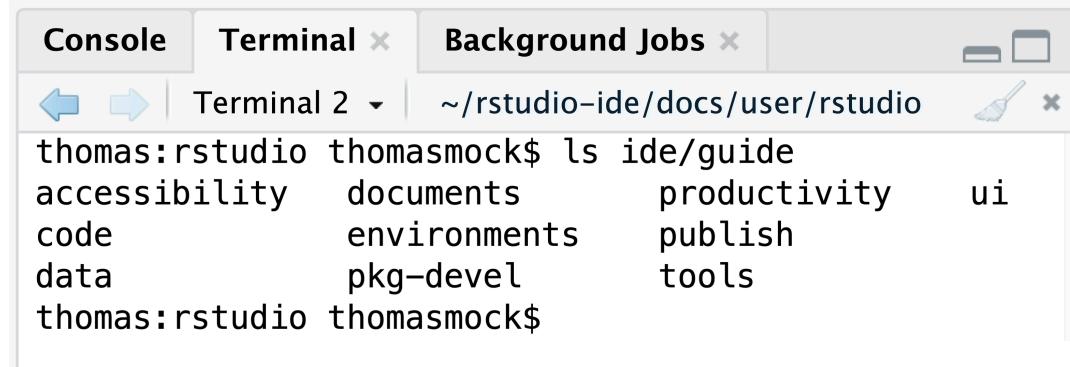
To use Git and GitHub, you need to have Git installed on your computer. You can download it from git-scm.com. After installation, you can check if Git is installed correctly by running the following command in your terminal:

```
git --version
```

We also need the gh command line tool to interact with GitHub. You can install it from cli.github.com. To install, go to [the releases page](#) and download the appropriate version for your operating system. For the Mac, it is the file named something like “Macos Universal” and the file will have a .pkg extension. You can install it by double-clicking the file after downloading it.

i Using the RStudio Terminal

If you are using RStudio, you can use the built-in terminal to run Git commands. To open the terminal, go to the “Terminal” tab in the bottom pane of RStudio. This allows you to run Git commands directly from RStudio without needing to switch to a separate terminal application.



The screenshot shows the RStudio interface with the “Terminal” tab selected. The terminal window displays the command `ls ide/guide` and its output, which lists several subdirectories: accessibility, documents, environments, pkg-devel, productivity, publish, and tools. The terminal prompt is `thomas:rstudio thomasmock$`.

```
Console Terminal x Background Jobs x
Terminal 2 ~ /rstudio-ide/docs/user/rstudio
thomas:rstudio thomasmock$ ls ide/guide
accessibility documents productivity ui
code environments publish
data pkg-devel tools
thomas:rstudio thomasmock$
```

For more details, see the [RStudio terminal documentation](#).

B.2. Configure Git

After installing Git, you need to configure it with your name and email address. This information will be used to identify you as the author of the commits you make. Run the following commands in your terminal, replacing “Your Name” and “you@example.com” with your actual name and email address:

```
git config --global user.name "Your Name"
git config --global user.email "you@example.com"
```

B.3. Create a GitHub account

If you don’t already have a GitHub account, you can create one for free at [github.com](#).

B.4. Login to GitHub CLI

After installing the GitHub CLI, you need to log in to your GitHub account. Run the following command in your terminal:

```
gh auth login
```

B.5. Introduction to Version Control with Git

Welcome to the world of version control! Think of Git as a “save” button for your entire project, but with the ability to go back to previous saves, see exactly what you changed, and even work on different versions of your project at the same time. It’s an essential tool for reproducible and collaborative research.

In this tutorial, we’ll learn the absolute basics of Git using the command line directly within RStudio.

B.5.1. Key Git Commands We’ll Learn Today:

- **git init:** Initializes a new Git repository in your project folder. This is the first step to start tracking your files.
 - **git add:** Tells Git which files you want to track changes for. You can think of this as putting your changes into a “staging area.”
 - **git commit:** Takes a snapshot of your staged changes. This is like creating a permanent save point with a descriptive message.
 - **git restore:** Discards changes in your working directory. It’s a way to undo modifications you haven’t committed yet.
 - **git branch:** Allows you to create separate timelines of your project. This is useful for developing new features without affecting your main work.
 - **git merge:** Combines the changes from one branch into another.
-

B.6. The Toy Example: An R Script

First, let's create a simple R script that we can use for our Git exercise. In RStudio, create a new R Script and save it as `data_analysis.R`.

```
# data_analysis.R

# Load necessary libraries
library(ggplot2)
library(dplyr)

# Create some sample data
data <- data.frame(
  x = 1:10,
  y = (1:10) ^ 2
)

# Initial data summary
summary(data)
```

B.7. Let's Get Started with Git!

Open the **Terminal** in RStudio (you can usually find it as a tab next to the Console). We'll be typing all our Git commands here.

B.7.1. Step 1: Initialize Your Git Repository

First, we need to tell Git to start tracking our project folder.

```
git init
```

You'll see a message like `Initialized empty Git repository in....`. You might also notice a new `.git` folder in your project directory (it might be hidden). This is where Git stores all its tracking information. Your default branch is automatically named `main`.

B. Git and GitHub

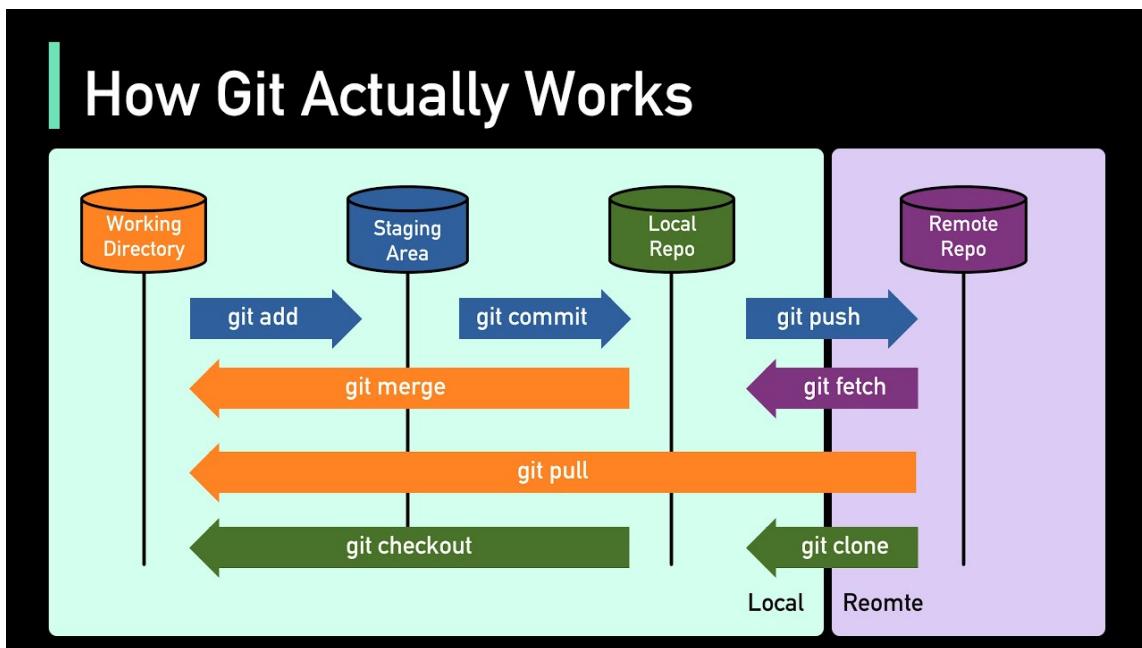


Figure B.1.: This is an overview of how git works along with the commands that make it tick. See [this video](#)

B.7.2. Step 2: Your First Commit

Now, let's add our `data_analysis.R` script to Git's tracking and make our first "commit."

1. Add the file to the staging area:

```
git add data_analysis.R
```

2. Commit the staged file with a message:

```
git commit -m "Initial commit: Add basic data script"
```

The `-m` flag lets you write your commit message directly in the command. Good commit messages are short but descriptive!

B.7.3. Step 3: Making and Undoing a Change

Let's modify our R script. Add a plotting section to the end of `data_analysis.R`.

```
# ... (keep the previous code)

# Create a plot
ggplot(data, aes(x = x, y = y)) +
  geom_point() +
  ggtitle("A Simple Scatter Plot")
```

Now, what if we decided we didn't want this change after all? We can use `git restore` to go back to our last committed version.

```
git restore data_analysis.R
```

If you look at your `data_analysis.R` file now, the plotting code will be gone!

B.7.4. Step 4: Branching Out

Branches are a powerful feature. Let's create a new branch to add our plot without messing up our `main` branch.

1. Create a new branch and switch to it:

B. Git and GitHub

```
git checkout -b add-plot
```

This is a shortcut for git branch add-plot and git checkout add-plot.

Now, re-add the plotting code to `data_analysis.R`.

```
# ... (keep the previous code)

# Create a plot
ggplot(data, aes(x = x, y = y)) +
  geom_point() +
  ggtitle("A Simple Scatter Plot")
```

Let's commit this change on our new `add-plot` branch.

```
git add data_analysis.R
git commit -m "feat: Add scatter plot"
```

B.7.5. Step 5: Seeing Branches in Action

Now for the magic of branches. Let's switch back to our `main` branch.

```
git checkout main
```

Now, open your `data_analysis.R` script in the RStudio editor. **The plotting code is gone!** That's because the change only exists on the `add-plot` branch. The `main` branch is exactly as we last left it.

Let's switch back to our feature branch.

```
git checkout add-plot
```

Check the `data_analysis.R` script again. **The plotting code is back!** This demonstrates how branches allow you to work on different versions of your project in isolation.

B.7.6. Step 6: Merging Your Work

Our plot is complete and we're happy with it. It's time to merge it back into our `main` branch to incorporate the new feature.

1. Switch back to the `main` branch, which is our target for the merge:

```
git checkout main
```

2. Merge the `add-plot` branch into `main`:

```
git merge add-plot
```

You'll see a message indicating that the merge happened. Now, your `main` branch has the updated `data_analysis.R` script with the plotting code!

C. Additional resources

- Base R Cheat Sheet
- Modern Data Visualization with R

C.1. AI

- chatGPT
- Gemini
- Claude
- DeepSeek
- Perplexity

D. Data Visualization with `ggplot2`

Start with this worked example to get a feel for the `ggplot2` package.

- <https://rkabacoff.github.io/datavis/IntroGGPLOT.html>

Then, for more detail, I refer you to this excellent `ggplot2` tutorial.

Finally, for more R graphics inspiration, see the [R Graph Gallery](#).

E. Matrix Exercises

E.1. Data preparation

For this set of exercises, we are going to rely on a dataset that comes with R. It gives the number of sunspots per month from 1749-1983. The dataset comes as a `ts` or time series data type which I convert to a matrix using the following code.

Just run the code as is and focus on the rest of the exercises.

```
data(sunspots)
sunspot_mat <- matrix(as.vector(sunspots), ncol=12, byrow = TRUE)
colnames(sunspot_mat) <- as.character(1:12)
rownames(sunspot_mat) <- as.character(1749:1983)
```

E.2. Exercises

- After the conversion above, what does `sunspot_mat` look like? Use functions to find the number of rows, the number of columns, the class, and some basic summary statistics.

```
ncol(sunspot_mat)
nrow(sunspot_mat)
dim(sunspot_mat)
summary(sunspot_mat)
head(sunspot_mat)
tail(sunspot_mat)
```

- Practice subsetting the matrix a bit by selecting:
 - The first 10 years (rows)
 - The month of July (7th column)
 - The value for July, 1979 using the rowname to do the selection.

E. Matrix Exercises

```
sunspot_mat[1:10,]  
sunspot_mat[,7]  
sunspot_mat['1979',7]
```

These next few exercises take advantage of the fact that calling a univariate statistical function (one that expects a vector) works for matrices by just making a vector of all the values in the matrix.

- What is the highest (max) number of sunspots recorded in these data?

```
max(sunspot_mat)
```

- And the minimum?

```
min(sunspot_mat)
```

- And the overall mean and median?

```
mean(sunspot_mat)  
median(sunspot_mat)
```

- Use the `hist()` function to look at the distribution of all the monthly sunspot data.

```
hist(sunspot_mat)
```

- Read about the `breaks` argument to `hist()` to try to increase the number of breaks in the histogram to increase the resolution slightly. Adjust your `hist()` and `breaks` to your liking.

```
hist(sunspot_mat, breaks=40)
```

Now, let's move on to summarizing the data a bit to learn about the pattern of sunspots varies by month or by year.

- Examine the dataset again. What do the columns represent? And the rows?

```
# just a quick glimpse of the data will give us a sense  
head(sunspot_mat)
```

- We'd like to look at the distribution of sunspots by month. How can we do that?

E. Matrix Exercises

```
# the mean of the columns is the mean number of sunspots per month.  
colMeans(sunspot_mat)  
  
# Another way to write the same thing:  
apply(sunspot_mat, 2, mean)
```

- Assign the month summary above to a variable and summarize it to get a sense of the spread over months.

```
monthmeans = colMeans(sunspot_mat)  
summary(monthmeans)
```

- Play the same game for years to get the per-year mean?

```
ymeans = rowMeans(sunspot_mat)  
summary(ymean)
```

- Make a plot of the yearly means. Do you see a pattern?

```
plot(ymean)  
# or make it clearer  
plot(ymean, type='l')
```

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