

# High-fidelity gates and mid-circuit erasure conversion in an atomic qubit

<https://doi.org/10.1038/s41586-023-06438-1>

Received: 8 May 2023

Accepted: 14 July 2023

Published online: 11 October 2023

 Check for updates

Shuo Ma<sup>1,2,7</sup>, Genyue Liu<sup>17</sup>, Pai Peng<sup>17</sup>, Bichen Zhang<sup>1</sup>, Sven Jandura<sup>3</sup>, Jahan Claes<sup>4,5</sup>, Alex P. Burgers<sup>16</sup>, Guido Pupillo<sup>3</sup>, Shruti Puri<sup>4,5</sup> & Jeff D. Thompson<sup>1</sup>✉

The development of scalable, high-fidelity qubits is a key challenge in quantum information science. Neutral atom qubits have progressed rapidly in recent years, demonstrating programmable processors<sup>1,2</sup> and quantum simulators with scaling to hundreds of atoms<sup>3,4</sup>. Exploring new atomic species, such as alkaline earth atoms<sup>5–7</sup>, or combining multiple species<sup>8</sup> can provide new paths to improving coherence, control and scalability. For example, for eventual application in quantum error correction, it is advantageous to realize qubits with structured error models, such as biased Pauli errors<sup>9</sup> or conversion of errors into detectable erasures<sup>10</sup>. Here we demonstrate a new neutral atom qubit using the nuclear spin of a long-lived metastable state in <sup>171</sup>Yb. The long coherence time and fast excitation to the Rydberg state allow one- and two-qubit gates with fidelities of 0.9990(1) and 0.980(1), respectively. Importantly, a large fraction of all gate errors result in decays out of the qubit subspace to the ground state. By performing fast, mid-circuit detection of these errors, we convert them into erasure errors; during detection, the induced error probability on qubits remaining in the computational space is less than 10<sup>-5</sup>. This work establishes metastable <sup>171</sup>Yb as a promising platform for realizing fault-tolerant quantum computing.

Neutral atoms in optical tweezer arrays are a rapidly developing field for quantum science<sup>11</sup>, including programmable quantum processors<sup>1,2</sup> and many-body simulators<sup>12</sup>. Recent advances include scaling to hundreds of atoms<sup>3,4</sup>, dual-species arrays with mid-circuit measurements and continuous reloading<sup>8,13</sup> and efficient architectures for quantum error correction<sup>10,14</sup>. The development of tweezer arrays using alkaline earth atoms<sup>5–7</sup> has enabled new functionality, such as tweezer-based atomic clocks<sup>15,16</sup> and long-lived nuclear spin qubits<sup>17–19</sup>.

An important feature of alkaline earth atoms is a metastable excited electronic state, which can be used to encode information instead of (or in addition to) the ground state<sup>10,20</sup>. This creates a number of unique possibilities including fast, high-fidelity excitation to the Rydberg state<sup>21</sup> and mid-circuit fluorescence measurements or laser cooling of ground state atoms. The latter feature is important for mid-circuit readout and qubit reloading, playing a role analogous to a second atomic species. Metastable qubits have been proposed for both neutral atoms<sup>10,20</sup> and ions<sup>22,23</sup> and have recently been demonstrated with <sup>171</sup>Yb<sup>+</sup> ions<sup>24,25</sup>.

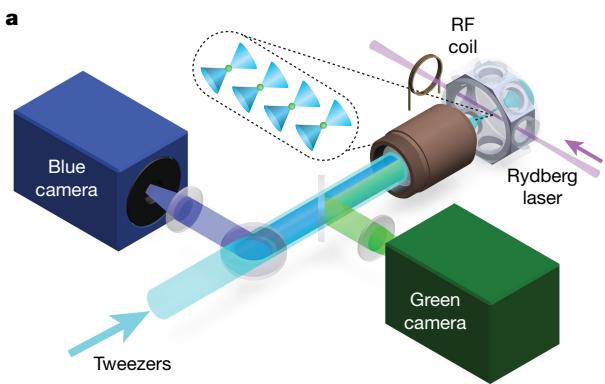
The metastable qubit encoding also enables mid-circuit detection of errors resulting in transitions to the ground state<sup>10,23</sup>. This converts these errors into erasure errors<sup>26,27</sup>, which are easier to correct in the context of fault-tolerant quantum computing<sup>10,28,29</sup>. If a large fraction of all errors are converted into erasures and the information about which qubits were erased can be extracted while preserving the quantum state of qubits that did not have errors, the resource overhead for fault-tolerant computing is substantially reduced. This concept has

stimulated new qubit designs in several platforms<sup>10,30–34</sup>, but has not been experimentally demonstrated.

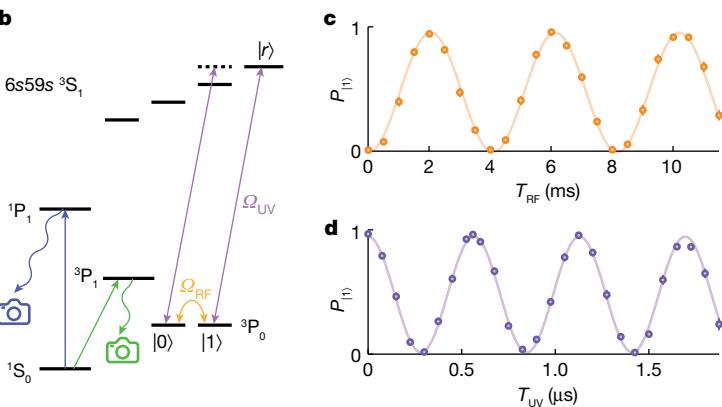
In this work, we demonstrate a qubit encoded in the nuclear spin of the metastable  $6s6p\ ^3P_0$  state in neutral <sup>171</sup>Yb. We demonstrate seconds-scale lifetimes and coherence times, single-qubit gates with  $\mathcal{F} = 0.9990(1)$  and two-qubit gates with  $\mathcal{F} = 0.980(1)$ , where the latter is enabled by a new gate design<sup>35</sup> and fast, single-photon excitation to the Rydberg state. A large fraction of the gate errors result in transitions out of the metastable state, to the atomic ground state. By performing fast (20 μs) imaging of ground state atoms<sup>36</sup>, we are able to detect these leakage errors mid-circuit, converting them into erasure errors, with a probability of less than 10<sup>-5</sup> of inducing an error on qubits remaining in the metastable state during detection. We show that 56% of single-qubit gate errors and 33% of two-qubit gate errors are detected in this manner. We conclude by discussing future opportunities for the metastable <sup>171</sup>Yb qubit, including improvements in the gate fidelity and erasure fraction, and possible extensions to mid-circuit qubit readout.

Our experiment begins by trapping individual <sup>171</sup>Yb atoms in an array of optical tweezers (Fig. 1a)<sup>18,19</sup>. We use optical pumping to initialize the qubit in the state  $|1\rangle = |6s6p\ ^3P_0, F=1/2, m_F=+1/2\rangle$  (Fig. 1b; see Methods and Extended Data Fig. 1 for details). Single-qubit rotations between  $|0\rangle = |6s6p\ ^3P_0, F=1/2, m_F=-1/2\rangle$  and  $|1\rangle$  are driven using a radio frequency (RF) magnetic field tuned to the nuclear spin Larmor frequency  $\omega_L = 2\pi \times 5.70$  kHz ( $|B| = 5.0$  G; Fig. 1c). Spin readout is implemented by removing atoms in  $|1\rangle$  from the trap (via excitation to the Rydberg state and subsequent autoionization<sup>18</sup>), and then

<sup>1</sup>Department of Electrical and Computer Engineering, Princeton University, Princeton, NJ, USA. <sup>2</sup>Department of Physics, Princeton University, Princeton, NJ, USA. <sup>3</sup>University of Strasbourg and CNRS, CESQ and ISIS (UMR 7006), aQCess, Strasbourg, France. <sup>4</sup>Department of Applied Physics, Yale University, New Haven, CT, USA. <sup>5</sup>Yale Quantum Institute, Yale University, New Haven, CT, USA. <sup>6</sup>Present address: Department of Electrical and Computer Engineering, College of Engineering, University of Michigan, Ann Arbor, MI, USA. <sup>7</sup>These authors contributed equally: Shuo Ma, Genyue Liu, Pai Peng. <sup>✉</sup>e-mail: jdthompson@princeton.edu



**Fig. 1 | Metastable  $^{171}\text{Yb}$  qubit.** **a**, Overview of the experimental apparatus, showing an array of optical tweezers inside a glass cell and cameras for acquiring non-destructive images (using the  $^1\text{S}_0 - ^3\text{P}_1$  transition, 556 nm,  $\Gamma = 2\pi \times 182$  kHz) and fast images (using the  $^1\text{S}_0 - ^1\text{P}_1$  transition, 399 nm,  $\Gamma = 2\pi \times 29$  MHz). **b**, Abbreviated  $^{171}\text{Yb}$  level diagram showing the ground state, imaging transitions and the nuclear spin sublevels within the metastable  $^3\text{P}_0$  state that encode the



qubit. Single-qubit gates are generated with an RF magnetic field  $\Omega_{RF}$  and entangling gates are implemented by coupling  $|1\rangle$  to a Rydberg state,  $|r\rangle$ , with an ultraviolet (UV) laser at 302 nm. **c**, Nuclear spin Rabi oscillation between  $|0\rangle$  and  $|1\rangle$ , with a  $\pi$ -pulse time of 2.0 ms. **d**, Rydberg Rabi oscillation between  $|1\rangle$  and  $|r\rangle$ , with a  $\pi$ -pulse time of 330 ns.

depumping the remaining metastable population back to the ground state before imaging. The combined fidelity of the state initialization and imaging is 0.981(9), which is limited by atom loss during the depumping step.

The absence of hyperfine coupling in the  $^3\text{P}_0$  level allows extremely long coherence times for the nuclear spin ( $T_1 = 23(14)$  s,  $T_2^* = 0.92(2)$  s), as demonstrated previously for nuclear spin qubits in the ground state<sup>17–19</sup>. Two-qubit operations are performed by selectively exciting the state  $|1\rangle$  to the Rydberg state  $|6s59s\ ^3\text{S}_1 F=3/2, m_f=3/2\rangle$  using a 302 nm laser (see Extended Data Fig. 2 for details). In contrast to the metastable state, the presence of hyperfine coupling in the Rydberg manifold results in a large Zeeman shift between magnetic sublevels in the Rydberg state, such that two-qubit operations can be performed much faster than  $\omega_L^{-1}$  (Fig. 1d)<sup>18</sup>. The same concept has been used to implement fast single-qubit rotations using a lower-lying excited state<sup>19</sup>.

The fidelity of idling and single-qubit operations is limited primarily by the finite lifetime of the metastable state (Fig. 2a), which is  $\Gamma_m^{-1} = 2.96(12)$  s under typical operating conditions. The decay rate depends strongly on the trap power and can be described as  $\Gamma_m = \Gamma_0 + \alpha P + \beta P^2$  (Fig. 2b). The constant term  $\Gamma_0 = 0.4(2)$  s<sup>-1</sup> includes background loss and radiative decay (0.05 s<sup>-1</sup>). The linear ( $\alpha = 0.20(7)$  s<sup>-1</sup> mW<sup>-1</sup>) and quadratic ( $\beta = 0.053(5)$  s<sup>-1</sup> mW<sup>-2</sup>) terms are attributed to Raman scattering and photoionization, respectively, where the latter is possible because the trapping laser energy ( $\lambda = 486.8$  nm) is above the two-photon ionization limit. However, both radiative decay and Raman scattering return the atom to the ground state (with suitable repumping of the other metastable state,  $^3\text{P}_2$ ), which enables eventual detection, as shown in Fig. 2c.

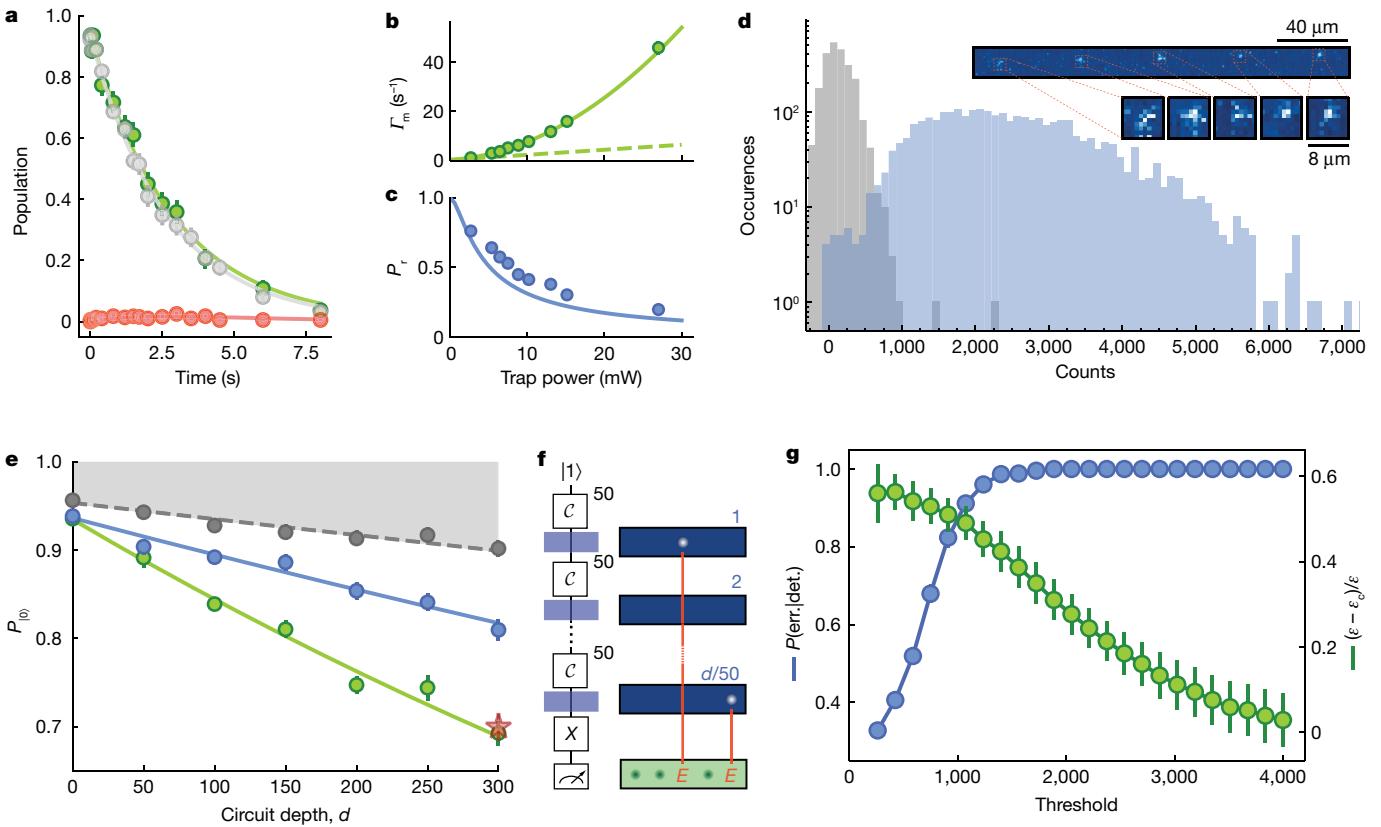
To detect decays to the ground state without disturbing qubits in the metastable state, we use fast fluorescence imaging<sup>36</sup> on the strong  $^1\text{S}_0 - ^1\text{P}_1$  transition. This transition is approximately 160 times faster than the  $^1\text{S}_0 - ^3\text{P}_1$  intercombination transition used to initialize the atom array and measure the final spin state<sup>7</sup>, which allows for shorter acquisition times at the expense of losing the atom after the image. This trade-off is favourable when probing for qubits that have already had errors, to minimize the probability of additional decays during the imaging time. By illuminating the array with counter-propagating beams near saturation, we can detect atoms in the ground state after a 20  $\mu\text{s}$  exposure, with a fidelity of 0.986 (Fig. 2d).

We now apply this technique to demonstrate mid-circuit detection of decay errors, converting them into erasures. We use a standard randomized benchmarking (RB) circuit with up to 300 single-qubit gates

and acquire a fast image after every 50 gates to probe for atoms that have decayed to the ground state (Fig. 2e). The average gate error rate is  $\epsilon = 1.0(1) \times 10^{-3}$ . However, by conditioning on the absence of a ground state atom in all of the erasure detection steps before the final qubit measurement (Fig. 2f), the error rate decreases to  $\epsilon_c = 4.5(3) \times 10^{-4}$ . Therefore, 56(4)% of the errors are detected mid-circuit and converted into erasure errors. Some of the errors that are not converted can be attributed to undetected loss (that is, background loss and photoionization,  $2 \times 10^{-4}$ ) and scattering back into the metastable state while repumping  $^3\text{P}_2$  on a non-ideal transition ( $1.0(6) \times 10^{-4}$ ). The remainder are errors within the metastable state (approximately  $1.5 \times 10^{-4}$ ) (see Extended Data Table 1 for a summary).

We now consider imperfections in the erasure detection process, which we divide into two types: errors induced on the qubits remaining in the metastable state and imperfect detection of atoms in the ground state. Qubits remaining in the metastable state suffer errors from the additional decay probability during the imaging time,  $P_d = 7 \times 10^{-6}$ , or from the off-resonant scattering of the imaging light. The latter effect is strongly suppressed by the large detuning between the  $^1\text{S}_0 - ^1\text{P}_1$  transition and any transitions originating from the metastable state (the nearest state is detuned by  $2\pi \times 22$  THz). We probe for scattering errors by continuously illuminating the atoms with the imaging light during the RB sequence (Fig. 2e, red star). No effect is observed, bounding this error at less than  $10^{-6}$  per imaging time. In Fig. 2g, we examine the image fidelity by varying the erasure detection threshold and tracking two quantities: the probability  $P(\text{err.}|\text{det.})$  that a qubit has an error at the end of the circuit, given that a detection event occurred, and the fraction of all errors that are detected before the end of the circuit,  $R_e = (\epsilon - \epsilon_c)/\epsilon$ . The first quantity is ideally 1 and decreases with false positive detections when the threshold is too low. The second quantity is also ideally 1 but is limited by the fraction of errors that are not detectable, as well as false negative detections. We find that a suitable threshold exists where essentially all detectable errors are detected, but the false positive rate remains small.

We now turn to two-qubit entangling gates. We implement a controlled-Z (CZ) Rydberg blockade gate using the time-optimal gate protocol of ref. 35, which is a continuous-pulse gate based on the symmetric controlled-Z (CZ) gate of ref. 37. The specific gate used in this work is further optimized to compensate for off-resonant transitions between both qubit states and other Rydberg levels (Fig. 3a,b). Precise control over the Rydberg laser pulse is achieved by coupling the laser into a UV-stable fibre<sup>38</sup> and monitoring the transmitted pulse using a



**Fig. 2 | Single-qubit gates with mid-circuit erasure conversion.** **a**, Lifetime of the  $^{171}\text{Yb}$  metastable qubit in an optical tweezer (power  $P = 0.76$  mW, depth  $U = 58$   $\mu\text{K}$ ). The green points show the total metastable state population ( $1/e$  decay time  $\Gamma_m^{-1} = 2.96(12)$  s), while the grey and red points show the population  $P_0$  in  $|0\rangle$ , after initializing in  $|0\rangle$  and  $|1\rangle$ , respectively. Fitting the  $|0\rangle$  and  $|1\rangle$  population yields an average spin-flip time  $T_1 = 23(14)$  s. **b**, Metastable state decay rate  $\Gamma_m$  as a function of trap power, showing a quadratic fit (see text) and its linear part (dashed line). **c**, Probability  $P_c$  of recovering an atom in the ground state after a decay from the metastable state. **d**, Histogram of camera counts from fast ( $20\ \mu\text{s}$ ) images on the  $^1\text{S}_0 - ^1\text{P}_1$  transition. The discrimination fidelity is 0.986. Inset, example single-shot fast image of a 5-site array. **e**, RB of single-qubit gates (**f**), using the circuit shown in panel **f**. After every 50 Clifford gates ( $\mathcal{C}$ ),

a fast image probes population in the ground state, converting the decay into an erasure error,  $E$ . The total error rate is  $\epsilon = 1.0(1) \times 10^{-3}$  (green), which falls to  $\epsilon_c = 4.5(3) \times 10^{-4}$  after conditioning on not detecting a ground state atom before the end of the circuit (blue). The total atom survival probability is shown in grey. The red star is from a second experiment with the fast imaging light left on continuously, showing no change. **g**, The threshold for detecting a ground state atom in the analysis of the fast images affects the erasure conversion performance. We quantify this using the probability of having an error at the end of the RB sequence conditioned on detecting an erasure,  $P(\text{err.}|\text{det.})$  (blue) and the fraction of all errors that are detected as erasures,  $(\epsilon - \epsilon_c)/\epsilon$  (green). A threshold near 700 is used in the analysis in panel **e**. In all panels, error bars denote  $\pm 1$  standard deviation.

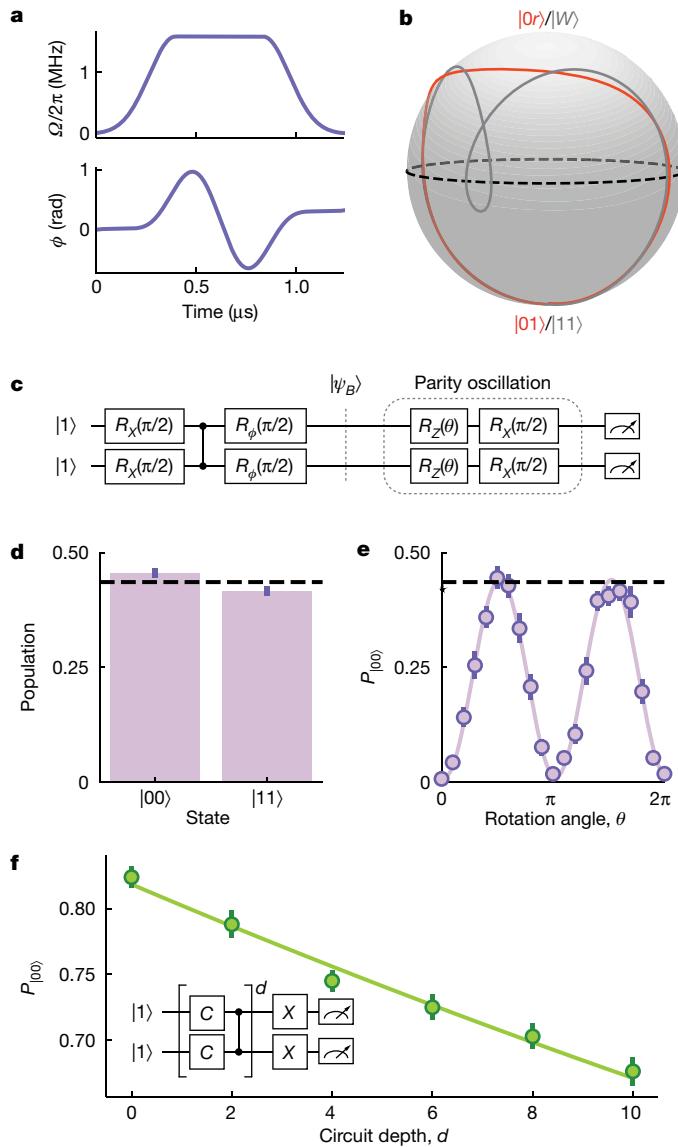
heterodyne receiver (see Extended Data Fig. 2 for details). A UV power of 6 mW is incident on the atoms, corresponding to a Rabi frequency  $\Omega_{\text{UV}} = 2\pi \times 1.6$  MHz.

To demonstrate the basic functionality of the gate, we prepare and measure a Bell state in parallel on five pairs of atoms (Fig. 3c). We obtain a raw Bell state fidelity of  $\mathcal{F} = 0.866(12)$  and estimate an intrinsic fidelity for the entanglement step of  $\mathcal{F} = 0.99(2)$  by separately characterizing state preparation and measurement (SPAM) errors. We use a different measurement circuit than previous works<sup>18,37</sup>, which increases certain SPAM errors but makes them easier to characterize. In our approach, we always record the fraction of events in the state  $|00\rangle$ , where both atoms are bright, using single-qubit rotations to map other desired observables onto this state. We then characterize the SPAM error by running the same sequence with the CZ gate removed, finding a SPAM fidelity of  $\mathcal{F}_{\text{sp}} = 0.872(6)$ . The intrinsic Bell state creation fidelity is estimated by renormalizing all measurement outcomes by  $\mathcal{F}_{\text{sp}}$ .

To characterize the performance of the CZ gate more precisely, we perform a randomized-benchmarking-type experiment with up to 10 CZ gates interspersed with random, global single-qubit rotations. We find an error probability of  $2.0(1) \times 10^{-2}$  per gate, corresponding to a fidelity of  $0.980(1)$ . We note that using global single-qubit gates invalidates the rigorous guarantees of two-qubit RB and is insensitive to

certain types of errors<sup>39</sup>. However, we have simulated this benchmarking approach using a realistic model of the atomic dynamics over a wide range of error rates and find that it is a good estimator of the true fidelity (Methods and Extended Data Fig. 3). From a detailed model with independently measured parameters, we infer that the leading sources of gate error are the finite lifetime of the Rydberg state ( $65(2)\ \mu\text{s}$ ,  $4 \times 10^{-3}$  error) and Doppler shifts ( $T = 2.9\ \mu\text{K}$ ,  $5 \times 10^{-3}$  error) (see Extended Data Table 2 for a summary).

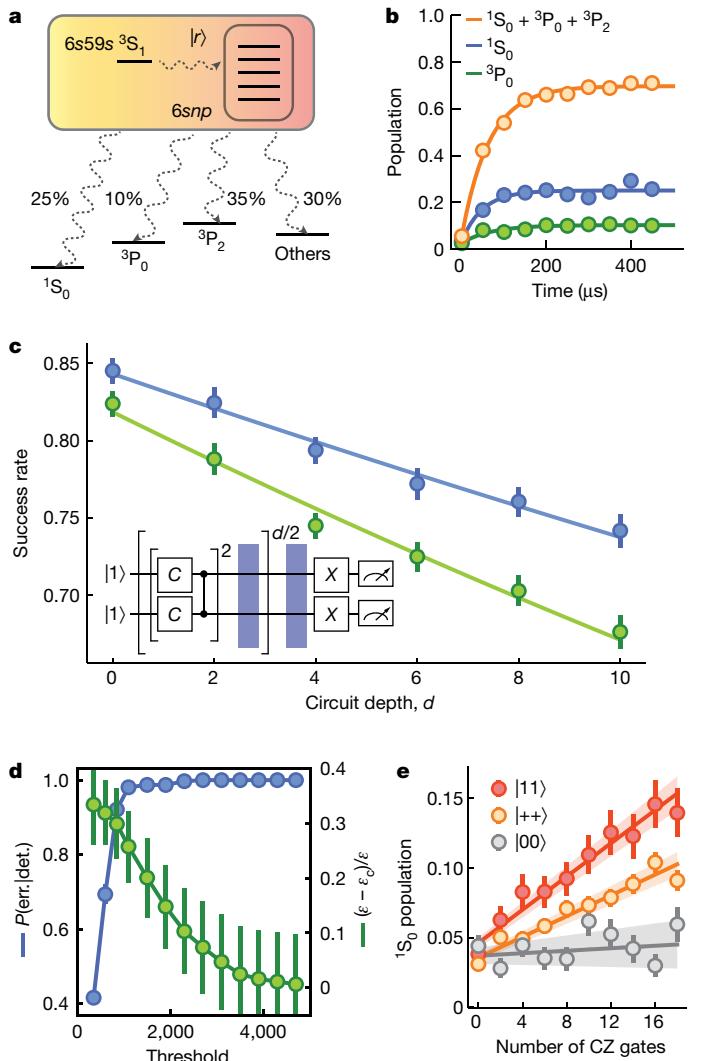
A large fraction of these errors result in leakage outside the qubit space, through spontaneous decay from  $|r\rangle$  to low-lying states or as population remaining in  $|r\rangle$  or other Rydberg states (populated via black-body radiation) at the end of the gate. Leakage errors are intrinsic to Rydberg gates in any atomic species and typically result in undetected loss<sup>14</sup>. By taking advantage of the unique property of alkaline earth atoms that the Rydberg states remain trapped in the optical tweezer by the  $\text{Yb}^+$  ion core polarizability<sup>40</sup>, we can recapture and detect this leaked population by waiting for it to decay. In Fig. 4b, we show that, for an atom initially prepared in  $|r\rangle$ , we recover 10% of the population in  $^3\text{P}_0$ , 25% in  $^1\text{S}_0$  and 35% in  $^3\text{P}_2$  after  $400\ \mu\text{s}$  (approximately 30% of the decays are unaccounted for). After repumping  $^3\text{P}_2$  via  $^3\text{S}_1$ , 51% of the population is in  $^1\text{S}_0$  and 19% is in  $^3\text{P}_0$ . The measured branching ratio back to  $^3\text{P}_0$  matches the theoretical prediction in ref. 10. However,



**Fig. 3 | Time-optimal two-qubit gates.** **a**, Laser amplitude (top) and phase (bottom) for the time-optimal CZ gate<sup>35</sup>. **b**, Bloch sphere trajectories during the gate in the  $\{|01\rangle, |0r\rangle\}$  subspace (red) and  $\{|11\rangle, |W\rangle\}$  subspace (grey). Here,  $|W\rangle = (|1r\rangle + |r1\rangle)/\sqrt{2}$ . **c**, Gate sequence used to prepare and characterize the Bell state  $|\psi_B\rangle = (|00\rangle + i|11\rangle)/\sqrt{2}$ . **d**, Population of  $|00\rangle$  and  $|11\rangle$  in the Bell state. The dashed line shows the probability of preparing and measuring the bright state  $|00\rangle$  without the CZ gate. **e**, Parity oscillations showing the coherence of the Bell state, measured using only the bright state population. The off-diagonal part of the Bell state density matrix is  $P_{c0} = 4A$ , where  $A$  is the  $\cos(2\theta)$  oscillation amplitude. The Bell state fidelity is  $(P_{00} + P_{11} + P_c)/2$ . **f**, Randomized circuit characterization of the two-qubit gate, with an error  $\epsilon = 2.0(1) \times 10^{-2}$  per gate.

further spectroscopy and modelling of the Yb Rydberg states are required to understand the lost population.

To convert two-qubit gate errors into erasures, we run the benchmarking circuit with interleaved fast imaging (after every two CZ gates). We find a lower error rate after conditioning on not detecting a ground state atom,  $\epsilon_c = 1.3(1) \times 10^{-2}$  per gate (Fig. 4c). This corresponds to converting approximately 33% of the errors into erasure errors. Our error model predicts that 60% of all gate errors are leakage, which is consistent with the experiment given that only half of the Rydberg leakage is detected (Methods). Waiting for the Rydberg population to decay increases the erasure detection time from 20  $\mu$ s



**Fig. 4 | Erasure conversion for two-qubit gates.** **a**, Population leaked into  $|r\rangle$  or other Rydberg states can be recovered by waiting for it to decay. The measured branching ratio into the (meta)stable levels is indicated in the diagram. **b**, The population recovery is measured by using different repumping conditions to separately measure the return to  $|1S_0$ ,  $|3P_0$ , and turning on all repumpers measures the total return to  $|1S_0$ ,  $|3P_0$  and  $|3P_2$ . **c**, Randomized circuit characterization of CZ gates with interleaved erasure detection after every two gates. The total error rate of  $\epsilon = 2.0(1) \times 10^{-2}$  per gate (green) is reduced to  $\epsilon_c = 1.3(1) \times 10^{-2}$  per gate (blue) after conditioning on not detecting an atom in the ground state before the end of the circuit. We note that the green curve is reproduced in Fig. 3f. **d**, Analysis of the erasure detection fidelity during two-qubit gates, following Fig. 2g. **e**, Erasure detection probability for different initial states under repetitive CZ gates. Linear fits are overlaid, with the shaded area marking one standard deviation. The erasure probability for  $|00\rangle$  is  $4(6) \times 10^{-4}$  per gate, which is consistent with zero.

to 420  $\mu$ s, increasing the decay probability on qubits without errors to  $P_d = 1.4 \times 10^{-4}$ .

Finally, we demonstrate that erasure errors occur asymmetrically from the qubit states  $|0\rangle$  and  $|1\rangle$ , which is another form of bias that is advantageous in the design of fault-tolerant systems<sup>29</sup>. In Fig. 4e, we show the probability per gate of detecting an erasure when preparing in  $|00\rangle$ ,  $|++\rangle$  and  $|11\rangle$ , using a longer sequence with up to 18 CZ gates (with no interleaved single-qubit rotations, to maintain the state populations in the computational basis). The probability of detecting a leaked qubit is much higher when the initial state has a probability of being in  $|1\rangle$ , as expected from the selective excitation of  $|1\rangle$  to the

Rydberg state<sup>14</sup>. We infer a lower bound on the ratio of the erasure probabilities of  $p_{11}/p_{00} > 15(9)$ .

Having demonstrated the basic properties of the metastable qubit and erasure conversion, we now reconsider the advantages and disadvantages of metastable qubit encoding. The main disadvantage is that the finite metastable state lifetime introduces an additional error channel that affects very slow operations and qubit storage. The lifetime is 2–3 times shorter than typical Raman-limited  $T_1$  times for hyperfine qubits in alkali atoms<sup>1,2</sup>, but the impact is offset by the fact that many of these decays can be detected, as demonstrated here. The metastable state decay is not relevant on the submicrosecond timescale of two-qubit gates, which are, instead, limited by the finite decay rate of the Rydberg state. The same decay channel is present for Rydberg gates in any atomic species and typically results in atom loss. The fact that the metastable qubit allows these decays to be recaptured and detected is a substantial advantage, which will become even more consequential as other sources of error are eliminated and Rydberg decays become dominant<sup>10,41</sup>. Using fast single-photon excitation from the metastable state, as demonstrated here, our error model predicts that large improvements in gate fidelity are achievable with modest laser upgrades (Methods).

There are several straightforward improvements to increase the fraction of errors that can be detected and converted into erasures. The fraction of detected metastable state decays can be increased by using an alternative repumping transition for  ${}^3P_2$  (Methods), a longer trapping wavelength to suppress photoionization and a better vacuum to reduce background losses. There is no apparent obstacle to detecting virtually all of the metastable state decays. In two-qubit gates, the fraction of all errors that are leakage will increase as the gate fidelity improves and Rydberg decays become the dominant error mechanism and could be as high as 98% (ref. 10). Composite pulses can also convert certain errors such as amplitude noise and Doppler shifts into erasures<sup>41,42</sup>. Finally, the detection fidelity of Rydberg leakage can be increased by identifying and repumping additional decay pathways, or by ionizing atoms in the Rydberg state at the end of the gate and detecting the  $\text{Yb}^+$  ions directly using fluorescence<sup>10,43</sup> or charged particle detectors, which have demonstrated 98% ion detection efficiency from an optical tweezer<sup>44</sup>.

The demonstrated high-fidelity control and mid-circuit erasure conversion establishes metastable  ${}^{171}\text{Yb}$  as a promising architecture for fault-tolerant quantum computing based on erasure conversion. In this context, the key property of this demonstration is that the quantum state of qubits that did not have erasures is unaffected by the erasure detection process. In an error correcting code, this will allow the erased qubits to be replaced using a moveable optical tweezer, such that the correct code state can be restored after measuring the error syndromes<sup>10</sup>. Erasure conversion may also be useful in other contexts, such as quantum simulation or metrology.

The detection protocols demonstrated in this work can also be adapted to mid-circuit qubit readout<sup>13,45,46</sup>, by selectively transferring one of the qubit levels back to the ground state (that is, using optical pumping). Subsequently transferring the other level and measuring the ground state population again would allow atom loss to be distinguished, which is also beneficial for error correction<sup>29</sup>. The metastable qubit will also enable mid-circuit reloading of new qubits, as demonstrated already with dual-species experiments<sup>13</sup>. Lastly, we note that while finalizing this manuscript, we became aware of recent, related work in refs. 47,48.

## Online content

Any methods, additional references, Nature Portfolio reporting summaries, source data, extended data, supplementary information,

acknowledgements, peer review information; details of author contributions and competing interests; and statements of data and code availability are available at <https://doi.org/10.1038/s41586-023-06438-1>.

- Bluvstein, D. et al. A quantum processor based on coherent transport of entangled atom arrays. *Nature* **604**, 451–456 (2022).
- Graham, T. M. et al. Multi-qubit entanglement and algorithms on a neutral-atom quantum computer. *Nature* **604**, 457–462 (2022).
- Ebadı, S. et al. Quantum phases of matter on a 256-atom programmable quantum simulator. *Nature* **595**, 227–232 (2021).
- Scholl, P. et al. Quantum simulation of 2D antiferromagnets with hundreds of Rydberg atoms. *Nature* **595**, 233–238 (2021).
- Cooper, A. et al. Alkaline-earth atoms in optical tweezers. *Phys. Rev. X* **8**, 041055 (2018).
- Norcia, M., Young, A. & Kaufman, A. Microscopic control and detection of ultracold strontium in optical-tweezer arrays. *Phys. Rev. X* **8**, 041054 (2018).
- Saskin, S., Wilson, J. T., Grinkemeyer, B. & Thompson, J. D. Narrow-line cooling and imaging of ytterbium atoms in an optical tweezer array. *Phys. Rev. Lett.* **122**, 143002 (2019).
- Singh, K., Anand, S., Pocklington, A., Kemp, J. T. & Bernien, H. Dual-element, two-dimensional atom array with continuous-mode operation. *Phys. Rev. X* **12**, 011040 (2022).
- Bonilla Ataides, J. P., Tuckett, D. K., Bartlett, S. D., Flammia, S. T. & Brown, B. J. The XZZX surface code. *Nat. Commun.* **12**, 2172 (2021).
- Wu, Y., Kolkowitz, S., Puri, S. & Thompson, J. D. Erasure conversion for fault-tolerant quantum computing in alkaline earth Rydberg atom arrays. *Nat. Commun.* **13**, 4657 (2022).
- Kaufman, A. M. & Ni, K.-K. Quantum science with optical tweezer arrays of ultracold atoms and molecules. *Nat. Phys.* **17**, 1324–1333 (2021).
- Browaeys, A. & Lahaye, T. Many-body physics with individually controlled Rydberg atoms. *Nat. Phys.* **16**, 132 (2020).
- Singh, K. et al. Mid-circuit correction of correlated phase errors using an array of spectator qubits. *Science* **380**, 1265–1269 (2023).
- Cong, I. et al. Hardware-efficient, fault-tolerant quantum computation with Rydberg atoms. *Phys. Rev. X* **12**, 021049 (2022).
- Norcia, M. A. et al. Seconds-scale coherence on an optical clock transition in a tweezer array. *Science* **366**, 93–97 (2019).
- Madjarov, I. S. et al. An atomic-array optical clock with single-atom readout. *Phys. Rev. X* **9**, 041052 (2019).
- Barnes, K. et al. Assembly and coherent control of a register of nuclear spin qubits. *Nat. Commun.* **13**, 2779 (2022).
- Ma, S. et al. Universal gate operations on nuclear spin qubits in an optical tweezer array of  $\text{Yb}$  171 atoms. *Phys. Rev. X* **12**, 021028 (2022).
- Jenkins, A., Lis, J. W., Senoo, A., McGrew, W. F. & Kaufman, A. M. Ytterbium nuclear-spin qubits in an optical tweezer array. *Phys. Rev. X* **12**, 021027 (2022).
- Chen, N. et al. Analyzing the Rydberg-based optical-metastable-ground architecture for  $\text{Yb}$  171 nuclear spins. *Phys. Rev. A* **105**, 052438 (2022).
- Madjarov, I. S. et al. High-fidelity entanglement and detection of alkaline-earth Rydberg atoms. *Nat. Phys.* **16**, 857–861 (2020).
- Allcock, D. T. C. et al. omg blueprint for trapped ion quantum computing with metastable states. *Appl. Phys. Lett.* **119**, 214002 (2021).
- Campbell, W. C. Certified quantum gates. *Phys. Rev. A* **102**, 022426 (2020).
- Yang, H.-X. et al. Realizing coherently convertible dual-type qubits with the same ion species. *Nat. Phys.* **18**, 1058–1061 (2022).
- Roman, C. H. Expanding the  ${}^{171}\text{Yb}^+$  Toolbox: The  ${}^2F_{7/2}$  State as Resource for Quantum Information Science. PhD thesis, UCLA (2021); <https://escholarship.org/uc/item/0mx6t24p>.
- Grassl, M., Beth, T. & Pellizzari, T. Codes for the quantum erasure channel. *Phys. Rev. A* **56**, 33–38 (1997).
- Bennett, C. H., DiVincenzo, D. P. & Smolin, J. A. Capacities of quantum erasure channels. *Phys. Rev. Lett.* **78**, 3217–3220 (1997).
- Barrett, S. D. & Stace, T. M. Fault tolerant quantum computation with very high threshold for loss errors. *Phys. Rev. Lett.* **105**, 200502 (2010).
- Sahay, K., Jin, J., Claes, J., Thompson, J. D. & Puri, S. High threshold codes for neutral atom qubits with biased erasure errors. Preprint at <https://arxiv.org/abs/2302.03063> (2023).
- Kubica, A., Haim, A., Vaknin, Y., Brandão, F. & Retzker, A. Erasure qubits: overcoming the  $T_1$  limit in superconducting circuits. Preprint at <https://arxiv.org/quant-ph/abs/2208.05461> (2022).
- Kang, M., Campbell, W. C. & Brown, K. R. Quantum error correction with metastable states of trapped ions using erasure conversion. *PRX Quantum* **4**, 020358 (2023).
- Teoh, J. D. et al. Dual-rail encoding with superconducting cavities. Preprint at <https://arxiv.org/quant-ph/abs/2212.12077> (2022).
- Tsunoda, T. et al. Error-detectable bosonic entangling gates with a noisy ancilla. *PRX Quantum* **4**, 020354 (2023).
- Lu, Y. et al. A high-fidelity microwave beamsplitter with a parity-protected converter. Preprint at <https://arxiv.org/quant-ph/abs/2303.00959> (2023).
- Jandura, S. & Pupillo, G. Time-optimal two- and three-qubit gates for Rydberg atoms. *Quantum* **6**, 712 (2022).
- Bergschneider, A. et al. Spin-resolved single-atom imaging of Li 6 in free space. *Phys. Rev. A* **97**, 063613 (2018).
- Levine, H. et al. Parallel implementation of high-fidelity multiqubit gates with neutral atoms. *Phys. Rev. Lett.* **123**, 170503 (2019).
- Colombe, Y., Slichter, D. H., Wilson, A. C., Leibfried, D. & Wineland, D. J. Single-mode optical fiber for high-power, low-loss UV transmission. *Optics Express* **22**, 19783 (2014).
- Baldwin, C. H., Bjork, B. J., Gaebler, J. P., Hayes, D. & Stack, D. Subspace benchmarking high-fidelity entangling operations with trapped ions. *Phys. Rev. Res.* **2**, 013317 (2020).

# Article

40. Wilson, J. et al. Trapping alkaline earth Rydberg atoms optical tweezer arrays. *Phys. Rev. Lett.* **128**, 033201 (2022).
41. Jandura, S., Thompson, J. D. & Pupillo, G. Optimizing Rydberg gates for logical-qubit performance. *PRX Quantum* **4**, 020336 (2023).
42. Fromontiel, C., Bluvstein, D. & Pichler, H. Protocols for Rydberg entangling gates featuring robustness against quasistatic errors. *PRX Quantum* **4**, 020335 (2023).
43. McQuillen, P., Zhang, X., Strickler, T., Dunning, F. B. & Killian, T. C. Imaging the evolution of an ultracold strontium Rydberg gas. *Phys. Rev. A* **87**, 013407 (2013).
44. Henkel, F. et al. Highly efficient state-selective submicrosecond photoionization detection of single atoms. *Phys. Rev. Lett.* **105**, 253001 (2010).
45. Deist, E. et al. Mid-circuit cavity measurement in a neutral atom array. *Phys. Rev. Lett.* **129**, 203602 (2022).
46. Graham, T. M. et al. Mid-circuit measurements on a neutral atom quantum processor. Preprint at <https://arxiv.org/abs/2303.10051> (2023).
47. Evered, S. J. et al. High-fidelity parallel entangling gates on a neutral-atom quantum computer. *Nature* <https://doi.org/10.1038/s41586-023-06481-y> (2023).
48. Scholl, P. et al. Erasure conversion in a high-fidelity Rydberg quantum simulator. *Nature* <https://doi.org/10.1038/s41586-023-06516-4> (2023).

**Publisher's note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Springer Nature or its licensor (e.g. a society or other partner) holds exclusive rights to this article under a publishing agreement with the author(s) or other rightsholder(s); author self-archiving of the accepted manuscript version of this article is solely governed by the terms of such publishing agreement and applicable law.

© The Author(s), under exclusive licence to Springer Nature Limited 2023

## Methods

### Experimental apparatus

We load a tweezer array from a three-dimensional magneto-optical trap operating on the  ${}^1S_0 \rightarrow {}^3P_1$  intercombination line. The tweezers are at a wavelength of  $\lambda = 486.78$  nm, which is magic for the ground state and the  ${}^3P_1, F=3/2, |m_F|=1/2$  excited states<sup>18</sup>. An acousto-optic deflector driven by an arbitrary waveform generator is used to create defect-free one-dimensional tweezer arrays via rearrangement<sup>49,50</sup>. We use approximately 4 mW per tweezer in the plane of the atoms for loading and rearrangement, corresponding to a trap depth of 300  $\mu\text{K}$ . After loading, a short blue-detuned cooling pulse is used to reach a temperature of approximately  $T = 5 \mu\text{K}$ . For determining the initial and final tweezer occupation, we image using the intercombination line transition, achieving a fidelity and survival probability of 0.995 in a 15 ms exposure time<sup>7</sup>. The images are acquired with an sCMOS camera (Photometrics Prime BSI). To perform fast imaging<sup>36</sup> for detecting atoms that have decayed to  ${}^1S_0$ , we use the  ${}^1S_0 \rightarrow {}^1P_1$  transition at 399 nm. We illuminate the atoms with a resonant retro-reflected beam at a power of  $I = 4I_{\text{sat}}$ . The image is acquired using an EMCCD camera (Nüvü HNU 512 Gamma) with EM gain = 1,000. We achieve a detection fidelity of 0.986 in 20  $\mu\text{s}$ . The survival probability of this imaging process is small but non-zero (2–5%), so we follow each blue image with an additional 80  $\mu\text{s}$  pulse to ensure that none of the atoms that decayed to the ground state are present in the final spin measurement image. The position spread of the atoms during the imaging is approximately 2  $\mu\text{m}$  (root mean square).

We can create arrays of up to 30 optical tweezers, limited by the available trapping laser power. To avoid Rydberg interactions during the spin readout, we use a spacing of  $d = 43 \mu\text{m}$  for the experiments in Fig. 2d, limiting the array to five sites. For the two-qubit experiments in Figs. 3 and 4, we use five dimers spaced by  $d = 43 \mu\text{m}$ , with a separation of 2.4  $\mu\text{m}$  between the atoms in each pair.

### Metastable state initialization and measurement

We initialize atoms into the  ${}^3P_0$  state using optical pumping, to avoid the need for a clock laser and state-insensitive tweezers for the clock transition. The optical pumping scheme is depicted in Extended Data Fig. 1a. A coherent two-photon transition (556 nm,  $\sigma^+$ -polarized; 1,539 nm,  $\pi$ -polarized) is used to excite atoms from the  ${}^1S_0, m_F = +1/2$  to the  ${}^3D_1, F = 3/2, m_F = +3/2$  state. The  $m_F$  levels in the excited state are split by 5.7 linewidths in a magnetic field, allowing energy-selective excitation of the  $m_F = 3/2$  sublevel, even in the presence of polarization imperfections. This state decays to  $|1\rangle$  with approximately 64% probability and returns to  ${}^1S_0$  (via  ${}^3P_1$ ) in most of the other cases (the branching ratio to  ${}^3P_2$  is 1% and this state is continuously repumped via  ${}^3S_1$  using a 770 nm laser with sidebands to address both  $F$  levels). The detuning of the 556 nm leg of the two-photon Raman transition is chosen to be resonant with the  ${}^3P_1, F = 3/2, m_F = 1/2$  excited state, to continuously pump atoms out of the  ${}^1S_0, m_F = -1/2$  state.

During this process, several per cent of the atoms end up in  $|0\rangle$ , because of off-resonant excitation to other  ${}^3D_1$  states and decays through  ${}^3P_2$ . To increase the purity in the  $|1\rangle$  state, we apply a short pulse of light at 649 nm ( $\sigma^+$ ), coupling  $|0\rangle$  to  ${}^3S_1, F = 1/2, m_F = 1/2$ . This removes the atom from  $|0\rangle$  with approximately 90% probability, after which we apply an additional cycle of repumping from the ground state. This process is repeated a second time.

The total duration of the optical pumping process is 500  $\mu\text{s}$  and the average number of scattered photons is less than two. We measure a temperature of 5.7  $\mu\text{K}$  for atoms in  ${}^3P_0$ , indicating minimal heating.

To measure the population in  ${}^3P_0$ , we pump atoms back from  ${}^3P_0$  to the ground state via  ${}^3S_1$  (Extended Data Fig. 1b), with continuous illumination from 770 nm to repump  ${}^3P_2$ . To make this measurement spin-selective, we first remove atoms in  $|1\rangle$  by exciting to  $|r\rangle$  and auto-ionizing the Rydberg population<sup>51</sup>. In addition to being destructive,

this step limits the density of tweezers, to avoid blockade effects. In future work, this step can be replaced with spin-selective optical pumping via  ${}^3S_1$  or  ${}^3D_1$  to allow non-destructive readout. Because the  ${}^3P_2$  state is anti-trapped in the 486 nm tweezer ( $U_{{}^3P_2}/U_{{}^3P_0} \approx -2$ ), we pulse off the traps for 3  $\mu\text{s}$  during this step, which results in a few per cent atom loss probability. This could be mitigated using multiple short modulation pulses or a different tweezer wavelength where  ${}^3P_2$  is trapped (that is, 532 nm<sup>52</sup>).

We characterize the fidelity of the initialization and readout process by preparing the states  $|0\rangle$  and  $|1\rangle$  using the procedures described above together with nuclear spin rotations. We observe the correct outcome 99.6(3)% of the time for  $|1\rangle$  (the dark state) and 96.6(8)% of the time for  $|0\rangle$  (the bright state), for an average initialization and readout fidelity of 98.1(9)%. We believe that the dominant error is loss during the pumping back to  ${}^3P_0$ .

Finally, we note several other experimental details. The initialization and readout are performed with a trap depth of 300  $\mu\text{K}$ , corresponding to a power of 4 mW per tweezer. During the gate operations, the trap is ramped down to 58  $\mu\text{K}$  (0.76 mW), which reduces Doppler shifts and atom loss from pulsing off the traps during the two-qubit gates. This cools the atoms further to  $T = 2.94 \mu\text{K}$ , measured from the Ramsey coherence time of the Rydberg state. The 770 nm repumper is left on continuously during the entire time the atom is in the metastable state, to rapidly repump any atoms that scatter or decay to  ${}^3P_2$ . This is not the ideal repumper configuration, as it has a 25% probability of pumping an atom back to  ${}^3P_0$ . This is evident in the finite spin-flip rate in Fig. 2a; repeating that measurement without the 770 nm repumper results in no observable spin flips, as expected from the absence of hyperfine coupling<sup>53</sup>. In the future, repumping  ${}^3P_2$  through a  ${}^3D_2$  state (that is, using transitions at 496.8 nm or 1,983 nm) would avoid repopulating  ${}^3P_0$ .

### Rydberg laser system and beam delivery

Atoms are excited to the Rydberg state using UV light at 302 nm. This light is produced in two steps. First, we generate approximately 1 W of 604 nm light through sum frequency generation in a 40 mm long periodically poled lithium niobate crystal using a titanium-sapphire laser at 980 nm (MSquared Solstis, 1 W) and an Er-doped fibre laser at 1,565 nm (NKT, 10 W)<sup>54</sup>. Then, this light is converted to 302 nm in a resonant cavity, achieving approximately 50 mW output power.

The cavity is followed by an always-on acousto-optic modulator for amplitude stabilization and a second, pulsed acousto-optic modulator to generate the gate pulses (Extended Data Fig. 2a). The pulsed light is coupled into a polarization-resistant UV fibre patchcord<sup>38</sup> (NKT LMA-PM-15) and delivered to a monolithic breadboard mounted directly next to the glass cell, where it is focused to a beam waist of  $w_0 = 10 \mu\text{m}$  at the atoms using an objective lens (Thorlabs LMU-3X-UVB). The power on the breadboard is approximately 6 mW. The entire breadboard is mounted on a motorized stage to align the beam to the atoms. The free-space optical path length after the fibre is less than 30 cm, which reduces sensitivity to air currents and temperature gradients. A photodiode on the breadboard monitors the pulse power. Additionally, approximately 10% of the light is picked off and coupled back into a second UV fibre and beat against the un-modulated UV laser in a heterodyne configuration. This allows the complex envelope of the laser pulse to be measured, to adjust the driving signal to compensate for phase transients during the rising and falling edges (Extended Data Fig. 2b,c).

### Characterization of SPAM errors

While we initialize and measure atoms in the tweezers with a fidelity of approximately 0.995, the qubit initialization and measurement are affected by additional errors. These errors are dominated by the loss of atoms, including loss during the optical pumping into and out of  ${}^3P_0$  (we believe that the return step is the dominant source of loss) and decay out of  ${}^3P_0$  during the gate sequence.

# Article

With the destructive spin readout scheme used in this work, qubits in  $|1\rangle$  cannot be distinguished from atom loss. However, the imaging errors are biased towards false negatives: from repeated imaging, we infer a false positive atom detection probability of  $4 \times 10^{-4}$ . Therefore, the dominant measurement error is to incorrectly label a bright site as dark, while the probability of labelling a dark site as bright is very low. Exploiting this bias, we devise an accurate method to correct this error by converting all observables to the probability of both atoms being bright  $P_{bb}$ . We first explain the theory of atom loss correction by measuring  $P_{bb}$  and then show how to determine the Bell state fidelity from only measurements of  $P_{bb}$ .

For a generic process,  $P_{bb}$  can be written as

$$P_{bb} = P_{(bb|nl)} P_{nl} + P_{(bb|loss)} P_{loss}, \quad (1)$$

where  $P_{nl}$  is the probability of no atom loss during the process,  $P_{loss}$  is the probability that at least one atom is lost, and  $P_{(bb|nl)}$  and  $P_{(bb|loss)}$  are the corresponding conditional probabilities of correctly measuring both atoms in the bright state. From the above discussion, the probability that a lost atom appears bright is negligible,  $P_{(bb|loss)} \approx 0$ , so  $P_{bb} = P_{(bb|nl)} P_{nl}$ . The value of  $P_{nl}$  can be measured independently by removing the CZ gate and blowout pulse. If the spin readout is perfect, then the conditional fidelity  $P_{(bb|nl)} = P_{bb}/P_{nl}$  gives the fidelity corrected for atom loss during the initialization and readout process. For completeness, we assume that the spin readout is perfect for now and provide a lower bound on the Bell state fidelity after introducing the detailed experimental scheme.

Here, we explain in detail how we apply this correction to the Bell state fidelity in Fig. 3 in the main text. The Bell state fidelity can be determined as  $\mathcal{F}_B = (P_{00} + P_{11} + P_c)/2$ , so we need to convert the three terms on the right-hand side to  $P_{bb}$ . Since  $|0\rangle$  is the bright state,  $P_{00}$  can be directly inferred from  $P_{bb}$ ,  $P_{11}$  can be measured by applying an additional nuclear spin  $\pi$  pulse and then measuring  $P_{bb}$ .

To measure  $P_c$ , we need an observable  $\mathcal{O}_c = |11\rangle\langle 00| + |00\rangle\langle 11|$ , which can be obtained using the parity oscillation circuit in Fig. 3c. This circuit can be represented as  $U = e^{-i\pi X/4} e^{-i\theta Z/2}$ , where  $X = \sigma_x^1 + \sigma_x^2$ ,  $Z = \sigma_z^1 + \sigma_z^2$ , with  $\sigma_x^j$ ,  $\sigma_z^j$  being the Pauli operator on  $j$ th atom. The probability of measuring  $P_{bb}$  is then  $P_{bb} = \text{Tr}(Up_U^\dagger \mathcal{O}_{bb})$ , with  $\mathcal{O}_{bb} = |00\rangle\langle 00|$ .

This is mathematically equivalent to measuring an effective observable

$$\begin{aligned} \mathcal{O}_\theta &= e^{i\theta Z/2} e^{i\pi X/4} \mathcal{O}_{00} e^{-i\pi X/4} e^{-i\theta Z/2} \\ &= \frac{1}{4} \begin{pmatrix} 1 & -ie^{i\theta} & -ie^{i\theta} & -e^{2i\theta} \\ ie^{-i\theta} & 1 & 1 & -ie^{i\theta} \\ ie^{-i\theta} & 1 & 1 & -ie^{i\theta} \\ -e^{-2i\theta} & ie^{-i\theta} & ie^{-i\theta} & 1 \end{pmatrix}. \end{aligned} \quad (2)$$

The term oscillating at  $2\theta$  is the desired observable,  $\mathcal{O}_c/4$ . By fitting the parity oscillation signal in Fig. 3e to  $A\cos(2\theta + \theta_0) + B$ , we obtain  $P_c = 4A$ .

In a second experiment, we measure the dimer survival probability  $P_{nl}$  without the CZ gate and spin blowout pulses. The intrinsic Bell state fidelity is estimated to be  $\mathcal{F}_B^c = \mathcal{F}_B/P_{nl}$ . In the experiment, we measure  $P_{00} = 0.46(1)$ ,  $P_{11} = 0.42(1)$ ,  $P_c = 0.86(2)$  and  $P_{nl} = 0.872(6)$ , yielding  $\mathcal{F}_B = 0.866(12)$  and a corrected value  $\mathcal{F}_B^c = 0.99(2)$ .

So far, we have assumed a perfect spin readout. Now we analyse the effect of spin readout infidelity and derive an approximate lower bound on the intrinsic Bell state fidelity  $\mathcal{F}_B^c$  in the presence of spin readout errors. In the following, we discuss only the probabilities conditioned on no atom loss and we drop the superscript  $c$  for simplicity. We define the single-atom spin readout true positive rate  $p_{TP}$  (an atom in  $|0\rangle$  appears bright) and false positive rate  $p_{FP}$  (an atom in  $|1\rangle$  appears bright). Given an underlying, true Bell state population  $P_{ij}$ , the measured population  $\tilde{P}_{ij}$  can be written as

$$\begin{aligned} \tilde{P}_{00} &= P_{00} p_{TP}^2 + (P_{01} + P_{10}) p_{TP} p_{FP} + P_{11} p_{FP}^2 \\ \tilde{P}_{11} &= P_{11} p_{TP}^2 + (P_{01} + P_{10}) p_{TP} p_{FP} + P_{00} p_{FP}^2, \end{aligned} \quad (3)$$

where the  $\tilde{P}_{11}$  is extracted by applying a  $\pi$  pulse and then measuring the double bright state population. The diagonal part of the Bell state fidelity is then

$$P_{00} + P_{11} = \frac{\tilde{P}_{00} + \tilde{P}_{11} - 2p_{TP} p_{FP}}{(p_{TP} - p_{FP})^2}. \quad (4)$$

To derive the coherence term, we rewrite equation 3 using the observables with imperfect spin readout  $\tilde{\mathcal{O}}_{bb} = p_{TP}^2 |00\rangle\langle 00| + p_{TP} p_{FP} (|11\rangle\langle 00| + |00\rangle\langle 11|) + p_{FP}^2 |11\rangle\langle 11|$ . We similarly define  $\tilde{\mathcal{O}}_\theta = e^{i\theta Z/2} e^{i\pi X/4} \tilde{\mathcal{O}}_{bb} e^{-i\pi X/4} e^{-i\theta Z/2}$ . The experimental signal  $\text{Tr}(\rho \tilde{\mathcal{O}}_\theta)$  contains a  $\cos(2\theta + \theta_0)$  oscillation term with amplitude  $1/[4(p_{TP} - p_{FP})^2]$ ; therefore, the measured coherence is  $\tilde{P}_c = \text{Tr}(\rho \tilde{\mathcal{O}}_\theta)$  with  $P_c$  the actual coherence. Therefore, actual Bell state fidelity  $\mathcal{F}_B$  is related to the measured fidelity  $\tilde{\mathcal{F}}_B$  via

$$\begin{aligned} \mathcal{F}_B &= \frac{\tilde{\mathcal{F}}_B - p_{TP} p_{FP}}{(p_{TP} - p_{FP})^2} \geq \frac{\tilde{\mathcal{F}}_B - p_{FP}}{(1 - p_{FP})^2} \\ &= \tilde{\mathcal{F}}_B + (2\tilde{\mathcal{F}}_B - 1)p_{FP} + (3\tilde{\mathcal{F}}_B - 2)p_{FP}^2 + O(p_{FP}^3) \geq \tilde{\mathcal{F}}_B, \end{aligned} \quad (5)$$

where the inequality in the second line is obtained by setting  $p_{TP} = 1$  (the inequality holds for  $p_{TP} \geq p_{FP}$ ) and the inequality in the last line holds as long as  $\tilde{\mathcal{F}}_B$  is much greater than  $1/2$  and  $p_{FP}$  is small. In our case,  $p_{FP} = 0.4\%$  and  $\tilde{\mathcal{F}}_B = 0.99(2)$ , so the measured value is a lower bound on the true value without spin readout errors.

## Two-qubit entangling gates

The two-qubit gate implemented in our experiment is adapted from the time-optimal gate in ref. 35. In that work, each atom is modelled as a three-level system  $\{|0\rangle, |1\rangle, |r\rangle\}$  with a perfect Rydberg blockade preventing a simultaneous excitation of both atoms to  $|r\rangle$  and with a coupling of  $|1\rangle$  and  $|r\rangle$  through a global laser with constant amplitude and time-dependent phase  $\phi(t)$ . Using the quantum optimal control method of gradient ascent pulse engineering (GRAPE)<sup>55,56</sup>, ref. 35 then determines the time-optimal pulse  $\phi(t)$  to implement a CZ gate.

This simple three-level model does not accurately describe our system, because of off-resonant coupling between both qubit states and other Rydberg levels (Extended Data Fig. 1d). To incorporate this effect, we use GRAPE to redesign our pulses under a new model that takes all of these additional transitions into consideration. All four sublevels of the  $6s59s\ ^3S_1, F=3/2$  Rydberg manifold are included:  $\{|r_{-3/2}\rangle, |r_{-1/2}\rangle, |r_{1/2}\rangle, |r_{3/2}\rangle\}$ . Taking the polarization of our Rydberg laser and the Clebsch–Gordon coefficients of each transition into account, the Hamiltonian of a single atom in the basis of  $\{|0\rangle, |1\rangle, |r_{-3/2}\rangle, |r_{-1/2}\rangle, |r_{1/2}\rangle, |r_{3/2}\rangle\}$  can then be written as

$$H_{sq} = \hbar \begin{pmatrix} -\Delta_m & 0 & \frac{\Omega e^{-i\phi}}{2} & 0 & \frac{\Omega e^{-i\phi}}{2\sqrt{3}} & 0 \\ 0 & 0 & 0 & \frac{\Omega e^{-i\phi}}{2\sqrt{3}} & 0 & \frac{\Omega e^{-i\phi}}{2} \\ \frac{\Omega e^{i\phi}}{2} & 0 & -3\Delta_r & 0 & 0 & 0 \\ 0 & \frac{\Omega e^{i\phi}}{2\sqrt{3}} & 0 & -2\Delta_r & 0 & 0 \\ \frac{\Omega e^{i\phi}}{2\sqrt{3}} & 0 & 0 & 0 & -\Delta_r & 0 \\ 0 & \frac{\Omega e^{i\phi}}{2} & 0 & 0 & 0 & 0 \end{pmatrix}. \quad (6)$$

Here,  $\Omega$  is the Rabi frequency and  $\phi$  is the phase of the Rydberg laser. The Zeeman splitting in the  ${}^3P_0$  and Rydberg manifolds is denoted by  $\Delta_m$  and  $\Delta_r$ , respectively. Because the Landé  $g$ -factor in the  ${}^3P_0$  manifold is more than three orders of magnitude smaller than the one in  $6s5s {}^3S_1 F=3/2$ , we set  $\Delta_m=0$  for simplicity. When taking both atoms and the van der Waals interaction into consideration, the full Hamiltonian of the system is then

$$H = H_{\text{sq}} \otimes \mathbb{I} + \mathbb{I} \otimes H_{\text{sq}} + \hbar \sum_{ijkl} V_{ijkl} |r_i\rangle\langle r_k| \otimes |r_j\rangle\langle r_l| \quad (7)$$

In the limit of strong van der Waals interaction ( $|V_{ijkl}| \gg \Omega$ ), any double-Rydberg excitation is strictly forbidden. In this case, one can separately calculate the dynamics of the system depending on its initial state, with each corresponding to an evolution in a five-dimensional subspace,

$$\begin{aligned} |00\rangle &\Rightarrow \{|00\rangle, |0r_{-3/2}\rangle, |0r_{1/2}\rangle, |r_{-3/2}0\rangle, |r_{1/2}0\rangle\}, \\ |01\rangle &\Rightarrow \{|01\rangle, |0r_{-1/2}\rangle, |0r_{3/2}\rangle, |r_{-3/2}1\rangle, |r_{1/2}1\rangle\}, \\ |11\rangle &\Rightarrow \{|11\rangle, |1r_{-1/2}\rangle, |1r_{3/2}\rangle, |r_{-1/2}1\rangle, |r_{3/2}1\rangle\}. \end{aligned}$$

We note that the dynamics of  $|01\rangle$  and  $|10\rangle$  are always the same and therefore the latter is omitted for brevity.

Given a specific value of  $\Delta_r/\Omega$ , a GRAPE optimization similar to ref. 35 can be implemented with our more accurate model. Instead of using a pulse with square amplitude, we fix  $\Omega(t)$  to have Gaussian rising and falling edges and total duration  $T$ . This minimizes the pulse bandwidth and reduces unwanted excitation of the other Rydberg state, while having negligible effect on the average population of the Rydberg state. We then find the laser phase  $\phi(t)$  minimizing the infidelity for a CZ gate. For the sake of the optimization, a piecewise constant approximation  $\phi(t) = \phi_n$  for  $t \in [Tn/N, T(n+1)/N]$  with  $N = 100 \gg 1$  pieces is made. The infidelity  $1 - \mathcal{F}$  can then be numerically minimized over the  $\phi_0, \dots, \phi_{N-1}$ , with the GRAPE algorithm providing an efficient way of calculating the gradient  $\nabla \mathcal{F}$ <sup>55</sup> in time  $\mathcal{O}(N)$ . Note that also a global phase  $\theta_0$  and a single-qubit phase  $\theta_1$  are included in the optimization, such that the desired evolution is given by  $|00\rangle \mapsto e^{i\theta_0} |00\rangle$ ,  $|01\rangle \mapsto e^{i(\theta_0+\theta_1)} |01\rangle$  and  $|11\rangle \mapsto -e^{i(\theta_0+2\theta_1)} |11\rangle$ .

For the experimental parameters of  $\Delta_r = 2\pi \times 9.3$  MHz and  $\Omega = 2\pi \times 1.6$  MHz,  $\Delta_r/\Omega = 5.8$ , we find a gate with infidelity  $1 - \mathcal{F} < 10^{-5}$ .

For deployment on the experiment, we use a parameterized version of the GRAPE-derived pulse in terms of a finite sum of Chebyshev polynomials,

$$\Delta(t) = \dot{\phi}(t) \approx \sum_{n=0}^{n_{\max}} c_n T_n \left( \frac{2t}{T} - 1 \right), \quad (8)$$

where  $T_n(x)$  is the  $n$ th Chebyshev polynomial of the first kind. We find that truncating the series at  $n_{\max} = 13$  does not affect the gate fidelity. This lower-dimensional parameterization is useful for experimental fine-tuning by scanning each coefficient around its nominal value, to correct for control errors and effects not included in our model.

### Noise model for two-qubit gates

To understand the sources of infidelities in our two-qubit gates, we have developed a numerical simulation combining the master equation formalism with the Monte Carlo method, based on the six-level model discussed above. It includes Markovian decay from the finite Rydberg state lifetime, coherent errors (imperfect Rydberg blockade and off-resonant excitation) and non-Markovian noise (Doppler shifts from atomic motion and laser phase and intensity noise). Non-Markovian effects are included using a Monte Carlo approach, by simulating the evolution under randomly generated noise traces and averaging the final result<sup>57</sup>.

The gate fidelity that we wish to estimate is defined as

$$\mathcal{F} = \int d\psi \langle \psi | U^\dagger \mathcal{E}(|\psi\rangle\langle\psi|) U |\psi\rangle, \quad (9)$$

where the integration is taken over the Haar measure in the two-qubit Hilbert space,  $\mathcal{E}$  is the quantum channel describing the gate and  $U$  is the corresponding unitary for an ideal CZ gate.

In practice, equation 9 is difficult to evaluate. Therefore, we use an equivalent expression in terms of the process fidelity  $\mathcal{F}_{\text{pro}}$  and the leakage  $L$ <sup>58</sup>:

$$\mathcal{F} = \frac{4\mathcal{F}_{\text{pro}} + 1 - L}{5}. \quad (10)$$

Here, the process fidelity is defined in terms of the superoperators  $S_U, S_{\mathcal{E}}$  of quantum channels  $U, \mathcal{E}$  as

$$\mathcal{F}_{\text{pro}} = \frac{1}{16} \text{Tr}(S_U^\dagger S_{\mathcal{E}}). \quad (11)$$

Leakage out of the computational space (arising from population decay from the Rydberg states or population left in the Rydberg state at the end of the gate<sup>10</sup>) is computed as

$$L = 1 - \text{Tr}[\mathcal{E}(1)]/4. \quad (12)$$

The parameters in the error model are determined from independent experiments. Exploiting the ability to trap Rydberg atoms<sup>40</sup>, we directly measure the Rydberg state lifetime, finding  $T_{1,r} = 65(2)$  μs. We use a Ramsey experiment to measure the Doppler shift and other quasi-static detuning errors and find a purely Gaussian decay with  $1/e$  decay time  $T_2^* = 5.7$  μs. This places an upper bound on the temperature of  $T \leq 2.94$  μK. We measure the laser phase noise before the second harmonic generation, using a high-finesse cavity as a frequency discriminator. Finally, we measure the laser intensity noise after the second harmonic generation.

We find that the leading sources of error are the Rydberg state decay ( $5 \times 10^{-3}$ ), detuning from Doppler shifts ( $5 \times 10^{-3}$ ), laser phase noise ( $2 \times 10^{-3}$ ) and imperfections in the laser pulse envelope ( $2 \times 10^{-3}$ ). Simulating these effects together gives a gate error of  $1.4 \times 10^{-2}$ , lower than the experimental value of  $2 \times 10^{-2}$  (Extended Data Table 2). This leaves an error of approximately  $6 \times 10^{-3}$  that is not accounted for in our model. The most plausible explanation is slow drifts in experimental parameters affecting the gate calibration, but further investigation is required to isolate and correct this error.

The model additionally predicts that 60% of the errors should be leakage errors, including decays from the Rydberg state during the gate and population trapped in the Rydberg state at the end of the gate. This is consistent with the observed erasure conversion fraction of 33% for the two-qubit gates (Fig. 4c) when correcting for the fact that we only detect 50% of the decays from the Rydberg state in  ${}^1S_0$ .

To achieve higher gate fidelities, the key parameter is the Rabi frequency. The Rydberg decay error decreases with the gate time, as  $1/\Omega_{\text{UV}}$ . The Doppler shift error decreases as  $1/\Omega_{\text{UV}}^2$ . Given that our current UV laser power of 6 mW is far from the highest power demonstrated at a similar wavelength<sup>59</sup>, the known error sources can all be suppressed below  $10^{-3}$  with straightforward improvements in laser power, phase noise and pulse shape control.

### Randomized circuit benchmarking validation

As noted in the text, the two-qubit benchmarking circuit used in Figs. 3f and 4c does not generate a rigorous fidelity estimate because we use global single-qubit rotations. It is completely insensitive to certain errors, such as a SWAP of the two qubits<sup>39</sup>. To assess the reliability of this estimate, we have simulated the exact benchmarking sequences

# Article

used in the experiment with the error model discussed in the previous section, varying the strength of each noise term over a large range to simulate a range of gate error rates, up to several times worse than the measured experimental value.

In Extended Data Fig. 3b, we compare the true gate error rates with those extracted from the simulated benchmarking circuit without erasure conversion and find that the benchmarking gives a good estimation of the error rate with a relative uncertainty of less than 10%.

## Data availability

The data reported in this manuscript are available in the Harvard Dataverse online repository at <https://doi.org/10.7910/DVN/TJ6OIF>.

49. Endres, M. et al. Atom-by-atom assembly of defect-free one-dimensional cold atom arrays. *Science* **354**, 1024–1027 (2016).
50. Barredo, D., de Léséleuc, S., Lienhard, V., Lahaye, T. & Browaeys, A. An atom-by-atom assembler of defect-free arbitrary two-dimensional atomic arrays. *Science* **354**, 1021–1023 (2016).
51. Burgers, A. P. et al. Controlling Rydberg excitations using ion-core transitions in alkaline-earth atom-tweezer arrays. *PRX Quantum* **3**, 020326 (2022).
52. Okuno, D. et al. High-resolution spectroscopy and single-photon Rydberg excitation of reconfigurable ytterbium atom tweezer arrays utilizing a metastable state. *J. Phys. Soc. Japan* **91**, 084301 (2022).
53. Dörscher, S. et al. Lattice-induced photon scattering in an optical lattice clock. *Phys. Rev. A* **97**, 063419 (2018).
54. Wilson, A. C. et al. A 750-mW, continuous-wave, solid-state laser source at 313 nm for cooling and manipulating trapped  ${}^9\text{Be}^+$  ions. *Appl. Phys. B* **105**, 741–748 (2011).
55. Khaneja, N., Reiss, T., Kehlet, C., Schulte-Herbrüggen, T. & Glaser, S. J. Optimal control of coupled spin dynamics: design of NMR pulse sequences by gradient ascent algorithms. *J. Magn. Reson.* **172**, 296–305 (2005).
56. Wilhelm, F. K., Kirchhoff, S., Machnes, S., Wittler, N. & Sugny, D. An introduction into optimal control for quantum technologies. Preprint at <https://arxiv.org/quant-ph/abs/2003.10132> (2020).
57. de Léséleuc, S., Barredo, D., Lienhard, V., Browaeys, A. & Lahaye, T. Analysis of imperfections in the coherent optical excitation of single atoms to Rydberg states. *Phys. Rev. A* **97**, 053803 (2018).
58. Wood, C. J. & Gambetta, J. M. Quantification and characterization of leakage errors. *Phys. Rev. A* **97**, 032306 (2018).
59. Lo, H.-Y. et al. All-solid-state continuous-wave laser systems for ionization, cooling and quantum state manipulation of beryllium ions. *Appl. Phys. B* **114**, 17–25 (2014).

**Acknowledgements** We acknowledge helpful conversations with S. Kolkowitz and M. Gullans. This work was supported by the Army Research Office (W911NF-1810215), the Office of Naval Research (N00014-20-1-2426), DARPA ONISQ (W911NF-20-10021), the National Science Foundation (QLCI grant OMA-2120757) and the Sloan Foundation. This research also received funding from the European Union's Horizon 2020 programme under the Marie Skłodowska-Curie project 955479 (MOQS), the Horizon Europe programme HORIZON-CL4-2021-DIGITAL-EMERGING-01-30 via the project 101070144 (EuRyQa) and from the French National Research Agency under the Investments of the Future Program project ANR-21-ESRE-0032 (aQCess).

**Author contributions** S.M., G.L., P.P. and B.Z. performed the experiments described in the main text and analysed the data. A.P.B. contributed to experiments developing the initialization and readout procedures for the metastable qubit. S.J. and G.P. performed theoretical modelling of optimal control gate sequences and collaborated with the experimental team on gate optimization. J.C., S.P., P.P. and J.D.T. developed approaches to benchmark gates in the presence of erasure errors. All authors discussed the results. S.M., G.L., P.P., B.Z. and J.D.T. wrote the manuscript with input from all authors.

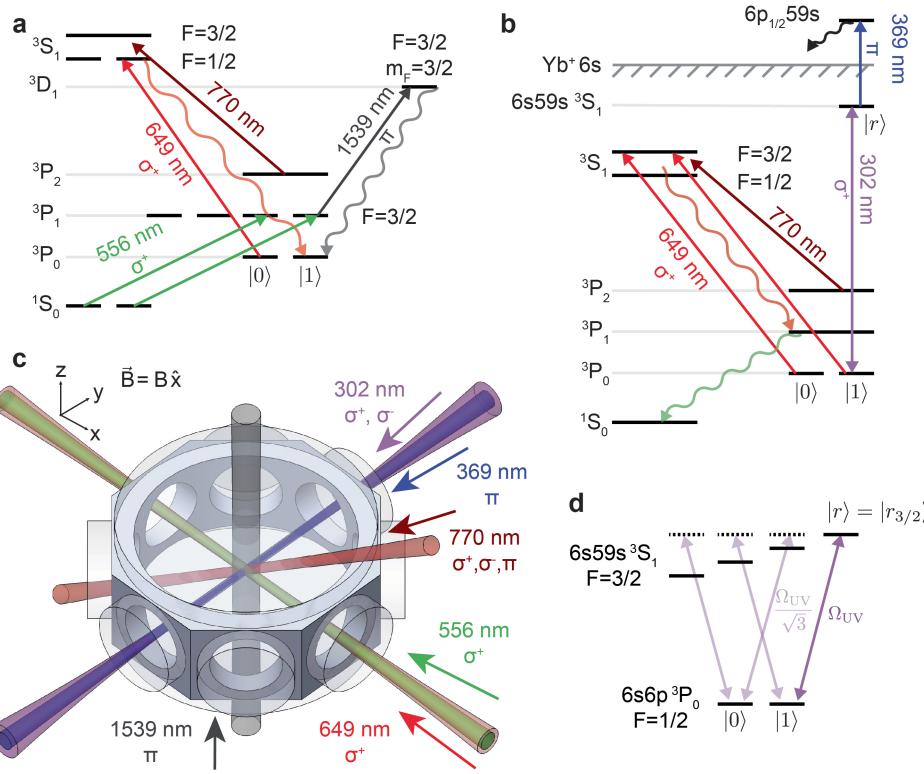
**Competing interests** G.P. is co-founder and shareholder of QPerfect.

### Additional information

**Correspondence and requests for materials** should be addressed to Jeff D. Thompson.

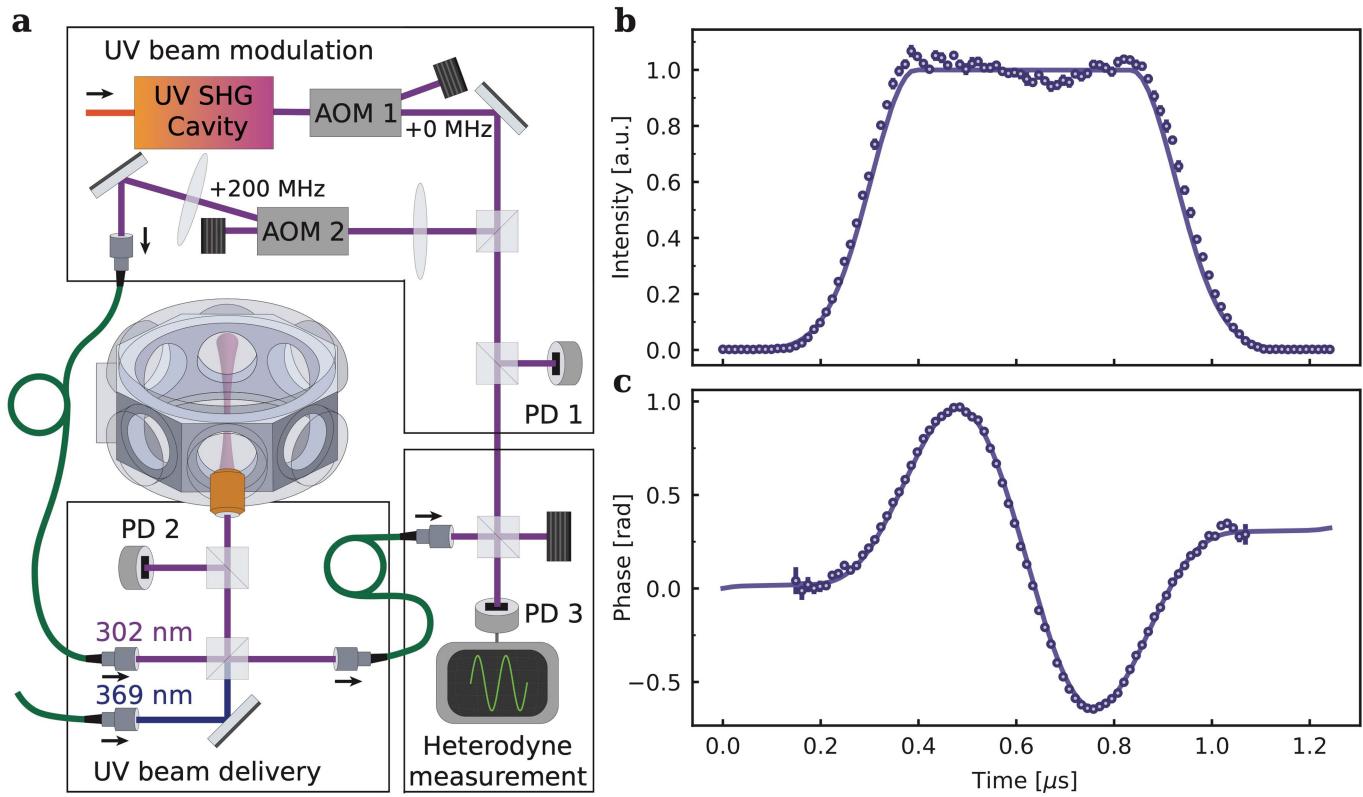
**Peer review information** *Nature* thanks Wolfgang Lechner and the other, anonymous, reviewer(s) for their contribution to the peer review of this work.

**Reprints and permissions information** is available at <http://www.nature.com/reprints>.



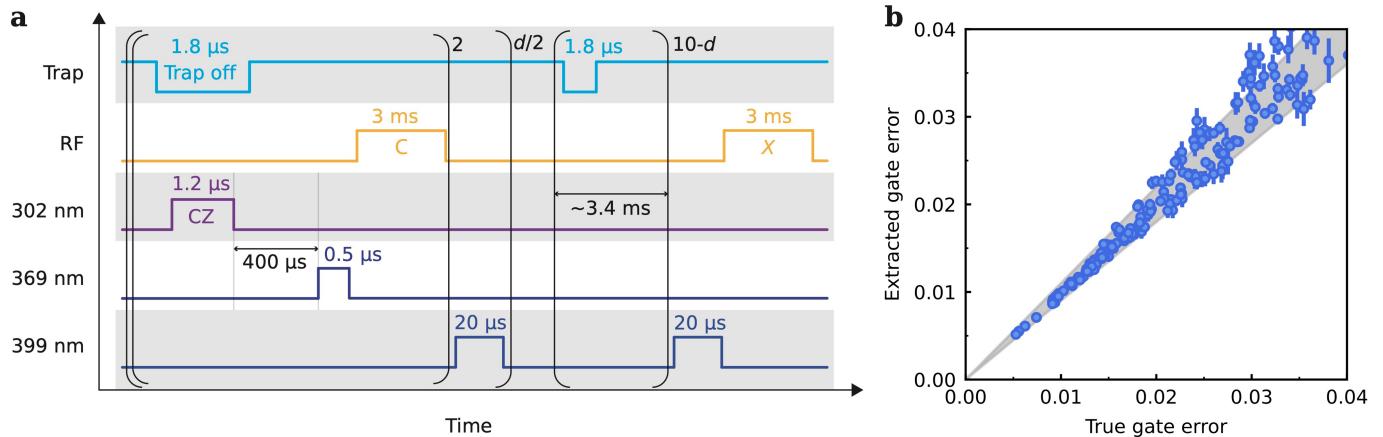
**Extended Data Fig. 1 | Level diagrams and laser beam geometry.** **a**, Partial level diagram showing the transitions used to optically pump into the state  $|1\rangle$  for initialization. **b**, Partial level diagram indicating the transitions used to measure the spin state in  ${}^3P_0$ . First, atoms in  $|1\rangle$  are removed from the trap using Rydberg excitation and subsequent autoionization. Then, all population in  ${}^3P_0$  is pumped back to  ${}^1S_0$  and imaged. **c**, Propagation directions and polarizations of the lasers addressing the atoms. The  $556\text{ nm}$  and  $399\text{ nm}$  imaging beams are not shown, but are co-propagating with the  $770\text{ nm}$  beam and retro-reflected.

The microscope objective used to project the tweezers and image the atoms (numerical aperture NA=0.6) is positioned above the glass cell. **d**, Partial level diagram showing the transitions between  ${}^3P_0$  and the Rydberg manifold used in this work. The detuning between the Rydberg states is 5.8 times larger than  $\Omega_{\text{UV}}$ . The  $302\text{ nm}$  beam is linearly polarized perpendicular to the magnetic field, which is constrained by the geometry of our apparatus. In the future, using a pure  $\sigma^+$ -polarized  $302\text{ nm}$  beam would increase the gate speed by a factor of  $\sqrt{2}$  for the same laser power.



**Extended Data Fig. 2 | Rydberg laser system.** **a**, The 302 nm light is generated by a resonant cavity. The output beam is power-stabilized by a servo formed by AOM1 and PD1, and pulses are generated by AOM2. The pulsed light is coupled into a fibre and delivered to a monolithic breadboard next to the glass cell. PD2 monitors the pulse power on the breadboard. To monitor the pulse phase, a small fraction of the light is sent back to the optical table with a second fibre,

and interfered with the un-modulated laser to form a beatnote on PD3 (at the frequency of AOM2). The beatnote is digitized and digitally demodulated to extract the amplitude and phase profiles shown in **b** and **c**, together with the target pulse shapes (solid lines). Programming AOM2 with a naive waveform results in phase distortion; the waveform shown in **c** is obtained after closed-loop correction.



**Extended Data Fig. 3 | Randomized circuit benchmarking experiment.**

**a**, Sequence of operations for the entangling gate randomized circuit benchmarking experiment (the horizontal axis is not to scale). **b**, Comparison of the simulated gate fidelity and simulated randomized circuit benchmarking fidelity for the error model discussed in the Methods. The strength of each

noise term is varied randomly around the nominal value expected for the experiment. The randomized circuit benchmarking infidelity is typically within 10% of the true gate error (shaded region), indicating that it is a good estimator of the true gate fidelity.

## Article

Extended Data Table 1 | Single-qubit gate error budget

Total gate error <sup>a</sup>	<b><math>1.0(1) \times 10^{-3}</math></b>
Erasure probability <sup>a</sup>	$5.5(3) \times 10^{-4}$
Background loss and photoionization <sup>b</sup>	$2 \times 10^{-4}$
Imperfect repumping <sup>b</sup>	$1.0(6) \times 10^{-4}$
Errors in qubit subspace <sup>c</sup>	$1.5 \times 10^{-4}$
Sum of all contributions	<b><math>1.0(1) \times 10^{-3}</math></b>

<sup>a</sup>Measured. <sup>b</sup>Computed from independently measured quantities. <sup>c</sup>Inferred.

Extended Data Table 2 | Two-qubit gate error budget

Total gate error <sup>a</sup>	<b><math>2.0(1) \times 10^{-2}</math></b>
Rydberg state lifetime <sup>b</sup>	$5 \times 10^{-3}$
Doppler shift <sup>b</sup>	$5 \times 10^{-3}$
Laser phase noise <sup>b</sup>	$2 \times 10^{-3}$
Imperfect pulse envelope <sup>b</sup>	$2 \times 10^{-3}$
Other, unknown <sup>c</sup>	$6 \times 10^{-3}$
Sum of all contributions	<b><math>2.0 \times 10^{-2}</math></b>

<sup>a</sup>Estimated from randomized circuit benchmarking. <sup>b</sup>Computed from independently measured quantities. <sup>c</sup>Inferred.