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# Modeling Influence in Text Corpora

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## Abstract

Identifying the most influential documents in a corpus is an important problem in many fields, ranging from information science and historiography to text summarization and news aggregation. We propose using changes in the linguistic content of these documents over time to predict the importance of individual documents within the collection and describe a dynamic topic model for both quantifying and qualifying the impact of each document in the corpus.

## 1 Introduction

Computing meaningful statistical measurements of the influence of a scientific article is an important and challenging problem. Such measurements are used to assess the quality of various academic instruments, such as journals, scientists, and universities. These so-called "impact factors" can play a large role in decisions surrounding funding, hiring, and publishing.

Knowing the impact of a scientific article is important for scientific research as well: finding and reading the influential articles of a field is central to good research practice. With unprecedented access to large corpora of scientific articles, modern researchers have instant access to a large catalog of previous work that might be important and interesting.

The traditional method of assessing the impact of an article is to analyze the citations to it. The impact factor of a journal, for example, is based largely on citation analysis; and this is intuitive: if more people have cited an article then more people have read it. It has had more impact on its field.

The notion of impact or influence goes beyond the small world of scientific research, however: legal documents, news stories, blog posts, sermons, and email all might have had an impact on other documents. But, how can we measure impact without citations? Moreover, citations only capture one kind of impact. All citations from an article are counted equally in an impact factor. However, some articles of a bibliography might be more related—or have influenced the authors more—than others.

The goal of this work is to develop an unsupervised method for determining the influence of a document. Our intuition is that language changes over time, and that influential documents contribute to this change. Our algorithm takes a sequence of documents as input and computes a scalar "influence" of each document. We validate our method by measuring how well the computed impact predicts citation. On a corpus of over 20 years of Computational Linguistics articles, we demonstrate that our method provides a citation-free measure of bibliometric impact.

This paper is organized as follows. We begin with a discussion of work related to this . We then describe the Document Influence Model (DIM), our unsupervised model for determining the influence of a document using the changes in language used by documents over time. We then provide details for inference with this model. We then discuss experimental results and provide examples of documents deemed influential by this model.

## 2 Related work

Much of the work in identifying influential documents has focused on additional forms of structure within a corpus such as hyperlinks or document citations. The utility of citation counts in gauging influence is a well-established in practice, supported by a wide body of research and practical applications. The *Impact Factor*, for example, a measure of the importance of a journal within a field of research, is based on citations to this journal’s articles [1]. The well-known Pagerank algorithm has likewise helped Google to find documents relevant to Web search queries [2]. In these cases, this structure has been very powerful: receiving a Nobel prize is highly correlated with citations to one’s work (before the prize is awarded), for example; and Google has become one of the world’s foremost search engines.

Much recent work has gone into understanding the interplay between corpus semantics and this link structure. Radev et al. have studied the relationship between semantic content of Web documents and the probability a hyperlink existing between them. Deitz et al. have used topic models, a formalism for identifying themes in corpora, to characterize the thematic significance of individual citations between documents [3].

### 2.1 Topic models

We will also build on *topic models*, a formalism for understanding themes in corpora. Examples of topic models include Latent Semantic Indexing (LSI) [4], probabilistic LSI (pLSI) [5], and Latent Dirichlet Allocation (LDA) [6]. In each of these models, each document is modeled as a mixture of *topics*, which can generally be interpreted as themes.

Existing work has aimed to explicitly predict these links using themes in a corpus. Cohn et al. have used topic models for inferring links (both hyperlinks and academic citations) between documents [7]. Relational Topic Models and Link-LDA have also been posited to model citations and hyperlink references in the Blogosphere, respectively [8, 9].

While this work is related to our goal, we do not aim to predict individual links between documents; we are primarily interested in understanding which documents are influential, and *how* these documents are influential. While the model in [7] can be interpreted as a stochastic process which mimics the generation of documents, we explicitly aim to use the evolution of topics *over time* to determine influential documents.

Various applications of topic models have addressed the evolution of themes over time. *Post-hoc* analyses have been performed to track the progression of ideas over time, identifying “hot” and “cold” topics in the Journal PNAS [10] and the ACL Anthology [11]. More direct methods for understanding the flow of ideas over time involve extensions of topic models to capture the temporal evolution of themes. The Dynamic Topic Model [12], makes a Markov assumption about how topics drift over discrete points in time and has been extended to a continuous model [13]. Topics over Time (TOT) [14] models topics as fixed distributions whose proportions over time are given by beta distributions, an assumption convenient for inference. The Dynamic Mixture Model (DMM) [15], effectively an online model, assumes a fixed set of topics but allows the topic proportion to vary over time. In contrast to the DTM, the DMM assumes that topics themselves do not evolve over time; only the (prior over) topic proportions change over time.

### 2.2 Dynamic Topic Models

In this work, we assume that influential documents change the language of their topics. The DTM is therefore a natural basis on which to build our model, the Document Influence Model. Before describing the DIM in detail, we give a quick review of LDA and the DTM; readers can refer for further details to the original work in [6] and [12]. In LDA, a corpus is associated with a parameter  $\alpha$  describing a Dirichlet prior over topic proportions assigned to each document, along with a set  $\beta$  of topics which describe themes as distributions over words.

In the DTM, documents at *each point in time* are associated with distinct  $\alpha_t$  (now as a logistic normal distribution) and topics  $\beta_t$ ; within each time point, documents are assumed to be generated by the LDA generative process. The DTM further assumes that these topics and topic proportions



marginal posterior  $l_{d,k}|\tilde{l}_{d,k} \sim \mathcal{N}(\tilde{l}_{d,k}, \sigma_l^2)$ <sup>1</sup>. The full variational posterior is then

$$q(\mathbf{d}) = \prod_{k=1}^K q(\beta_{k,1}, \dots, \beta_{k,T} | \tilde{\beta}_{k,1}, \dots, \tilde{\beta}_{k,T}) \quad (2)$$

$$\times \prod_{t=1}^T \left( \prod_{d=1}^{D_t} q(\theta_{t,d} | \gamma_{t,d}) q(l_{t,d} | \tilde{l}_{t,d}) \prod_{n=1}^{N_{t,d}} q(\mathbf{z}_{t,d,n} | \phi_{t,d,n}) \right) \quad (3)$$

The evidence can be bounded from below using Jensen's inequality. Maximizing this lower bound corresponds to minimizing the variational distribution's KL divergence with the true posterior. This lower bound and details of optimizing it are provided in the appendix.

While inference for this model is similar to that described in [12], some updates are new or significantly different. Here we focus on the update equation for the new parameter  $\tilde{l}$  and changes to the update equations for  $\phi$ , the variational parameter for  $z$ , and the new parameters  $\tilde{l}$ . We provide a derivation of the update for  $\beta$  in an appendix, and readers can refer to [12] for further details on optimizing this parameter.

**Document regression** As suggested by the generative model given in section 3, the update for  $\tilde{l}$  is the solution to a regression problem. This solution is:

$$\tilde{l}_{t,k} \leftarrow \left( \frac{\sigma_d^2}{\sigma_d^2} I + \left( (\mathbf{W}_{t,k} \circ \phi_{t,k})^T \Lambda_{\exp(-2\tilde{m}+2\tilde{V})} (\mathbf{W}_{t,k} \circ \phi_{t,k}) \right) \right. \quad (4)$$

$$\left. + \Lambda_{(\mathbf{W}_{t,k} \circ \mathbf{W}_{t,k} \circ (\phi_{t,k} - \phi_{t,k} \circ \phi_{t,k}))^T \exp(-2\tilde{m}+2\tilde{V})} \right)^{-1} \\ (\mathbf{W}_{t-f,k} \circ \phi)^T \left( \exp(-\tilde{m}_{t,k} + \tilde{V}_{t,k}/2) \circ (\tilde{m}_{t+f,k} - \tilde{m}_{t,k} + \tilde{V}_{t,k}) \right), \quad (5)$$

where  $\circ$  refers to the Hadamard element-wise product and  $\Lambda_{\vec{x}}$  refers to a diagonal matrix having the elements of  $\vec{x}$  on its diagonal.  $\mathbf{W}$  here is the term-document matrix, and  $\tilde{m}$  and  $\tilde{V}$  are the variational expectation and variance of  $\beta$ , as described in [12].

This update provides some insight into how the model works: it assumes that document weights are generated by a regularized linear regression with a random design matrix  $X := \mathbf{W} \circ \phi$ . This update has some very nice properties. First, regularization is enforced by three separate forces: the prior over document weights, the variance  $\sigma^2$  of topic drifts, and the variance  $\phi(1 - \phi)$  of the topics assigned to each word; we address the importance of this regularization in Section ?? . Because the topic distribution for each document is nearly sparse, with suitable transformations of  $W$  (such as column normalization), the document weights for a given topic can also be made sparse (in the sense that most weights are close to 0).

In the variational implementation of LDA [6], the  $\phi$  updates are accomplished in a single pass. In the Document Influence Model, we cannot fully optimize  $\phi$  in a single pass, but we can approximate it in each pass using an additional parameter  $\lambda_n$  and the principal branch  $W_0$  of the Lambert function

<sup>1</sup>In general, we may abuse notation and refer to the vector  $\tilde{l}_{t,k}$  of all document weights at time  $t$  for topic  $k$ ; notation should be evident from context.

<sup>2</sup> as follows [17]:

$$\begin{aligned}
A_k &:= \frac{2}{\sigma^2} \exp(-2\tilde{m}_{t,n,k} + 2\tilde{V}_{t,n,k})(\tilde{l}_{t,k,d_n}^2 w_{d_n}^2) \\
B_k &:= \Psi(\gamma_i) - \Psi\left(\sum_{j=1}^K \gamma_j\right) \\
&\quad + \tilde{m}_{t,n,k} - 1 + \lambda_{n,s} \\
&\quad + \frac{1}{\sigma^2} (\tilde{m}_{t+f,n,k} - \tilde{m}_{t,n,k} + \tilde{V}_{t,n,k}) \exp(-\tilde{m}_{t,n,k} + \tilde{V}_{t,n,k}/2) \tilde{l}_{t,k,d_n} w_{t,d,n} \\
&\quad - \frac{1}{\sigma^2} \exp(-2\tilde{m}_{t,n,k} + 2\tilde{V}_{t,n,k})(\tilde{l}_{t,k,d_n} w_{t,d,n} D_{n,k}) \\
&\quad - \frac{1}{2\sigma^2} \exp(-2\tilde{m}_{t,n,k} + 2\tilde{V}_{t,n,k}) w_{t,d,n}^2 (\tilde{l}_{t,k,d_n}^2 + \sigma_{\tilde{l}_{D_t}}^2) \\
\phi_{n,k} &\leftarrow - \frac{W(-A_k e^{B_k})}{A_k}.
\end{aligned} \tag{6}$$

Here  $D_{n,k} := \sum_d \phi_{d,n,k} \tilde{l}_{t,d,k} w_{t,n} := \left( (\mathbf{W}_t \circ \phi_{t,k}) \tilde{l}_{t,k} \right)_n$  can be stored with each update of  $\tilde{l}$ . Here  $A_k$  is the coefficient of  $\phi$ , while  $B_k$  is the constant term (detailed in supplementary material). When  $A_k$  and  $\sigma_{\tilde{l}_{D_t}}^2$  are small (as is usually the case), this formula gives the same result as that found by LDA.

We then normalize  $\phi_{n,k}$  over the topics  $k$  and update  $\lambda_n$ :

$$\lambda_{n,s+f} \leftarrow - \frac{\sum_K A_k \phi_k + B_k - \log(\phi_{n,k})}{K} + \lambda_{n,s}.$$

For further details on the derivation of this update, please see supplementary material.

The update for  $\tilde{\beta}$  is similar to the update in [12] and can be determined from the evidence lower bound. We provide further details in the Appendix.

## 5 Experiments

We have designed the Document Influence Model to identify highly influential documents using only the changes in language over time. To confirm that this model is finding patterns of influence, we have validated it on a corpus in which documents have been annotated with internal citation counts. In this section we describe two experiments designed to understand whether there exists a relationship to existing influence metrics and to understand how to set the model’s parameters. We also give some intuition into the model by showing papers deemed influential by it and illustrating two documents in detail.

### 5.1 Methodology

**Predicting citations** The principal experiment aims to determine whether the influence score is correlated with citation counts. We fit a model over a standard corpus using each document’s true date. We perform this experiment with  $\sigma_l^2 = 0.00001$ , letting  $f = 2, 6$ , or  $10$ . For simplicity, we restrict to a single topic, although we have successfully run this model with multiple topics.

**Varying  $\sigma_d^2$**  We also ran a set of experiments to understand when this model best matches citation data. Here we vary  $\sigma_d^2$ , the variance of document weights, for a one-topic model, selecting a range of values between  $1e-10$  and  $5e-2$ . Changing  $\sigma_d^2$  amounts to changing regularization in Formula 4: smaller  $\sigma_d^2$  yields higher regularization.

### 5.2 Data

The *ACL Anthology* is a collection of papers spanning several decades in the field of computational linguistics. Joseph and Radev et al. have constructed the ACL Anthology Network from this corpus, annotating references and collecting various network statistics including paper citation counts,

<sup>2</sup>The Lambert function  $W(y)$  is the solution to  $xe^x = y$  and is implemented in GSL.

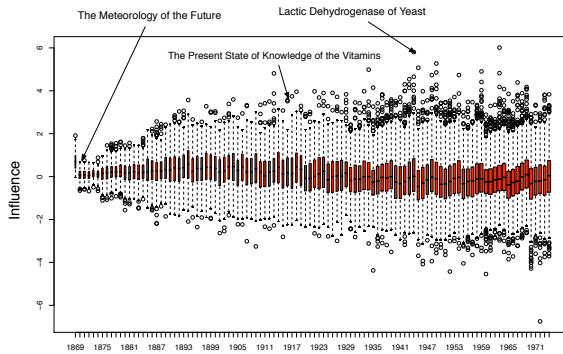


Figure 2: Document weights as a function of date. Titles of outliers are labeled.

author citation counts, and Pagerank [18] [19]. We fit the DIM on the all documents in the ACL Anthology Network for which dates were available. This included 11115 documents, from 1965 to 2007, discretized into two-year periods. To focus on high-content words, we restricted the corpus to plural nouns and common singular nouns using the TreeTagger part-of-speech tagger [20], for a total word count of 10,718,210 and a vocabulary of size 4,148.

To illustrate the DIM in a corpus where there is no citation information, we fit a one-topic DIM to the full text of Nature magazine from 1869 to the present. The box plot of posterior influences is illustrated, with some of the high impact articles identified. The DIM provides a new exploratory tool for scientific corpora, like this one, for which bibliometric information is difficult to obtain.

### 5.3 Results

We verified the relationship between the posterior influence and a notion of bibliometric impact. We fit linear regression models for each year of the ACL corpus of the log of citations (plus one) against the posterior influence. We plot the coefficient in Figure 3. To test its significance, we shuffled the impact factors 100 times and reran the regression, plotted in gray. (This is a permutation test.)

Figure 2 indicates that there is a definitive relationship between our estimate of influence and the number of citations of a document. We emphasize that our estimate of impact is based only on the way language has changed. From this information alone, we were able to infer a quantity that is predictive of bibliometric impact.

We also fit a 20 topic DIM model to the ACL data. Here we found a more significant relationship between posterior influence and citation. Specifically, the single-topic model achieved an adjusted R2 of 0.07, i.e., it captured 7% of the variance. The 20 topic model achieved an adjusted R2 of 0.18. This is a marked improvement. Moreover, we can investigate which topics contributed to the signal for further exploratory analysis.

### 5.4 Example influential documents

What are the most influential documents found by the DIM? In the supplementary material we provides a list of documents deemed most influential by the DIM in the ACL Anthology, along with their median citation counts, and Figure 4 shows a distribution of scores, with several outliers labeled. Here the ACL Anthology was prepared per Section 5.2 with  $\sigma_d^2 = 0.00001$  and  $f = 2$ .

**Measuring the influence of terms** To better understand the model, and the regression in Equation 4 in particular, we can see which terms are “pulling” on a specific document. We define the “residual improvement” (RI) as follows. Given a linear regression  $X\beta = Y + E$ , some covariate index  $c$ , and a response index  $r$ , the RI is given by  $(X_{r,-c}\beta_{-c} - Y_r)^2 - E_r^2$ , where the subscript  $-c$  denotes omission of a column or row from these respective vectors. This metric provides an indication of the significance of a covariate in the prediction of a particular feature. In our case, we omit documents to determine their impact on prediction of certain terms changing within the topic. This can be interpreted as the “pull” of individual terms on documents; inversely, it can be interpreted

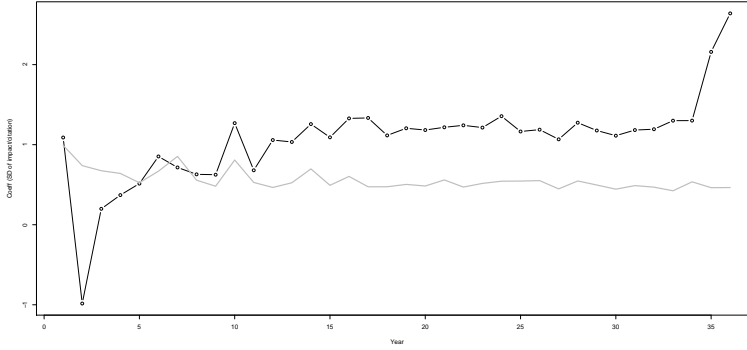


Figure 3: Coefficients of posterior influence regressed on log citations.

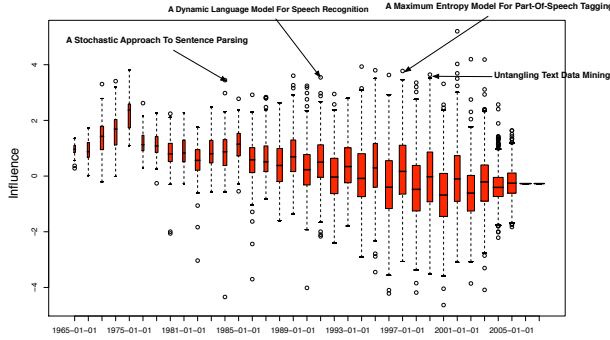


Figure 4: Document weights as a function of date. Titles of outliers are labeled.

as the direction a document helps to “push” a term. We can illustrate this metric with documents having scores at both the high and low extremes in the ACL Anthology.

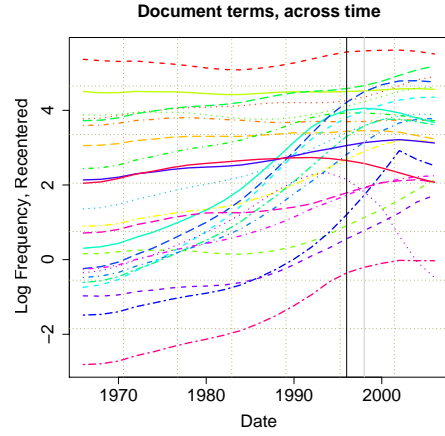
The article *A Maximum Entropy Model For Part-Of-Speech Tagging* was the highest-influence document published in 1996. It had 215 citations in the ACL Anthology. Figure 5 shows this document in greater detail, illustrating a collection of its terms which most closely match the language of the corpus (i.e., have high values in  $\mathbf{W} \circ \phi$ ). The most “significant” term (by RI) that this document is contributing to the language of the topic, for example, is “word”; following this are “model”, “feature”, and “datum”, terms suggestive of the shift toward classification and probabilistic methods in the language of the corpus. The *least* significant term, by contrast, is “identity”; its negative weight, however, is trivial.

*An Ascription-Based Approach To Speech Acts* was the article in the ACL Anthology deemed *least* influential by the model in 1996. In contrast to *A Maximum Entropy Model*, it had zero citations. Figure 5 provides a closer view of this document, illustrating both the dynamics of this document’s vocabulary over time and the terms towards which this document most contributes. Fits for the terms “speech” and “goal” were helped by this document, because its negative score corresponds to these words decreasing when the document appeared. The fit for “example”, however, was hurt by this document; conversely, it pulled this document in the positive direction.

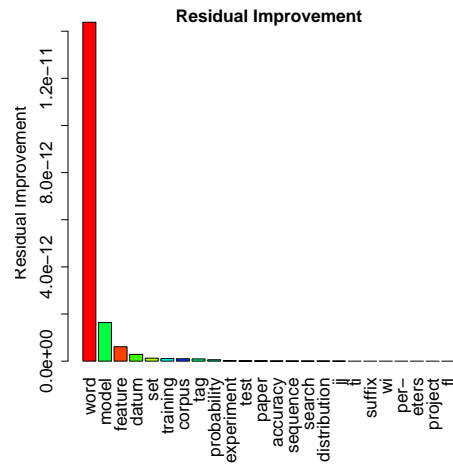
## 6 Discussion and future work

We have presented a model for identifying candidate influential documents, including details of a variational implementation and experiment results. While this model is modest, its good performance in identifying influential documents based solely on the changes in a corpus’s language is a promising start.

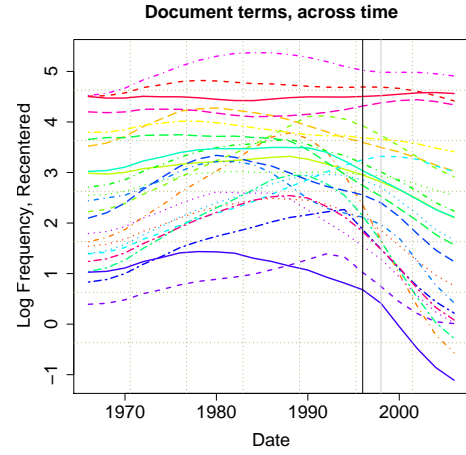
***A Maximum Entropy Model For Part-Of-Speech Tagging***  
**Score: 3.63**



word	accuracy
model	sequence
feature	search
datum	distribution
set	jj
training	ti
corpus	suffix
tag	wi
probability	per-
experiment	eters
test	project
paper	fl



***An Ascription-Based Approach To Speech Acts***  
**Score: -4.22**



speech	number
system	effect
goal	intention
belief	proposition
speaker	environment
representation	attitude
agent	hearer
plan	treatment
act	precondition
level	dialogue
condition	example
theory	set

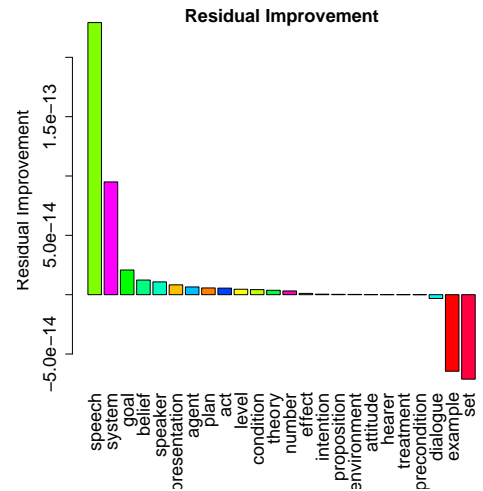


Figure 5: Selected documents from the ACL Anthology having highest and lowest scores in 1996.



In future work we hope to experiment with several variants of this model. We suspect, for example, that a model in which the influence of a document is smeared out over a period of time – through an *envelope* of influence, instead of being applied instantaneously – may be a more realistic model of the influence of a document. We further expect that using a nonnegative prior over the influence of a document will yield a more realistic model of a document’s influence and minimize *post-hoc* transformation of scores such as capping. In addition, we hope to explore a richer set of models of the flow of ideas, including models of topics as birth and death processes (also noted in [12]) and tracking which documents may influence other documents.

We also hope to better understand this model in the context of traditional metrics of influence, such as academic citations, when such metrics are available. Understanding when this model and citation counts differ, for example, will help us to understand where our metric may fall short when applied to corpora in the wild. Furthermore, such comparisons will provide insight not just into this model, but also possibly into shortcomings or assumptions of these well-established metrics.

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