strategy

March 17, 2024

```
[184]: import yfinance as yf
      spy_data = yf.download('SPY', start='2010-01-01', end='2023-12-31')['Adj Close']
      gld_data = yf.download('GLD', start='2010-01-01', end='2023-12-31')['Adj Close']
      vix_data = yf.download('GLD', start='2010-01-01', end='2023-12-31')['Adj Close']
      spy_returns = spy_data.pct_change().dropna()
      gld_returns = gld_data.pct_change().dropna()
      vix_returns = gld_data.pct_change().dropna()
      # spy_annual_returns = (1 + spy_returns).resample('Y').prod() - 1
      # gld_annual_returns = (1 + gld_returns).resample('Y').prod() - 1
      correlation_spy_gold = spy_returns.corr(gld_returns)
      correlation_matrix = pd.concat([spy_returns, gld_returns, vix_returns], axis=1).
       ⇔corr()
      correlation_matrix.columns = ['SPY', 'GLD', 'VIX']
      correlation_matrix.index = ['SPY', 'GLD', 'VIX']
      print(correlation_matrix)
      [********* 100%%********* 1 of 1 completed
      [********* 100%%********* 1 of 1 completed
              SPY
                        GI.D
     SPY 1.000000 0.044096 0.044096
     GLD 0.044096 1.000000 1.000000
     VIX 0.044096 1.000000 1.000000
[164]: import yfinance as yf
      import pandas as pd
      start date = '2017-01-01'
      end date = '2024-01-01'
      # Select 6 random stocks
      stock_symbols = ['GOOGL', 'CYCC', 'NPV', 'AMZN', 'PTLC', 'NFLX']
      # stock_symbols = ['SPY']
      #select Gold eth and volatility (VIX)
      gold_symbol = 'GLD'
      vix_symbol = '^VIX'
```

```
# Retrieve historical data
      stocks_data = yf.download(stock_symbols, start=start_date, end=end_date,_u
        →progress=False)['Adj Close']
      gold_data = yf.download(gold_symbol, start=start_date, end=end_date,_u
        ⇔progress=False)['Adj Close']
      vix_data = yf.download(vix_symbol, start=start_date, end=end_date,__
        →progress=False)['Adj Close']
      stocks_data.head(), gold_data.head(), vix_data.head()
[164]: (Ticker
                        AMZN
                                CYCC
                                          GOOGL
                                                       NFLX
                                                                 NPV
                                                                           PTLC
       Date
       2017-01-03 37.683498 1641.0 40.400501 127.489998 9.640063 22.482380
       2017-01-04 37.859001 1584.0 40.388500 129.410004 9.662382 22.675312
       2017-01-05 39.022499 1608.0 40.651001 131.809998 9.721887 22.665012
       2017-01-06 39.799500 1611.0 41.260502 131.070007 9.692138 22.721207
       2017-01-09 39.846001 1800.0 41.359001 130.949997 9.766520 22.674374,
       Date
       2017-01-03
                    110.470001
       2017-01-04 110.860001
       2017-01-05 112.580002
       2017-01-06
                    111.750000
       2017-01-09
                     112.669998
       Name: Adj Close, dtype: float64,
       Date
       2017-01-03
                     12.85
       2017-01-04
                    11.85
       2017-01-05
                    11.67
       2017-01-06
                     11.32
       2017-01-09
                     11.56
       Name: Adj Close, dtype: float64)
[165]: # Calculate daily returns for the stocks, gold, and VIX
      stock_daily_returns = stocks_data.pct_change().dropna()
      gold_daily_returns = gold_data.pct_change().dropna()
      vix_daily_returns = vix_data.pct_change().dropna()
      # Annualize the daily returns to get a sense of the yearly performance
      # approximately 252 trading days in a year
      stock_annual_returns = (1 + stock_daily_returns).resample('Y').prod() - 1
      gold_annual_returns = (1 + gold_daily_returns).resample('Y').prod() - 1
      vix_annual_returns = (1 + vix_daily_returns).resample('Y').prod() - 1
```

Simulate the \$1 portfolio across the selected stocks for simplicity

Here, I assume equal weighting for each stock in the portfolio

portfolio_daily_returns = stock_daily_returns.mean(axis=1)

```
portfolio_annual_returns = (1 + portfolio_daily_returns).resample('Y').prod() -u
41
annual_returns = pd.DataFrame({
    'Portfolio': portfolio_annual_returns,
    'Gold': gold_annual_returns,
    'VIX': vix_annual_returns
})
annual_returns
Portfolio Gold VIX
```

```
[165]: Portfolio Gold VIX

Date

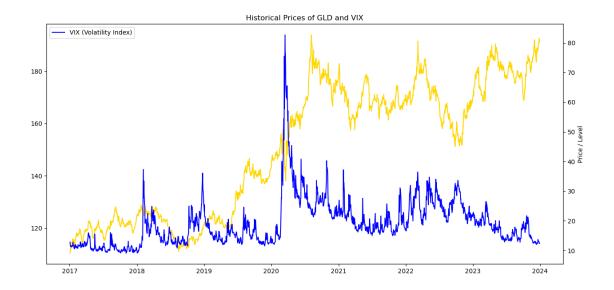
2017-12-31 0.134611 0.119308 -0.140856
2018-12-31 -0.047909 -0.019410 1.302536
2019-12-31 0.297390 0.178557 -0.457907
2020-12-31 0.315459 0.248146 0.650943
2021-12-31 0.093736 -0.041489 -0.243077
2022-12-31 -0.440453 -0.007721 0.258420
2023-12-31 0.179076 0.126916 -0.425473
```

```
[166]: import matplotlib.pyplot as plt
plt.figure(figsize=(15, 7))

# Plot GLD data
plt.plot(gold_data.index, gold_data, label='GLD (Gold ETF)', color='gold')
# plt.plot(stocks_data.index, stocks_data, label='stock', color='red')

# Plot VIX data
plt.twinx()
plt.plot(vix_data.index, vix_data, label='VIX (Volatility Index)', color='blue')
plt.title('Historical Prices of GLD and VIX')
plt.xlabel('Date')
plt.ylabel('Price / Level')
plt.legend(loc='upper left')

plt.show()
```

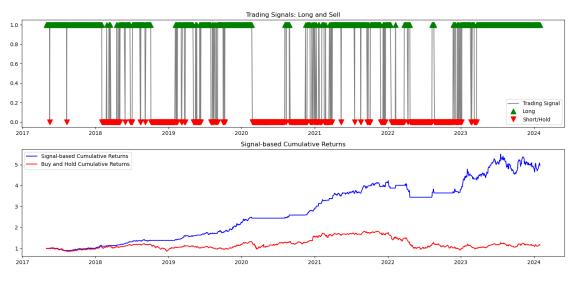


```
[167]: import yfinance as yf
       import pandas as pd
       import numpy as np
       start date = '2017-05-01'
       end_date = '2024-02-01'
       stock_symbols = ['GOOGL', 'CYCC', 'NPV', 'AMZN', 'PTLC', 'NFLX']
       gold symbol = 'GLD'
       vix_symbol = '^VIX'
       stocks_data = yf.download(stock_symbols, start=start_date, end=end_date,_
        →progress=False)['Adj Close']
       gold_data = yf.download(gold_symbol, start=start_date, end=end_date,__
        →progress=False)['Adj Close']
       vix_data = yf.download(vix_symbol, start=start_date, end=end_date,__
        →progress=False)['Adj Close']
       daily_returns = stocks_data.pct_change().fillna(0)
       # Assuming equal weight
       weights = np.full(len(stock_symbols), 1 / len(stock_symbols))
       portfolio_daily_return = daily_returns.dot(weights)
       \# Calculate the indicator: difference between the normalized values of GLD and \sqcup
        \hookrightarrow VTX
       indicator = (gold_data / gold_data.mean()) - (vix_data / vix_data.mean())
       # Generate trading signals based on the indicator: 1 for long, 0 for hold
       signals = np.where(indicator > 0, 1, 0)
```

```
trading_returns = portfolio_daily_return * signals
       # cumulative returns
       signal_cumulative_returns = (1 + trading_returns).cumprod()
       # Buy-and-hold strategy
       buy_and_hold_cumulative_returns = (1 + portfolio_daily_return).cumprod()
       comparison = pd.DataFrame({
           'Signal-Based': signal cumulative returns,
           'Buy-and-Hold': buy_and_hold_cumulative_returns
       })
       comparison
[167]:
                   Signal-Based Buy-and-Hold
      Date
       2017-05-01
                       1.000000
                                     1.000000
       2017-05-02
                       1.008387
                                     1.008387
       2017-05-03
                       0.998085
                                     0.998085
       2017-05-04
                       0.992450
                                     0.992450
       2017-05-05
                       0.984348
                                     0.984348
       2024-01-25
                       4.948815
                                     1.151569
       2024-01-26
                       4.982716
                                     1.159458
       2024-01-29
                       5.083900
                                     1.183003
       2024-01-30
                       5.018424
                                     1.167767
       2024-01-31
                       4.943985
                                     1.150446
       [1700 rows x 2 columns]
[187]: import matplotlib.pyplot as plt
       signals_df = pd.DataFrame(signals, index=stocks_data.index, columns=['Signal'])
       signal_cumulative_returns_df = pd.DataFrame(signal_cumulative_returns,_u
        →index=stocks_data.index, columns=['Cumulative Returns'])
       plt.figure(figsize=(15, 7))
       #Long (1) as green, sell (0) as red
       plt.subplot(2, 1, 1)
       plt.plot(signals_df.index, signals_df['Signal'], label='Trading Signal', |
        ⇔color='gray')
       plt.plot(signals_df[signals_df['Signal'] == 1].index,__
        ⇔signals_df['Signal'][signals_df['Signal'] == 1], '^', label='Long', □
        ⇔color='green', markersize=10)
```

Apply the signals to the portfolio's daily returns

```
plt.plot(signals_df[signals_df['Signal'] == 0].index,__
 signals_df['Signal'][signals_df['Signal'] == 0], 'v', label='Short/Hold',
 ⇔color='red', markersize=10)
plt.title('Trading Signals: Long and Sell')
plt.legend()
# Plot the signal-based cumulative returns
plt.subplot(2, 1, 2)
plt.plot(signal_cumulative_returns_df.index,__
 signal_cumulative_returns_df['Cumulative_Returns'], label='Signal-based_
 →Cumulative Returns', color='blue')
plt.plot(buy and hold cumulative returns, label='Buy and Hold Cumulative_1
 →Returns', color="red")
plt.title('Signal-based Cumulative Returns')
plt.legend()
plt.tight_layout()
plt.show()
```



```
[169]: trading_returns = portfolio_daily_return * signals
    trading_returns_percentage = trading_returns * 100
    trading_returns_percentage.name = 'Trading Returns (%)'
    trading_returns_percentage.to_csv('trading_returns.csv', index=True)
    print(trading_returns_percentage)
```

Date 2017-05-01 0.000000 2017-05-02 0.838702 2017-05-03 -1.021645 2017-05-04 -0.564590

```
2017-05-05
                -0.816389
     2024-01-25
                 1.333816
     2024-01-26
                 0.685030
     2024-01-29
                 2.030713
     2024-01-30
                -1.287917
     2024-01-31
                -1.483310
     Name: Trading Returns (%), Length: 1700, dtype: float64
[170]: spy_returns.corr(trading_returns_percentage)
[170]: 0.20344650814113435
[171]: factors_df = pd.read_csv('ff_research.csv', index_col=0)
      factors df.index = pd.to datetime(factors df.index, format='\%Y\mathbb{m}\mathbb{d}\d')
      factors_df
[171]:
                Mkt-RF
                        SMB
                             HML
                                  RMW
                                        CMA
                                               R.F
                 0.21 0.25 -0.13 -0.17 -0.50 0.003
      2017-05-01
                  0.03 -0.47 -0.21 0.40 -0.35 0.003
      2017-05-02
      2017-05-03 -0.19 -0.52 0.22 -0.04 0.13 0.003
      2024-01-25
                 0.46 0.20 0.56 -0.19 0.55 0.022
      2024-01-26 -0.02 0.35 -0.27 0.22 -0.02 0.022
      2024-01-30 -0.13 -0.96 0.84 1.00 0.13 0.022
      2024-01-31 -1.74 -0.89 -0.30 -0.21 0.37 0.022
      [1700 rows x 6 columns]
[172]: CVNA = yf.download('CVNA', start='2017-05-01', end='2024-02-01')['Adj Close']
      COST = yf.download('CVNA', start='2017-05-01', end='2024-02-01')['Adj Close']
      cvna_daily_return = CVNA.pct_change().fillna(0)
      cost_daily_return = COST.pct_change().fillna(0)
      cvna daily return.name = "cvna"
      cost_daily_return.name = "cost"
     [******** 100%%********* 1 of 1 completed
     [******** 100%%********* 1 of 1 completed
[173]: print(trading_returns_percentage)
      print(CVNA)
      print(COST)
      print(factors_df)
      combined data = pd.concat([trading_returns_percentage, cvna_daily_return,_
       ⇔cost_daily_return, factors_df], axis=1)
```

combined_data

```
Date
2017-05-01
              0.000000
2017-05-02
              0.838702
2017-05-03
             -1.021645
2017-05-04
             -0.564590
2017-05-05
             -0.816389
2024-01-25
              1.333816
2024-01-26
              0.685030
2024-01-29
              2.030713
2024-01-30
             -1.287917
2024-01-31
             -1.483310
Name: Trading Returns (%), Length: 1700, dtype: float64
Date
2017-05-01
              10.770000
2017-05-02
              10.100000
2017-05-03
               8.720000
2017-05-04
               9.980000
2017-05-05
              10.920000
2024-01-25
              41.000000
2024-01-26
              41.799999
2024-01-29
              44.919998
2024-01-30
              44.139999
2024-01-31
              43.060001
Name: Adj Close, Length: 1700, dtype: float64
Date
2017-05-01
              10.770000
2017-05-02
              10.100000
2017-05-03
               8.720000
2017-05-04
               9.980000
2017-05-05
              10.920000
2024-01-25
              41.000000
2024-01-26
              41.799999
2024-01-29
              44.919998
2024-01-30
              44.139999
2024-01-31
              43.060001
Name: Adj Close, Length: 1700, dtype: float64
            Mkt-RF
                     SMB
                                        CMA
                           HML
                                  RMW
                                                RF
2017-05-01
              0.21 0.25 -0.13 -0.17 -0.50
                                            0.003
              0.03 -0.47 -0.21 0.40 -0.35
2017-05-02
                                             0.003
2017-05-03
             -0.19 -0.52 0.22 -0.04 0.13
                                             0.003
2017-05-04
              0.02 -0.13 -0.36 0.36 -0.71
                                             0.003
              0.46 0.11 0.00 -0.22 0.65
2017-05-05
                                             0.003
```

```
2024-01-25
                   0.46 0.20 0.56 -0.19 0.55 0.022
      2024-01-26
                  -0.02 0.35 -0.27 0.22 -0.02 0.022
      2024-01-29
                  0.85 0.89 -0.59 -1.13 -0.31
                                                 0.022
                  -0.13 -0.96 0.84 1.00 0.13 0.022
      2024-01-30
                  -1.74 -0.89 -0.30 -0.21 0.37 0.022
      2024-01-31
      [1700 rows x 6 columns]
[173]:
                  Trading Returns (%)
                                                          Mkt-RF
                                                                   SMB
                                                                         HML
                                           cvna
                                                    cost
                                                                              RMW \
                             0.000000 0.000000 0.000000
                                                            0.21 0.25 -0.13 -0.17
      2017-05-01
      2017-05-02
                             0.838702 -0.062210 -0.062210
                                                            0.03 -0.47 -0.21 0.40
                            -1.021645 -0.136634 -0.136634
                                                           -0.19 -0.52 0.22 -0.04
      2017-05-03
                                                            0.02 -0.13 -0.36 0.36
      2017-05-04
                            -0.564590 0.144495 0.144495
      2017-05-05
                            -0.816389 0.094188 0.094188
                                                            0.46 0.11 0.00 -0.22
                                                             •••
      2024-01-25
                             1.333816 -0.024506 -0.024506
                                                            0.46 0.20 0.56 -0.19
      2024-01-26
                             0.685030 0.019512 0.019512
                                                           -0.02 0.35 -0.27 0.22
                             2.030713 0.074641 0.074641 0.85 0.89 -0.59 -1.13
      2024-01-29
      2024-01-30
                            -1.287917 -0.017364 -0.017364
                                                           -0.13 -0.96 0.84 1.00
                           -1.483310 -0.024468 -0.024468 -1.74 -0.89 -0.30 -0.21
      2024-01-31
                   CMA
                           RF
      2017-05-01 -0.50
                        0.003
      2017-05-02 -0.35
                        0.003
      2017-05-03 0.13
                        0.003
      2017-05-04 -0.71
                        0.003
      2017-05-05 0.65 0.003
      2024-01-25 0.55 0.022
      2024-01-26 -0.02 0.022
      2024-01-29 -0.31 0.022
      2024-01-30 0.13 0.022
      2024-01-31 0.37 0.022
      [1700 rows x 9 columns]
[189]: combined_data[['Trading Returns (%)','cvna', 'cost','Mkt-RF', 'RF']].corr()
[189]:
                           Trading Returns (%)
                                                             cost
                                                                     Mkt-RF \
                                                   cvna
      Trading Returns (%)
                                      1.000000 0.186368 0.186368 0.214614
                                              1.000000
      cvna
                                      0.186368
                                                         1.000000 0.448296
      cost
                                      0.186368
                                              1.000000
                                                         1.000000 0.448296
      Mkt-RF
                                      0.214614 0.448296
                                                         0.448296 1.000000
      RF
                                      0.009322 0.033140 0.033140 -0.010049
```

RF

```
Trading Returns (%) 0.009322
cvna 0.033140
cost 0.033140
Mkt-RF -0.010049
RF 1.000000
```

```
[190]: import statsmodels.api as sm
Y = combined_data['Trading Returns (%)']
X = combined_data[['cvna', 'cost', 'Mkt-RF', 'RF']]
X = sm.add_constant(X)

model = sm.OLS(Y, X).fit()
print(model.summary())
```

OLS Regression Results

Dep. Variable:	Trading Returns (%)	R-squared:	0.056
Model:	OLS	Adj. R-squared:	0.055
Method:	Least Squares	F-statistic:	33.72
Date:	Sun, 17 Mar 2024	<pre>Prob (F-statistic):</pre>	3.64e-21
Time:	16:37:03	Log-Likelihood:	-2333.2
No. Observations:	1700	AIC:	4674.
Df Residuals:	1696	BIC:	4696.
DC W 1 3			

Df Model: 3
Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025	0.975]
const cvna cost Mkt-RF RF	0.0805 0.8223 0.8223 0.1275 1.0678	0.033 0.193 0.193 0.020 3.480	2.421 4.259 4.259 6.222 0.307	0.016 0.000 0.000 0.000 0.759	0.015 0.444 0.444 0.087 -5.757	0.146 1.201 1.201 0.168 7.893
Omnibus: Prob(Omnibus) Skew: Kurtosis:	:	295.781 0.000 0.383 10.413		•		2.006 3933.997 0.00 3.75e+16

Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The smallest eigenvalue is 1.95e-30. This might indicate that there are strong multicollinearity problems or that the design matrix is singular.

```
[176]: coefs = pd.DataFrame({
    'Coefficients': model.params,
    'Standard Error': model.bse,
    't Stat': model.tvalues,
    'P-value': model.pvalues,
    'Lower 95%': model.conf_int()[0],
    'Upper 95%': model.conf_int()[1]
})
print(coefs)
```

```
Coefficients Standard Error
                                      t Stat
                                                   P-value Lower 95% \
const
           0.080489
                           0.033253 2.420527 1.560249e-02
                                                             0.015268
                                                             0.443634
cvna
           0.822334
                           0.193080 4.259033 2.165702e-05
                           0.193080 4.259033 2.165702e-05
           0.822334
                                                             0.443634
cost
Mkt-RF
           0.127466
                           0.020486 6.221973 6.171428e-10
                                                             0.087285
RF
           1.067766
                           3.479747 0.306852 7.589940e-01 -5.757284
       Upper 95%
```

const 0.145709 cvna 1.201035 cost 1.201035 Mkt-RF 0.167647 RF 7.892816