

Determinant of 2x2 Matrix

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$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \quad \det(A) = ad - bc$$

$$B = \begin{bmatrix} 3 & 5 \\ -1 & 1 \end{bmatrix} \quad \begin{aligned} \det(B) &= (3)(1) - (-5)(-1) \\ &= 3 + 5 \\ &= 8 \end{aligned}$$

Inverse of a 2x2 Matrix

$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \quad A^{-1} = \frac{1}{|A|} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$$

$$B = \begin{bmatrix} 3 & -4 \\ -1 & 2 \end{bmatrix} \quad \begin{aligned} \det(B) &= (3)(2) - (-4)(-1) \\ &= 2 \end{aligned}$$

$$B^{-1} = \frac{1}{2} \begin{bmatrix} 3 & 4 \\ -1 & 2 \end{bmatrix} = \begin{bmatrix} 1.5 & 2 \\ -0.5 & 1 \end{bmatrix}$$

4x4 matrix Addition

$$\begin{bmatrix} 1 & 6 & 4 & 5 \\ 4 & -4 & 8 & 6 \\ 4 & -4 & 8 & 7 \\ 4 & -4 & 8 & -9 \end{bmatrix} + \begin{bmatrix} 2 & -6 & 9 & -4 \\ 4 & 5 & -1 & -3 \\ 4 & 5 & -1 & 7 \\ 4 & -2 & 5 & -1 \end{bmatrix} = \begin{bmatrix} 3 & 0 & 13 & 1 \\ 8 & 1 & 7 & 3 \\ 8 & 1 & 7 & 14 \\ 8 & -6 & 13 & -10 \end{bmatrix}$$

4x4 Matrix Subtraction

$$\begin{bmatrix} 1 & 6 & 4 & 5 \\ 4 & -4 & 8 & 6 \\ 4 & -4 & 8 & 7 \\ 4 & -4 & 8 & -9 \end{bmatrix} - \begin{bmatrix} 2 & -6 & 9 & -4 \\ 4 & 5 & -1 & -3 \\ 4 & 5 & -1 & 7 \\ 4 & -2 & 5 & -1 \end{bmatrix} = \begin{bmatrix} -1 & 12 & -5 & 9 \\ 0 & -9 & 9 & 9 \\ 0 & -9 & 9 & 0 \\ 0 & -2 & 3 & -8 \end{bmatrix}$$

4x4 Matrix Multiplication

$$\begin{bmatrix} 1 & 6 & 4 & 5 \\ 4 & -4 & 8 & 6 \\ 4 & -4 & 8 & 7 \\ 4 & -4 & 8 & -9 \end{bmatrix} \begin{bmatrix} 2 & -6 & 9 & -4 \\ 4 & 5 & -1 & -3 \\ 4 & 5 & -1 & 7 \\ 4 & -2 & 5 & -1 \end{bmatrix}$$

$$\begin{aligned} & (1 \times 2 + 6 \times 4 + 4 \times 4 + 5 \times 4) = 34 \quad (1 \times -6 + 6 \times 5 + 4 \times 5 + 5 \times -2) = 34 \\ & (1 \times 9 + 6 \times (-1) + 4 \times (-1) + 5 \times 5) = 24 \quad (1 \times -4 + 6 \times -3 + 4 \times 7 + 5 \times (-1)) = 1 \\ & (4 \times 2 + -4 \times 4 + 8 \times 4 + 6 \times 4) = 48 \quad (4 \times -6 + (-4) \times 5 + 8 \times 5 + 6 \times (-2)) = -16 \\ & (4 \times 9 + -4 \times -1 + 8 \times (-1) + 6 \times 5) = 62 \quad (4 \times -4 + -4 \times -3 + 8 \times 7 + 6 \times -1) = 46 \\ & (4 \times 2 + -4 \times 4 + 8 \times 4 + 7 \times 4) = 52 \quad (4 \times -6 + -4 \times 5 + 8 \times 5 + 7 \times -2) = -18 \\ & (4 \times 9 + -4 \times -1 + 8 \times -1 + 7 \times 5) = 67 \quad (4 \times -4 + -4 \times -3 + 8 \times 7 + 7 \times -1) = 45 \\ & (4 \times 2 + -4 \times 4 + 8 \times 4 + -9 \times 4) = -12 \quad (4 \times -6 + -4 \times 5 + 8 \times 5 + -9 \times -2) = 14 \\ & (4 \times 9 + (-4) \times (-1) + 8 \times -1 + -9 \times 5) = -13 \quad (4 \times -4 + -4 \times -3 + 8 \times 7 + -9 \times -1) = 61 \end{aligned}$$

$$= \begin{bmatrix} 34 & 24 & 48 & 62 \\ 46 & -18 & 67 & 45 \\ -12 & 14 & -13 & 61 \end{bmatrix}$$

Cross Product of 2 Vectors.

$$\vec{a} = \begin{bmatrix} a_1 \\ a_2 \\ a_3 \end{bmatrix} \quad \vec{b} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix} \quad \vec{a} \times \vec{b} = \begin{bmatrix} a_2 b_3 - a_3 b_2 \\ a_3 b_1 - a_1 b_3 \\ a_1 b_2 - a_2 b_1 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ -7 \\ 1 \end{bmatrix} \times \begin{bmatrix} 5 \\ 2 \\ 4 \end{bmatrix} = \begin{bmatrix} -7 \cdot 4 - 1 \cdot 2 \\ 1 \cdot 5 - (-7) \cdot 4 \\ 1 \cdot 2 - (-7) \cdot 5 \end{bmatrix} = \begin{bmatrix} -30 \\ 1 \\ 37 \end{bmatrix}$$