

## Homework 2 Written

The pdf you submit must look exactly like this with the answers and all supporting works shown on the the page with the question.

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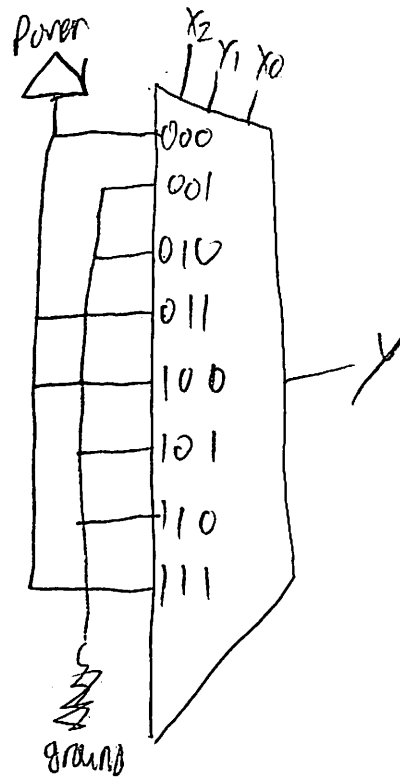
Partner First Name

Partner Student ID

1. (4 points) Given only an 8-1 multiplexer and constants 0 and 1 implement a circuit that behaves like the following function:  $m_0 + m_3 + m_4 + m_7$ . There are 3 input variables for this problem  $x_2, x_1, x_0$ .

First draw a truth table

$x_2$	$x_1$	$x_0$	$y$
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

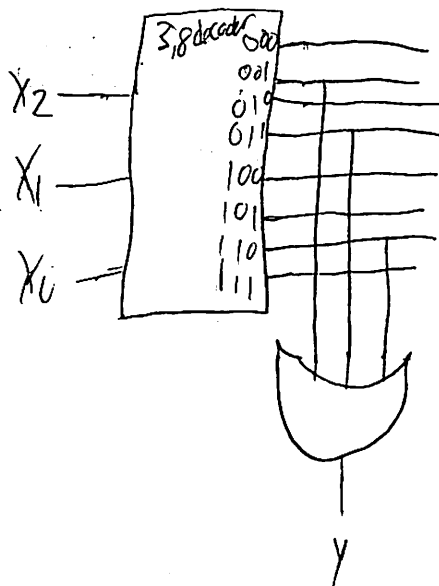


2. (3 points) Given only an 3-8 one hot decoder and an OR gate implement a circuit that behaves like the following function:  $m_1 + m_3 + m_6$  There are 3 input variables for this problem

$x_2, x_1, x_0$

Truth table

$x_2$	$x_1$	$x_0$	$y$
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	0



3. (3) Given only a mux, a not gate, and a 2 input OR gate implement a circuit that behaves like the following function:  $M_2 \times M_4 \times M_6$ . There are 3 input variables for this problem  $x_2, x_1, x_0$ .

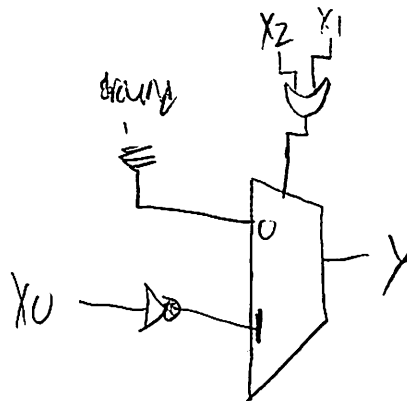
	$x_2$	$x_1$	$x_0$	$Y$
0	0	0	0	1
1	0	0	1	1
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	1
6	1	1	0	0
7	1	1	1	1

$x_2 \backslash x_0$	00	01	11	10
0	1	0	0	0
1	1	1	1	1

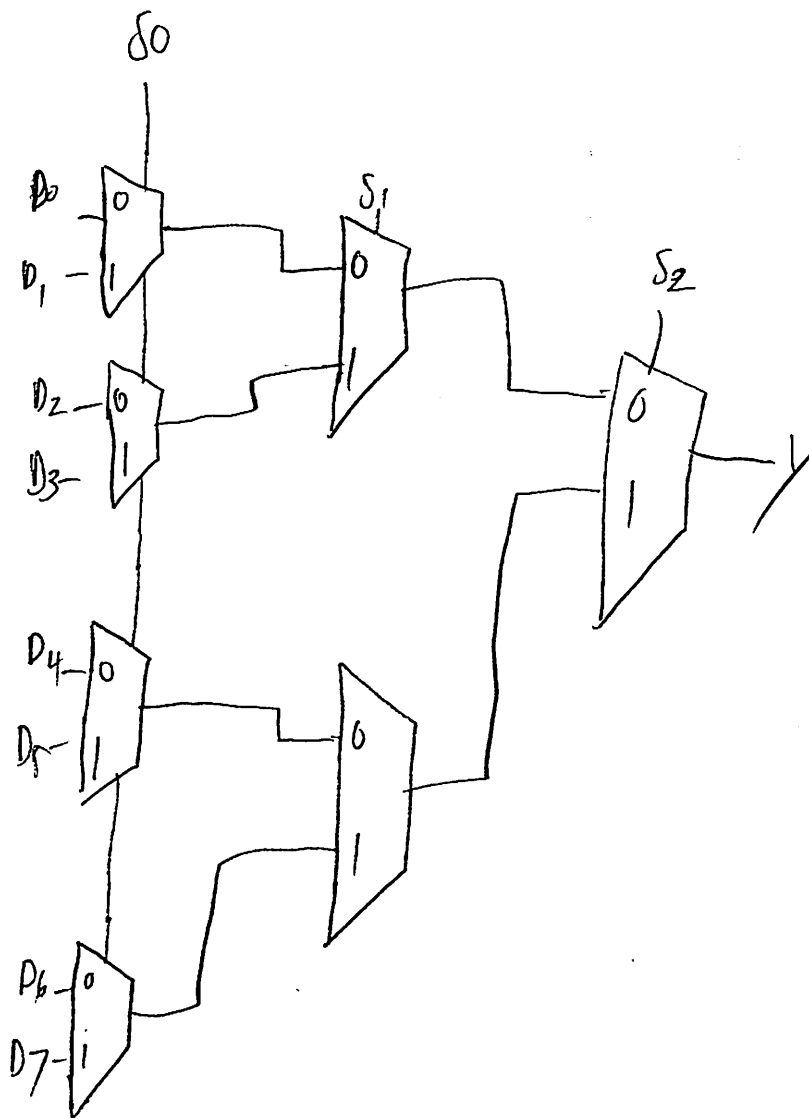
POS:  $(x_0 + \bar{x}_1)(x_0 + \bar{x}_2)$

SOP:  $\bar{x}_2 \bar{x}_1 + x_0$

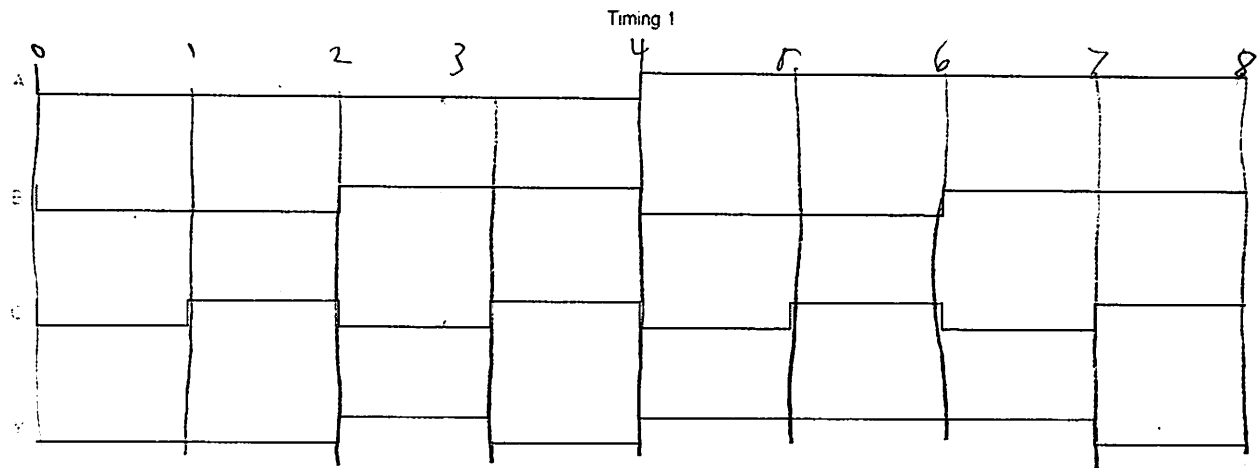
$x_2$	$x_1$	$Y$
0	1	$\bar{x}_0$
1	0	$\bar{x}_0$
1	1	$\bar{x}_0$



4. (3 points) Use only 2 – 1 multiplexers to create an 8-1 multiplexer.

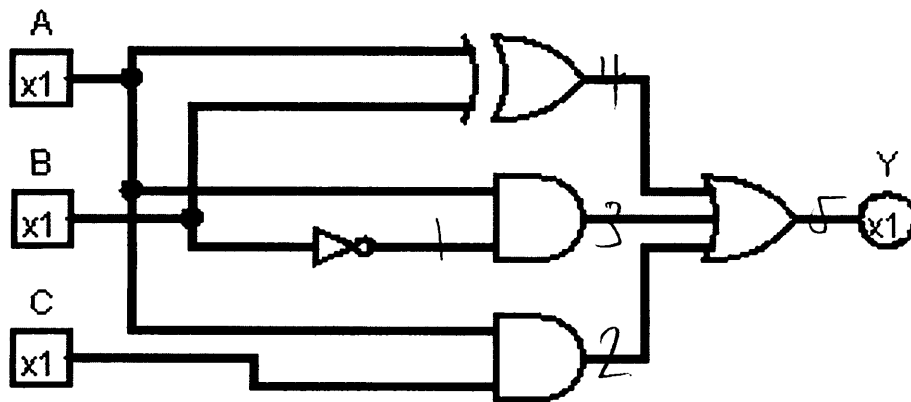


5. (4) Fill in the truth table based on the following timing diagram. Assume no delays in the circuit.



A	B	C	Y
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	0

6. (8) Give the following circuit and delays complete the timing diagram.



Element	Delay
NOT	1
AND	2
XOR	4
OR	1

$$Y = (A \oplus B) + (\bar{B}A) + (AC)$$

A	B	C	Y
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1

# Timing 2

A 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100

B 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100

C 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100

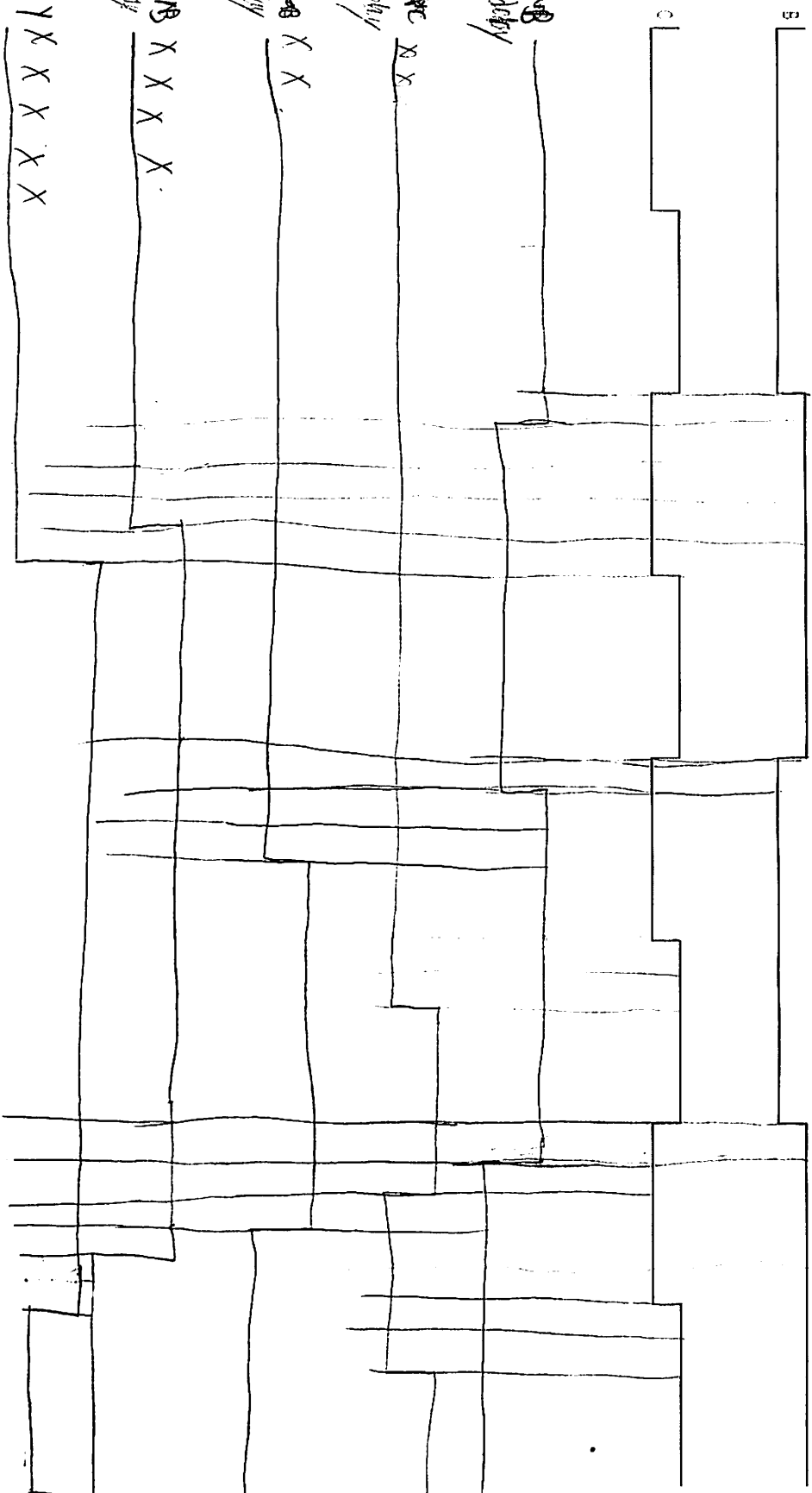
SB  
1 day

AC  
2 day

ACB  
2 day

ANB  
4 day

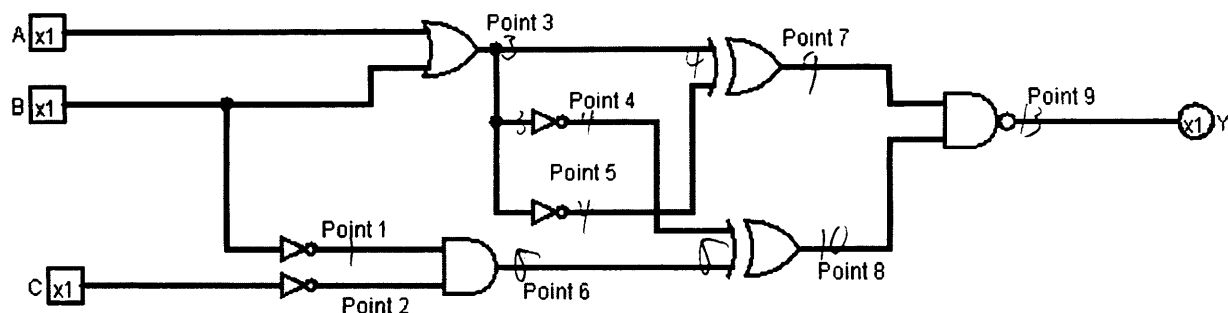
S delay





7. (4.5 points) Given the following circuit and the propagation delays in the following table, what are the propagation delays at each marked point? There are 9 separate points.

Component	Delay
Not	1 ns
OR	3 ns
XOR	5 ns
NAND	3 ns
AND	4 ns

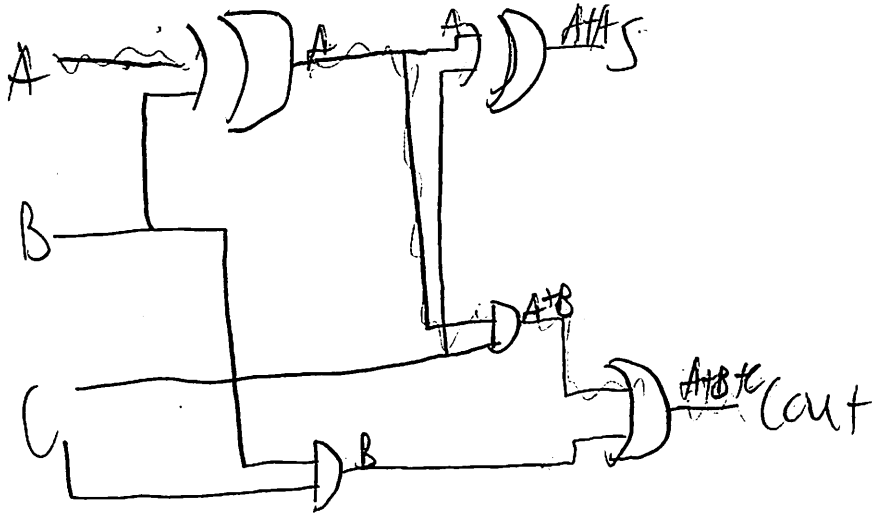


Point	Delay
1	1
2	1
3	3
4	4
5	4
6	5
7	9
8	10
9	13

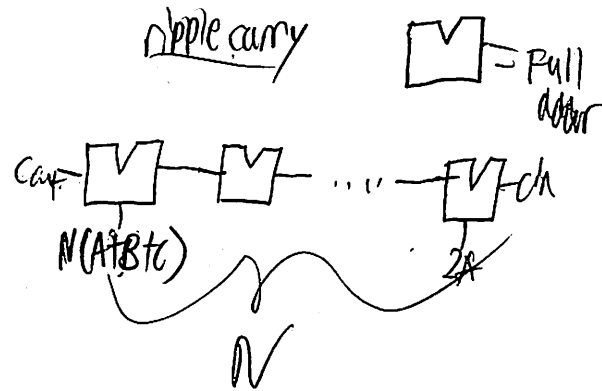
8. (3 points) Given that each XOR gate has a delay of  $A$  ns, each AND gate has a delay of  $B$  ns, and each OR gate has a delay of  $C$  ns, what is the propagation delay of the worst case path in an  $N$  bit ripple carry adder? Assume that the delays between the elements are close enough that the worst case path is the one that contains the most elements along it.

For the worst case path, the signal must pass through the most gates. In an N-bit ripple carry adder, the worst case path is the one that contains the most elements along it. The delay is  $4N$ .

For a full adder it has 2 XOR gates, 2 ANDs, and 1 OR gate. A ripple carry adder uses  $N$  full adders for it to work. To get the propagation delays we need to calculate the propagation delay for a Full adder and multiply it by  $N$ .



XOR =  $A+B$   
 AND =  $AB$   
 OR =  $C$



$$N(A+B+C)$$