

# Government 10: Quantitative Political Analysis

Sean Westwood

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  - ▶ There is a relationship between both height and income, and attractiveness, but the effects of our predictors are not consistent.
  - ▶ Observation: tall poor people are seen as just as attractive as short rich people.



## Visualizing this relationship



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- ▶ Is the relationship between educational attainment and political participation different for men and women?
- ▶ Does the effect of perceived national security threats on immigration attitudes differ among liberals and conservatives?

## What is an interaction term?

An interaction term in regression captures the combined effect of two (or more) variables on the outcome, beyond their individual effects.

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Now let's account for the interaction:

$$\text{VoterSupport} = \alpha + \beta_1 \text{EconPerf} + \beta_2 \text{RegimeType} + \beta_3 (\text{EconPerf} \times \text{RegimeType}) + \mu$$

## The components of an interaction model

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- ▶  $\mu$  represents the error term

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Interpretation Tips: - A positive interaction term means the effect of one variable increases when the other variable increases. - A negative interaction term means the effect of one variable decreases as the other variable increases. - Example: If  $\beta_3$  is positive, higher education might increase income more for men than for women (or vice versa if negative).

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$$\text{Expected Political Participation} = 10.01 + 3.22 \times 15 + (-1.87) \times 1 + 1.5 \times (15 \times 1) = 78.94$$



# National security threats, immigration attitudes, and ideology

Does the effect of perceived national security threats on immigration attitudes differ among liberals and conservatives?

$$\text{Expected Immigration Attitude} = \alpha + \beta_1 \times \text{NationalSecurityThreat} + \beta_2 \times \text{PoliticalIdeology} + \beta_3 \times (\text{NationalSecurityThreat} \times \text{PoliticalIdeology})$$

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What is the expected immigration attitudes for liberals where national security threat is 10

$$\text{Expected Immigration Attitude} = 20 + 1.5 \times 10 - 5 + 2 \times (10 \times 1) = 50$$

# How to run a model with an interaction term in R

Running a model with interaction between Education and Gender

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```
model <- lm(Income ~ Education * Gender, data = dataset)
```

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- ▶ Example: How does media consumption influence political beliefs?
- ▶ Importance: Drives the research by clarifying the issue, variables, and possible directions of investigation.

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- ▶ Purpose: To create a foundation for empirical testing and establish expectations for research outcomes.

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- ▶ **Regression Model:**

$$\text{Voter Turnout} = \alpha + \beta_1 \times \text{Community Engagement} + \beta_2 \times \text{Education} + \beta_3 \times \text{Income}$$

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- ▶ **Regression Model:**

$$\text{Trust in Government} = \alpha + \beta_1 \times \text{Economic Inequality} + \beta_2 \times \text{Education} + \beta_3 \times \text{Political Ideology}$$



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- ▶ **Regression Model:**

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### ► Regression Model:

$$\text{Political Ideology} = \alpha + \beta_1 \times \text{Education Level} + \beta_2 \times \text{Income} + \beta_3 \times \text{Age}$$