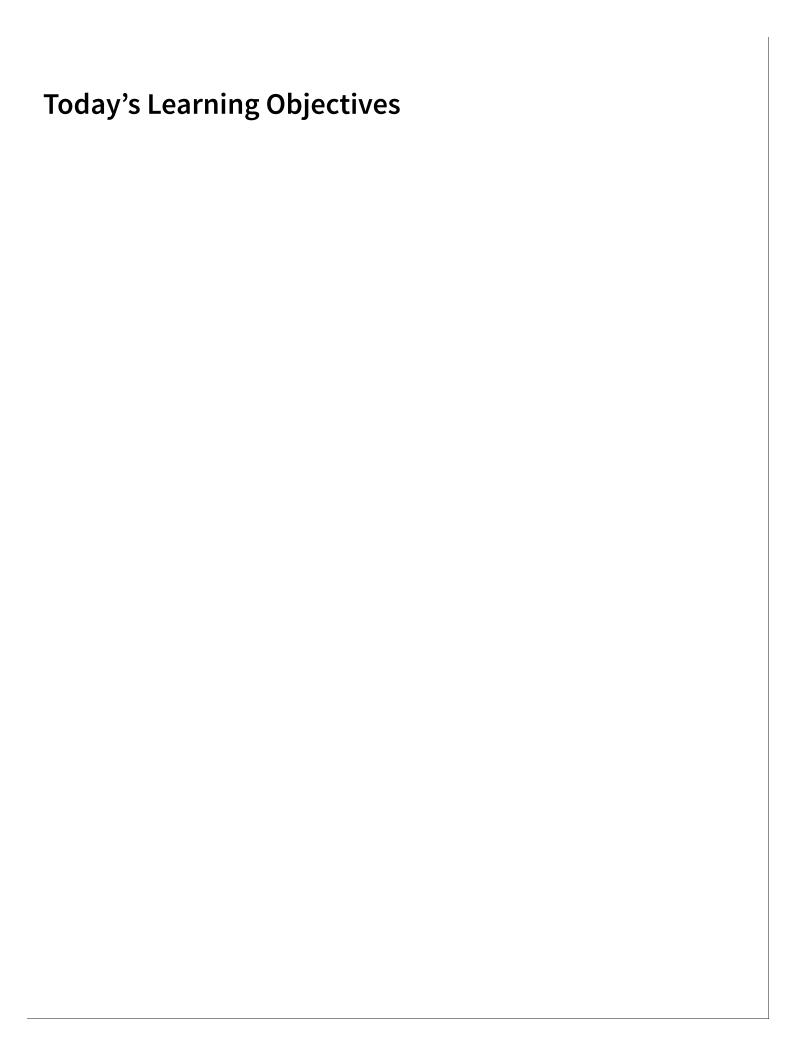
Week 2, Class 4

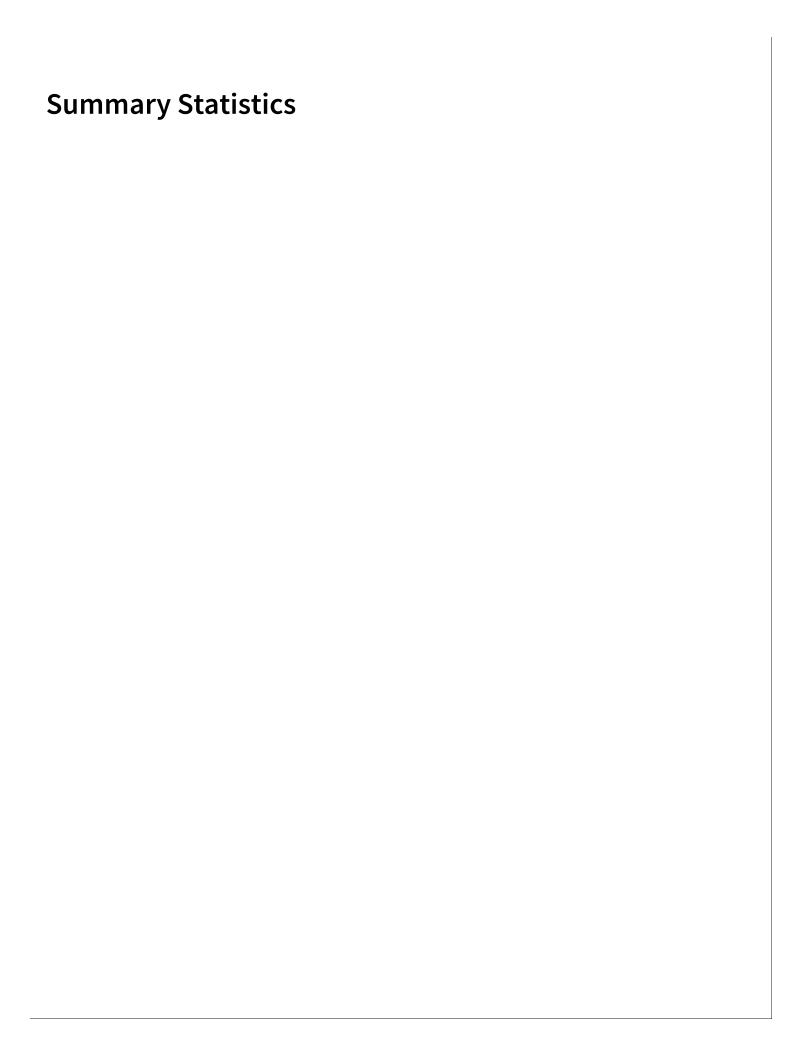
Summary Statistics

Sean Westwood



By the End of Class You Will:

- Understand central tendency: mean, median, mode
- Know when to use each measure of center
- Calculate measures of spread: range, variance, standard deviation
- Use group_by() and summarise() for data analysis



Why Do We Need Summary Statistics?

The Problem: Raw data with thousands of observations is overwhelming

The Solution: Summary statistics reduce complexity while preserving key

information

Goal: Describe the "typical" or "central" value in our data

Congressional Approval Example

Congressional approval helps us understand public trust in political institutions **Dataset Description**:

- congress_approval: Approval rating for Congress (0-100 scale)
- party_id: Respondent's party affiliation (Democrat, Republican, Independent)
- age: Respondent's age
- education: Education level (High School, Some College, Bachelor's, etc.)
- income_category: Income bracket (\$30k-\$60k, etc.)
- region: Geographic region (Midwest, South, etc.)

```
# A tibble: 10 × 7
   respondent_id age education
                                    party_id
                                                 income_category region
           <dbl> <dbl> <chr>
                                     <chr>
                                                 <chr>
                  31 Some College Independent $30k-$60k
                    68 Bachelor's Republican $30k-$60k
                                                                 South
                   41 Some College Republican
                                                 $30k-$60k
                                                                  South
                    75 Bachelor's Democrat
19 Some College Democrat
                                    Democrat
                                                                  South
                                                 $60k-$100k
                                                                 West
                    55 Some College Republican
                                                 $30k-$60k
                                                                 South
                    27 Some College Democrat
                                                 $60k-$100k
                                                                 Midwest
                    49 High School Republican
                                                Under $30k
                                                                 West
                                    Republican Under $30k
                    57 Bachelor's
                                                                 Midwest
              10
                   56 High School Democrat
10
                                                 Over $100k
                                                                 South
# i 1 more variable: congress_approval <dbl>
```

The Mean (Average)

$$\bar{x} = \frac{\sum_{i=1}^{n} x_i}{n}$$

What this notation means:

- \bar{x} (x-bar): The sample mean
- $\sum_{i=1}^{n}$: Sum from the first observation (i=1) to the last (i=n)
- x_i : Each individual value in our dataset
- n: Total number of observations

```
1 # Calculate mean approval rating
2 mean_approval <- mean(approval$congress_approval, na.rm = TRUE)
3 mean_approval</pre>
```

[1] 28.70509

Interpretation: On average, presidential approval was 28.7%

The Median (Middle Value)

Definition: The value that splits the data in half

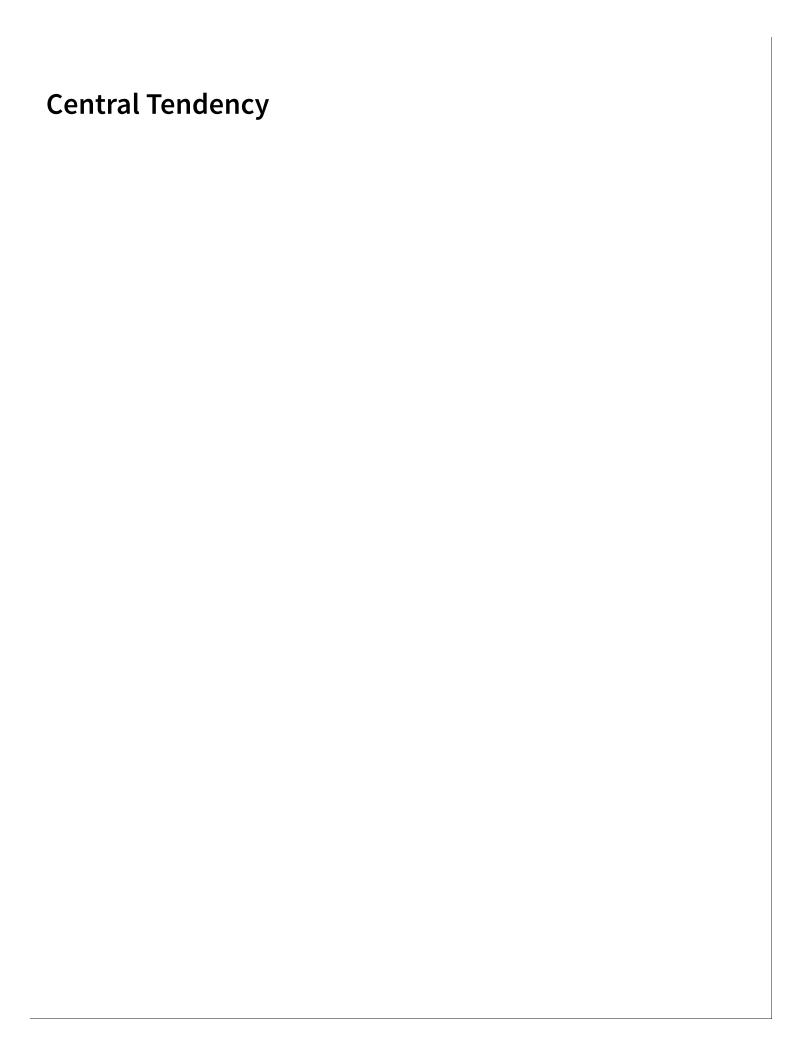
```
# Calculate median approval rating
median_approval <- median(approval$congress_approval, na.rm = TRUE)
median_approval</pre>
```

[1] 28.50776

The Mode (Most Common Value)

Definition: The value that appears most frequently

```
# Find mode using count
approval %>%
count(congress_approval, sort = TRUE) %>%
head(5)
```



What is Central Tendency?

Definition: Central tendency describes where the "center" or "typical" value of a dataset lies.

Three main measures:

- 1. Mean (average): Mathematical center
- 2. Median (middle): Positional center
- 3. Mode (most common): Most frequent value

Key Insight: Different measures of central tendency can tell different stories about the same data, especially when distributions are skewed or have outliers

When Distributions Aren't Symmetric

Real data often has:

- Outliers: Extreme values that don't fit the typical pattern
- Skewness: Data stretched more in one direction than the other
- Multiple modes: More than one common value

Why this matters: Different shapes require different approaches to finding the "typical" value

Understanding Outliers

Definition: Data points that are unusually far from other observations **Examples in political data**:

- A presidential approval rating of 90% during a crisis
- A candidate spending \$500 million in a typical House race
- A voter turnout of 95% in a large precinct

Impact on measures:

- Mean: Very sensitive to outliers (gets "pulled" toward them)
- Median: Resistant to outliers (stays stable)
- Mode: Usually unaffected by outliers

Understanding Skewness

Left-skewed (negative skew):

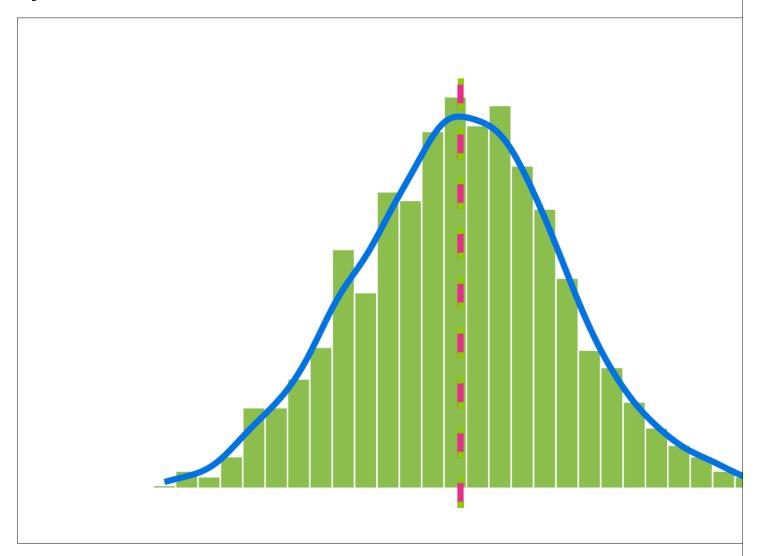
- Long tail extends toward lower values
- Mean < Median
- Example: Test scores when most students do well

Right-skewed (positive skew):

- Long tail extends toward higher values
- Mean > Median
- Example: Income data (few very wealthy people)

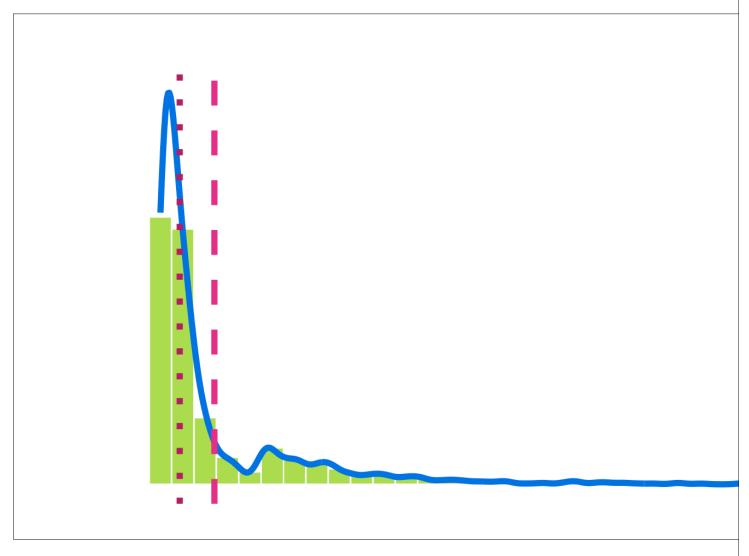
Campaign spending, wealth, and many political variables are typically rightskewed

Symmetric Distribution



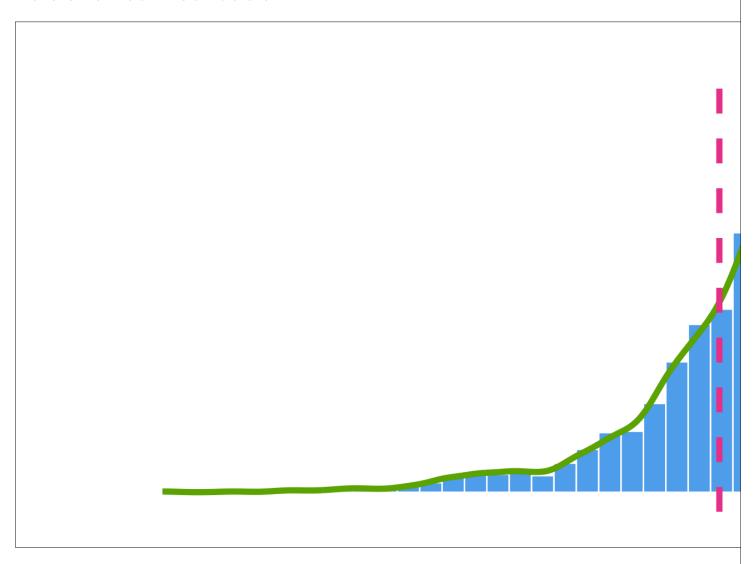
All three measures are similar

Right-Skewed Distribution

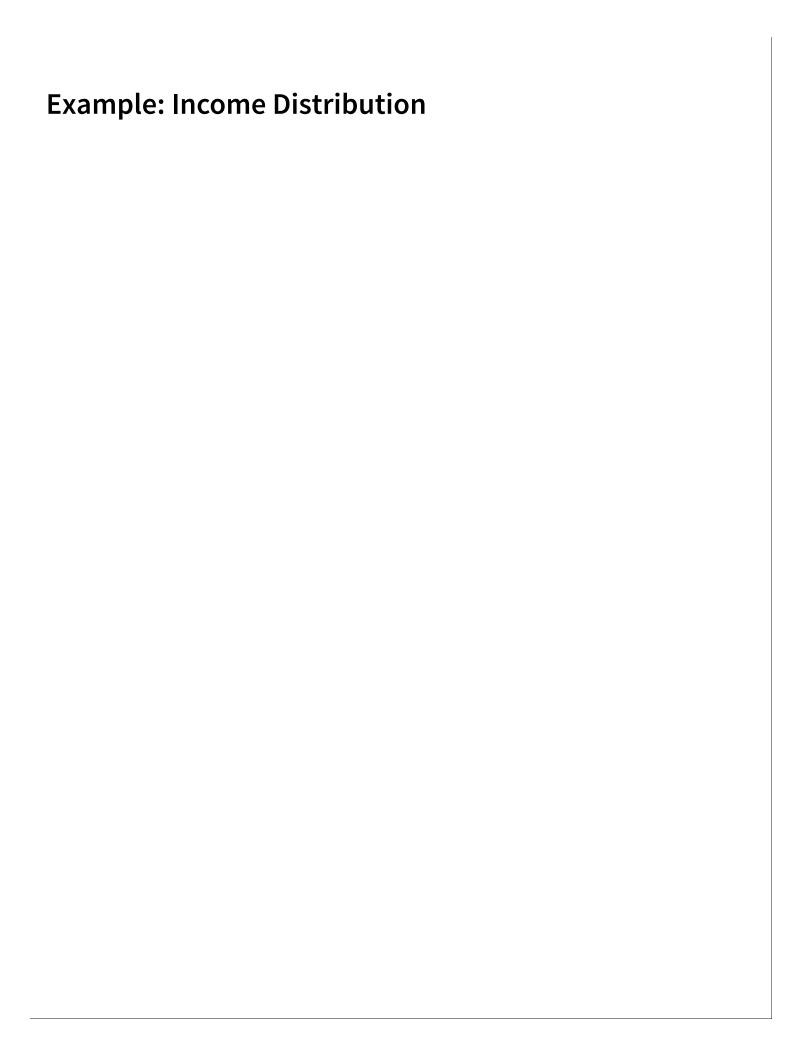


Mean pulled toward high values

Left-Skewed Distribution



Mean pulled toward low values



Why This Matters

```
# Calculate all three measures
mean_income <- mean(income)
median_income <- median(income)
median_income <- income(which.max(tabulate(match(income, unique(income))))]

print(paste("Mean:", round(mean_income, 0)))

[1] "Mean: 83264"

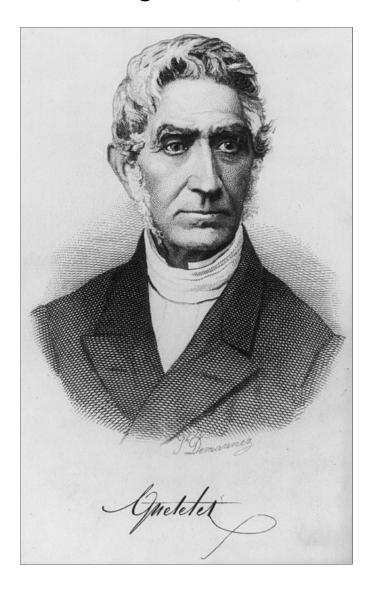
print(paste("Median:", round(median_income, 0)))

[1] "Median: 54176"</pre>
```

Notice: Mean is much higher than median due to wealthy outliers

Historical Context: Adolphe Quetelet					

The "Average Man" (1835)

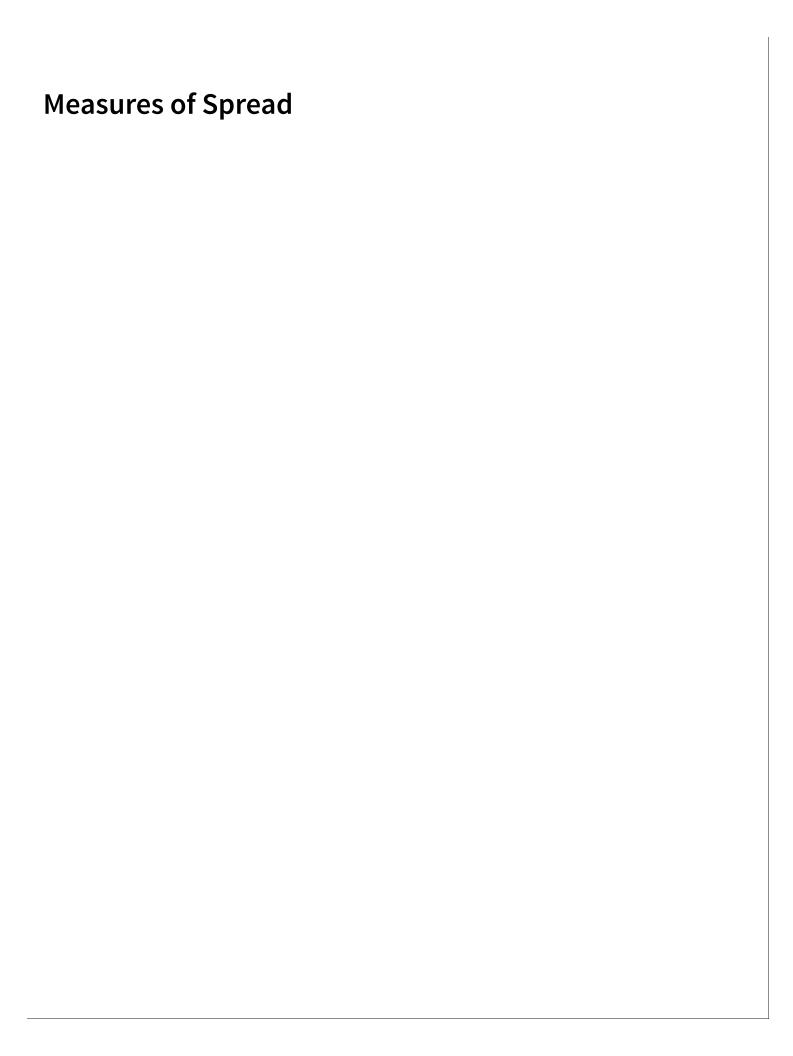


Adolphe Quetelet: Belgian statistician who pioneered the use of statistics in social science

Wanted to understand the "average man" (l'homme moyen) and devloped anthropetry and BMI

- Measured physical characteristics of soldiers
- Calculated average height, weight, chest measurements, etc.
- **Identified** Human physical traits follow predictable patterns (distributions)

Unfortuantely, he was a racist and used his work to justify eugenics



Why Central Tendency Isn't Enough

Consider two datasets with the same mean:

- Midterm Dataset A: 48, 49, 50, 51, 52 (mean = 50)
- Midterm Dataset B: 10, 30, 50, 70, 90 (mean = 50)

Question: Are these datasets the same?

Means are not enough! We need measures of **spread** or **variability**.

Range

Definition: Difference between maximum and minimum values

```
# Calculate range for approval ratings
approval %>%
summarise(
    min_approval = min(congress_approval, na.rm = TRUE),
    max_approval = max(congress_approval, na.rm = TRUE),
    range = max_approval - min_approval
)
```

Limitation: Sensitive to outliers, ignores distribution shape

Variance and Standard Deviation

Variance:

$$s^2 = \frac{\sum_{i=1}^{n} (x_i - \bar{x})^2}{n-1}$$

Standard Deviation:

$$s = \sqrt{s^2}$$

Understanding the notation:

- s^2 = sample variance (s-squared)
- s = sample standard deviation
- x_i = each individual observation (i = 1, 2, 3, ... n)
- \bar{x} = sample mean (x-bar)
- n = sample size

Understanding Variance and Standard Deviation

What do they measure?

- Variance: Average of squared distances from the mean
- Standard Deviation: Typical distance observations are from the mean
- Both measure "spread" how much data points vary around the center

Step-by-Step Calculation Example

Step 1: Find the mean

Step 2: Calculate deviations from mean

Value	Mean	Deviation $(x_i - ar{x})$	Squared Deviation $(x_i - ar{x})^2$	
45	50	-5	25	
48	50	-2	4	
50	50	0	0	
52	50	2	4	
55	50	5	25	

Step 3: Sum the squared deviations

$$\sum (x_i - \bar{x})^2 = 25 + 4 + 0 + 4 + 25 = 58$$

Step 4: Calculate variance

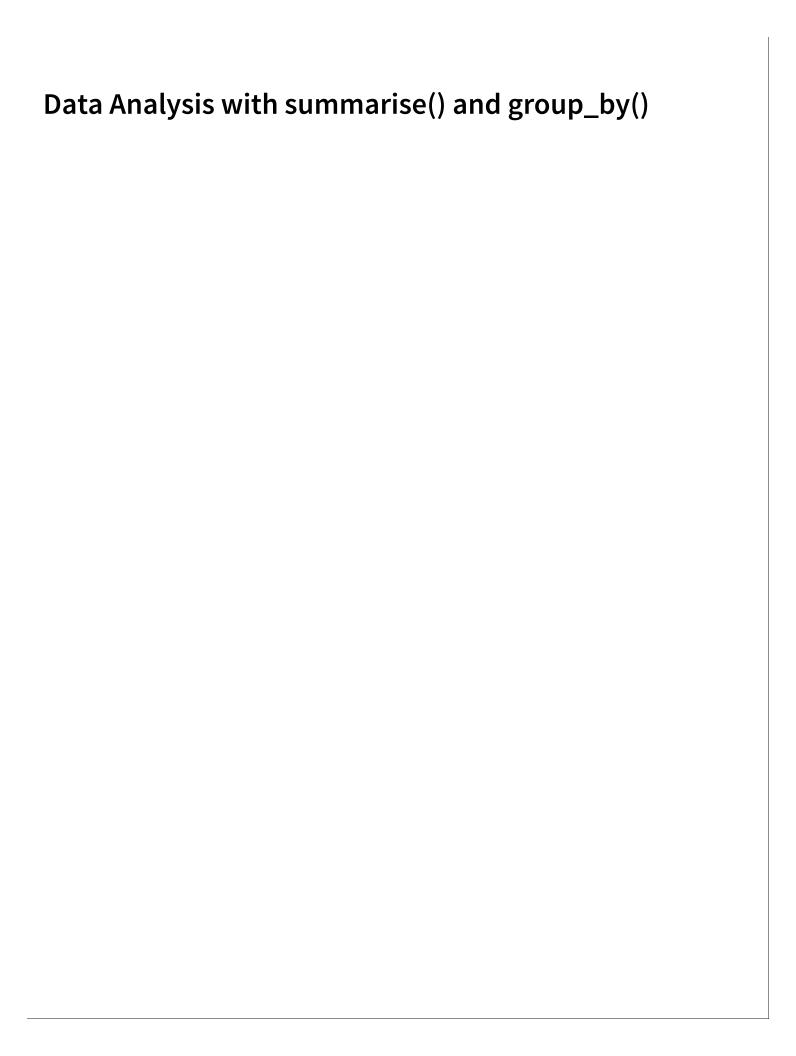
$$s = \sqrt{\frac{58}{5-1}} = \sqrt{\frac{58}{4}} = 3.81$$

Variance and Standard Deviation: With R

```
# Calculate variance and standard deviation
approval %>%
summarise(
variance = var(congress_approval, na.rm = TRUE),
std_dev = sd(congress_approval, na.rm = TRUE),
mean = mean(congress_approval, na.rm = TRUE)

)
```

```
# A tibble: 1 × 3
variance std_dev mean
<dbl> <dbl> <dbl> 1
183. 13.5 28.7
```



The summarise() Function

Purpose: Create summary statistics from your data

Components of summarise():

• Input: A data frame

• Output: A single row with your calculated statistics

• Functions: Any function that returns a single value (mean, median, sd, n, etc.)

Basic summarise() Example

```
# Load congressional data
congress <- read_csv("../../data/HSall_members.csv")

# Single summary of the entire dataset
congress %>%
summarise(
total_members = n(),  # Count of rows
avg_ideology = mean(nominate_dim1, na.rm = TRUE),  # Mean
median_ideology = median(nominate_dim1, na.rm = TRUE),  # Median
spread_ideology = sd(nominate_dim1, na.rm = TRUE),  # Standard deviation
min_ideology = min(nominate_dim1, na.rm = TRUE),  # Minimum
max_ideology = max(nominate_dim1, na.rm = TRUE)  # Maximum

)

# Maximum
# Maximum
# Maximum
# Maximum
```

Key insight: summarise() reduces your entire dataset to a single row of summary statistics

Adding group_by() for Subgroup Analysis

But what if we want to compare the mean ideology of Republicans vs. Democrats?

group_by(): Apply summarise() to subgroups instead of the entire dataset

```
# Same summary, but BY party
congress %>%
group_by(party_code) %>%
summarise(
count = n(),
avg_nominate_dim1 = mean(nominate_dim1, na.rm = TRUE),
median_nominate_dim1 = median(nominate_dim1, na.rm = TRUE),
sd_nominate_dim1 = sd(nominate_dim1, na.rm = TRUE)
)
```

```
# A tibble: 53 × 5
  party_code count avg_nominate_dim1 median_nominate_dim1 sd_nominate_dim1
1 1
2 1060
                              0.539
                              0.0829
                                                    0.204
                                                                       0.207
3 108
                                                                       0.188
                             -0.0103
                                                   -0.002
                                                                      NA
NA
4 1111
                              0.907
                                                    0.907
5 1116
                              0.068
                                                    0.068
                 13
6 112
                             -0.039
                                                    0.02
                                                                       0.377
                 9
7 114
                              0.298
                                                   0.361
                                                                       0.141
8 117
                             -0.00900
                                                   -0.00900
                                                                       0.255
                395
                              0.240
-0.0615
                                                                       0.241
0.275
9 1275
                                                   0.286
10 13
# i 43 more rows
```

Grouping Multiple Variables

You can group by multiple variables to create more detailed breakdowns:

```
# Summary by party AND chamber
congress %>%
group_by(party_code, chamber) %>%
summarise(
count = n(),
avg_nominate_dim1 = mean(nominate_dim1, na.rm = TRUE),
.groups = "drop" # Removes grouping after summarise
)
```

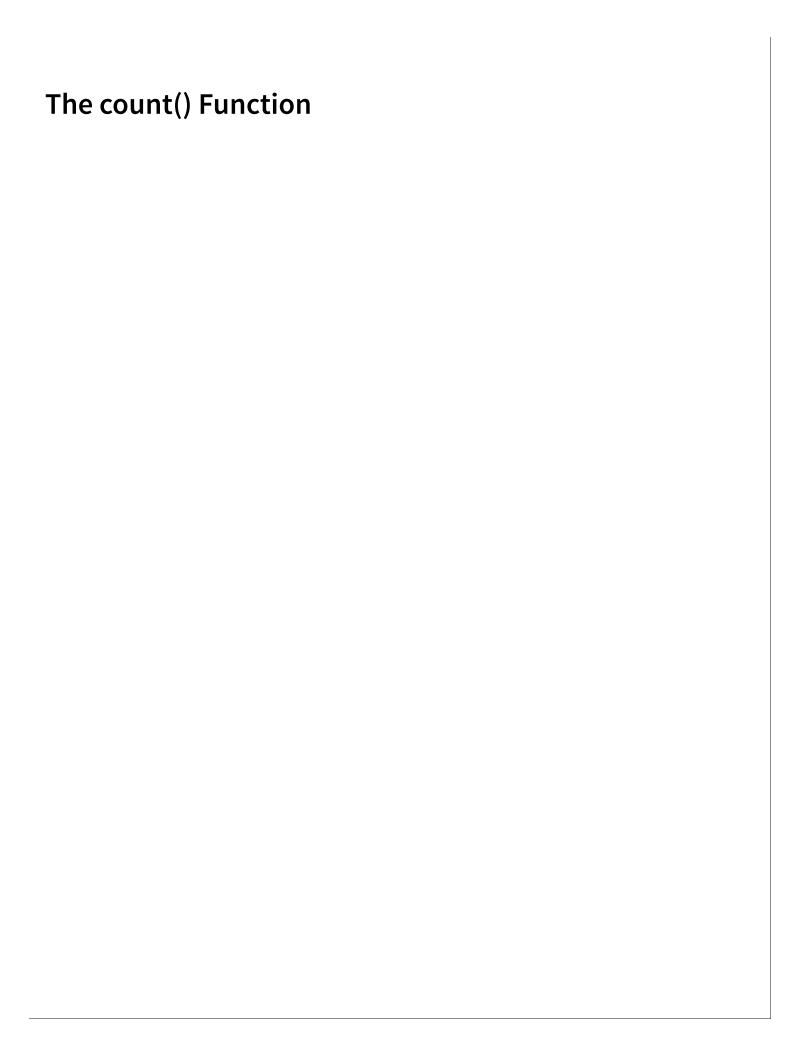
```
# A tibble: 93 × 4
  party_code chamber
                       count avg_nominate_dim1
            <chr>
  <chr>>
                                        0.521
             House
             President
                         196
                                       0.598
             Senate
4 1060
             House
                                       -0.177
                                       0.231
             Senate
                                       -0.0103
6 108
7 1111
8 1116
             Senate
House
                                       0.907
0.068
9 112
             House
                          10
                                       -0.200
10 112
             Senate
                                        0.499
# i 83 more rows
```

Note: .groups = "drop" removes grouping after summarise() to avoid unexpected behavior

Comprehensive Statistical Summaries

Create complete statistical profiles for each group:

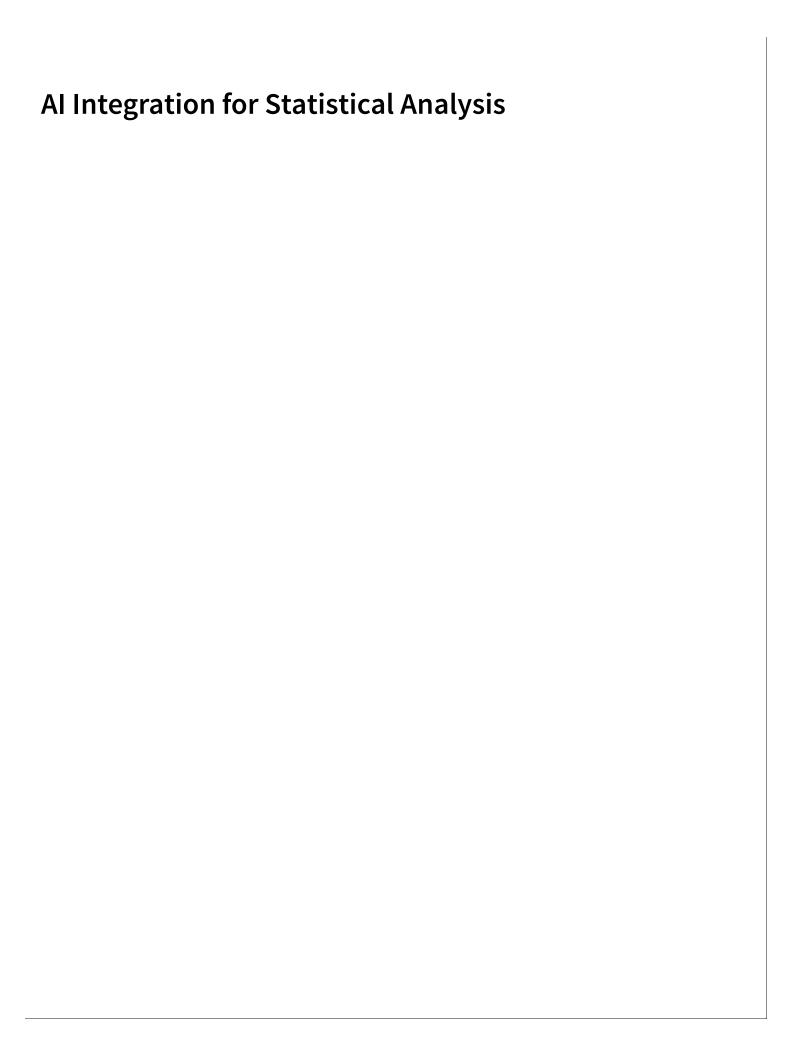
```
# A tibble: 53 × 7
  party_code count mean_ideology median_ideology min_ideology max_ideology
              <dbl>
                847
                            0.539
                                            0.585
                                                         -0.921
2 1060
3 108
                           0.083
-0.01
                                           0.204
-0.002
                11
8
                                                         -0.177
                                                                       0.252
                                                                       0.232
                                                         -0.261
4 1111
                            0.907
                                            0.907
                                                          0.907
                                                                       0.907
5 1116
                            0.068
                                            0.068
                                                          0.068
                                                                       0.068
6 112
                           -0.039
                                            0.02
                                                         -0.559
                                                                       0.499
                 9
7 114
                           0.298
                                            0.361
                                                         0.011
                                                                       0.406
8 117
                           -0.009
                                            -0.009
                                                         -0.189
                                                                       0.171
9 1275
                395
                           0.24
                                            0.286
                                                         -0.538
                                                                       0.682
10 13
              1976
                           -0.061
                                            -0.077
                                                         -0.996
                                                                       0.919
# i 43 more rows
# i 1 more variable: std_dev <dbl>
```



Counting Observations

```
1 # Count with conditions
2 congress %>%
3  filter(nominate_dim1 > 0.6) %>%
4  count(party_code, sort = TRUE)
```

```
# A tibble: 16 × 2
party_code n
<chr> <int>
1 Republican 1347
2 1 395
3 5000 72
4 13 29
5 29 24
6 1275 20
7 22 17
8 8888 13
9 7777 5
10 Democrat 5
11 300 3
12 8000 2
13 1111 1
14 1346 1
```



Effective Prompts for Summary Statistics

For choosing the right measure:

"I have presidential approval rating data that might have outliers. Should I use mean or median to summarize it? Please explain the difference and provide R code for both."

For grouping analysis:

"Help me write tidyverse code to calculate mean, median, and standard deviation of vote_share, grouped by party_code and state_abbrev. Explain what you did. My dataframe is called congress and it looks like this: <insert glimpse()>"

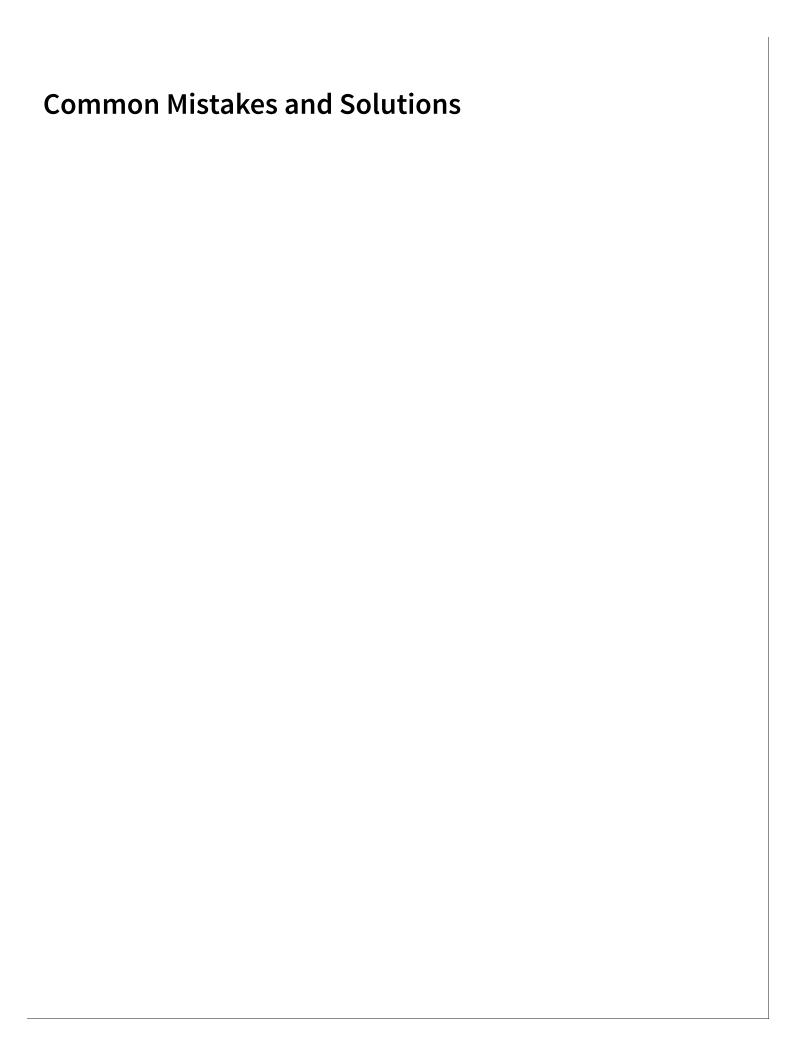
Interpreting Results with AI

For understanding patterns:

"I calculated that Republican candidates have a mean vote share of 0.52 and Democrats have 0.48, with standard deviations of 0.15 and 0.18 respectively. What does this tell me about voting patterns?"

AI helps you understand:

- What the numbers mean in context
- Whether differences are meaningful
- What questions to ask next



Forgetting to Handle Missing Values

```
1 # This might give NA if there are missing values
2 test_data <- c(1, 2, 3, NA, 5)
3 mean(test_data) # Returns NA

[1] NA

1 # Solution: use na.rm = TRUE
2 mean(test_data, na.rm = TRUE) # Returns 2.75

[1] 2.75</pre>
```

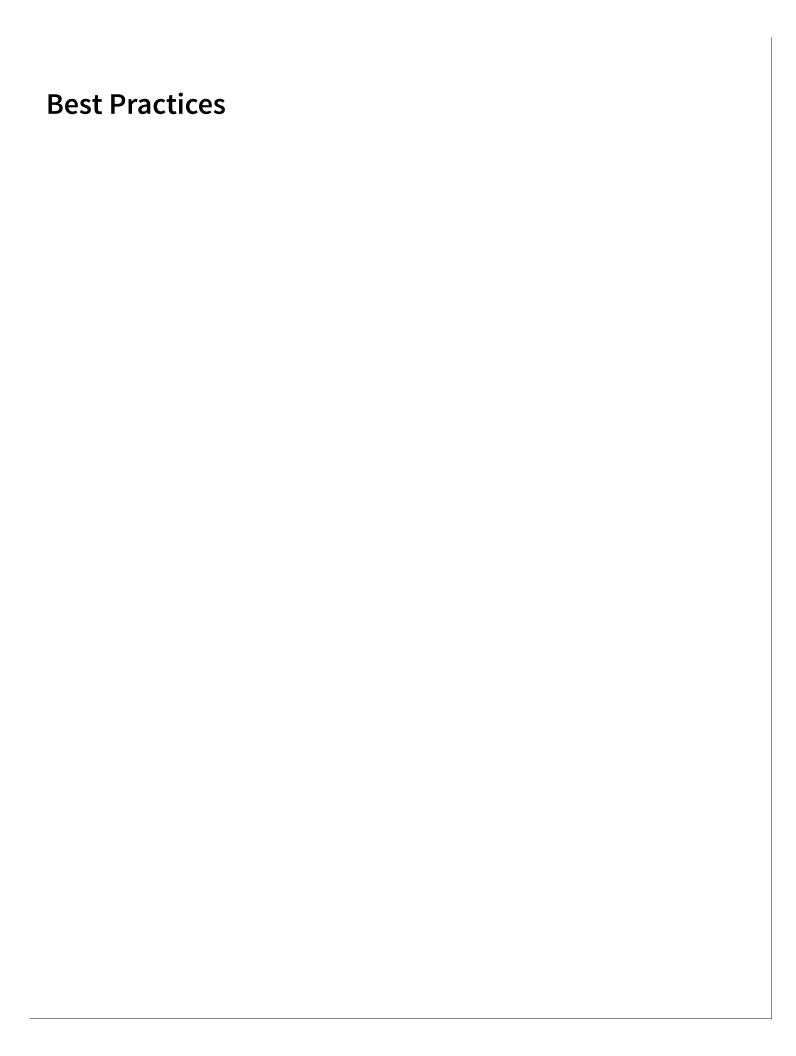
Choosing the Wrong Measure

Use Mean When:

- Data is roughly symmetric
- You want to include all values
- Making predictions

Use Median When:

- Data has outliers
- Data is skewed
- Describing "typical" experience



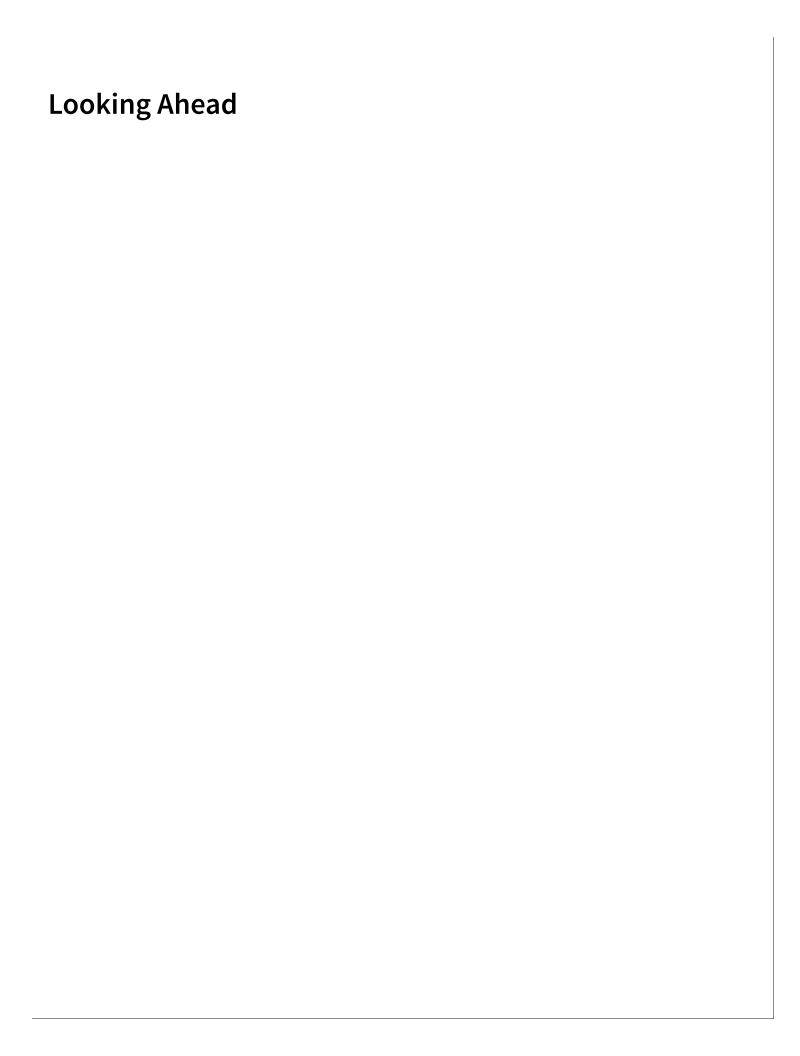
Report Multiple Measures

```
# Comprehensive summary
approval %>%
summarise(
n = n(),
mean = mean(congress_approval, na.rm = TRUE),
median = median(congress_approval, na.rm = TRUE),
sd = sd(congress_approval, na.rm = TRUE),
min = min(congress_approval, na.rm = TRUE),
max = max(congress_approval, na.rm = TRUE)
max = max(congress_approval, na.rm = TRUE)
mutate(across(where(is.numeric), round, 2))
```

Think About Context

Numbers without context are meaningless

- Is a 5-point difference in approval ratings large?
- What's a typical range for vote shares?
- How do current values compare to historical patterns?



Next Week Preview

Research Designs:

- Experimental vs observational studies
- Natural experiments
- The fundamental problem of causal inference
- When can we make causal claims?

Key Concepts to Remember

- Mean includes all values but sensitive to outliers
- Median resistant to outliers, good for skewed data
- Standard deviation measures spread around the mean
- group_by() + summarise() powerful for comparing groups
- Context matters interpret statistics in real-world terms

Questions?

Key takeaway: Summary statistics are tools for understanding data patterns. Choose the right tool for your data and always interpret results in context. Next class: We'll learn about different research designs and when we can make causal claims from data.

