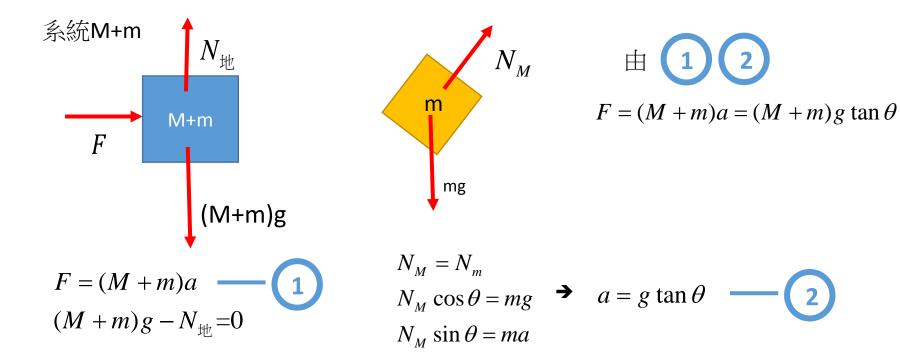
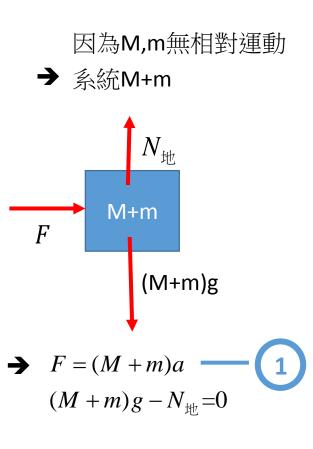
A small block of mass *m* rests on the sloping side of a wedge of mass *M* which itself rests on a horizontal frictionless table as shown in Fig. 1.

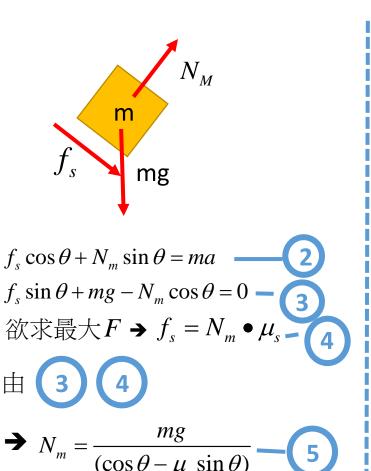
(i) Assuming all surfaces are frictionless, draw the free-body diagram and determine the magnitude of the force F that must be applied to *M* so that m remains in a fixed position relative to *M*.

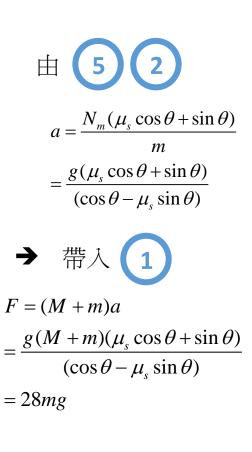
Sol: 因M,m無相對運動 →分析系統



(ii) Now consider the coefficient of static friction is μ_s between the small block and the wedge (the table is still frictionless), draw the free-body diagram for each block and determine the maximum horizontal force F applied to M such that the small block m to remain at a constant height above the table. Assume M = 3m = 2 Kg, $\mu_s = 1.0$, $\mu_k = 0.6$, And $\theta = 37^0$.

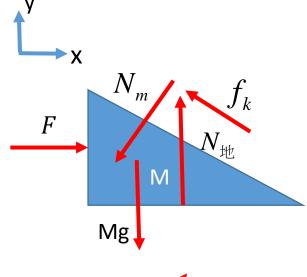


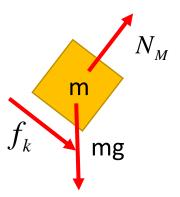




(iii) If F = 30 mg, determine the acceleration of each block.

30mg > 28mg → M,m有相對運動





a': acceleration of m relative to $M \rightarrow a_v' / a_x' = -\tan \theta$

$$a_{x} = A_{x} + a_{x}'$$

$$a_y = a_y' = -a_x' \tan \theta$$

$$N_{M} \sin \theta + f_{k} \cos \theta = m(A_{x} + a_{x}^{\prime})$$

$$N_{M}\cos\theta - f_{k}\sin\theta - mg = ma_{v}' = -ma_{x}'\tan\theta$$

$$F - N_m \sin \theta - f_k \cos \theta = MA_x$$

$$f_k = \mu_k N_M$$

$$\frac{27}{25}N_m = mA_x + ma_x'$$

$$\frac{11}{25}N_m - mg = -\frac{3}{4}ma_x'$$

$$30mg - \frac{27}{25}N_m = 3mA_s$$

$$A_{x} = \frac{609}{76} g$$

$$a_x' = -\frac{444}{228} g$$

$$a_{y}' = \frac{111}{76} g$$

$$N_m = \frac{425}{76} m$$

$$\frac{27}{25}N_{m} = mA_{x} + ma_{x}'$$

$$\frac{11}{25}N_{m} - mg = -\frac{3}{4}ma_{x}'$$

$$30mg - \frac{27}{25}N_{m} = 3mA_{x}$$

$$A_{x}' = -\frac{444}{228}g$$

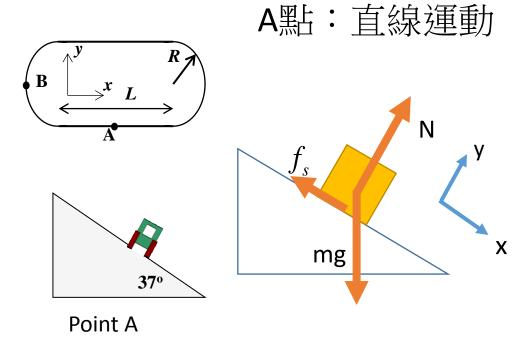
$$a_{y}' = \frac{111}{76}g$$

$$A_{y} = a_{y}' = \frac{111}{76}g$$

$$A_{y} = a_{y}' = \frac{111}{76}g$$

Car racing track: The length of straight track is $L = 1000 \, m$ and the radius of the two curved track is $R = 100 \, m$. The whole track is banked inward as shown in Fig. 2 with angle 37° . A car racer is driving a car, mass $m = 2000 \, kg$, with constant speed $v_0 = 10 \, m/s$ along the track. The static frictional coefficient μ_s of the track is 0.8. Assume $g = 10 \, m/s^2$. Consider two positions A and B on the track.

(A) What is the frictional force, magnitude and direction, at the position A?

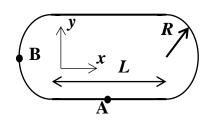


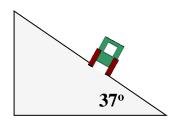
 $x: mg \sin 37^{\circ} - f_s = 0$

 $y: mg\cos 37^{\circ} - N = 0$

 $f_s = mg \sin 37^\circ = 12000(N)$ 延斜面朝上

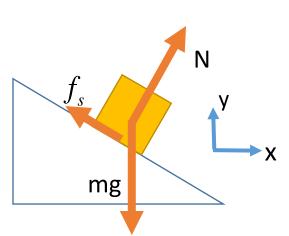
(B) What is the frictional force, magnitude and direction, at the position B?





Point B

B點:圓週運動



 $x: N \sin 37^{\circ} - f_s \cos 37^{\circ} = ma_c = m \frac{v_0^2}{R}$ $y: mg - N \cos 37^{\circ} - f_s \sin 37^{\circ} = 0$

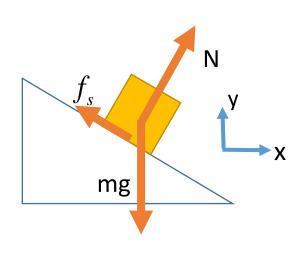
$$\frac{4}{5}N + \frac{3}{5}f_s = 10m$$

$$\frac{3}{5}N - \frac{4}{5}f_s = m$$

$$N = \frac{43}{5}m = 17200(N)$$

$$f_s = \frac{26}{5}m = 10400(N)$$

(C)Now this car racer wants to increase the speed. What is the maximum speed v_{max} he can reach?



$$x: f_s \cos 37^\circ + N \sin 37^\circ = ma_c = m \frac{v_{\text{max}}^2}{R}$$

$$y : mg + f_s \sin 37^\circ - N \cos 37^\circ = 0$$

$$v_{\text{max}} \rightarrow f_s = N \bullet \mu_S$$

$$: \frac{12}{25}N - \frac{4}{5}N = -10m \qquad \implies \qquad N = \frac{125}{2}m$$

$$y: \frac{12}{25}N - \frac{4}{5}N = -10m \qquad \Rightarrow \qquad N = \frac{125}{2}m$$

$$X: \frac{16}{25}N + \frac{3}{5}N = m\frac{v_{\text{max}}^2}{100} \qquad \Rightarrow \qquad v_{\text{max}} = 5\sqrt{310} \text{ (m/s}^2)$$

A small bead of mass $\,m\,$ is constrained to slide without friction inside a circular vertical hoop of radius $\,r\,$ which rotates about a vertical axis (Fig.3) at a frequency $\,f\,$.

- (a) Determine the angle θ where the bead will be in equilibrium that is , where it will have no tendency to move up or down along the hoop.
- (b) If f = 2.00 rev/s and r = 22.0 cm, what is θ ?
- (c) Can the bead ride as high as the center of the circle $(\theta = 90^{\circ})$? Explane.

