

2. Calculate the built-in voltage of a PN junction in which the p and n regions are doped equally with  $5 \times 10^{16}$  atoms/cm<sup>3</sup>. Assume  $n_i = 1.5 \times 10^{10}$ /cm<sup>3</sup>.

(a) (5%) With the terminals left open, what is the width of the depletion region?

$$N_A = N_D = 5 \times 10^{16} \text{ atoms/cm}^3, N_A = 1.5 \times 10^{10} / \text{cm}^3$$

$$V_0 = V_T \ln \left( \frac{N_A N_D}{n_i^2} \right) = 25.9 \ln \left( \frac{5 \times 10^{16} \times 5 \times 10^{16}}{(1.5 \times 10^{10})^2} \right) = 918 \text{ mV}$$

$$\Sigma C_s = (11.7 \times 8.854 \times 10^{-14} \text{ F/cm}) \times 1.036 \times 10^{-12} = 0.2 \text{ kM}$$

$$W = \sqrt{\frac{2 \epsilon_s \epsilon_0 V_0}{q (N_A + N_D)}} = \sqrt{\frac{2 \times 1.036 \times 10^{-12} \times 0.918}{1.6 \times 10^{-19} \times (5 \times 10^{16} + 5 \times 10^{16})}} = 0.2 \text{ kM}$$

(b) (10%) and how far does it extend into the p and n regions?

$$x_n = W \frac{N_D}{N_A + N_D} = 0.1 \text{ kM}$$

$$x_p = W \frac{N_A}{N_A + N_D} = 0.1 \text{ kM}$$

- (c) (5%) If the cross-sectional area of the junction is  $20 \mu\text{m}^2$ , find the magnitude of the charge stored on either side of the junction.

$$A = 20 \text{ kM}^2 = 20 \times 10^{-8} \text{ cm}^2$$

$$Q_j = A q \left( \frac{N_A N_D}{N_A + N_D} \right) W = 20 \times 10^{-8} \times 1.6 \times 10^{-19} \left( \frac{5 \times 10^{16}}{2} \right) \times 0.2 \times 10^{-4} = 1.6 \times 10^{-14} \text{ C}$$

3. (20%) Consider an n-channel MOSFET with  $t_{ox} = 6 \text{ nm}$ ,  $\mu_n = 460 \text{ cm}^2/\text{V}\cdot\text{s}$ ,  $V_t = 0.5 \text{ V}$ , and  $W/L = 10$ . Find the drain current in the following cases:

(a)  $v_{GS} = 2.5 \text{ V}$  and  $v_{DS} = 1.0 \text{ V}$

$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}} = \frac{3.45 \times 10^{-17}}{6 \times 10^{-9}} = 5.75 \times 10^{-9} \text{ F/m}^2$$

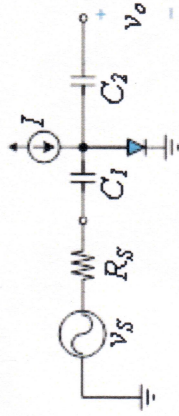
$$V_{ov} = V_{GS} - V_t = 2 \text{ V}$$

$$k_n = \mu_n C_{ox} \frac{W}{L} = 2.645 \text{ mA/V}^2$$

$$I_D = k_n (V_{GS} - V_t)^2 = 1.5 \text{ V}$$

(b)  $v_{GS} = 2.0 \text{ V}$  and  $v_{DS} = 1.5 \text{ V}$

5. (20%) A signal attenuator as shown in below with the attenuation factor controlled by the value of the dc current  $I$ , and  $v_S$  is a sinusoidal signal. Capacitors  $C_1$  and  $C_2$  are very large; their function is to couple the signal to and from the diode but block the dc current from flowing into the signal source or the load (not shown in this drawing).



(a) Use the diode small-signal model to show that the signal component of the output voltage is

$$v_o = v_s \frac{V_T}{V_T + IR_S}$$

$$r_d = \frac{V_T}{I}$$

$$V_o = V_S \times \frac{r_d}{r_d + R_S} = V_S \frac{V_T/I}{V_T/I + R_S}$$

$$= V_S \frac{V_T}{V_T + IR_S}$$

- (b) If  $v_S = 10 \text{ mV}$ , find  $v_o$  for  $I = 1 \text{ mA}$ ,  $0.1 \text{ mA}$ , and  $1 \mu\text{A}$ . Let  $R = 1 \text{ k}\Omega$ . At what value of  $I$  does  $v_o$  become one-half of  $v_S$ ?

$$V_o = \frac{V_S}{2} = 5 \text{ mV}$$