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Basics of Neural Network Programming

Vectorization

What is vectorization?

$$z = \underbrace{w^T x}_{\text{dot product}} + b$$

Non-vectorized:

$$z = 0$$

for i in $\text{range}(n-x)$:

$$z += w[i] * x[i]$$

$$z += b$$

$$w = \begin{bmatrix} : \\ : \\ : \end{bmatrix} \quad x = \begin{bmatrix} : \\ : \\ : \end{bmatrix}$$

$$w \in \mathbb{R}^{n_x}$$

$$x \in \mathbb{R}^{n_x}$$

Vectorized

$$z = \underbrace{\text{np.dot}(w, x)}_{w^T x} + b$$

\Rightarrow GPU } SIMD - single instruction
 \Rightarrow CPU } multiple data.



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More vectorization examples

Neural network programming guideline

Whenever possible, avoid explicit for-loops.

Neural network programming guideline

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$$u = Av$$

$$u_i = \sum_j A_{ij} v_j$$

$$u = \text{np.zeros}(n, 1)$$

for i ... ←

for j ... ←

$$u[i] += A[i][j] * v[j]$$

$$u = \text{np.dot}(A, v)$$

Vectors and matrix valued functions

Say you need to apply the exponential operation on every element of a matrix/vector.

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow u = \begin{bmatrix} e^{v_1} \\ e^{v_2} \\ \vdots \\ e^{v_n} \end{bmatrix}$$

```
→ u = np.zeros((n,1))  
→ for i in range(n):  
    → u[i]=math.exp(v[i])
```

```
import numpy as np  
u = np.exp(v)  
  
np.log(v)  
np.abs(v)  
np.maximum(v, 0)  
v**2  
1/v
```

Logistic regression derivatives

$$J = 0, \quad \boxed{\cancel{dw_1 = 0, dw_2 = 0}}, \quad db = 0$$

$$dw = np.zeros((n-x, 1))$$

→ for i = 1 to n:

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J += -[y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})]$$

$$dz^{(i)} = a^{(i)}(1 - a^{(i)})$$

↓
for j=1...n_x
dw_j += ...

$$\boxed{\begin{aligned} \cancel{dw_1 += x_1^{(i)} z^{(i)}} \\ \cancel{dw_2 += x_2^{(i)} z^{(i)}} \\ db += dz^{(i)} \end{aligned}}$$

$$n_x = 2$$

$$dw += x^{(i)} dz^{(i)}$$

$$J = J/m, \quad \boxed{\cancel{dw_1 = dw_1/m, dw_2 = dw_2/m}}, \quad db = db/m$$

$$dw /= m.$$



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Broadcasting in Python

Broadcasting example

Calories from Carbs, Proteins, Fats in 100g of different foods:

| | ↓ Apples | ↓ Beef | ↓ Eggs | ↓ Potatoes |
|---------|-------------|-----------|-----------|---------------|
| Carb | 56.0 | 0.0 | 4.4 | 68.0 |
| Protein | 1.2 | 104.0 | 52.0 | 8.0 |
| Fat | 1.8 | 135.0 | 99.0 | 0.9 |

= A
(3,4)



59 cal

$$\frac{56}{59} \approx 94.9\%$$

Calculate % of calories from Carb, Protein, Fat. Can you do this without explicit for-loop?

```
cal = A.sum(axis = 0)
```

```
percentage = 100 * A / (cal.reshape(1, 4))
```

↑(3,4) / (1,4)

Broadcasting example

$$\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 100 \\ 100 \\ 100 \\ 100 \end{bmatrix} \quad \text{100}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 200 & 300 \\ 100 & 200 & 300 \end{bmatrix}$$

$(m,n) \quad (2,3) \quad (1,n) \rightsquigarrow (m,n) \quad (2,3)$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 100 & 100 \\ 200 & 200 & 200 \end{bmatrix} =$$

$(m,n) \quad (m,1) \rightsquigarrow (m,n)$



General Principle

$$\begin{array}{ccc} (m, n) & + & (1, n) \\ \text{matrix} & \times & \rightsquigarrow (m, n) \\ \hline & / & \end{array}$$

$$\begin{array}{ccc} (m, 1) & + & \mathbb{R} \\ \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} & + & 100 \\ [1 \ 2 \ 3] & + & 100 \end{array} = \begin{bmatrix} 101 \\ 102 \\ 103 \end{bmatrix} = [101 \quad 102 \quad 103]$$

Matlab/Octave: bsxfun



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A note on python/
numpy vectors

Python Demo

Python / numpy vectors

```
import numpy as np
```

```
a = np.random.randn(5)
```

```
a = np.random.randn(5, 1)
```

```
a = np.random.randn(1, 5)
```

```
assert(a.shape == (5, 1))
```