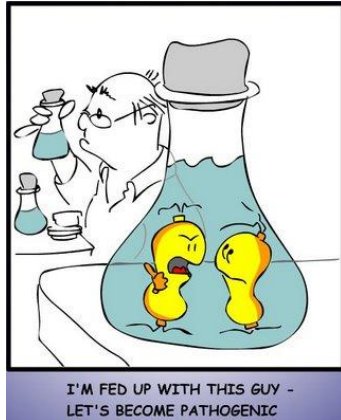


Evolution Simulations

Motivating Factors

- Understanding evolution of pathogen virulence
 - Ex: Different food sources elicit fast changes to bacterial virulence (Ketola, et al)
- Bioengineering of organisms
 - Ex: Programmed Evolution for Optimization of Orthogonal Metabolic Output in Bacteria (Eckdahl, et al)



"I find that they evolve
better under pressure."

Outline of Simulations

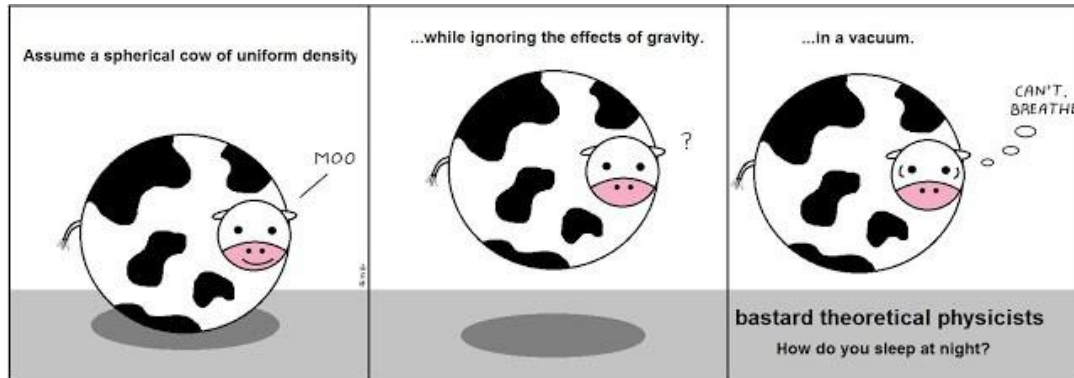
- Population of organisms (\mathbf{G}) in an Environment ($\mathbf{E}(\mathbf{G},t)$) that potentially changes with time
- The Environment has finite resources that the organisms need
- Each organism has:
 - A genotype (\mathbf{g})
 - A birth rate $\mathbf{b}(\mathbf{g}, \mathbf{E}(\mathbf{G},t))$
 - A death rate $\mathbf{d}(\mathbf{g}, \mathbf{E}(\mathbf{G},t))$
 - A mutation rate $\mathbf{m}(\mathbf{g}, \mathbf{E}(\mathbf{G},t))$

Central Questions

- What distribution of genotypes in the population are stable in stable environments?
- What happens to the genotype distribution as the resources in the environment change?
- What is the time frame in which the genotype distribution evolves?

Particular System

- Organism have n genes and $n + 1$ possible genotypes
- Genes are binary: can be 'A' or 'B'
- The Environment has 3 resources
 - 'Water' with capacity $C_W \gg 1$ that is consumed by every organism
 - Food A with capacity $C_A \gg 1$ is consumed by organisms with 'A' genes
 - Food B with capacity $C_B \gg 1$ is consumed by organisms with 'B' genes



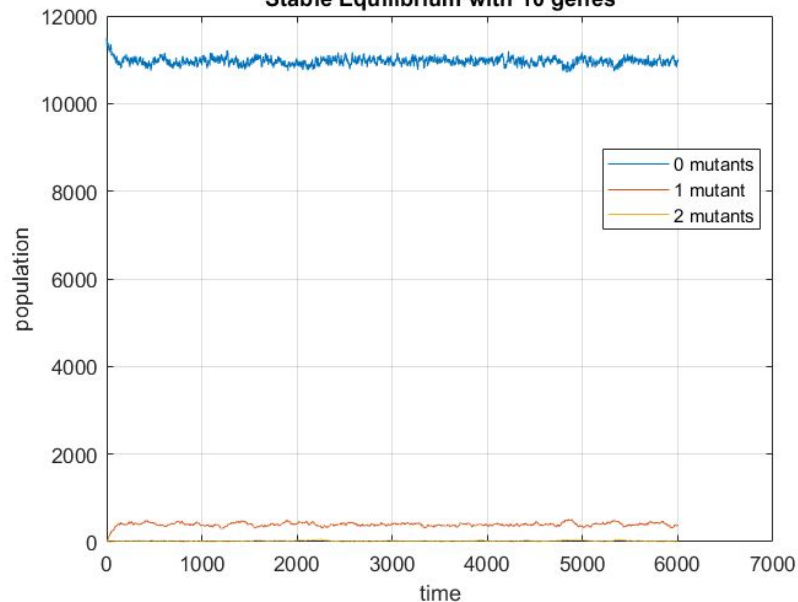
Key Functions

- death rate = constant
- mutation rate = constant
- birth rate =

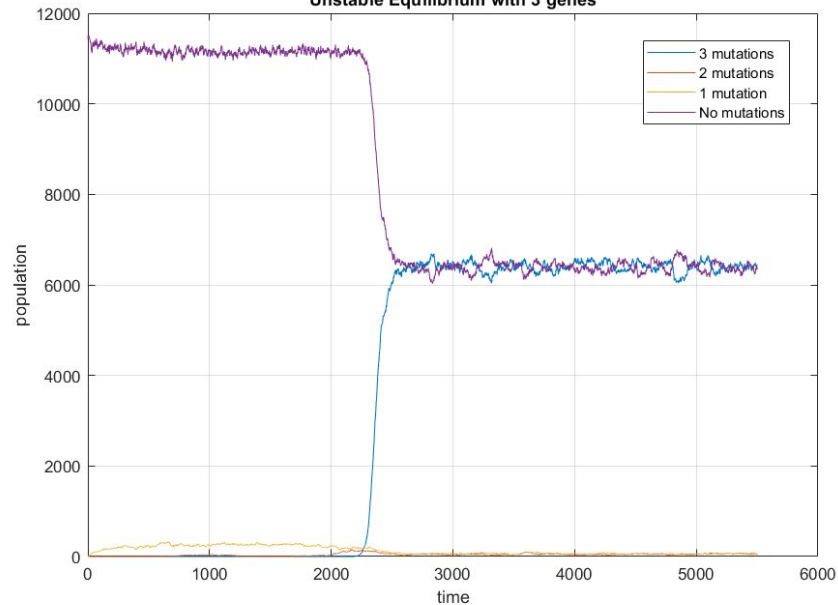
$$\left(\frac{m}{n}(b_A + r_A(m, n))e^{\frac{-1}{C_A} \sum \frac{m_i}{n}} + \frac{n-m}{n}(b_B + r_B(m, n))e^{\frac{-1}{C_B} \sum \frac{n-m_i}{n}}\right)e^{\frac{-N}{C_W}}$$

Experiment #1: Equilibria

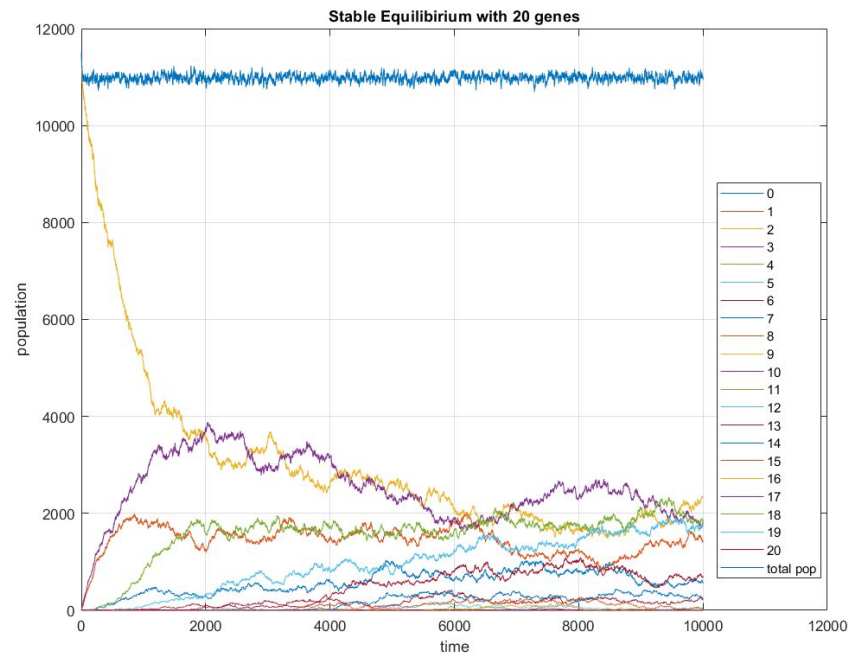
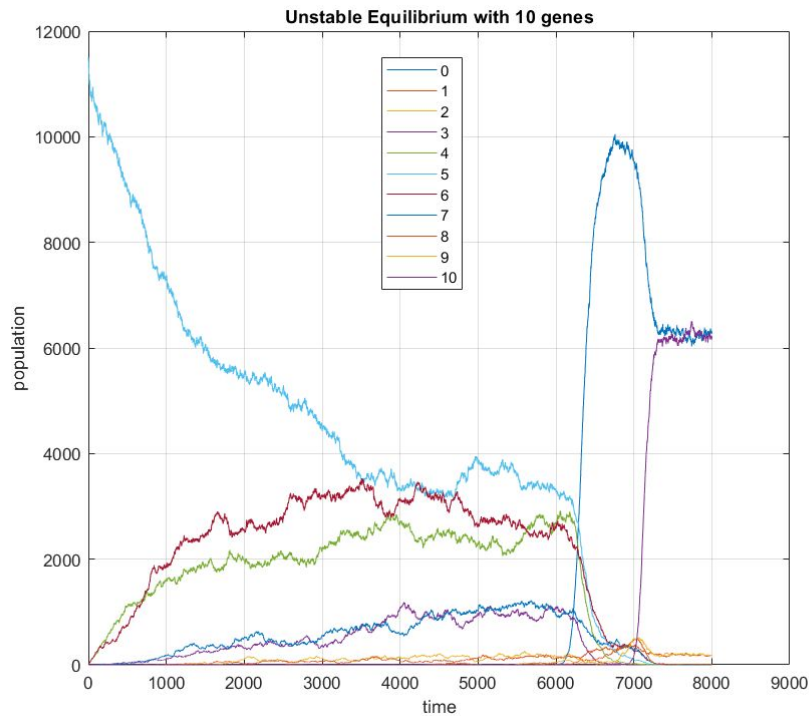
Stable Equilibrium with 10 genes



Unstable Equilibrium with 3 genes



Experiment #1: Equilibria



Evolution Forces

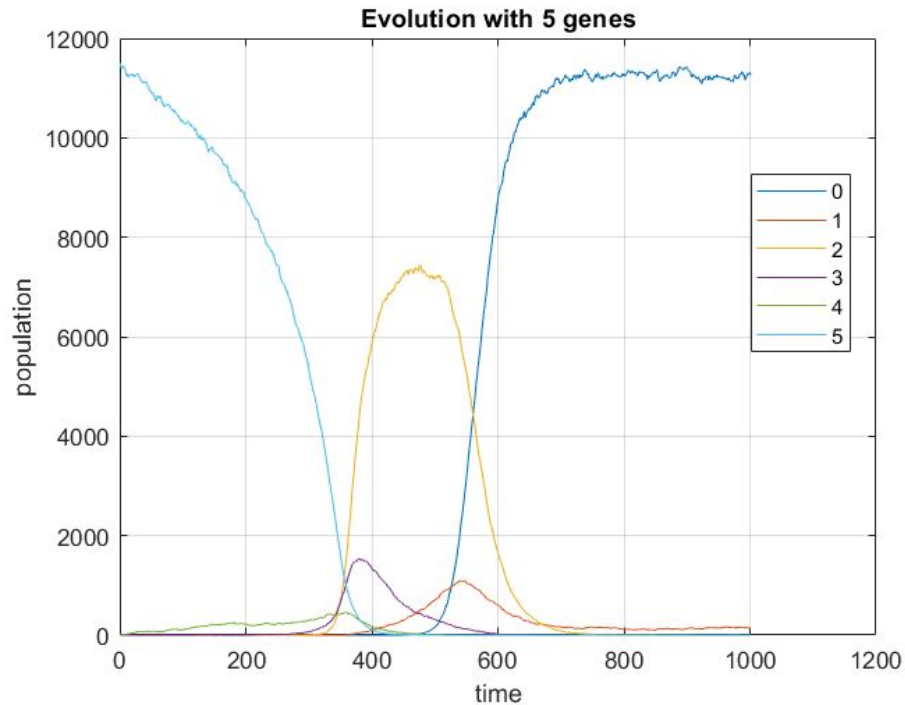
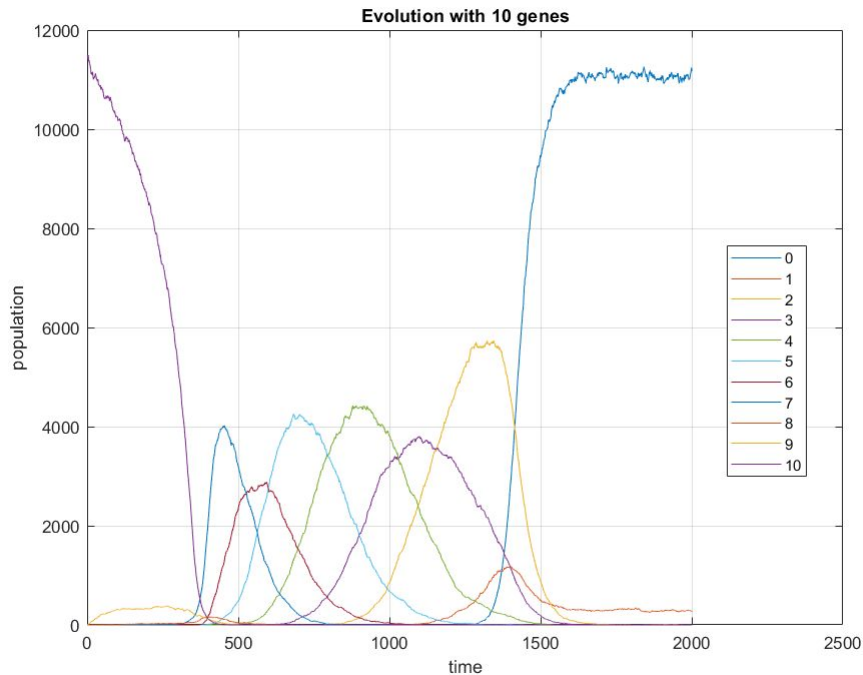
A population of a given genotype is favorable to grow when:

$$\left(\frac{m}{n}(b_A + r_A(m, n))e^{\frac{-1}{C_A} \sum \frac{m_i}{n}} + \frac{n-m}{n}(b_B + r_B(m, n))e^{\frac{-1}{C_B} \sum \frac{n-m_i}{n}}\right)e^{\frac{-N}{C_W}} + M \cdot G > d$$

And the homogeneous genomes will always be favorable when:

$$r_i e^{\frac{-N}{C_i}} > \frac{1}{n}(1 - e^{\frac{-N}{C_i}})$$

Experiment #2: Evolution



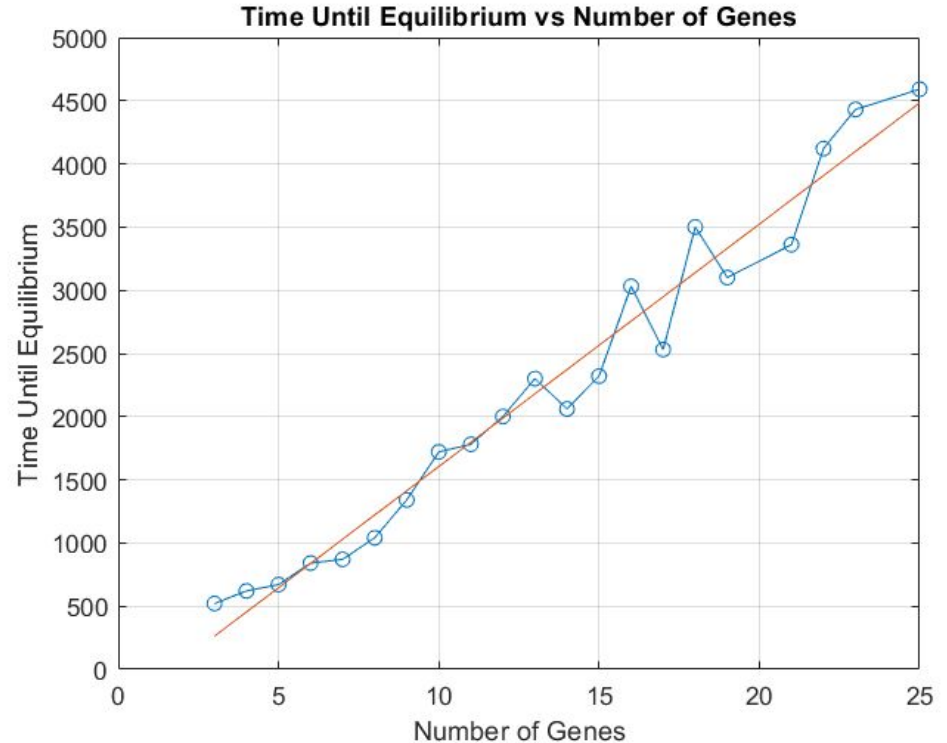
Experiment #3: Time to Recovery

- Increasing the number of genes
 - Increases the probability of mutations
 - Decreases the marginal difference between genotypes that differ by one gene

My prediction: Exponential Curve

Experiment #3: Time to Recovery

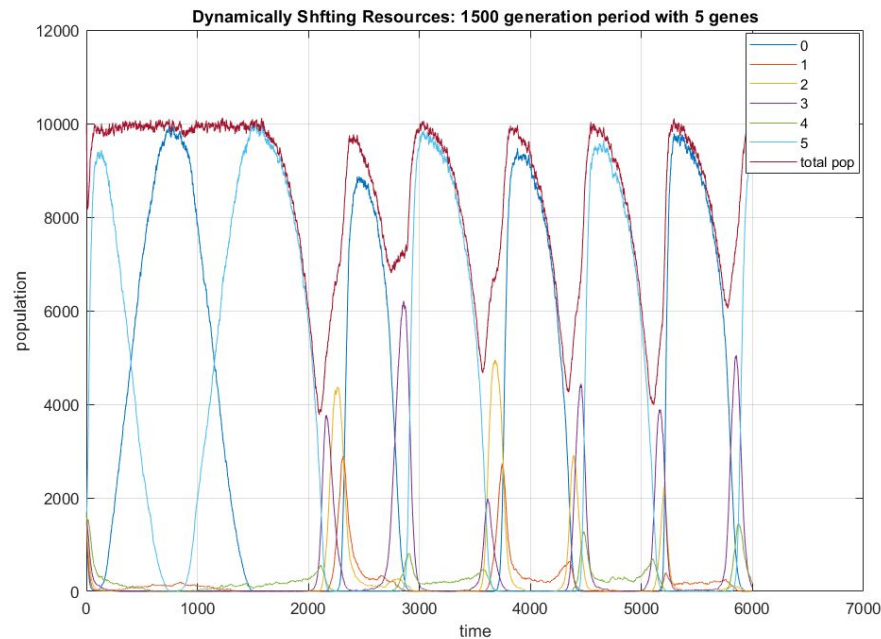
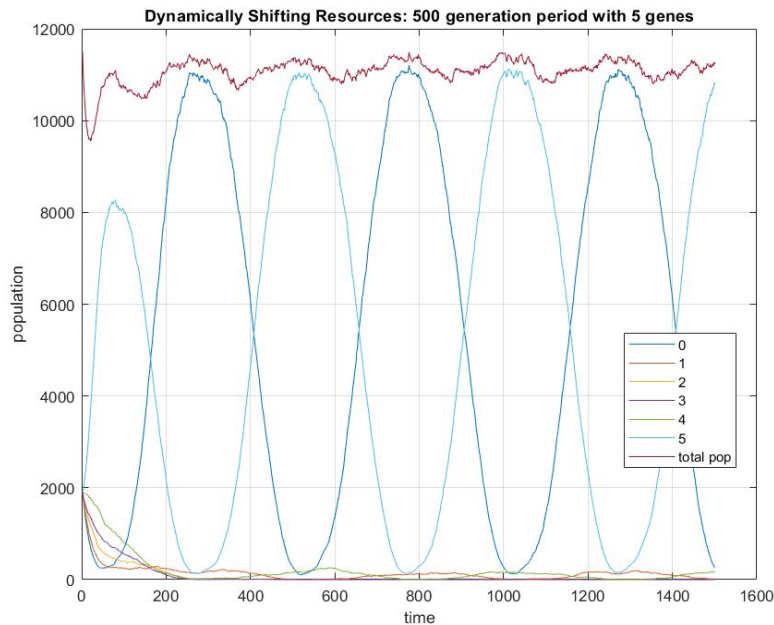
$$\text{time} = -313 + 192n$$



Next Steps

- Look at more complex dynamics of changing resources
- Make time dependent predictions
- Look at more complex gene models

Bonus: Dynamically Changing Resources



Conclusions

- Just because a nearby genotype is favored, doesn't mean we will find it in the population
- Manipulating selection forces is a potentially powerful tool to manipulate the genotype of a population
- Realistic analyses of gene transformation is not necessarily computationally feasible with my framework

Acknowledgements

- QinQin Yu
- Oskar Hallatschek
- *Evolutionary Dynamics* by Martin Nowak

Questions?