Prove
$$\ell_1(\theta_1)$$
 $\ell_2(\theta_2) \subseteq SO(n)$:

$$det(R_1) = det(R_2) = 1$$

$$R_1^T R_1 = R_2^T R_2 = I$$

$$R_1 R_1 = R_2 R_2 = I$$

$$(R_1 R_2)^{-1} R_1 R_2 = I$$

$$(R_1 R_2)^{\mathsf{T}} R_1 R_2 = R_2^{\mathsf{T}} R_1^{\mathsf{T}} R_1 R_2$$

$$= R_2^{\mathsf{T}} R_2$$

$$(R_1 R_2)^{\mathsf{T}} R_1 R_2 = \mathcal{I}$$

$$del(R_iR_i) = del(R_i)del(R_i)$$

$$= \underline{l \cdot l} = 1$$

$$2) g_{i}(x_{i}, y_{i}, \theta_{i}) \in SE(2)$$

$$\longrightarrow g_{i} = \begin{bmatrix} R_{i}(\Theta_{i}) \begin{bmatrix} x_{i} \end{bmatrix} & R_{i}(\Theta) \in SO(2)_{i} \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x_{i} \end{bmatrix} \in \mathbb{R}^{2N}$$

$$9_{1}9_{2} = \begin{bmatrix} R_{1}(\theta_{1}) \begin{bmatrix} x_{1} \\ y_{1} \end{bmatrix} \begin{bmatrix} R_{2}(\theta) \begin{bmatrix} x_{1} \\ y_{1} \end{bmatrix} \end{bmatrix}$$

$$= \begin{bmatrix} R_{1}(\theta_{1}) & 0 \end{bmatrix} \begin{bmatrix} R_{2}(\theta_{1}) & 0 \end{bmatrix}$$

$$= \begin{bmatrix} n_1(\theta_1) & \rho_1 \\ 0 & I \end{bmatrix} \begin{bmatrix} n_2(\theta_1) & \rho_2 \\ 0 & I \end{bmatrix}$$

$$\begin{bmatrix} n_1 \rho_2 & \rho_1 \\ 0 & I \end{bmatrix}$$

$$= \begin{bmatrix} n_1 \rho_2 & n_1 \rho_2 + \rho_1 \\ 0 & 1 \end{bmatrix}$$

Therefore the product
$$91(x_1,14_1,14_1)$$
 $92(x_2,4_2,14_1)$ has form $\begin{bmatrix} RGSO(2) & PEIR^{2x_1} \end{bmatrix}$

3. Honogues trasformatin in SE(2):

Take a change of coordinate for w frame to 5 fine of post -: use a interestiale frame: ay ax $9 \text{ km} = \begin{bmatrix} R \text{ km} & 0 \\ 0 & 1 \end{bmatrix} + R \text{ km} = \begin{bmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{bmatrix}$ $9 \text{ Ab} = \begin{bmatrix} I & P \text{ AD} \\ 0 & 1 \end{bmatrix} + P \text{ Ab} = \begin{bmatrix} I \\ 0 \end{bmatrix}$ TW = [TW] = GA GB TB "r = vector position of r in the " frame "= " - vector with a trailing 1 TU = [RWA 0] [7 PA6] TO

3. The [Rwg RwgPab] To:

a generalized transbrouten has been decomposed into a

roboten and a translater.

The order of operations we shall usually use

the order of operations we shall usually use is robation— I translation, because it we branched first, will be revolving our coursinate representation about the origin on a moment arm as well.

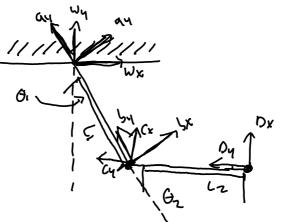
If the order were revesed; we $Gwc = \begin{bmatrix} I & Rwc \\ O & I \end{bmatrix} Pwc = \begin{bmatrix} I \\ O \end{bmatrix}$ $Gcc = \begin{bmatrix} Rcs & Pcs \\ O & I \end{bmatrix}, Pcs = \begin{bmatrix} \frac{\sqrt{2}}{2} - I \\ \frac{\sqrt{2}}{2} \end{bmatrix}$ $Gwc Gcs = \begin{bmatrix} I & Rwc \end{bmatrix} Pcs = \begin{bmatrix} \frac{\sqrt{2}}{2} - I \\ \frac{\sqrt{2}}{2} \end{bmatrix}$

Conc Coro =

[I Anc] [RC15 Pers] difference:

- [Res Pers + Purc] the rotation is his version has its own version has its own version has its own (RC15, RC15).

4. Dingram of how frames were defined:



$$G_{NA} = \begin{bmatrix} R_{NA}(\theta_l) & \begin{bmatrix} 0 \\ 0 \end{bmatrix} \end{bmatrix}$$
, $R_{NA} = \begin{bmatrix} c_{S}(\theta_l) & c_{S}(\theta_l) \\ sin(\theta_l) & c_{S}(\theta_l) \end{bmatrix}$

 $G_{AB} = \begin{bmatrix} I & \begin{bmatrix} -L_1 \\ -L_1 \end{bmatrix} \end{bmatrix}$

Gas = I [-ln]

Transformation matrices:

 $G_{DC} = \begin{bmatrix} R_{DC}(\Theta) & \begin{bmatrix} 0 \\ 0 \end{bmatrix} \end{bmatrix} R_{DC} = \begin{bmatrix} C_{DS}(\Theta_{Z}) & -5\dot{\gamma}(\Theta_{1}) \\ 0 & 1 \end{bmatrix}$ $C_{DC} = \begin{bmatrix} C_{DS}(\Theta_{Z}) & -5\dot{\gamma}(\Theta_{1}) \\ 0 & 1 \end{bmatrix}$