Colour experiment

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Introduction

This analysis looks at the sign variants used in a colour naming game between signers of different sign languages meeting after 1 week of interaction and after 3 weeks of interaction. The data was collected by Kang Suk Byun (Kang-Suk.Byun@mpi.nl).

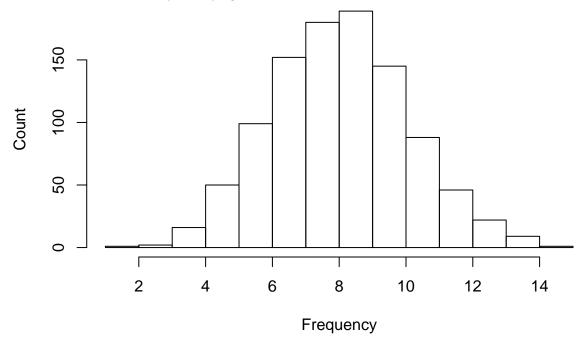
The analysis tries to predict the relative frequency of each variant within a colour category in week 3, based on measures from week 1.

Data

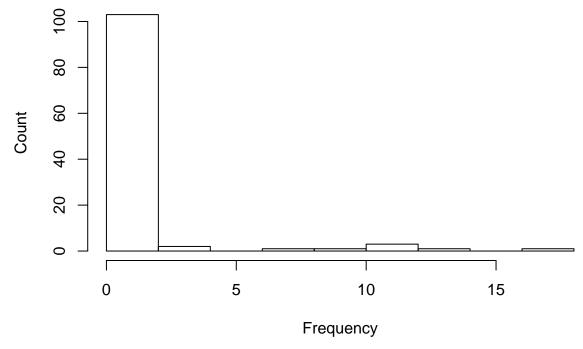
- colour: Code of the target colour
- colourName: English name of the target colour
- sign: label for the variant produced
- freq_week_1_total: Total number of occurances of the variant in the first week, across all colour contexts.
- freq_week_4_total: Total number of occurances of the variant in the final week, across all colour contexts.
- freq_week_1: Number of occurances of the variant used during the given target colour context in week 1.
- freq_week_4: Number of occurances of the variant used during the given target colour context in the final week.
- prop_week_1: Same as freq_week_1, but as a proportion of all variants used in the given colour context.
- prop_week_4: Same as freq_week_4, but as a proportion of all variants used in the given colour context.
- origin: The origin language of the sign. For many, identifying an origin is not possible, so is labelled "None"
- iconic: Old variable
- check: The number of times this variable was used in a checking turn.
- indexical: Is the variant non-indexical, indexical or indexical of the body?
- inventedBy: The name of the first signer to use this variant in the experiment.
- TryMarked: The number of times this sign was used in try-marking.
- Teach: The number of times this sign was explicitly taught.
- averageLength_week_1: Average time to produce the variant in milliseconds
- average Trial Length week 1: Average time for completing the trial for the given target colour.
- BodyAnchor: Is the variant body-anchored (redundant with 'indexical')

Poisson regression

This study uses a mixed effects regression model with poisson distributions. Most standard regression analyses assume that the values they are trying to model come from a normal distribution, like this:



However, the main variable for this study is the frequency of sign variants, with a strong skew and many zero values:



Instead of using a normal distribution as the basis for the statistical model or transforming the data (which is difficult anyway because of the large number of zero counts), we can use a poisson distribution. This also has the advantage of only predicting whole, non-negative numbers, which makes sense for this data because a variant can't be used half a time or a negative number of times.

Load libraries

```
library(ggplot2)
library(lme4)
library(Rmisc)
library(dplyr)
library(sjPlot)
library(gridExtra)
```

Load data

```
variants = read.csv('.../data/processedData/variants_summary.csv', stringsAsFactors = F)
There is only 1 variant for 'white'. Therefore, we remove it from this statistical analysis.
variants = variants[variants$colourName!='white',]
Some variants need to be removed:
variants = variants[!variants$sign %in%
            c("SAME",
              "DIFFERENT",
              "DO NOT UNDERSTAND").1
Transform some variables.
# The range of values for 'Teach' is very small:
table(variants$Teach)
##
## 0 1 2 3
## 92 7 1 3
# So we'll turn it into a binary category:
# variants that were never taught and variants that were
variants$Teach = as.factor(variants$Teach >0)
# Similar for checking
variants$check.any = as.factor(variants$check>0)
# ... and T-1
variants$T_minus_1.any = as.factor(variants$T_minus_1>0)
# Transform total frequency
variants$freq_week_1_total.logcenter =
  log(variants$freq_week_1_total + 1)
variants$freq_week_1_total.logcenter = scale(variants$freq_week_1_total.logcenter)
# cut TryMarking into two categories
variants$TryMarked.any = as.factor(variants$TryMarked>0)
# transform length
variants$averageLength_week_1.logcenter = log(variants$averageLength_week_1)
```

```
variants$averageLength_week_1.logcenter =
    scale(variants$averageLength_week_1.logcenter)

variants$indexical = as.factor(variants$indexical)

# Make inventedBy deviation coding
# (deviation from the grand mean)
variants$inventedBy = as.factor(variants$inventedBy)
contrasts(variants$inventedBy) = contr.sum(length(levels(variants$inventedBy)))

listofsigns = variants[,c("colourName","sign")]
write.csv(listofsigns,"../results/descriptive/ListOfVariants.csv", fileEncoding = 'utf-8')
```

LMER models

Each model predicts the frequency of a variant in week 4, with a random intercept by colourName. The random intercept allows some colours to have higher variant frequencies than others. This is useful because we know that signs for some colours are converged on quickly, making their frequencies within those colours potentially higher. In other words, the use of a particular variant to refer to a given colour is not entirely independent of the use of another variant to refer to the same colour.

Random slopes allow the strength of the effect of a factor to be different for each colour concept. Only indexicality is theoretically relevant here: it is possible that an indexical strategy, particularly body-indexical signs, would be more effective for some colours than others. For example, the body affords indexicality for black (hair) and red (tongue), but not green. We can check whether this is true by comparing a baseline model to one with a random slope for indexicality.

```
## Data: variants
## Models:
## m0: freq_week_4 ~ 1 + (1 | colourName)
## m1: freq_week_4 ~ 1 + (1 + indexical || colourName)
## Df AIC BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## m0 2 430.24 435.51 -213.12 426.24
## m1 8 347.92 368.99 -165.96 331.92 94.323 6 < 2.2e-16 ***</pre>
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Indeed, a random slope for indexicality significantly improves the model. It is difficult to think of a theoretical reason why different colours would be affected differently for other variables. Given that random slopes make the model more complex, these are left out.

```
We begin with a null model and gradually add predictor variables, using model comparison to judge the
significance of each variable.
# Null model
m0 = glmer(freq_week_4 ~
           + (1 + indexical || colourName) ,
           data=variants, family=poisson,
           control=gcontrol)
# add indexicality
mIndx = glmer(freq_week_4 ~
                indexical +
                (1 + indexical || colourName) ,
              data=variants, family=poisson,
              control=gcontrol)
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control
## $checkConv, : unable to evaluate scaled gradient
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control
## $checkConv, : Model failed to converge: degenerate Hessian with 1 negative
## eigenvalues
# add whether the variant is explicitly taught
mTeach = glmer(freq_week_4 ~
                 1 +
                 indexical +
                 Teach +
                 (1 + indexical || colourName) ,
               data=variants, family=poisson,
               control=gcontrol)
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control
## $checkConv, : unable to evaluate scaled gradient
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control
## $checkConv, : Model failed to converge: degenerate Hessian with 2 negative
## eigenvalues
mTry = glmer(freq_week_4 ~
               1 +
               indexical +
               Teach +
               TryMarked.any +
               (1 + indexical || colourName) ,
             data=variants, family=poisson,
             control=gcontrol)
mChk = glmer(freq_week_4 ~
```

```
indexical +
               Teach +
               TryMarked.any +
               check.any +
               (1 + indexical || colourName) ,
             data=variants, family=poisson,
             control=gcontrol)
mTm1 = glmer(freq_week_4 ~
               indexical +
               Teach +
               TryMarked.any +
               check.any +
               T_minus_1.any +
               (1 + indexical || colourName) ,
             data=variants, family=poisson,
             control=gcontrol)
mFrq = glmer(freq_week_4 ~
               indexical +
               Teach +
               TryMarked.any +
               check.any +
               T_minus_1.any +
               freq_week_1_total.logcenter +
               (1 + indexical || colourName) ,
             data=variants, family=poisson,
             control=gcontrol)
mLen = glmer(freq_week_4 ~
               indexical +
               Teach +
               TryMarked.any +
               check.any +
               T_minus_1.any +
               freq_week_1_total.logcenter +
               averageLength_week_1.logcenter +
               (1 + indexical || colourName) ,
             data=variants, family=poisson,
             control=gcontrol)
mInv = glmer(freq_week_4 ~
               1 +
               indexical +
               Teach +
               TryMarked.any +
               check.any +
               T_minus_1.any +
               freq_week_1_total.logcenter +
```

```
averageLength_week_1.logcenter +
               inventedBy +
               (1 + indexical || colourName) ,
             data=variants, family=poisson,
             control=gcontrol)
mTchXTry = glmer(freq_week_4 ~
                   1 +
                   indexical +
                   Teach +
                   TryMarked.any +
                   check.any +
                   T_minus_1.any +
                   freq_week_1_total.logcenter +
                   averageLength_week_1.logcenter +
                   inventedBy +
                   Teach : TryMarked.any +
                   (1 + indexical || colourName) ,
                 data=variants, family=poisson,
                 control=gcontrol)
# Interaction of teaching and checking causes severe
# convergence issues
# m10 = glmer(freq_week_4 ~
               1 +
#
               indexical +
#
               Teach +
#
               TryMarked.any +
               check.any +
#
#
               T_{minus_1.any} +
#
               freq_week_1_total.logcenter +
#
               averageLength_week_1.logcenter +
#
               inventedBy +
#
               Teach : TryMarked.any +
#
               Teach : check.any +
#
              (1 + indexical | | colourName) ,
#
             data=variants, family=poisson,,
#
             control=gcontrol)
mTryXChk = glmer(freq_week_4 ~
                   indexical +
                   Teach +
                   TryMarked.any +
                   check.any +
                   T_minus_1.any +
                   freq_week_1_total.logcenter +
                   averageLength_week_1.logcenter +
                   inventedBy +
                   Teach : TryMarked.any +
                   TryMarked.any : check.any +
                   (1 + indexical || colourName) ,
                 data=variants, family=poisson,
```

control=gcontrol)

```
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control
## $checkConv, : unable to evaluate scaled gradient
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control
## $checkConv, : Model failed to converge: degenerate Hessian with 1 negative
## eigenvalues
```

Results

Model comparison test:

```
anova(m0,mIndx,mTeach,mTry,mChk,mTm1,mFrq,mLen,mInv,mTchXTry,mTryXChk)
```

```
## Data: variants
## Models:
## m0: freq_week_4 ~ 1 + (1 + indexical || colourName)
## mIndx: freq_week_4 ~ 1 + indexical + (1 + indexical || colourName)
## mTeach: freq_week_4 ~ 1 + indexical + Teach + (1 + indexical || colourName)
## mTry: freq_week_4 ~ 1 + indexical + Teach + TryMarked.any + (1 + indexical ||
## mTry:
            colourName)
## mChk: freq_week_4 ~ 1 + indexical + Teach + TryMarked.any + check.any +
## mChk:
             (1 + indexical || colourName)
## mTm1: freq_week_4 ~ 1 + indexical + Teach + TryMarked.any + check.any +
            T_minus_1.any + (1 + indexical || colourName)
## mTm1:
## mFrq: freq_week_4 ~ 1 + indexical + Teach + TryMarked.any + check.any +
            T_minus_1.any + freq_week_1_total.logcenter + (1 + indexical | |
## mFrq:
            colourName)
## mLen: freq_week_4 ~ 1 + indexical + Teach + TryMarked.any + check.any +
            T_minus_1.any + freq_week_1_total.logcenter + averageLength_week_1.logcenter +
## mLen:
## mLen:
             (1 + indexical || colourName)
## mInv: freq_week_4 ~ 1 + indexical + Teach + TryMarked.any + check.any +
## mInv:
            T_minus_1.any + freq_week_1_total.logcenter + averageLength_week_1.logcenter +
            inventedBy + (1 + indexical || colourName)
## mInv:
## mTchXTry: freq_week_4 ~ 1 + indexical + Teach + TryMarked.any + check.any +
                 T_minus_1.any + freq_week_1_total.logcenter + averageLength_week_1.logcenter +
## mTchXTry:
## mTchXTry:
                 inventedBy + Teach:TryMarked.any + (1 + indexical || colourName)
## mTryXChk: freq_week_4 ~ 1 + indexical + Teach + TryMarked.any + check.any +
## mTryXChk:
                 T_minus_1.any + freq_week_1_total.logcenter + averageLength_week_1.logcenter +
                 inventedBy + Teach:TryMarked.any + TryMarked.any:check.any +
## mTryXChk:
## mTryXChk:
                 (1 + indexical || colourName)
##
                 AIC
                        BIC
                               logLik deviance
                                                 Chisq Chi Df Pr(>Chisq)
            8 347.92 368.99 -165.958
## mO
                                       331.92
## mIndx
           10 344.42 370.77 -162.211
                                       324.42 7.4928
                                                                0.023603 *
## mTeach
          11 312.12 341.11 -145.062
                                       290.12 34.2994
                                                            1 4.725e-09 ***
## mTry
           12 251.27 282.88 -113.634
                                       227.27 62.8550
                                                            1 2.225e-15 ***
## mChk
           13 223.73 257.98 -98.864
                                       197.73 29.5393
                                                            1 5.479e-08 ***
## mTm1
           14 225.46 262.35 -98.732
                                       197.46 0.2641
                                                            1
                                                                0.607326
           15 219.89 259.41 -94.947
                                       189.89 7.5706
                                                                0.005933 **
## mFrq
                                                            1
           16 211.49 253.65 -89.745
                                       179.49 10.4039
## mLen
                                                                0.001258 **
## mInv
           19 204.45 254.51 -83.227
                                       166.45 13.0367
                                                            3
                                                                0.004558 **
## mTchXTry 20 202.24 254.93 -81.120
                                       162.24 4.2144
                                                                0.040083 *
```

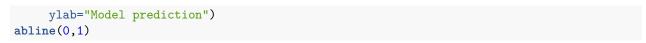
```
## mTryXChk 21 204.23 259.56 -81.114 162.23 0.0116 1 0.914352
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Choose a final model for the beta values.
```

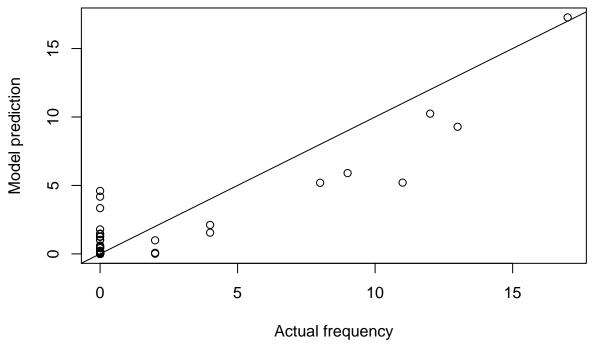
finalModel = mTchXTry

Full summary:

summary(finalModel)

```
## Generalized linear mixed model fit by maximum likelihood (Laplace
     Approximation) [glmerMod]
## Family: poisson (log)
## Formula:
## freq_week_4 ~ 1 + indexical + Teach + TryMarked.any + check.any +
       T_minus_1.any + freq_week_1_total.logcenter + averageLength_week_1.logcenter +
       inventedBy + Teach:TryMarked.any + (1 + indexical | colourName)
##
##
      Data: variants
## Control: gcontrol
##
##
        AIC
                BIC
                      logLik deviance df.resid
                       -81.1
##
      202.2
              254.9
                                162.2
##
## Scaled residuals:
               1Q Median
                               3Q
## -2.1441 -0.2155 -0.0676 -0.0302 16.3373
## Random effects:
## Groups
                Name
                                  Variance Std.Dev. Corr
## colourName
                                 1.058e-15 3.252e-08
                 (Intercept)
## colourName.1 indexicalNo
                                  1.534e+00 1.239e+00
                                  1.472e+01 3.836e+00 -0.19
##
                 indexicalYes
                 indexicalYes-body 7.921e-01 8.900e-01 0.13 0.95
## Number of obs: 103, groups: colourName, 6
##
## Fixed effects:
##
                                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                  -6.6273
                                              1.3638 -4.859 1.18e-06 ***
## indexicalYes
                                   1.8474
                                              3.9586 0.467 0.640724
## indexicalYes-body
                                   2.4641
                                              0.9572
                                                      2.574 0.010046 *
## TeachTRUE
                                   4.6230
                                              1.4988 3.085 0.002039 **
## TryMarked.anyTRUE
                                                       3.877 0.000106 ***
                                   4.3366
                                              1.1187
## check.anyTRUE
                                   1.3284
                                              0.5562
                                                      2.388 0.016924 *
                                              0.7393 -1.727 0.084082 .
## T_minus_1.anyTRUE
                                  -1.2771
## freq_week_1_total.logcenter
                                              0.4075
                                                      3.125 0.001776 **
                                   1.2736
## averageLength_week_1.logcenter -0.1773
                                              0.2081 -0.852 0.394206
## inventedBy1
                                   -0.2732
                                              0.4287 -0.637 0.523947
## inventedBy2
                                   0.8704
                                              0.5757
                                                       1.512 0.130564
## inventedBy3
                                   1.0671
                                              0.5754
                                                      1.855 0.063650 .
## TeachTRUE:TryMarked.anyTRUE
                                  -3.1701
                                              1.5464 -2.050 0.040362 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation matrix not shown by default, as p = 13 > 12.
## Use print(x, correlation=TRUE) or
     vcov(x)
                if you need it
Check the predictions:
plot(variants$freq_week_4, exp(predict(finalModel)),
    xlab="Actual frequency",
```





These are the variants used in the final week:

variants[variants\$freq_week_4>0,c("colourName","sign", 'freq_week_4')]

##		${\tt colourName}$				sign	freq_week_4
##	1	red		2			
##	2	red			RED(N	(HTUOI	12
##	6	brown	IX: 'BACK	OF	ONE'S	HAND'	13
##	15	brown			IX:	WATCH	4
##	28	black				${\tt BLACK}$	17
##	39	green			GREEN-	-CHEST	8
##	47	green			CC	DRRECT	2
##	74	yellow			YELLOW	(ISL)	9
##	76	yellow			SI	GNING	2
##	87	pink			F	LOWER	11
##	92	pink			IX:7	ONGUE	4

There were 11 variants that had a frequency of greater than 0 in the final week.

The model predicts 8 of these correctly, missing 3 variants (RED(FRONTLET), CORRECT, SIGNING).

The model predicts a further 10 variants should have been observed in the final week but were not observed in reality:

##		colourName	sign
##	8	brown	IX:ARM
##	23	brown	IX:FOREST
##	36	green	GREEN-NSL
##	58	yellow	RED (MOUTH)
##	65	yellow	BRIGHT
##	86	yellow	WHITE
##	88	pink	RED(FRONTLET)

```
## 90 pink BRIGHT
## 93 pink RED(MOUTH)
## 100 pink SIGNING
```

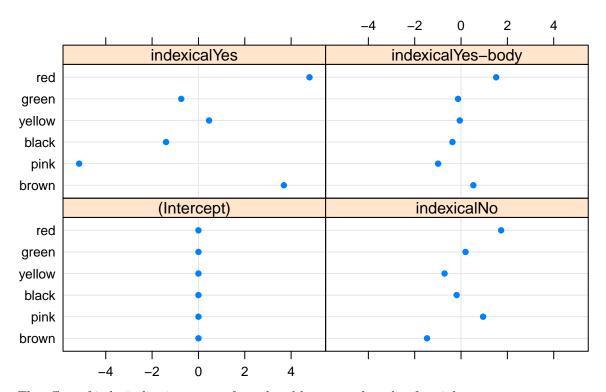
Random slopes results

We can plot the random slopes below:

```
dotplot(ranef(finalModel))
```

\$colourName

colourName



The effect of indexicality is stronger for red and brown, and weaker for pink.

Check whether the coefficients are radically different with a full random effects structure:

```
##
## Pearson's product-moment correlation
##
## data: fixef(finalModel) and fixef(finalModelFull)
## t = 5.8026, df = 11, p-value = 0.0001188
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.6080844 0.9599652
## sample estimates:
```

cor ## 0.8681874

The correlation is high, suggesting that the extra random slopes would not have a big effect on the results.

Summary

Here is a summary of the main results:

There was a significant main effect of indexicality (beta = 1.8, log likelihood difference = 3.7, df = 2, Chi Squared = 7.49, p = 0.024). (beta for body-indexical = 0.853). Indexical variants were more frequent in the final week.

There was a significant main effect of teaching (beta = 4.6, log likelihood difference = 17, df = 1, Chi Squared = 34.3, p = 4.7e-09). Teaching increased the frequency of variants in the final week.

There was a significant main effect of try marking (beta = 4.3, log likelihood difference = 31, df = 1, Chi Squared = 62.85, p = 2.2e-15). Variants that were try marked more often were more frequent in the final week.

There was a significant main effect of checking (beta = 1.3, log likelihood difference = 15, df = 1, Chi Squared = 29.54, p = 5.5e-08). Variants used in a checking context were more frequent in the final week.

There was no significant main effect of use in repair initiation (T-1) (beta = -1.3 , log likelihood difference = 0.13 , df = 1 , Chi Squared = 0.26 , p = 0.61).

There was a significant main effect of frequency in week 1 (beta = 1.3, log likelihood difference = 3.8, df = 1, Chi Squared = 7.57, p = 0.0059). More frequent forms in the first week were more likely to be more frequent in the final week.

There was a significant main effect of sign length (beta = -0.18, log likelihood difference = 5.2, df = 1, Chi Squared = 10.4, p = 0.0013). Shorter signs were more frequent in the final week.

There was a significant main effect of first user (invented By) (log likelihood difference = 6.5, df = 3, Chi Squared = 13.04, p = 0.0046). Signs invented by the signer from Nepal were less frequent in the final week.

There was a significant interaction between try marking and teaching (beta = -3.2, log likelihood difference = 2.1, df = 1, Chi Squared = 4.21, p = 0.04). The effect of teaching was bigger when the variant was also often try marked (see graphs below).

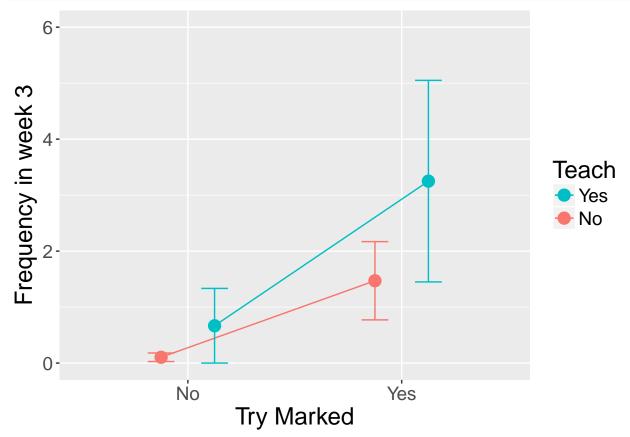
We also found some evidence that the effect of indexicality is more important for black and red, and less important for green and pink.

Graphs

Teaching and Try marking

Plot the interaction between teaching and try marking. Variants are more frequent in the final week if they were both taught and try marked. However, the second plot shows that there are actually relatively few taught variants, suggesting that the results may not generalise well.

```
sumStats2 = summarySE(variants, measurevar="freq_week_4",
                      groupvars=c("TryMarked.any", "Teach"))
sumStats2$TryMarked.any = c("No","Yes")[as.numeric(sumStats2$TryMarked.any)]
dodge <- position_dodge(width=0.5)</pre>
main.plot <- ggplot(sumStats2,</pre>
    aes(x = TryMarked.any, y = freq_week_4, colour=Teach)) +
  geom_point(position=dodge, size=4) +
  geom_line(aes(group=Teach),position=dodge) +
  geom_errorbar(aes(ymax=freq_week_4+se, ymin=freq_week_4-se), width=0.25,position=dodge) +
  xlab("Try Marked") +
  ylab("Frequency in week 3") +
  coord cartesian(ylim=c(0,6)) +
  scale_color_discrete(breaks=c(TRUE,FALSE),
                       labels=c("Yes","No"),
                       name="Teach") +
  theme(text=element_text(size=18))
main.plot
```



```
aes(x = TryMarked.any, y = freq_week_4, colour=Teach)) + geom_jitter()
   15 -
freq_week_4
   10 -
                                                                                  Teach
                                                                                   FALSE
                                                                                   TRUE
    5 -
    0 -
                       FALSE
                                                        TRUE
                                   TryMarked.any
## pdf
##
Plot of the marginal effects of the predicted probabilities for each fixed effect:
x = sjp.glmer(finalModel, 'eff',
          vars=c("indexical",'check.any','averageLength_week_1.logcenter',
             'freq_week_1_total.logcenter'),
          facet.grid = F,
          prnt.plot = F)
## Interaction terms in model have been ignored. Use `sjp.int()` to plot effects of interaction terms.
# Rescale frequency back to real values
freq.m = x$plot.list[[3]]$data$x
xplot.list[[3]]$data$x =
  exp(freq.m*
```

ggplot(variants,

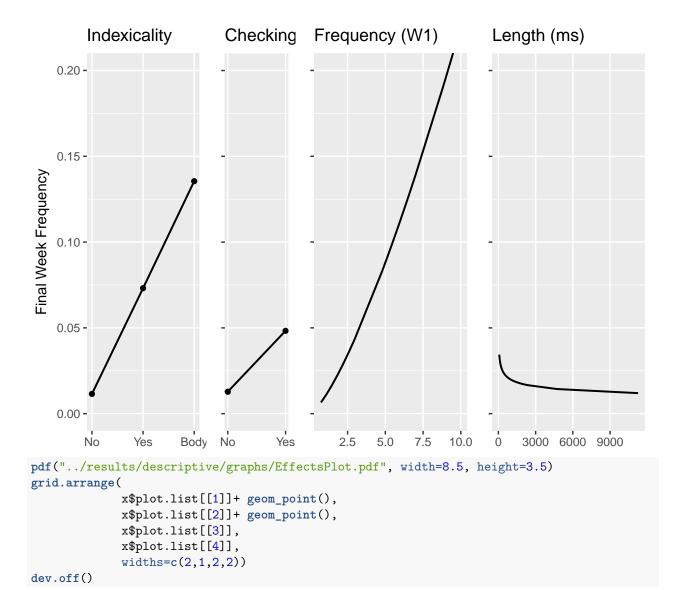
attr(variants\$freq_week_1_total.logcenter, 'scaled:scale') +
attr(variants\$freq_week_1_total.logcenter, 'scaled:center') -1)

attr(variants\$averageLength_week_1.logcenter, 'scaled:scale') +

Rescale length back to real values
len.m = x\$plot.list[[4]]\$data\$x
x\$plot.list[[4]]\$data\$x =

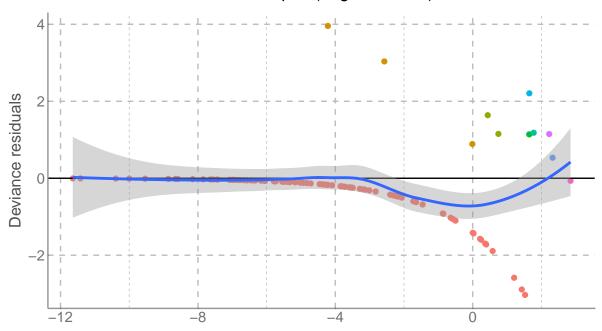
exp(len.m*

```
attr(variants$averageLength_week_1.logcenter, 'scaled:center') -1)
x$plot.list[[1]]$labels$title = "Indexicality"
x$plot.list[[1]]$scales$scales[[1]]$labels = c("No", "Yes", "Body")
x$plot.list[[2]]$labels$title = "Checking"
x$plot.list[[2]]$scales$scales[[1]]$labels = c("No","Yes")
x$plot.list[[3]]$labels$title = "Frequency (W1)"
x$plot.list[[4]]$labels$title = "Length (ms)"
for(i in 1:4){
  xplot.list[[i]]$coordinates$limits$y = c(0,0.2)
  if(i>1){
   x$plot.list[[i]]$theme =
     list(
        panel.grid.minor.x = element_blank(),
        axis.text.y = element_blank(),
        axis.line.y=element_blank())
  } else{
   x$plot.list[[i]]$theme = list(panel.grid.minor.x = element_blank())
 x$plot.list[[i]]$labels$y = element_blank()
x$plot.list[[1]]$labels$y = "Final Week Frequency"
grid.arrange(
             x$plot.list[[1]]+ geom_point(),
             x$plot.list[[2]]+ geom_point(),
             x$plot.list[[3]],
             x$plot.list[[4]],
             widths=c(2,1,2,2))
```

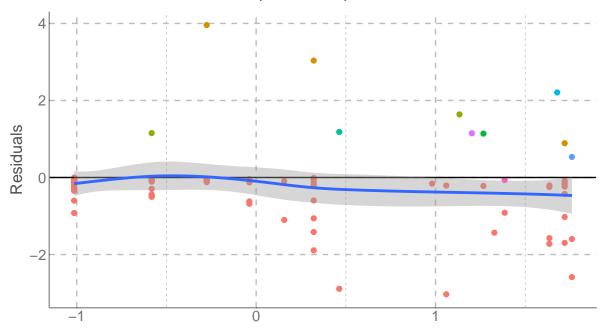


pdf ## 2 sjp.glmer(finalModel, 'ma')

Residual plot (original model)



Log-predicted values Linear relationship between predictor and residuals



freq_week_1_total.logcenter

