Language and earings management: controlling for linguistic history

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Introduction

This document shows the statistical procedure and R code for testing the relationship between strong/weak FTR and accrual based earnings management (AAM), with and without controls for language family.

We start by describing the variables, then showing how the data was loaded and linked to the language family data. We then demonstrate that the AAM is best modelled with a gamma distribution (see later in the document for the same test with gaussian distributions).

The mixed effects modelling section runs the main statistical models with and without controls for language family.

The next sections demonstrate a series of alterantive tests, including:

- Assuming a gaussian distribution
- A decision tree analysis that takes into account non-linear effects and interactions.
- A visualisation of differences between language families
- A test that uses continuous historical distances from a phylogenetic tree
- An OLS regression with cluster robust standard errors

Variables

Each observation in the data is a single company within a particular country.

• AAM: accrual-based earnings management, following Kothari et al. (2005).

- strongftr: Whether the main language of the country has a 'strong' Future Tense Reference system, according to Chen (2013).
- mainLanguageFamily (constructed below): The language family of the main language(s) in the company's country.

Country-level economic predictors:

- invpro: Investor protection score, based on the anti-director index from Djankov et al. (2008)
- ggr: Country GDP growth rate

Country-level cultural predictors:

- pd: Power distance index, based on Hofstede (2001)
- indiv: Individualism/collectivism score, based on Hofstede (2001)
- mas: Masculinity/femininity score, based on Hofstede (2001)
- ua: Uncertainty avoidance score, based on Hofstede (2001)
- 1to: Long-/short-term orientation score, based on Hofstede (2001);
- indul: Indulgence, based on Hofstede (2001);

Company-level economic predictors:

- SIZE: Company size, measured as the natural logarithm of total assets adjusted for inflation rate
- BTM: Company book value of common equity divided by common value of equity;
- LEV: Company leverage, measured as short- and long- term debt divided by total assets
- ROA: Company return on assets, measured as income before extraordinary items divided by total assets
- MEET: Dummy variable that takes one for firm-year observations with actual annual EPS greater than or equal to consensus analyst earnings forecast, zero otherwise.
- LOSS: Dummy variable that takes one for firm-year observations with negative income before extraordinary items, zero otherwise.

Load libraries

```
library(lme4)
library(sjPlot)
library(REEMtree)
library(rpart)
library(mart.plot)
library(MASS)
library(ggplot2)
library(RColorBrewer)
library(MCMCglmm)
library(ape)
library(caper)
library(stargazer)
library(dplyr)
library(lattice)
```

Load data

Match each country to its main language and language family:

```
countryMainLanguageFamily =
  read.csv("../data/raw/CountryMainLanguageToLanguageFamily.csv",
    stringsAsFactors = F)

d$mainLanguageFamily =
  countryMainLanguageFamily[
    match(as.character(d$loc),
        countryMainLanguageFamily$Country.Code),
    ]$Family
```

Remove countries with many main language families:

Remove cases with missing data:

```
keyVar = c("invpro","pd","indiv","mas",
    "ua","lto","indul","ggr","SIZE",
    "BTM","LEV","ROA","MEET","LOSS")
d2 = d2[complete.cases(d2[,keyVar,]),]
```

Table of languages:

```
data.frame(
  tapply(d2$strongftr,as.character(d2$loc),head,n=1)
       tapply.d2.strongftr..as.character.d2.loc...head..n...1.
##
## AUS
                                                                  1
## AUT
                                                                  0
## BEL
                                                                  0
## BGR
                                                                  1
## BRA
                                                                  0
## CAN
                                                                  1
## CHE
                                                                 0
## CHL
                                                                  1
## CHN
                                                                 0
## COL
                                                                  1
## CZE
                                                                  1
## DEU
                                                                  0
                                                                 0
## DNK
## EGY
                                                                  1
## ESP
                                                                  1
## FIN
                                                                  0
## FRA
                                                                  1
## GBR
                                                                  1
## GRC
                                                                  1
## HKG
                                                                  0
## HUN
                                                                  1
## IDN
                                                                 0
## IND
                                                                  1
## IRL
                                                                  1
## ITA
                                                                  1
## JOR
                                                                  1
## JPN
                                                                  0
## KOR
                                                                  1
## LTU
                                                                  1
                                                                  0
## LUX
## LVA
                                                                  1
## MAR
                                                                  1
## MEX
                                                                  1
## MYS
                                                                  0
## NLD
                                                                  0
## NOR
                                                                  0
## NZL
                                                                  1
## PAK
                                                                  1
## PER
                                                                  1
## PHL
                                                                  1
## POL
                                                                  1
## PRT
                                                                  1
## ROU
                                                                  1
## RUS
                                                                  1
## SGP
                                                                  1
## SWE
                                                                  0
## THA
                                                                  1
## TUR
                                                                  1
## TWN
                                                                  0
```

USA 1

Convert to factors:

```
d2$mainLanguageFamily = factor(d2$mainLanguageFamily)
d2$MEET = factor(d2$MEET)
d2$LOSS = factor(d2$LOSS)
d2$strongftr = factor(d2$strongftr)
```

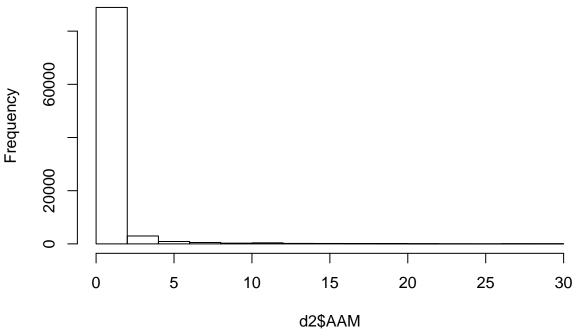
Scale and center varaibles:

Modelling AAM with a gamma distribution

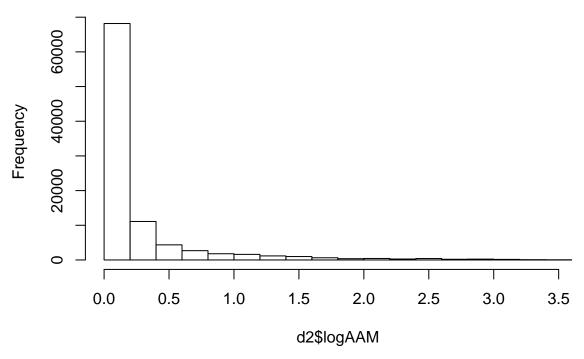
The distribution of the AAM variable is highly skewed and values below zero are not permitted:

hist(d2\$AAM)

Histogram of d2\$AAM



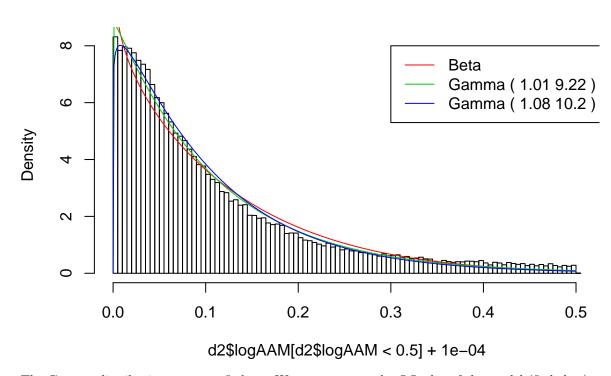
Histogram of d2\$logAAM



If we assume a Gaussian distribution, the statistical models below produce very poor fits, as can be seen in this QQ plot below:

We can compare how Beta and Gamma distributions fit the log data:

Log AAM



The Gamma distribution seems to fit best. We can compare the QQ plot of the model (fit below):

Normal Q-Q Plot

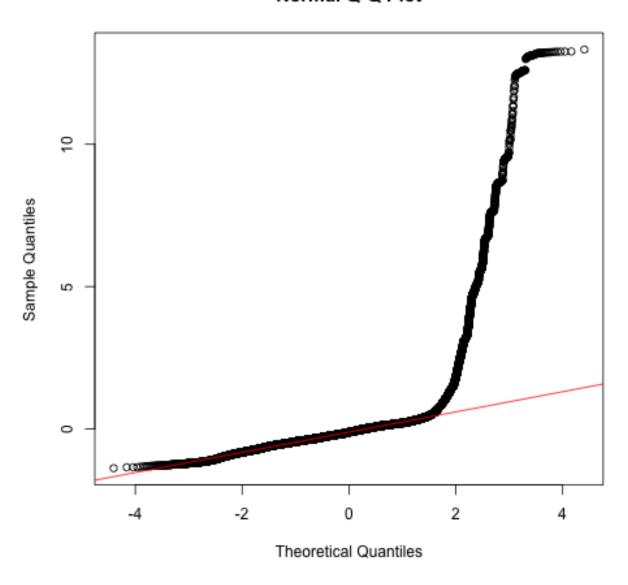


Figure 1: QQ plot for a model with a Gaussian distribution

Normal Q-Q Plot

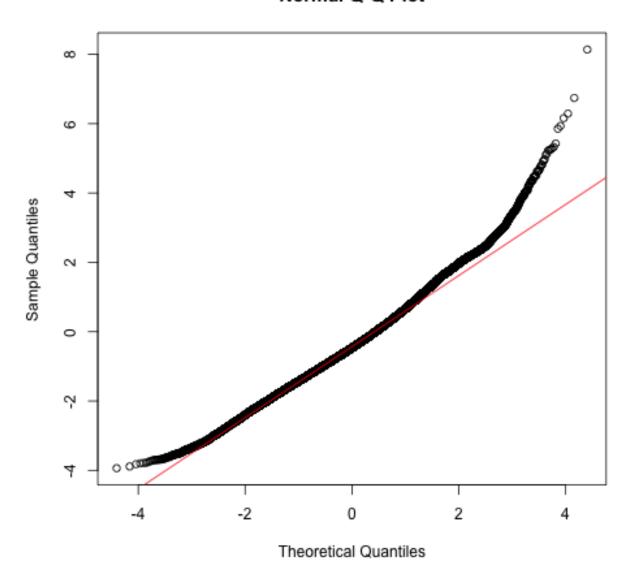


Figure 2: QQ plot for the model with a Gamma distribution

Still not perfect at higher levels, but much better than the Gaussian models.

Mixed effects modelling

Fit a model with a Gamma distribution (without language family controls, with a random intercept by family and with a random intercept and slope):

Now we add a random intercept for each language family:

We also add a random slope for FTR by language family:

Use model comparison to see if the random effects are explaining variance in the model:

anova(mA1Gamma,mB1Gamma,mB2Gamma)

```
## Data: d2
## Models:
## mA1Gamma: logAAM + 1e-04 \sim pd + indiv + mas + ua + lto + indul + ggr +
                 invpro + SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) +
## mA1Gamma:
## mA1Gamma:
                 (1 | indus) + strongftr
## mB1Gamma: logAAM + 1e-04 \sim pd + indiv + mas + ua + lto + indul + ggr +
## mB1Gamma:
                 invpro + SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) +
## mB1Gamma:
                 (1 | indus) + (1 | mainLanguageFamily) + strongftr
## mB2Gamma: logAAM + 1e-04 \sim 1 + pd + indiv + mas + ua + lto + indul + ggr +
## mB2Gamma:
                 invpro + SIZE + BTM + LEV + ROA + MEET + LOSS + strongftr +
## mB2Gamma:
                 (1 | fyear) + (1 | indus) + (1 + I(as.numeric(strongftr)) |
```

```
## mB2Gamma:
                 mainLanguageFamily)
##
            Df
                   AIC
                            BIC logLik deviance
                                                  Chisq Chi Df Pr(>Chisq)
## mA1Gamma 19 -135645 -135465 67841
                                        -135683
## mB1Gamma 20 -138253 -138064
                                        -138293 2609.94
                                                                 < 2.2e-16 ***
                                 69146
## mB2Gamma 22 -138423 -138215
                                 69233
                                        -138467 173.94
                                                                 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Check that the model is producing a sensible distribution:
modelPredictions = exp(predict(mB1Gamma))-0.0001
par(mfrow=c(1,2))
hist(modelPredictions[modelPredictions<1],main="Predicted")</pre>
hist(d2$logAAM[d2$logAAM<1],main="Actual")</pre>
                   Predicted
                                                                   Actual
     15000
Frequency
                                              Frequency
                                                    5000
     5000
                                                    5000
                                                                        0.6 0.8
          0.0 0.2 0.4 0.6 0.8 1.0
                                                        0.0 0.2 0.4
                                                                                   1.0
    modelPredictions[modelPredictions < 1]
                                                        d2\log AM[d2\log AM < 1]
par(mfrow=c(1,1))
png("../results/misc/qqplot_Gamma.png")
qqnorm(resid(mB1Gamma))
qqline(resid(mB1Gamma),col=2)
dev.off()
## pdf
##
     2
Model results:
summary(mA1Gamma)
## Generalized linear mixed model fit by maximum likelihood (Laplace
     Approximation) [glmerMod]
```

Formula: $logAAM + 1e-04 \sim pd + indiv + mas + ua + lto + indul + ggr +$

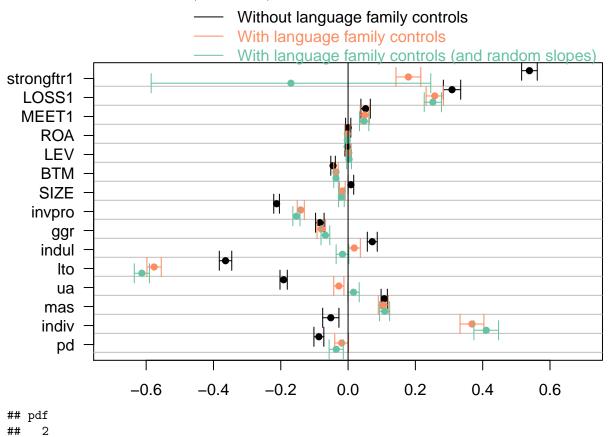
Family: Gamma (log)

```
##
       invpro + SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) +
##
       (1 | indus) + strongftr
##
      Data: d2
##
##
         AIC
                   BIC
                         logLik deviance df.resid
## -135644.9 -135465.2
                         67841.5 -135682.9
                                               94688
## Scaled residuals:
     Min
              1Q Median
                            3Q
                                  Max
## -0.821 -0.619 -0.338 0.225 34.398
## Random effects:
## Groups
                         Variance Std.Dev.
## fyear
             (Intercept) 0.2003
                                  0.4476
                                  0.3436
## indus
             (Intercept) 0.1181
## Residual
                         1.4813
                                  1.2171
## Number of obs: 94707, groups: fyear, 20; indus, 9
##
## Fixed effects:
                Estimate Std. Error t value Pr(>|z|)
## (Intercept) -1.628030
                          0.126587 -12.861 < 2e-16 ***
              -0.086784
                           0.007523 -11.535 < 2e-16 ***
## pd
## indiv
                                    -4.175 2.98e-05 ***
               -0.051336
                           0.012296
## mas
                           0.004742 22.651
               0.107415
                                            < 2e-16 ***
## ua
              -0.191481
                           0.005521 -34.685 < 2e-16 ***
## lto
              -0.364160
                          0.009434 -38.600 < 2e-16 ***
## indul
               0.071917
                           0.007524
                                     9.559
                                            < 2e-16 ***
                          0.006459 -12.987
## ggr
               -0.083885
                                            < 2e-16 ***
                           0.004301 -49.407 < 2e-16 ***
## invpro
              -0.212485
## SIZE
               0.008388
                           0.004261
                                     1.968
                                               0.049 *
## BTM
               -0.044603
                           0.003439 -12.970 < 2e-16 ***
## LEV
              -0.002114
                           0.003680 -0.575
                                               0.566
## ROA
               0.000377
                           0.003958
                                     0.095
                                               0.924
                                     7.306 2.75e-13 ***
## MEET1
               0.052116
                           0.007133
## LOSS1
                0.308902
                           0.013138
                                    23.512 < 2e-16 ***
               0.538942
                           0.011844 45.505 < 2e-16 ***
## strongftr1
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation matrix not shown by default, as p = 16 > 12.
## Use print(x, correlation=TRUE) or
##
       vcov(x)
                      if you need it
summary(mB1Gamma)
## Generalized linear mixed model fit by maximum likelihood (Laplace
     Approximation) [glmerMod]
   Family: Gamma (log)
## Formula: logAAM + 1e-04 \sim pd + indiv + mas + ua + lto + indul + ggr +
##
       invpro + SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) +
##
       (1 | indus) + (1 | mainLanguageFamily) + strongftr
##
      Data: d2
##
##
         AIC
                   BIC
                          logLik deviance df.resid
```

```
## -138252.8 -138063.7
                        69146.4 -138292.8
                                              94687
##
## Scaled residuals:
               1Q Median
                               3Q
      Min
                                      Max
## -0.8377 -0.6265 -0.3331 0.2380 30.7849
##
## Random effects:
## Groups
                       Name
                                  Variance Std.Dev.
## fyear
                       (Intercept) 0.1944
                                           0.4409
## indus
                       (Intercept) 0.1172
                                           0.3424
## mainLanguageFamily (Intercept) 1.0054
                                           1.0027
## Residual
                                  1.4246
                                           1.1936
## Number of obs: 94707, groups: fyear, 20; indus, 9; mainLanguageFamily, 9
##
## Fixed effects:
##
                Estimate Std. Error t value Pr(>|z|)
                          0.311399 -5.814 6.11e-09 ***
## (Intercept) -1.810417
              -0.019086
                          0.010443 -1.828 0.067599 .
## indiv
               0.368239
                          0.018089 20.357 < 2e-16 ***
## mas
               0.104654
                          0.007575 13.816 < 2e-16 ***
## ua
              -0.027408
                          0.007689 -3.564 0.000365 ***
## lto
              -0.576462
                          0.010866 -53.050 < 2e-16 ***
## indul
               0.018231
                          0.009269
                                    1.967 0.049193 *
              -0.079519
                          0.006515 -12.205
                                           < 2e-16 ***
## ggr
                          0.005364 -26.213 < 2e-16 ***
## invpro
              -0.140606
## SIZE
              -0.017009
                          0.004316 -3.941 8.11e-05 ***
## BTM
              -0.036026
                          0.003404 -10.583 < 2e-16 ***
## LEV
                                    0.563 0.573636
               0.002055
                          0.003653
## ROA
              -0.002173
                          0.003933
                                   -0.553 0.580529
## MEET1
               0.049932
                          0.007059
                                    7.074 1.51e-12 ***
## LOSS1
               0.257498
                          0.013082 19.683 < 2e-16 ***
## strongftr1
              0.179187
                          0.018866
                                    9.498 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation matrix not shown by default, as p = 16 > 12.
## Use print(x, correlation=TRUE) or
##
       vcov(x)
                      if you need it
summary(mB2Gamma)
## Generalized linear mixed model fit by maximum likelihood (Laplace
     Approximation) [glmerMod]
  Family: Gamma (log)
## Formula: logAAM + 1e-04 \sim 1 + pd + indiv + mas + ua + lto + indul + ggr +
       invpro + SIZE + BTM + LEV + ROA + MEET + LOSS + strongftr +
##
##
       (1 | fyear) + (1 | indus) + (1 + I(as.numeric(strongftr)) |
##
      mainLanguageFamily)
##
     Data: d2
##
         AIC
                  BIC
                         logLik deviance
                                           df.resid
## -138422.8 -138214.7
                        69233.4 -138466.8
                                              94685
##
## Scaled residuals:
```

```
1Q Median
                               3Q
## -0.8383 -0.6263 -0.3326 0.2380 31.1752
##
## Random effects:
##
  Groups
                      Name
                                               Variance Std.Dev. Corr
## fyear
                      (Intercept)
                                               0.2067
                                                        0.4547
  indus
                      (Intercept)
                                               0.1191
                                                        0.3452
##
   mainLanguageFamily (Intercept)
                                               0.3341
                                                        0.5780
                      I(as.numeric(strongftr)) 0.3950
##
                                                        0.6285
                                                                 -0.14
## Residual
                                               1.4226
                                                        1.1927
## Number of obs: 94707, groups: fyear, 20; indus, 9; mainLanguageFamily, 9
##
## Fixed effects:
##
               Estimate Std. Error t value Pr(>|z|)
## (Intercept) -1.620150
                          0.268547 -6.033 1.61e-09 ***
## pd
              -0.035222
                          0.010760 -3.273 0.00106 **
## indiv
                          0.018691 21.966 < 2e-16 ***
               0.410556
## mas
               0.108590
                          0.007622 14.248 < 2e-16 ***
## ua
               0.016182
                          0.008635
                                    1.874 0.06095 .
## lto
              -0.612745
                          0.011464 -53.448 < 2e-16 ***
## indul
              -0.016606
                          0.009617 -1.727 0.08420 .
## ggr
              -0.067387
                          0.006620 -10.180 < 2e-16 ***
                          0.005415 -28.347 < 2e-16 ***
## invpro
              -0.153494
## SIZE
              -0.019870
                          0.004320 -4.599 4.24e-06 ***
## BTM
              -0.035865
                          0.003402 -10.543 < 2e-16 ***
## LEV
               0.002873
                          0.003653
                                    0.787 0.43156
## ROA
              -0.002389
                          0.003930 -0.608 0.54317
## MEET1
               0.047748
                          0.007056
                                    6.767 1.32e-11 ***
                          0.013080 19.268 < 2e-16 ***
## LOSS1
               0.252019
                          0.211944 -0.801 0.42319
## strongftr1 -0.169746
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation matrix not shown by default, as p = 16 > 12.
## Use print(x, correlation=TRUE) or
##
      vcov(x)
                     if you need it
```

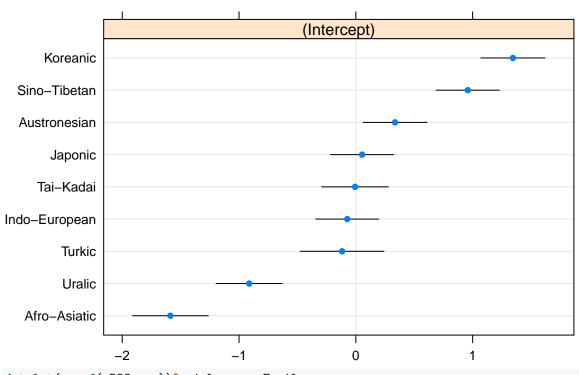
Plot fixed effects for all models (code hidden):



View random effects for language family

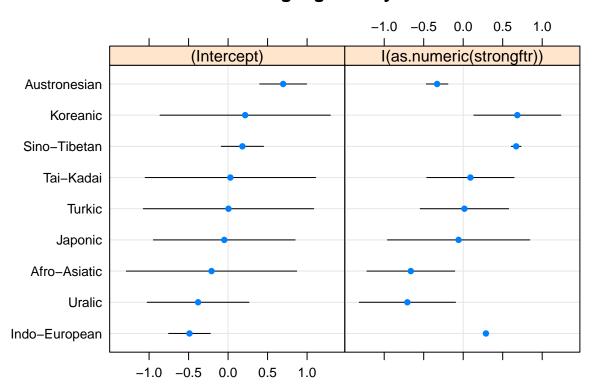
dotplot(ranef(mB1Gamma))\$mainLanguageFamily

mainLanguageFamily



dotplot(ranef(mB2Gamma))\$mainLanguageFamily

mainLanguageFamily



Summary

Without a random intercept by main language family: There was a significant main effect of FTR (beta = 0.54, log likelihood difference = 1000, df = 1, Chi Squared = 2036.03, p = 0).

With a random intercept by main language family: There was a significant main effect of FTR (beta = 0.18 , log likelihood difference = 45 , df = 1 , Chi Squared = 89.4 , p = 3.2e-21).

Other effects

Below are some statistics for other effects, using the same method as above:

```
resOther = data.frame(
  Label = NA,
  Beta = NA,
  loglikDiff = NA,
  df = NA,
  chisq.test = NA,
  p = NA, stringsAsFactors = F)
for(v in c("pd",'indiv','mas',
           'ua', 'lto', 'indul', 'ggr',
           'SIZE', "BTM", "LEV", "ROA")){
  mAOther0 = update(mA1Gamma, paste("~ . -",v))
  mAOtherAnova = anova(mAOtherO, mA1Gamma)
  mBOtherO = update(mB2Gamma, paste("~ . -",v))
  mBOtherAnova = anova(mBOtherO,mB2Gamma)
  mARes = getMEText(mAOtherAnova,"X",summary(mA1Gamma)$coef[v,],returnText = F)
  mBRes = getMEText(mBOtherAnova,"X",summary(mB2Gamma)$coef[v,],returnText = F)
  resOther = rbind(resOther, c(paste(v,": No controls"), mARes))
  resOther = rbind(resOther, c(paste(v,": With Controls"),mBRes))
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
## control$checkConv, : Model failed to converge with max|grad| = 0.00113304
## (tol = 0.001, component 1)
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
## control$checkConv, : Model failed to converge with max|grad| = 0.00145232
## (tol = 0.001, component 1)
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
## control$checkConv, : Model failed to converge with max|grad| = 0.00135493
## (tol = 0.001, component 1)
resOther = resOther[!is.na(resOther$Label),]
print(resOther)
##
                     Label
                              Beta loglikDiff df chisq.test
## 2
                                                    130.74 2.8e-30
          pd : No controls
                           -0.087
                                           65 1
## 3
        pd: With Controls -0.035
                                           5.4 1
                                                       10.75
                                                                0.001
## 4
        indiv : No controls
                            -0.051
                                           8.7 1
                                                       17.43
                                                                3e-05
## 5
    indiv : With Controls
                              0.41
                                           230 1
                                                      451.83 2.9e-100
## 6
         mas : No controls
                              0.11
                                           240 1
                                                      489.6 1.7e-108
## 7
       mas : With Controls
                              0.11
                                           100 1
                                                     200.99 1.3e-45
## 8
          ua : No controls
                             -0.19
                                           610 1
                                                     1212.6 1.1e-265
## 9
        ua: With Controls 0.016
                                           1.8 1
                                                        3.51
                                                                0.061
## 10
         lto : No controls
                             -0.36
                                           760 1
                                                     1522.8
## 11
       lto : With Controls
                                          1500 1
                                                     2900.95
                                                                    0
                             -0.61
        indul : No controls
                             0.072
                                           45 1
                                                       90.36
## 12
                                                                2e-21
                                           1.5 1
## 13 indul : With Controls -0.017
                                                        2.98
                                                                0.084
## 14
         ggr: No controls -0.084
                                           86 1
                                                     171.49 3.5e-39
## 15
       ggr: With Controls -0.067
                                           53 1
                                                     105.06 1.2e-24
## 16
        SIZE: No controls 0.0084
                                           1.9 1
                                                        3.88
                                                                0.049
## 17 SIZE : With Controls
                            -0.02
                                           11 1
                                                       21.11 4.3e-06
```

```
## 18
         BTM: No controls -0.045
                                          80 1
                                                    160.06 1.1e-36
## 19
       BTM: With Controls -0.036
                                          53 1
                                                    106.91 4.6e-25
       LEV: No controls -0.0021
## 20
                                        0.16 1
                                                      0.33
                                                               0.57
## 21
       LEV: With Controls 0.0029
                                        0.31 1
                                                      0.62
                                                               0.43
## 22
         ROA: No controls 0.00038
                                      0.0045 1
                                                      0.01
                                                               0.92
       ROA: With Controls -0.0024
                                        0.19 1
## 23
                                                      0.37
                                                               0.54
resOther2 = cbind(
 resOther[seq(1,nrow(resOther)-1,by=2),c("Label","Beta","p")],
 resOther[seq(2,nrow(resOther),by=2),c("Beta","p")])
write.csv(resOther2,"../results/BetaResults_OtherVariables.csv",row.names = F)
```

Alternative tests

Gaussian distribution model

Model A: no controls for language family

Model mAO is a baseline model and model mA1 adds the effect for FTR.

Look at the estiamtes for variables within model mA1:

```
summary(mA1)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula:
## AAM.scaled ~ invpro + pd + indiv + mas + ua + lto + indul + ggr +
       SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) + (1 |
##
##
       indus) + strongftr
##
     Data: d2
##
## REML criterion at convergence: 256954.1
##
## Scaled residuals:
##
      Min
                1Q Median
## -1.4990 -0.3712 -0.1335 0.1310 14.2360
##
## Random effects:
                         Variance Std.Dev.
## Groups
## fyear
             (Intercept) 0.04171 0.2042
             (Intercept) 0.01485 0.1218
## indus
## Residual
                         0.88034 0.9383
## Number of obs: 94707, groups: fyear, 20; indus, 9
##
## Fixed effects:
##
                Estimate Std. Error t value
                           0.063450
                                      2.422
## (Intercept) 0.153654
## invpro
              -0.100554
                           0.003510 -28.644
                                      2.088
## pd
                0.012819
                           0.006140
## indiv
                0.013771
                           0.009557
                                      1.441
## mas
                0.063738
                           0.003837 16.610
## ua
               -0.062749
                           0.004456 - 14.081
## lto
               -0.124885
                           0.007243 -17.241
## indul
                0.031991
                           0.006528
                                      4.901
              -0.091870
                           0.005601 -16.401
## ggr
               0.036230
                           0.003744
                                     9.677
## SIZE
## BTM
               -0.010561
                           0.003274
                                    -3.225
## LEV
                0.006785
                           0.003353
                                     2.023
```

```
0.014690
                         0.003787
## ROA
                                    3.879
## MEET1
               0.031684 0.006293 5.035
## LOSS1
               0.167342
                         0.011696 14.308
             0.149591
                          0.010309 14.511
## strongftr1
##
## Correlation matrix not shown by default, as p = 16 > 12.
## Use print(x, correlation=TRUE) or
      vcov(x)
                     if you need it
```

Compare the fit of the two models to assess the effect of FTR:

anova(mA0,mA1)

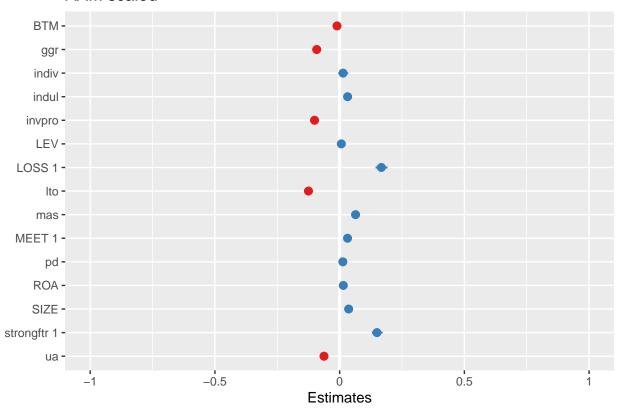
```
## refitting model(s) with ML (instead of REML)
## Data: d2
## Models:
## mAO: AAM.scaled ~ 1 + invpro + pd + indiv + mas + ua + lto + indul +
           ggr + SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) +
## mAO:
## mAO:
           (1 | indus)
## mA1: AAM.scaled ~ invpro + pd + indiv + mas + ua + lto + indul + ggr +
           SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) + (1 |
## mA1:
           indus) + strongftr
      Df
            AIC
                  BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## mAO 18 257063 257234 -128514
                                257027
## mA1 19 256855 257035 -128409 256817 210.38
                                                 1 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Plot fixed effects:

```
plot_model(mA1,type="est",p.kr = F)
```

 $\mbox{\tt \#\#}$ Computing p-values via Wald-statistics approximation (treating t as Wald z).

AAM scaled



Model B: with controls for language family

Model mB0 is the same as mA0, but with controls for language family. Model mB1 adds the FTR variable to the model for comparison.

```
mB0= update(mA0, ~.+(1 | mainLanguageFamily))
mB1= update(mB0, ~.+strongftr)
```

Look at the estimates for mB1:

```
summary(mB1)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula:
## AAM.scaled ~ invpro + pd + indiv + mas + ua + lto + indul + ggr +
##
       SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) + (1 |
##
       indus) + (1 | mainLanguageFamily) + strongftr
##
      Data: d2
##
## REML criterion at convergence: 256343.6
##
## Scaled residuals:
       Min
                1Q Median
##
                                       Max
## -1.4757 -0.3765 -0.1269 0.1357 14.2536
## Random effects:
## Groups
                       Name
                                   Variance Std.Dev.
## fyear
                       (Intercept) 0.04165 0.2041
## indus
                       (Intercept) 0.01531
                                            0.1237
## mainLanguageFamily (Intercept) 0.10018
                                            0.3165
## Residual
                                   0.87436 0.9351
## Number of obs: 94707, groups: fyear, 20; indus, 9; mainLanguageFamily, 9
##
## Fixed effects:
##
                Estimate Std. Error t value
## (Intercept)
               0.246953
                           0.124566
                                       1.983
## invpro
               -0.099264
                           0.004529 -21.919
## pd
                0.055776
                           0.009174
                                      6.079
## indiv
                0.162885
                           0.014282
                                    11.405
## mas
                0.039045
                           0.006110
                                      6.390
                                     -7.262
## ua
               -0.047815
                           0.006584
               -0.220395
## lto
                           0.009085 - 24.259
## indul
                0.016509
                           0.007498
                                      2.202
## ggr
               -0.102036
                           0.005758 -17.720
## SIZE
                0.020039
                           0.003848
                                     5.207
## BTM
               -0.010632
                           0.003271
                                     -3.251
## LEV
                                      2.690
                0.009026
                           0.003355
## ROA
                0.015726
                           0.003775
                                      4.165
## MEET1
                0.030613
                           0.006273
                                      4.880
## LOSS1
                0.140498
                           0.011720
                                     11.988
## strongftr1
                0.021657
                           0.016910
                                      1.281
##
## Correlation matrix not shown by default, as p = 16 > 12.
## Use print(x, correlation=TRUE) or
##
       vcov(x)
                      if you need it
```

Compare the two models to assess the significance of the FTR variable:

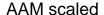
```
anova(mB0,mB1)
```

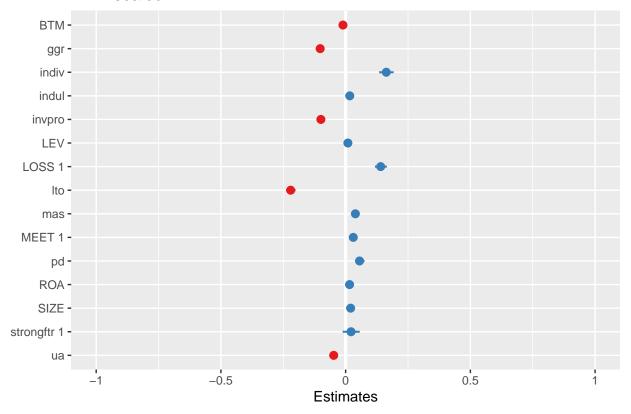
```
## refitting model(s) with ML (instead of REML)
## Data: d2
## Models:
## mBO: AAM.scaled ~ invpro + pd + indiv + mas + ua + lto + indul + ggr +
           SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) + (1 |
## mBO:
## mBO:
            indus) + (1 | mainLanguageFamily)
## mB1: AAM.scaled ~ invpro + pd + indiv + mas + ua + lto + indul + ggr +
           SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) + (1 |
## mB1:
## mB1:
            indus) + (1 | mainLanguageFamily) + strongftr
##
            AIC
                    BIC logLik deviance Chisq Chi Df Pr(>Chisq)
      Df
## mB0 19 256254 256434 -128108
                                  256216
## mB1 20 256254 256443 -128107
                                  256214 1.6614
                                                           0.1974
```

Plot fixed effects with controls for language family:

```
plot_model(mB1,type="est",p.kr = F)
```

Computing p-values via Wald-statistics approximation (treating t as Wald z).



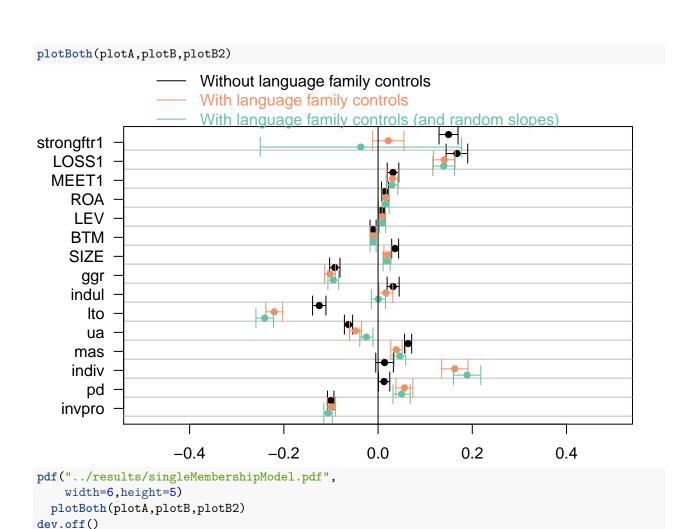


Random slopes for FTR

Test if adding a random slope for FTR by language family significantly improves the fit of the model:

```
mB2 = lmer(AAM.scaled ~ 1 +
             invpro +
             pd + indiv + mas + ua + lto + indul +
             ggr +
             SIZE + BTM + LEV + ROA +
             MEET + LOSS +
             strongftr +
             (1 | fyear) +
             (1 | indus) +
             (1 + strongftr | mainLanguageFamily),
           data = d2
anova (mB1, mB2)
## refitting model(s) with ML (instead of REML)
## Data: d2
## Models:
## mB1: AAM.scaled ~ invpro + pd + indiv + mas + ua + lto + indul + ggr +
## mB1:
           SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) + (1 |
            indus) + (1 | mainLanguageFamily) + strongftr
## mB2: AAM.scaled ~ 1 + invpro + pd + indiv + mas + ua + lto + indul +
## mB2:
            ggr + SIZE + BTM + LEV + ROA + MEET + LOSS + strongftr +
## mB2:
            (1 | fyear) + (1 | indus) + (1 + strongftr | mainLanguageFamily)
            AIC
                    BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## mB1 20 256254 256443 -128107
                                  256214
## mB2 22 256180 256388 -128068
                                  256136 78.319
                                                     2 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Yes, model fit significantly improves. The effect of FTR is even weaker:
summary(mB2)
## Linear mixed model fit by REML ['lmerMod']
## Formula: AAM.scaled ~ 1 + invpro + pd + indiv + mas + ua + lto + indul +
##
       ggr + SIZE + BTM + LEV + ROA + MEET + LOSS + strongftr +
##
       (1 | fyear) + (1 | indus) + (1 + strongftr | mainLanguageFamily)
     Data: d2
##
##
## REML criterion at convergence: 256260.6
## Scaled residuals:
      Min
               1Q Median
                                3Q
## -1.4711 -0.3755 -0.1230 0.1344 14.2610
##
## Random effects:
## Groups
                       Name
                                   Variance Std.Dev. Corr
## fyear
                       (Intercept) 0.04225 0.2055
## indus
                       (Intercept) 0.01569 0.1253
##
   mainLanguageFamily (Intercept) 0.04333 0.2082
                       strongftr1 0.07239 0.2691
                                                     0.60
## Residual
                                   0.87352 0.9346
## Number of obs: 94707, groups: fyear, 20; indus, 9; mainLanguageFamily, 9
##
## Fixed effects:
```

```
Estimate Std. Error t value
## (Intercept) 0.2949707 0.1012130
                                      2.914
## invpro
             -0.1061720 0.0045831 -23.166
               0.0499991 0.0093405
## pd
                                      5.353
## indiv
               0.1890539 0.0147841 12.788
## mas
              0.0464436 0.0062111
                                     7.478
## ua
              -0.0248139 0.0071357 -3.477
## lto
              -0.2406902 0.0094705 -25.415
## indul
              0.0007689 0.0076796
                                      0.100
## ggr
              -0.0950665 0.0058169 -16.343
## SIZE
              0.0181445 0.0038528
                                     4.709
## BTM
              -0.0105549 0.0032700 -3.228
                                     2.829
## LEV
               0.0094880 0.0033542
## ROA
               0.0161278 0.0037749
                                     4.272
## MEET1
               0.0295640 0.0062706
                                     4.715
## LOSS1
               0.1391878 0.0117246 11.871
## strongftr1 -0.0366099 0.1089020 -0.336
## Correlation matrix not shown by default, as p = 16 > 12.
## Use print(x, correlation=TRUE) or
       vcov(x)
##
                      if you need it
Calculate p-value for effect of FTR:
mB2_noFTR = update(mB2, ~. - strongftr)
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
## control$checkConv, : Model failed to converge with max|grad| = 0.00586163
## (tol = 0.002, component 1)
anova(mB2,mB2_noFTR)
## refitting model(s) with ML (instead of REML)
## Data: d2
## Models:
## mB2 noFTR: AAM.scaled ~ invpro + pd + indiv + mas + ua + lto + indul + ggr +
                 SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) + (1 |
## mB2 noFTR:
## mB2 noFTR:
                 indus) + (1 + strongftr | mainLanguageFamily)
## mB2: AAM.scaled ~ 1 + invpro + pd + indiv + mas + ua + lto + indul +
            ggr + SIZE + BTM + LEV + ROA + MEET + LOSS + strongftr +
## mB2:
            (1 | fyear) + (1 | indus) + (1 + strongftr | mainLanguageFamily)
##
                         BIC logLik deviance Chisq Chi Df Pr(>Chisq)
                  AIC
## mB2_noFTR 21 256178 256377 -128068
                                       256136
            22 256180 256388 -128068
                                        256136 0.1409
                                                                 0.7073
Plot fixed effects:
plotA = get_model_data(mA1,type="est")
## Computing p-values via Wald-statistics approximation (treating t as Wald z).
plotB = get_model_data(mB1,type="est")
## Computing p-values via Wald-statistics approximation (treating t as Wald z).
plotB2 = get_model_data(mB2,type="est")
## Computing p-values via Wald-statistics approximation (treating t as Wald z).
```



2

pdf

Summary of Gaussian model

Without a random intercept by main language family: There was a significant main effect of FTR (beta = 0.15, log likelihood difference = 110, df = 1, Chi Squared = 210.38, p = 1.1e-47).

With a random intercept by main language family: There was no significant main effect of FTR (beta = 0.022, log likelihood difference = 0.83, df = 1, Chi Squared = 1.66, p = 0.2).

Decision tree

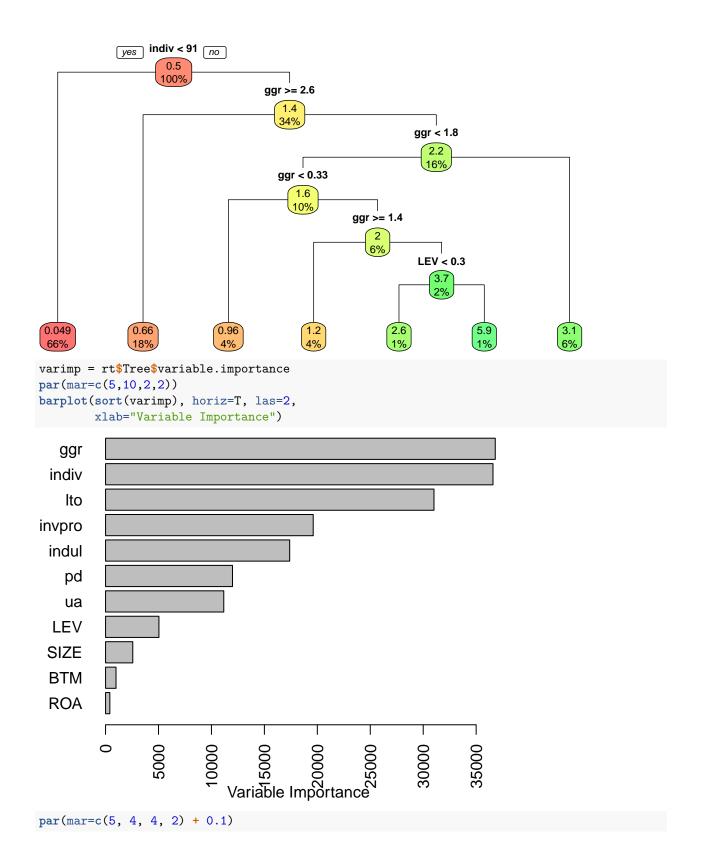
A decision tree is a machine learning technique that tries to find patterns in data. It finds a series of yes/no questions which divide datapoints into partitions that look similar. 'Variable importance' is a measure of how influential each variable is in making decisions in the tree. This is a useful way of spotting patterns in the data that linear models might miss. In this case, if FTR is a good predictor, we would expect it to appear on the tree and have relatively high variable importance.

The package REEMtree allows the inclusion of random effects for year, industry type and main language family.

The tree below shows the yes/no questions at each branch in the tree. Coloured boxes show the mean AAM value and proportion of the data in that node. As it turns out, FTR does not appear on the tree. The most important factors are ggr and indiv.

```
## Warning: Cannot retrieve the data used to build the model (so cannot determine roundint and is.binar)
## To silence this warning:
## Call rpart.plot with roundint=FALSE,
## or rebuild the rpart model with model=TRUE.
```

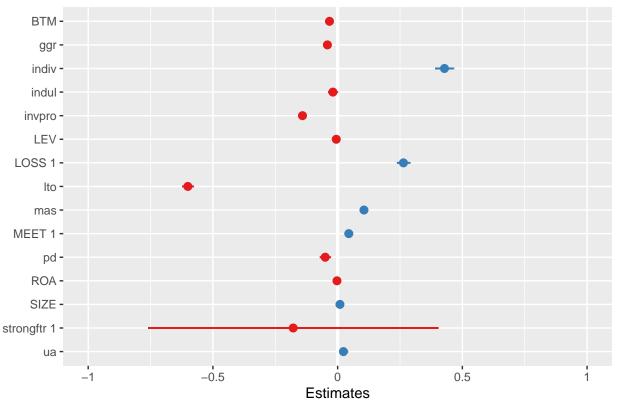
Colour



Random slopes

We can take a colser look at the random slopes for each language family:

log AAM+1 e-04



```
plot_model(mB2GammaFamily,type="slope",vars="strongftr",show.legend = T)
```

```
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : at -0.005

## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : radius 2.5e-05

## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : all data on boundary of neighborhood. make span bigger

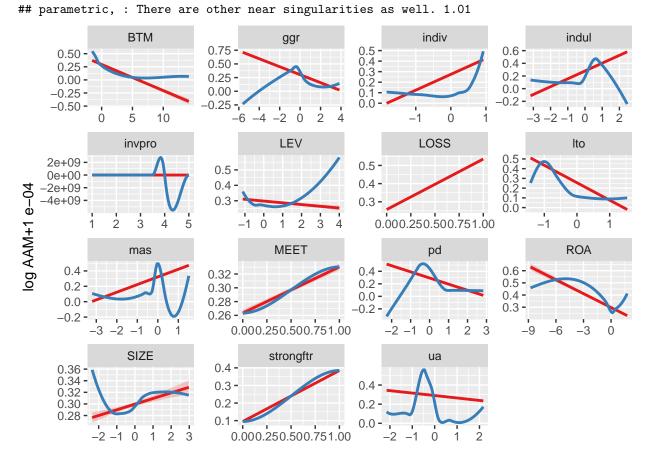
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : pseudoinverse used at -0.005

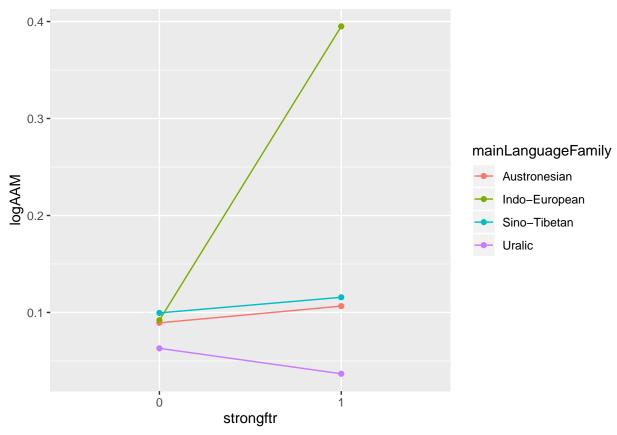
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : neighborhood radius 0.005

## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : reciprocal condition number 1

## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
```

```
## parametric, : There are other near singularities as well. 1.01
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : zero-width neighborhood. make span bigger
## Warning: Computation failed in `stat_smooth()`:
## NA/NaN/Inf in foreign function call (arg 5)
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : pseudoinverse used at -0.005
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : neighborhood radius 1.005
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : reciprocal condition number 1.2094e-25
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : There are other near singularities as well. 1.01
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : pseudoinverse used at -0.005
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : neighborhood radius 1.005
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
## parametric, : reciprocal condition number 4.1506e-26
## Warning in simpleLoess(y, x, w, span, degree = degree, parametric =
```





Model just for Indo-European languages:

```
mB1GammaIE = update(mA1Gamma,data=d2[d2$mainLanguageFamily=="Indo-European",])
summary(mB1GammaIE)
```

```
## Generalized linear mixed model fit by maximum likelihood (Laplace
##
     Approximation) [glmerMod]
  Family: Gamma (log)
##
## Formula: logAAM + 1e-04 \sim pd + indiv + mas + ua + lto + indul + ggr +
##
       invpro + SIZE + BTM + LEV + ROA + MEET + LOSS + (1 | fyear) +
##
       (1 | indus) + strongftr
##
      Data: d2[d2$mainLanguageFamily == "Indo-European", ]
##
##
        AIC
                 BIC
                       logLik deviance df.resid
## -39726.8 -39555.3 19882.4 -39764.8
                                          61616
##
## Scaled residuals:
      Min
              1Q Median
                            3Q
                                  Max
```

```
## -0.828 -0.632 -0.348 0.239 32.297
##
## Random effects:
                    Variance Std.Dev.
## Groups Name
## fyear
          (Intercept) 0.2689
                          0.5186
## indus
          (Intercept) 0.2729
                          0.5224
## Residual
                    1.4590
                           1.2079
## Number of obs: 61635, groups: fyear, 20; indus, 9
##
## Fixed effects:
            Estimate Std. Error t value Pr(>|z|)
## (Intercept) -0.326899
                    0.179284 -1.823 0.068249 .
                     0.013969 26.452 < 2e-16 ***
## pd
            0.369494
## indiv
                     0.021595 10.317 < 2e-16 ***
            0.222795
## mas
            0.244858
                     0.008143 30.071 < 2e-16 ***
## ua
            -0.534176
                     0.013590 -39.305 < 2e-16 ***
## lto
           -0.483764
                     0.016041 -30.158 < 2e-16 ***
                     0.013145 -0.191 0.848203
## indul
           -0.002516
            ## ggr
                    0.010503 -43.841 < 2e-16 ***
## invpro
            -0.460481
## SIZE
           -0.006982 0.005361 -1.302 0.192786
## BTM
            ## LEV
           ## ROA
           ## MEET1
           0.015266 0.008982 1.700 0.089207 .
## LOSS1
            ## strongftr1 -0.105764 0.026846 -3.940 8.16e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation matrix not shown by default, as p = 16 > 12.
## Use print(x, correlation=TRUE) or
##
     vcov(x)
                 if you need it
```

Phylogenetic test

cdata = data.frame(
 FTR = DP.FTR,
 AAM = DP.AAM,
 LTO = DP.LTO,

lang = names(DP.FTR)

cdata = cdata[cdata\$lang!="",]

Much of the data is linked to the Indo-European language family. We can use a phylogenetic tree (Bourckaert et al., 2012) to investigate the relationship between AAM and FTR when taking more fine-grained distinctions in linguistic history.

Subset of variables for the indo-european language family:

```
dIE = d[d$mainLanguageFamily=="Indo-European",]
dIE$DPlaceLang =
   countryMainLanguageFamily[
   match(as.character(dIE$loc),
        countryMainLanguageFamily$Country.Code),
   ]$DPlaceLang
```

Load tree and drop languages that are not in the dataset:

Run a regression using the phylogenetic tree as a variance-covariance matrix.

```
# Priors
prior.PN<-list(
   G=list(
    G1=list(V=1,nu=0.002)),
   R=list(V=1,nu=0.002))
# Chain length
burnin = 100000
postBurnin =100000
thin = 10
# Run the model
set.seed(1289)
phyloModel0<-MCMCglmm(
   AAM ~ FTR,
   random=~lang,</pre>
```

```
ginverse=list(
   lang=inverseA(tree)$Ainv),
prior = prior.PN,
verbose=FALSE,
family="gaussian",
data = cdata,
nitt=burnin+postBurnin,
thin=thin,
burnin=burnin)
```

Results:

```
summary(phyloModel0)
```

```
##
  Iterations = 100001:199991
## Thinning interval = 10
## Sample size = 10000
##
## DIC: 24.39859
##
## G-structure: ~lang
##
##
       post.mean 1-95% CI u-95% CI eff.samp
## lang
          1.395 0.0002236
                              4.025
                                       578.1
##
   R-structure: ~units
##
##
        post.mean 1-95% CI u-95% CI eff.samp
          0.597 0.0001479
## units
                               1.568
  Location effects: AAM ~ FTR
##
##
##
              post.mean 1-95% CI u-95% CI eff.samp pMCMC
## (Intercept)
                -0.7944 -2.4719
                                   0.6958
                                            1485.2 0.310
                 0.9332 -0.4488
                                   2.3000
## FTR1
                                             905.9 0.188
```

There is no significant relationship between AAM and FTR.

Do the same test for Long-Term Orientation:

```
set.seed(12829)
phyloModelLTO<-MCMCglmm(
   AAM ~ LTO,
   random=~lang,
   ginverse=list(
     lang=inverseA(tree)$Ainv),
   prior = prior.PN,
   verbose=FALSE,
   family="gaussian",
   data = cdata,
   nitt=burnin+postBurnin,
   thin=thin,
   burnin=burnin)
summary(phyloModelLTO)</pre>
```

```
##
## Iterations = 100001:199991
## Thinning interval = 10
## Sample size = 10000
## DIC: 49.44665
##
## G-structure: ~lang
##
##
       post.mean 1-95% CI u-95% CI eff.samp
## lang 0.4891 0.0001196
                          2.849
##
## R-structure: ~units
##
##
        post.mean 1-95% CI u-95% CI eff.samp
## units 0.8295 0.0003182
                           1.571
                                       1090
##
## Location effects: AAM ~ LTO
##
             post.mean 1-95% CI u-95% CI eff.samp pMCMC
##
## (Intercept) -0.02423 -0.78404 0.72067 9630 0.9426
## LTO
             -0.44768 -0.89869 -0.01900
                                           8875 0.0476 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

OLS with clustered errors

Run a robust OLS regression, then print the results when clustering standard errors by language family. The results below were run using STATA code:

```
# No clustering
```

. reg AAM_scaled strongftr1 invpro pd indiv mas ua lto indul ggr size btm lev roa meet1 loss1, robust

Linear regression

Number of obs = 94,707 F(15, 94691) = 451.86 Prob > F = 0.0000 R-squared = 0.0731 Root MSE = .96283

| Robust AAM_scaled | Coef. Std. Err. t P>|t| [95% Conf. Interval] strongftr1 | .1317505 .0033255 39.62 0.000 .1252326 .1382685

- # With clustering by language family
- . reg AAM_scaled strongftr1 invpro pd indiv mas ua lto indul ggr size btm lev roa meet1 loss1, robust cluster(mainLanguageFamily)

Linear regression

Number of obs = 94,707 F(7, 8) = . Prob > F = . R-squared = 0.0731 Root MSE = .96283

(Std. Err. adjusted for 9 clusters in mainLanguageFamily)
