

## 1. FITTING ONE RESONANCE

Following the TeachSpin Quantum Analogs manual, we model the system close to a resonance frequency as a damped, driven, harmonic oscillator. Let  $p$  denote the air pressure, let  $\omega_0$  denote the specific resonance frequency, and let  $\gamma$ , and take  $K$  and  $\gamma$  to be constants corresponding to the power of the speaker and the damping of the system respectively. Then, we have the linear differential equation

$$\frac{d^2 p}{dt^2} + 2\gamma \frac{dp}{dt} + \omega_0^2 p = K \cos(\omega t)$$

Then, we solve for the amplitude  $A$  of the steady state solution, which will give the long term behavior of the resonance. Combining the solution to the amplitude  $A$  with the assumption  $\omega_0 \gg \gamma$ , this simplifies to the model.

$$|A(\omega)| = \frac{K}{\sqrt{(\omega_0 - \omega)^2 + \lambda^2}}$$

For some variable  $\lambda$ . This gives a model for fitting a single peak. Combining this with the MATLAB Curve Fitting Toolbox with free variables  $K$ ,  $\omega_0$ , and  $\lambda$ , we can accurately fit the given data such as in `/**/`.