

## Homework 8: Formal Aspects ( Due Friday November 9)

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November 5, 2018

### 1 HERMETIAN OPERATORS (30 POINTS)

1. **Prove** that the eigenvalues of a hermetian operator are real. **Hint: use the definition of a hermetian operator**
2. **Prove** that the eigenstates of a hermetian operator are orthogonal. **Hint: assume that  $\psi_1$  and  $\psi_2$  are two eignestates of the same hermetian operator with different eigenvalues. Then, use the definition of a hermetian operator.**

### 2 MANIPULATIONS (40 POINTS)

1. Do problem 3.4 in Griffiths' book
2. Do problem 3.5 in Griffiths' book

### 3 AN EIGENVALUE PROBLEM (30 POINTS)

The Hamiltonian of a two-level system is given by

$$\hat{H} = \begin{bmatrix} \hbar\omega & \hbar\epsilon \\ \hbar\epsilon & \hbar\omega \end{bmatrix}, \quad (3.1)$$

where  $\omega > \epsilon$ . **Find** the eigen-energies and eigenstates of this Hamiltonian.