

\*  $C(t)$  is a parabola,  $v(t)$  is linear

The change in  $n(t)$  is given by its derivative,

$$\begin{aligned}\frac{dn}{dt} = n'(t) &= \frac{d}{dt}(c(t)v(t)) \\ &= c(t) \cdot \frac{dv}{dt} + v(t) \cdot \frac{dc}{dt} \quad (c(t)v'(t) + v(t)c'(t)) \\ &= (4-t^2)(3) + (1+3t)(-2t) \\ &\quad \uparrow \quad \quad \quad \uparrow \\ &\quad \frac{d}{dt}(1+3t)=3 \quad \quad \frac{d}{dt}(4-t^2)=-2t\end{aligned}$$

$$\begin{aligned}\text{So } n'(t) &= 12 - 3t^2 - 2t - 6t^2 \\ &= -9t^2 - 2t + 12\end{aligned}$$

1) Since initially means  $t=0$ ,  $n'(0) = -9(0) - 2(0) + 12 > 0$   
so initially,  $n(t)$  is increasing.

2) A change in behavior can happen at a critical point,  
where  $n'(t) = 0$ . We have to solve

$$-9t^2 - 2t + 12 = 0 \quad \text{by the quadratic formula}$$

$$t = \frac{2 \pm \sqrt{4 - 4(9)(12)}}{-18} = -\frac{1}{9} \pm \frac{\sqrt{109}}{9} \approx -1.27, \quad \uparrow \quad 1.049$$

the critical point is  $t \approx 1.05$  sec

this one makes  
sense since it  
is positive