Lecture 10

CIS 341: COMPILERS

Announcements

- Homework 3: Compiling LLVMlite
- Goal:
 - Familiarize yourself with (a subset of) the LLVM IR
 - Implement a translation down to (inefficient) X86lite
- Due: Monday, Feb. 26th

it is nearly too late to **START EARLY!!**

MIDTERM EXAM

- Thursday, March 1st in class
- Coverage: interpreters / program transformers / x86 / calling conventions / IRs / LLVM / Lexing / Parsing
- See examples on the web pages

Creating an abstract representation of program syntax.

PARSING

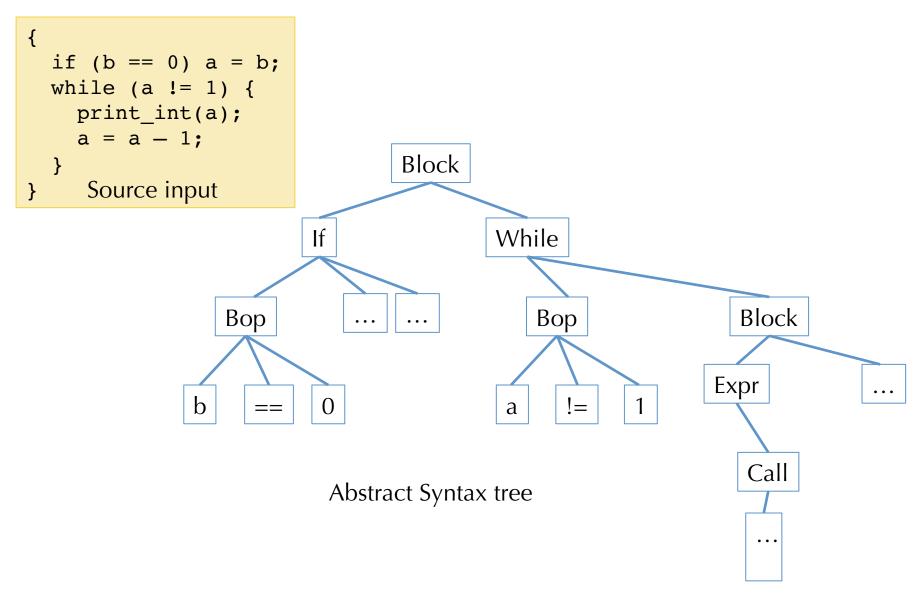
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Today: Parsing

```
Source Code
(Character stream)
if (b == 0) { a = 1; }
                                                             Lexical Analysis
Token stream:
 if
           b
                      0
                                               0
                ==
                                          =
                                                                   Parsing
Abstract Syntax Tree:
                                    Intermediate code:
         If
                                                                Analysis &
                                     %cnd = icmp eq i64 %b, 0
                                                             Transformation
                         None
     Εq
              Assn
                                     br il %cnd, label %12,
                                    label %13
                                    12:
                                     store i64* %a, 1
 b
                                     br label %13
                                    13:
                                                                  Backend
Assembly Code
 cmpq %eax, $0
 jeg 12
 jmp 13
```

12:

Parsing: Finding Syntactic Structure



Syntactic Analysis (Parsing): Overview

- Input: stream of tokens (generated by lexer)
- Output: abstract syntax tree
- Strategy:
 - Parse the token stream to traverse the "concrete" syntax
 - During traversal, build a tree representing the "abstract" syntax
- Why abstract? Consider these three different concrete inputs:

- Note: parsing doesn't check many things:
 - Variable scoping, type agreement, initialization, ...

Specifying Language Syntax

- First question: how to describe language syntax precisely and conveniently?
- Last time: we described tokens using regular expressions
 - Easy to implement, efficient DFA representation
 - Why not use regular expressions on tokens to specify programming language syntax?
- Limits of regular expressions:
 - DFA's have only finite # of states
 - So... DFA's can't "count"
 - For example, consider the language of all strings that contain balanced parentheses – easier than most programming languages, but not regular.
- So: we need more expressive power than DFA's

CONTEXT FREE GRAMMARS

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Context-free Grammars

Here is a specification of the language of balanced parens:

$$S \mapsto (S)S$$

 $S \mapsto \varepsilon$

Note: Once again we have to take care to distinguish meta-language elements (e.g. "S" and "→") from object-language elements (e.g. "(").*

- The definition is *recursive* S mentions itself.
- Idea: "derive" a string in the language by starting with S and rewriting according to the rules:
 - Example: $S \mapsto (S)S \mapsto ((S)S)S \mapsto ((\epsilon)S)S \mapsto ((\epsilon)S)\epsilon \mapsto ((\epsilon)\epsilon)\epsilon = (())$
- You can replace the "nonterminal" S by its definition anywhere
- A context-free grammar accepts a string iff there is a derivation from the start symbol

CFGs Mathematically

- A Context-free Grammar (CFG) consists of
 - A set of *terminals* (e.g., a lexical token or ε)
 - A set of *nonterminals* (e.g., S and other syntactic variables)
 - A designated nonterminal called the start symbol
 - A set of productions: $LHS \mapsto RHS$
 - LHS is a nonterminal
 - RHS is a *string* of terminals and nonterminals
- Example: The balanced parentheses language:

$$S \mapsto (S)S$$

 $S \mapsto \varepsilon$

$$S \mapsto \varepsilon$$

How many terminals? How many nonterminals? Productions?

Another Example: Sum Grammar

A grammar that accepts parenthesized sums of numbers:

$$S \mapsto E + S \mid E$$

$$E \mapsto number \mid (S)$$

e.g.:
$$(1 + 2 + (3 + 4)) + 5$$

Note the vertical bar '|' is shorthand for multiple productions:

$$S \mapsto E + S$$

 $S \mapsto E$
 $E \mapsto number$
 $E \mapsto (S)$

4 productions

2 nonterminals: S, E

4 terminals: (,), +, number

Start symbol: S

Derivations in CFGs

- Example: derive (1 + 2 + (3 + 4)) + 5
- $S \mapsto E + S \mid E$ $E \mapsto \text{number} \mid (S)$

•
$$S \mapsto E + S$$

$$\mapsto (\underline{\mathbf{S}}) + S$$

$$\mapsto$$
 (**E** + S) + S

$$\mapsto$$
 (1 + **S**) + S

$$\mapsto$$
 (1 + **E** + S) + S

$$\mapsto$$
 (1 + 2 + **S**) + S

$$\mapsto$$
 (1 + 2 + **E**) + S

$$\mapsto$$
 (1 + 2 + (**S**)) + S

$$\mapsto$$
 (1 + 2 + (**E** + S)) + S

$$\mapsto$$
 (1 + 2 + (3 + **S**)) + S

$$\mapsto$$
 (1 + 2 + (3 + **E**)) + S

$$\mapsto$$
 (1 + 2 + (3 + 4)) + **S**

$$\mapsto$$
 (1 + 2 + (3 + 4)) + **E**

$$\mapsto$$
 (1 + 2 + (3 + 4)) + 5

For arbitrary strings α , β , γ and production rule $A \mapsto \beta$ a single step of the derivation is:

$$\alpha A \gamma \mapsto \alpha \beta \gamma$$

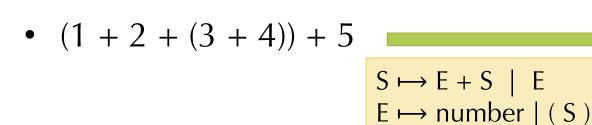
($substitute \beta$ for an occurrence of A)

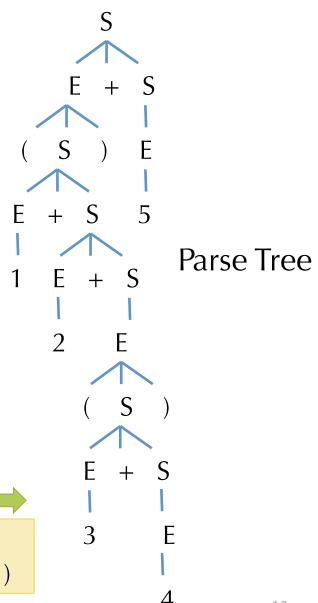
In general, there are many possible derivations for a given string

Note: Underline indicates symbol being expanded.

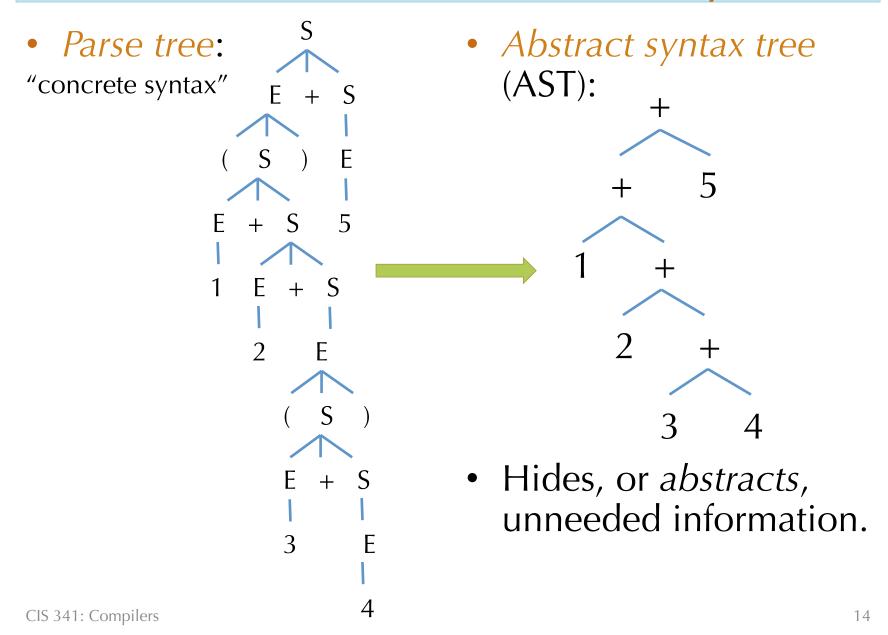
From Derivations to Parse Trees

- Tree representation of the derivation
- Leaves of the tree are terminals
 - In-order traversal yields the input sequence of tokens
- Internal nodes: nonterminals
- No information about the order of the derivation steps





From Parse Trees to Abstract Syntax



Derivation Orders

- Productions of the grammar can be applied in any order.
- There are two standard orders:
 - Leftmost derivation: Find the left-most nonterminal and apply a production to it.
 - Rightmost derivation: Find the right-most nonterminal and apply a production there.
- Note that both strategies (and any other) yield the same parse tree!
 - Parse tree doesn't contain the information about what order the productions were applied.

Example: Left- and rightmost derivations

- Leftmost derivation:
- $\mathbf{S} \mapsto \mathbf{E} + \mathbf{S}$ \mapsto (**S**) + S \mapsto (**E** + S) + S \mapsto (1 + **S**) + S \mapsto (1 + **E** + S) + S \mapsto (1 + 2 + **S**) + S \mapsto (1 + 2 + **E**) + S \mapsto (1 + 2 + (**S**)) + S \mapsto (1 + 2 + (**E** + S)) + S \mapsto (1 + 2 + (3 + **S**)) + S \mapsto (1 + 2 + (3 + **E**)) + S \mapsto (1 + 2 + (3 + 4)) + **S** \mapsto (1 + 2 + (3 + 4)) + **E**

 \mapsto (1 + 2 + (3 + 4)) + 5

Rightmost derivation:

$$\underline{S} \mapsto E + \underline{S} \\
\mapsto E + \underline{E} \\
\mapsto \underline{E} + 5$$

$$\mapsto (\underline{S}) + 5$$

$$\mapsto (E + \underline{S}) + 5$$

$$\mapsto (E + E + \underline{S}) + 5$$

$$\mapsto (E + E + (\underline{S})) + 5$$

$$\mapsto (E + E + (E + \underline{S})) + 5$$

$$\mapsto (E + E + (E + \underline{E})) + 5$$

$$\mapsto (E + E + (E + \underline{E})) + 5$$

$$\mapsto (E + E + (E + \underline{E})) + 5$$

$$\mapsto (E + E + (E + \underline{A})) + 5$$

$$\mapsto (E + E + (A + A)) + 5$$

$$\mapsto (E + A + A) + 5$$

$$\mapsto (A + A + A) + 5$$

Loops and Termination

- Some care is needed when defining CFGs
- Consider:

$$\begin{array}{ccc} S & \longmapsto & E \\ E & \longmapsto & S \end{array}$$

- This grammar has nonterminal definitions that are "nonproductive".
 (i.e. they don't mention any terminal symbols)
- There is no finite derivation starting from S, so the language is empty.
- Consider: $S \mapsto (S)$
 - This grammar is productive, but again there is no finite derivation starting from S, so the language is empty
- Easily generalize these examples to a "chain" of many nonterminals, which can be harder to find in a large grammar
- Upshot: be aware of "vacuously empty" CFG grammars.
 - Every nonterminal should eventually rewrite to an alternative that contains only terminal symbols.

Associativity, ambiguity, and precedence.

GRAMMARS FOR PROGRAMMING LANGUAGES

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Associativity

Consider the input: 1 + 2 + 3

$$S \mapsto E + S \mid E$$

 $E \mapsto \text{number} \mid (S)$

Leftmost derivation: Rightmost derivation:

$$\underline{S} \mapsto \underline{E} + S$$

$$\mapsto 1 + \underline{S}$$

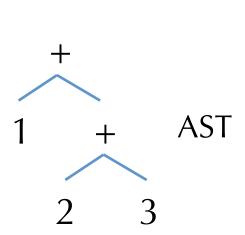
$$\mapsto 1 + \underline{E} + S$$

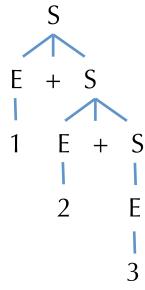
$$\mapsto 1 + 2 + \underline{S}$$

$$\mapsto 1 + 2 + \underline{E}$$

$$\mapsto 1 + 2 + 3$$

$$\underline{S} \mapsto \underline{E} + S$$
 $\underline{S} \mapsto E + \underline{S}$
 $\mapsto 1 + \underline{S}$ $\mapsto E + E + \underline{S}$
 $\mapsto 1 + \underline{E} + S$ $\mapsto E + E + \underline{E}$
 $\mapsto 1 + 2 + \underline{S}$ $\mapsto E + \underline{E} + 3$
 $\mapsto 1 + 2 + \underline{S}$ $\mapsto \underline{E} + 2 + 3$
 $\mapsto 1 + 2 + 3$ $\mapsto 1 + 2 + 3$





Parse Tree

Associativity

- This grammar makes '+' *right associative*...
- The abstract syntax tree is the same for both 1 + 2 + 3 and 1 + (2 + 3)
- Note that the grammar is right recursive...

$$S \mapsto E + S \mid E$$

 $E \mapsto \text{number} \mid (S)$

- How would you make '+' left associative?
- What are the trees for "1 + 2 + 3"?

Ambiguity

Consider this grammar:

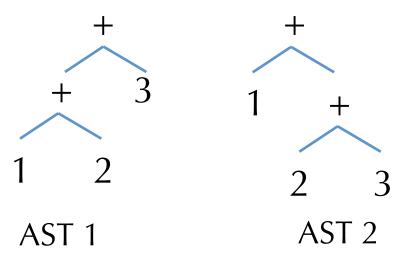
$$S \mapsto S + S \mid (S) \mid number$$

- Claim: it accepts the <u>same</u> set of strings as the previous one.
- What's the difference?
- Consider these two leftmost derivations:

$$- \underline{\mathbf{S}} \mapsto \underline{\mathbf{S}} + S \mapsto 1 + \underline{\mathbf{S}} \mapsto 1 + \underline{\mathbf{S}} + S \mapsto 1 + 2 + \underline{\mathbf{S}} \mapsto 1 + 2 + 3$$

$$- \underline{\mathbf{S}} \mapsto \underline{\mathbf{S}} + S \mapsto \underline{\mathbf{S}} + S \mapsto 1 + \underline{\mathbf{S}} + S \mapsto 1 + 2 + \underline{\mathbf{S}} \mapsto 1 + 2 + 3$$

- One derivation gives left associativity, the other gives right associativity to '+'
 - Which is which?

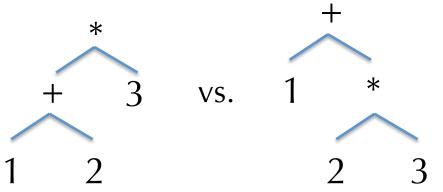


Why do we care about ambiguity?

- The '+' operation is associative, so it doesn't matter which tree we pick. Mathematically, x + (y + z) = (x + y) + z
 - But, some operations aren't associative. Examples?
 - Some operations are only left (or right) associative. Examples?
- Moreover, if there are multiple operations, ambiguity in the grammar leads to ambiguity in their *precedence*
- Consider:

$$S \mapsto S + S \mid S * S \mid (S) \mid number$$

- Input: 1 + 2 * 3
 - One parse = (1 + 2) * 3 = 9
 - The other = 1 + (2 * 3) = 7



Eliminating Ambiguity

- We can often eliminate ambiguity by adding nonterminals and allowing recursion only on the left (or right).
- Higher-precedence operators go farther from the start symbol.
- Example:

$$S \mapsto S + S \mid S * S \mid (S) \mid number$$

- To disambiguate:
 - Decide (following math) to make '*' higher precedence than '+'
 - Make '+' left associative
 - Make '*' right associative
- Note:
 - S₂ corresponds to 'atomic' expressions

$$S_0 \mapsto S_0 + S_1 \mid S_1$$

 $S_1 \mapsto S_2 * S_1 \mid S_2$
 $S_2 \mapsto \text{number} \mid (S_0)$

Context Free Grammars: Summary

- Context-free grammars allow concise specifications of programming languages.
 - An unambiguous CFG specifies how to parse: convert a token stream to a (parse tree)
 - Ambiguity can (often) be removed by encoding precedence and associativity in the grammar.
- Even with an unambiguous CFG, there may be more than one derivation
 - Though all derivations correspond to the same abstract syntax tree.
- Still to come: finding a derivation
 - But first: menhir

parser.mly, lexer.mll, range.ml, ast.ml, main.ml

DEMO: BOOLEAN LOGIC

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