$$\int_0^\infty \ln |S(i\omega)| d\omega = \pi \sum_k Re(p_k) - \frac{\pi}{2} \sigma_y$$