

$$H = -g\sigma(t)\hat{I}\otimes\sigma_z\otimes\hat{q} + g\hat{I}_x\otimes\sigma_x\otimes\hat{I}.$$