$$|L(x,q) - L(y,q)| \le L_L|x - y|.$$