$$|\beta(I)| \le \frac{1}{|\mu|}$$
 with $\sigma = \pm \arctan\left(\left|\frac{I-1}{I}\right|\sqrt{\frac{(1/\mu)^2 - \beta(I)^2}{\alpha(I)^2 - (1/\mu)^2}}\right)$.