$$\theta(u) - \theta(u^k) + \left(u - u^k, \alpha u^k + S^*\lambda^k + (\frac{1}{r}I - sS^*S)(u^k - u^{k-1}) \right) \geq 0, \forall u \in L^2(\mathcal{O}).$$