$$\hat{f}_{X|\tilde{Z}}(x \mid \tilde{Z}) - f_{X|\tilde{Z}}(x \mid \tilde{Z}) = O_P\left(\frac{1}{\sqrt{n\pi_Z h^d}} + h^2\right),$$