$$g = \tan(f/2)$$
, $\sin(f) = \frac{2g}{1+g^2}$, $\cos(f) = \frac{1-g^2}{1+g^2}$, $df = \frac{2}{1+g^2}dg$,