$$||x|^{\alpha} \tilde{f}_k||_{L^2} = 1$$
 and  $||x|^{\gamma} (-\Delta)^{-s/2} \tilde{f}_k||_{L^r} \to S$ .