$$\dot{\theta} = (1 - \cos \theta) + (1 + \cos \theta)\eta,$$