$$S_H(\psi) = \operatorname{Im}\langle \psi, P_H i \log \Delta_H \psi \rangle,$$