

$$\int_0^{\infty} \ln |S(i\omega)| d\omega = \pi \sum_k \operatorname{Re}(p_k) - \frac{\pi}{2} \sigma_y$$