$$\langle u_1^t - u_1, u_j \rangle = \langle u_1^t, u_j \rangle = \frac{u_j^* E u_1}{\lambda_1 - \lambda_j} t + o(t).$$