$$\frac{1}{2^{t/2}}e^{i\theta(x)} = \langle x|V|+^t\rangle = \langle x|\sum_j c_j K_j|+^t\rangle = \frac{1}{2^{t/2}}\sum_j c_j e^{i\theta_j(x)}$$