

$$\langle A_2 U, U \rangle_{\mathcal{H}_2} = -ia ||\nabla y||^2 + 2i \operatorname{Im} \int_0^\infty g(s) \langle y, \eta^t \rangle \, ds$$