$$\delta S_n = -\int dx^+ H_n.$$