$$E_x(z,t) = \sum_{r=-\infty}^{\infty} a_r e^{-j[(\omega + r\omega_m)t - (\beta + r\beta_m)z]},$$