$$||\mathcal{A}(S) - \frac{1}{n} \sum_{i=1}^{n} x_i||_2 = \Omega\left(\min\left(1, \frac{d}{\epsilon n}\right)\right).$$