$$\phi(x,t) = e^{-i\mu t/\hbar} \left[ \sqrt{n_0} + \frac{1}{\sqrt{L}} \sum_k \left( a_k e^{ikx} + a_k^{\dagger} e^{-ikx} \right) \right].$$