

$$\int_0^{\infty} \Delta(x+1) dx = \int_0^{\infty} \Delta(x) dx = 1.$$