

$$\frac{\tilde{\beta}_l}{2n} \pm \frac{1}{p(n)},$$