$$\mathcal{F} = \left(\frac{\pi v}{\sin \pi v}\right) (a\cos \beta - ia\sin \beta)^{v-1},$$