

$$C_1 = (1 + \alpha)^{2N} - 1 \geq 0.$$