

$$\mathbb{E}[|\zeta_s|] \stackrel{N \rightarrow \infty}{=} \lim_{N \rightarrow \infty} \mathbb{E}[|\zeta_s| \wedge N] \leq \frac{1}{\alpha} M_s.$$