

$$\frac{\partial f^l}{\partial r_*} = -i\omega f^l, \quad \frac{\partial \psi^l}{\partial r_*} = -i\omega \psi^l, \quad \frac{\partial \psi^{*l}}{\partial r_*} = -i\omega \psi^{*l}.$$