$$du^2 + f_a^2(u)dv^2$$