

$$\int_1^n \frac{|T_n(v)|}{v^2} + \frac{|T'_n(v)|}{v} dv \leq C^i \left( 1 + \int_1^n \frac{1}{v^{3/2}} \left( \int_1^n \frac{1}{\sqrt{u}} F_{p,2i}(u,v) du \right) dv \right) \leq C^i,$$