$$\Theta_{m,n}^{(1,2)} = (\alpha_1^2 - \alpha_2^2) (c_1^{-2} - c_2^{-2})^{-1},$$