

$$\limsup_{T \rightarrow \infty} \frac{1}{T} \sum_{t=1}^T 1[d(\pi^*(X_t), \pi^i(X_t)) \geq 2^{-i}] \leq 2^{-i},$$