$$H_{\text{int}}^{(i)} = \chi(\tau_i)Q(\tau_i)\phi[x(\tau_i)],$$