$$\frac{\xi^\sigma f(\xi)^p}{(f^m)'(\xi)/\xi} = \frac{\xi^{\sigma+2} f(\xi)^p}{m f(\xi)^m Y(\xi)} = C \frac{X^{(m-p)/(m-1)}}{Y} \to 0,$$