$$\beta_N = \sum_{j=0}^{N} B_{Nj} \alpha_j,$$