$$\phi^* = \sqrt{\delta_{\alpha}} \tanh \sqrt{\frac{\delta_{\alpha}}{2}} (t - t_0).$$