$$\mathbb{E}\left[\int_{S_l^1}^{S_l^2} f\left(y_1, \bar{c}^1\right) d\kappa\right] \ge 0 \ge \mathbb{E}\left[\int_{S_l^1}^{S_l^2} f\left(y_2, \bar{c}^2\right) d\kappa\right].$$