

$$H_{\text{int}} = \sum_{a=1,2} \sum_k \hbar g_k^a \left( \sigma_a b_k^{(a)\dagger} + \sigma_a^\dagger b_k^a \right),$$