

$$\chi_8^{A_{2,3}}(q, x_1^i, x_2^i) = \chi_8^{A_2}(x_1^i, x_2^i) \chi_{[-3/2, 0, 0]}^{A_{2,-3/2}}(q, x_1^i, x_2^i),$$