

$$\nabla^2(\sigma^1 + a/2 v) = \sigma^1 + a/2 \nabla^2 v + v \nabla^2 \sigma^1 + a/2 + \nabla v \otimes \nabla \sigma^1 + a/2 \otimes \nabla v,$$