$$|V_{\alpha}(s)| \le \frac{1}{1-\eta} \left[1 + \alpha \kappa + \dots + (\alpha \kappa)^{T-1} \right] w(s).$$