$$\tilde{U}^{(1n)} Z \tilde{U}^{(1n)\dagger} = \varpi^{nc(c-d)/2} Z X^{nc^2}$$

$$\tilde{U}^{(1n)} X \tilde{U}^{(1n)\dagger} = X,$$