

$$\lim_{r \rightarrow 0} b^*(x(0)) = f_r(K; x(0)).$$