

$$ds^2 = -\frac{r^2}{L^2}f(r)dt^2 + \frac{L^2}{r^2}f(r)^{-1}dr^2 + r^2dx^2,$$