$$c_2 = \frac{(\sqrt{\alpha} - \sqrt{\beta})^2}{K^{d-1}(d-1)!} - \frac{\gamma \log(\alpha/\beta)}{2(d-1)!} - 1 > 0.$$