$$(J_{S,i})_C = (J_{S_i,b_i^0})_{C_i}.$$