$$\partial_t(v + D^\alpha v) = \partial_x \mathcal{L}v$$