

$$v(r) = v_{\infty} \left(1 - \frac{bR_0}{r} \right)^{\beta},$$