$$\frac{\sin\left(\sqrt{\rho - 1 - 2\lambda_1^{L+y}}x\right)}{\sin\left(\sqrt{\rho - 1 - 2\lambda_1^{L+y}}\right)} \frac{\sin\left(\sqrt{\rho - 1 - 2\lambda_1^{L}}\right)}{\sin\left(\sqrt{\rho - 1 - 2\lambda_1^{L}}x\right)} \to 1$$