$$\frac{\tilde{\beta}_l}{2^n} \pm \frac{1}{p(n)},$$