

$$Z_t = Z_{t_0} + \sum_{j=0}^{\infty} (Z_{\Pi_{i+1}(t)} - Z_{\Pi_i(t)}).$$