$$\frac{dC[t]}{da_{ij}^{(p)}} = \sum_{n=1}^{N} S_n \frac{\partial f_n}{\partial \hat{y}_n} \frac{\partial \hat{y}_n}{\partial a_{ij}^{(p)}}$$