$$U_{\text{eff}}(\omega) = U - \frac{\lambda W \Omega^2}{\Omega^2 - \omega^2}$$