$$\int_{d}^{T} \zeta(x, y) g(y; d) \, dy < \infty.$$