$$\phi^* = \sqrt{\delta_\alpha} \tanh \sqrt{\frac{\delta_\alpha}{2}}(t - t_0).$$