$$g_{k-1}(y) = (2k-1)y^{k-1} - (y^{k-2} + \dots + y + 1)$$