$$H = -g\delta(t)\hat{I} \otimes \hat{\sigma}_z \otimes \hat{q} + g'\hat{L}_x \otimes \hat{\sigma}_x \otimes \hat{I}.$$