$$t'(\bar{p}_j) = \frac{g_j^2 \bar{p}_j}{\sigma^2 m_j + g_j \bar{p}_j} > 0,$$