$$\lim_{r \to 0} b^*(x(0)) = \tilde{f}_{\tau}(K; x(0)).$$