$$\omega_2 = -\frac{\partial \alpha}{\partial t} = -\beta \left(\lambda_3 + \lambda_4\right) \frac{1}{2} \sin 2\alpha$$