$$u_{\mu}R^{\mu}_{\ \nu\rho\sigma} = -\left[\nabla_{\rho}, \nabla_{\sigma}\right]u_{\nu}\,,$$