$$\hat{S}_0(s,t) = -\frac{\hat{v}(s)\exp\left(-\int_0^s \frac{g(0)-g(s')}{\hat{v}(s')}ds'\right)}{g(0)\hat{\gamma}_0\hat{\alpha}(s)}e^{-g(0)t}.$$