$\mathcal{P}^{\mathtt{x}_1}$ and