$$\mathcal{L}_r = \mathcal{L}\left(\varphi\left(\mathbf{R}\right), \mathbf{G}_n\right)$$