$$\mathcal{I}_{\pm}(N) = \chi \mod N : \chi \text{ imprimitive }, \chi \neq \chi_0 , \chi(-1) = \pm 1 ,$$