$$\left(\sum_{i=1}^{n} \lambda_i v_i\right) \phi_\beta(\alpha) = \sum_{i=1}^{n} \lambda_i^\alpha v_i.$$