$$S_i = \varphi \in S_\lambda \mid \chi(S \setminus Z_\varphi) = -i$$
.