$\tau(G) := (H_i/H_i')_{1 \le i \le p+1} \text{ and } \varkappa(G) := (\ker(T_{G,H_i}))_{1 \le i \le p+1}$