$$(Y_0, Y_1) = \frac{\sqrt{(Y_2)^2 + \alpha^2}}{2} (\pm (y + y^{-1}), (y - y^{-1})).$$