$$P_{n,l} = P_l(|n| + l/2 + \theta) + O(1/P_{n,l}),$$