$$\frac{\ell_i(p_0)}{\ell_i(p_0) + 2\sinh^{-1}\left(\frac{\cosh\left(\frac{\ell_i(p_1)}{2}\right)}{\varepsilon}\right)} \le \frac{\ell_i(p_0)}{\ell_i(p_3)}$$