$$\int_d^T \zeta(x,y) g(y;d) \, dy < \infty.$$