

$$\frac{J^2}{W^2} \times \frac{J\sqrt{N}}{W/N^2} \gtrsim 1$$

$$\Rightarrow J \gtrsim W/N^{5/6}$$