$$\delta_{\omega}(t'-t) = \frac{\omega}{2\pi} \sum_{m} e^{\imath m \omega(t'-t)},$$