$$\mathcal{L}^{(i,j+1)} = \frac{1}{a_0^{L-j-1} - b_0^{L-j-1}L(L+1)} \cdot (2(L+1) + i - 2j)\mathcal{L}^{(i,j)}.$$