$$\hat{H}(z) = \alpha_0(z)\hat{J}_0 + \alpha(z)(\hat{J}_+ + \hat{J}_-),$$