$$\prod_{j=k}^{m} \frac{c_j}{\sqrt{n-j+2}} \le \left(\frac{1}{t(\alpha)} \sqrt{\frac{1+\epsilon}{1-\epsilon}}\right)^{m-k+1} c_k^{m-k+1}.$$