

$$\phi^* = \sqrt{\delta_a} \tanh \sqrt{\frac{\delta_a}{2}} (t - t_0).$$