$$w_k^{(q)}(x;y) = \Xi_{\phi_k}(y)W_k^{(q)}(x-y).$$