$$l_{cut}(Y; \beta, \tau, \sigma, \pi_0) = -\log(p(Y|\beta, \tau)) - \log(p_{cut}(Y|\sigma)) + \log(p(Y|\sigma))$$