$$\text{tr}([\rho_A \otimes \rho_B] \ln \rho_s) \leq \text{tr}([\rho_A \otimes \rho_B] \ln[\rho_A \otimes \rho_B]) = -S(\rho_A) - S(\rho_B).$$