

$$g_t: \mathcal{O}_{\min}^{T+1, t+1} \rightarrow \mathbb{R}^{n_v}, \quad G_j: \mathcal{O}_{\min}^{T+1, t+1} \rightarrow \mathbb{R}^{n_v \times n_v},$$