$$Z_i(r_*) \sim e^{-i\omega r_*} + \mathcal{R}^{(i)}e^{i\omega r_*}, \quad r_* \to \infty.$$