

$$f(iz) = \frac{1}{2\pi i} \int_{a-i\infty}^{a+i\infty} d\mu \, \Phi(\mu) y^{-\mu}.$$