$$\frac{dC[t]}{d\theta_i} = S_i \left(\frac{\partial f_i}{\partial \theta_i}\right) + \sum_{n=1}^{N} S_n \left(f_n'(\hat{y}_n[t]) \sum_{p=1}^{P} a_{ni}^{(p)} \frac{\partial}{\partial \theta_i} g_i \left(z_i[t-p], \theta_i\right)\right)$$