$$\widetilde{\mathbb{E}}[|\tilde{\zeta}_s|] := \lim_{N \to \infty} \ \widetilde{\mathbb{E}}[|\tilde{\zeta}_s| \wedge N] \leq s^{\frac{1}{\alpha}} M_z.$$