

$$0 \leq -\operatorname{cov}(\sigma^T \nu_x, \nu_\theta) = \nu(1 - \nu).$$