$$|f_n(\mu)| \le c_K$$
 and  $\left| \frac{\partial f_n}{\partial \mu}(x,\mu) \right| \le c_K (1+|x|^p)$