

$$\frac{1}{d_2^2} = \frac{NS}{2\alpha_1\epsilon q} = \frac{N}{2} \left(\frac{S}{q} \right)^{\frac{1}{2}}$$