$$\frac{\partial}{\partial s}G(x,s) = \left(-\frac{\partial}{\partial x}F(x) + \frac{\partial^2}{\partial x^2}\right)G(x,s).$$