$$N_c^q = f_{c^q}(N_q, U_c)$$