

$$\tau(G) := (H/H)_{\leq p+1} \text{ and } \chi(G) := \ker(\Gamma_G, H)_{\leq p+1}$$