

## Laboratory practice No. 1: Algorithm complexity

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### 3) Practice for final project defense presentation

**Note:**

For the exercise 1.1 we implemented two different algorithms, one designed by ourselves and another designed by a fellow student. For most of the analysis we will use the later since it proved more consistent. However, we believe our algorithm may have an advantage for certain cases that will be studied in what follows. Our algorithm was denominated  $\text{subCadenaMax}(s1, s2)$ , where  $s1$  and  $s2$  are strings. The other algorithm was denominated  $\text{lcs}(l, j, X, Y)$ , where  $X$  and  $Y$  are strings,  $i$  and  $j$  are integers.

#### 3.1

For  $\text{lcs}()$ :

Worst case:

$$T(p) = T(p-1) + T(p-1) + c3 = c3((2^{**}p)-1) + c4*2^{**}p-1$$

With  $c_i$  constant

Then

$T(p) = O(2^{**}p)$  with  $p$  being the sum of the length of the two strings

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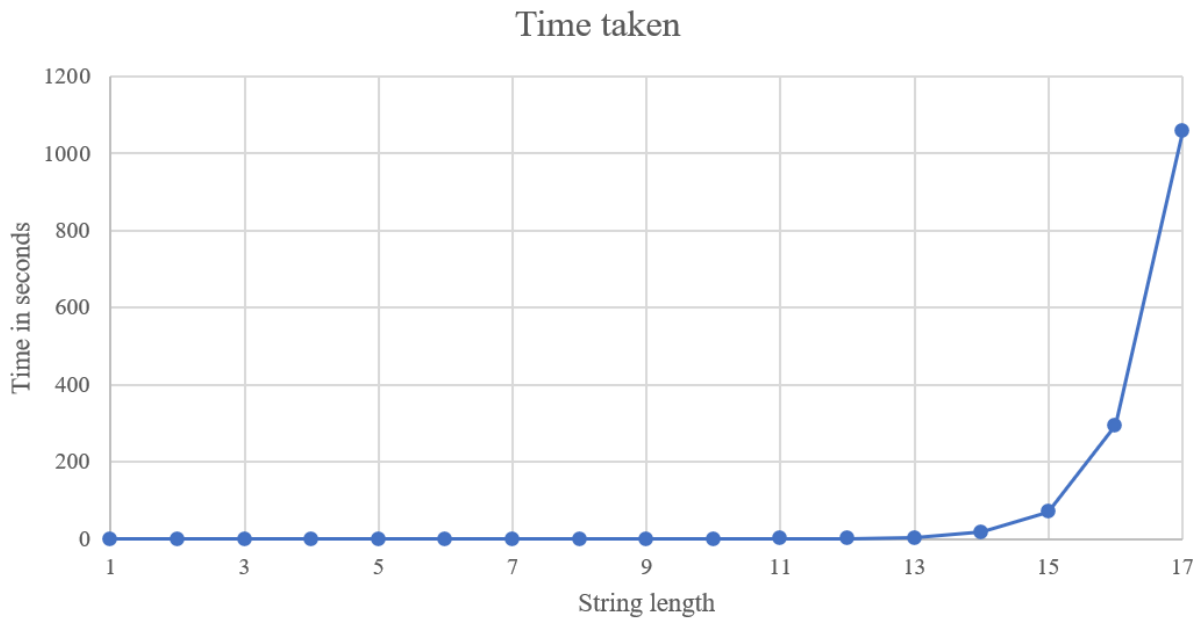


## ESTRUCTURA DE DATOS 1

### Código ST0245

### 3.2

We can see the exponential function that we calculate in the previous step. As the length of the string increases, we see a large increase in the time take for the algorithm to be executed.



We cannot execute the algorithm with a string with a length of 20 for the long waiting time required, with a length of 17 the algorithm takes 1059,26 seconds or 17 minutes to be executed.

With this scenario we can conclude that this type of algorithm is not suitable for the type of necessity. A DNA strand with a length of 300,000 is extremely inefficient apply recursion.

### 3.3

For lcs. Since the algorithm appears to grow exponentially, such an enormous data set, such a large string, would take an even more enormous amount of time to process. In addition, one does not wish to compare just two strings of DNA, but several between each other. This makes the algorithm impractical for this application.

### 3.4

The method `groupSum5(int start, int[] nums, int target)` tells us if it is possible to generate a given int number by adding up different combinations of numbers in an int array, with the additional constraint that all multiples of five contained in the array must be used and that, if the value immediately following a multiple of five is a one, it must not be chosen.

The method requires three parameters: an int denominated start, an int list denominated nums and another int denominated target, in that order.

start represents the position of nums where the search will begin. nums is the array of values to be added up. target is the number we wish to determine if it is possible to generate. The

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## ESTRUCTURA DE DATOS 1

### Código ST0245

method evaluates every possible combination of numbers of nums until it finds one which addition equals target, then it returns Boolean True. If it can't find any combination that fits the requirements, it returns false.

The method functions recursively by using start to represent the position of a number in nums, that may be subtracted or not from target. If by the end of the process target equals zero, it means that there is a combination of numbers in nums that fits the requirements. It goes as follows:

if the current number is a multiple of five, such number is subtracted from the target number, then groupSum() is called again but evaluating the next number in nums, and finally the value returned by this new call is returned as well. This guarantees that multiples of five are always used in the calculation. Similarly, if the number in the current position is a one, and the previous number was a 5, the current number is not subtracted and everything else goes as described. This ensures the second condition is satisfied.

On the other hand, if the number is not as the above, two different calls to groupSum() are generated, one where the current number is subtracted and another where it is not. In this case, the method returns true if any of the paths also returns true, since that means there exist a fitting combination.

Finally, when we reach the end of the array (that is, when target equals the length of nums), we evaluate if target equals zero. If it does, the method returns true, false is returned otherwise.

### 3.5

Let  $T(n)$  be the complexity function of each exercise, then

#### 3.5.1 triangle exercise

We get

$$T(n) = c_1 + c_2 + c_0 \text{ if } n = 0$$

$$T(n) = T(n-1) + c_4 = c_4n + c_5 \text{ else}$$

with  $c_i$  being a constant

then

$$T(n) = O(n) \text{ with } n \text{ being the number of rows of the triangle}$$

#### 3.5.2 bunnyEars2 exercise

We get

$$T(n) = c_1 + c_2 + c_0 \text{ if } n = 0$$

$$T(n) = T(n-1) + T(n-1) + c_5 = c_5((2^{**}n) - 1) + c_6 \cdot 2^{**}n - 1 \text{ else}$$

with  $c_i$  being a constant

then

$$T(n) = O(2^{**}n) \text{ with } n \text{ being the number of bunnies}$$

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## ESTRUCTURA DE DATOS 1

### Código ST0245

#### 3.5.3 sumDigits exercise

We get

$$T(m) = c_1 + c_2 + c_0 \text{ if } m \leq 1$$

$$T(m) = T(m-1) + c_4 = c_4m + c_5 \text{ else}$$

with  $c_i$  being a constant

then

$T(m) = O(m)$  with  $m$  being the number of digits of the evaluated number  $n$

#### 3.5.4 count7 exercise

We get

$$T(m) = c_1 + c_2 + c_3 + c_0 \text{ if } m = 1$$

$$T(m) = T(m-1) + T(1) + c_5 \text{ else}$$

$$\text{However } T(1) = c_3 + c_2 + c_1$$

Then

$$T(m) = T(m-1) + c_7 = c_7m + c_8 \text{ else}$$

with  $c_i$  being a constant

Then

$T(m) = O(m)$  with  $m$  being the number of digits of the evaluated number  $n$

#### 3.5.5 fibonacci exercise

We get

$$T(m) = c_0 + c_1 + c_2, \text{ if } n \leq 1$$

$$T(m) = c_3 + T(m-1) + T(m-2) = T(n) = c_3 \cdot 2^{**}m + c_4 \text{ else}$$

with  $c_i$  being a constant

then

$T(m) = O(2^{**}m)$  with  $m$  being the number of digits of the evaluated number  $n$

#### 3.5.6 groupSum6 exercise

We get

$$T(n) = c_0 + c_1 + c_2 + c_3 + c_4 \text{ if } n = 0$$

Worst case is

$$T(n) = T(n-1) + T(n-1) + C = C \cdot ((2^{**}n) - 1) + c_{11} \cdot 2^{**}n - 1$$

with  $c_i$  being a constant

then

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## ESTRUCTURA DE DATOS 1

### Código ST0245

$T(n) = O(2^{**}n)$  with  $n$  being the length of the array evaluated nums

#### 3.5.7 groupNoAdj exercise

We get

$$T(n) = c_0 + c_1 + c_2 + c_3 + c_4 \text{ if } n = 0$$

Worst case is

$$T(n) = T(n-2) + T(n-1) + C = \text{Fibonacci's recursive equation} = c_8 \cdot 2^{**}n + c_9$$

with  $c_i$  being a constant

then

$$T(n) = O(2^{**}n) \text{ with } n \text{ being the length of the array evaluated nums}$$

#### 3.5.8 groupSum5 exercise

We get

$$T(n) = c_0 + c_1 + c_2 + c_3 + c_4 \text{ if } n = 0$$

Worst case is

$$T(n) = T(n-1) + T(n-1) + C = C \cdot ((2^{**}n)-1) + c_9 \cdot 2^{**}n-1$$

with  $c_i$  being a constant

then

$$T(n) = O(2^{**}n) \text{ with } n \text{ being the length of the array evaluated nums}$$

#### 3.5.9 groupSumClump exercise

We get

$$T(n) = c_0 + c_1 + c_2 + c_3 + c_4 \text{ if } n = 0$$

Worst case is

$$T(n) = T(n-1) + T(n-1) + C = C \cdot ((2^{**}n)-1) + c_{11} \cdot 2^{**}n-1$$

with  $c_i$  being a constant

then

$$T(n) = O(2^{**}n) \text{ with } n \text{ being the length of the array evaluated nums}$$

#### 3.5.10 splitArray exercise

We get

$$T(n) = c_0 + c_1 + c_2 + c_3 + c_4 \text{ if } n = 0$$

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## ESTRUCTURA DE DATOS 1

### Código ST0245

Worst case is

$$T(n) = c_8 * n + c_9 + c_1 + C * ((2^{**}n) - 1) + c_{18} * 2^{**}n - 1 + c_{18} + c_4 + C$$

with  $c_i$  and  $C$  being constants

Note that split array is depended of two auxiliar functions whose complexities were calculated in order to calculate the lather.

then

$$T(n) = O(2^{**}n) \text{ with } n \text{ being the length of the array evaluated nums}$$

**Note: A step by step process for all the calculations is shown as comments inside the code.**

#### 4) Practice for midterms

**4.1** 1.c, 2.c, 3.b.

**4.2** Line 9:

floodFillUtil(screen, x+1, y+1, prevC, newC, N, M)

Line 10:

floodFillUtil(screen, x-1, y-1, prevC, newC, N, M)

Line 11:

floodFillUtil(screen, x-1, y+1, prevC, newC, N, M)

Line 12:

floodFillUtil(screen, x-1, y-1, prevC, newC, N, M)

**4.3** b.  $T(n, m) = C * n * m^{**2}$

**4.4** c.  $T(n) = T(n-1) + T(n-2) + c$ , que es  $O(2^{**}n)$

**4.5** Line 3:

return True

Line 4:

b.  $!f(s.charAt(0) == s.charAt(s.length() - 1))$

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