

LECTURE 6

SUMMARY

1. Distributed CSP.....	1
2. Path finding problems ([1], Section 4.3).....	6

1. Distributed CSP

- if the problem is to **allocate tasks or resources to multiple agents** and there exists **inter-agents constraints**
 - ⇒ the problem can be formalized as a distributed CSP (DCSPs)
 - each task/resource is a **variable**
 - the **possible assignments** are values
- many application problems in DAI can be formalized as distributed CSPs
 - interpretation problems
 - assignment problems
 - multiagent truth maintenance tasks

How can the CSP formalization be related to DAI?

- the variables of the CSP are distributed among agents
 - each process/agent corresponds to a variable
 - the processes act asynchronously to solve the CSP
 - ⇒ **asynchronous search algorithms**
 - the processes that have links to X_i are called **neighbors** of X_i
 - **assumption**:
 - a process *knows* the identifiers of its neighbors
- the **communication model**:
 - **processes/agents** communicate by sending messages
 - a process can send messages to other processes iff
 - the process knows the addresses/identifiers of other processes
 - the delay in delivering a message is finite
 - for the transmission between the any pair of processes, messages are received in the order in which there were sent

1.1 Filtering algorithm (FA)

- assures **arc** consistency
- idea of the FA
 - each process communicates its domain to its neighbors
 - and removes values that cannot satisfy constraints from its domain
 - the process X_i performs the following procedure **REVISE**(X_i , X_j) for each neighboring process X_j

procedure REVISE(X_i , X_j)
for all $v_i \in D_i$ **do**

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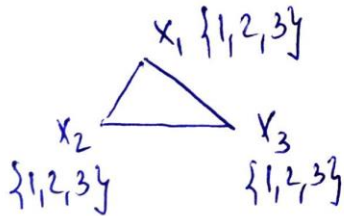
    if there is no value  $v_j \in D_j$  such that  $v_j$  is consistent with  $v_i$  then
        @delete  $v_i$  from  $D_i$ 
    endif
endfor
endREVISE

```

- if some value of the domain of X_i is removed by performing **REVISE** \Rightarrow
 - process X_i sends the new domain to neighboring processes
 - if X_i receives a new domain from a neighboring process X_j , the procedure **REVISE**(X_i, X_j) is performed again

!!! the execution order of the processes is arbitrary

- e.g., for the **3-queens** problem



- a) X_1 : **REVISE**(X_1, X_2) removes 2
 X_2 : **REVISE**(X_2, X_3) removes 2
 X_3 : **REVISE**(X_3, X_2) removes 2
- b) X_1 : **REVISE**(X_1, X_3) removes 1, 3
 \Rightarrow the domain of $X_1 = \emptyset$
 overconstrained

In general, the FA cannot solve a DCSP

- it should be considered a preprocessing procedure
- is invoked before the application of other search methods
 - reduces the domains of variables for the search procedure

1.2 Hyper-Resolution based Consistency Algorithm

- a CSP is **k -consistent** iff the following condition is satisfied
 - given any instantiation of any $k - 1$ variables satisfying all the constraints among those variables, it is possible to find an instantiation of any k -th variable such that these k variable values satisfy all the constraints among them.
- the FA achieves **2-consistency**
- a **k -consistency** algorithm transform a given problem into an equivalent **k -consistent** CSP
- a CSP is **strongly k -consistent** if
 - the problem is **k -consistent**
 - and
 - is **j -consistent** for all $j < k$

Theorem

- if the CSP has n variables and is **strongly n -consistent**

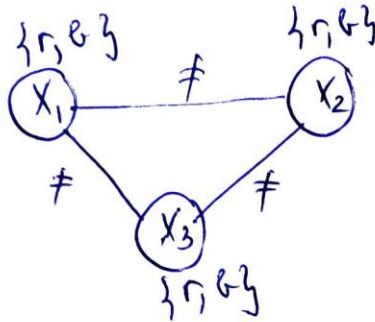
\Rightarrow

a solution can be obtained without any trial-and-error exploration

- for a any instantiation of $k-1$ variables, one can always find at least one consistent value for the k -th variable

The HR-based consistency algorithm

- uses the **hyperresolution rule** (HR)
- all constraints are represented as a **nogood**
 - a prohibited combination of variables values
 - e.g.,



- a constraint between X_1 and X_2 can be represented as two nogoods:
 1. $\{X_1=\text{red}, X_2=\text{red}\} \leftrightarrow \neg (X_1=\text{red} \wedge X_2=\text{red})$
 2. $\{X_1=\text{blue}, X_3=\text{blue}\} \leftrightarrow \neg (X_1=\text{blue} \wedge X_3=\text{blue})$

since the domain of X_1 is $\{\text{red}, \text{blue}\} \Rightarrow$

 3. $(X_1=\text{red} \vee X_1=\text{blue})$

- the HR rule combines
 - nogoods (1., 2.) and
 - the condition that one variable takes one value from its domain (3.)

and generates a **new nogood**

$$4. \{X_2=\text{red}, X_3=\text{blue}\} \leftrightarrow \neg (X_2=\text{red} \wedge X_3=\text{blue})$$

- if the following propositions hold

$$\begin{aligned} &\neg (p_1 \wedge p_2) \\ &\neg (p_3 \wedge p_4) \\ &(p_1 \vee p_3) \end{aligned}$$

\Rightarrow

$$\neg (p_2 \wedge p_4)$$

- the HR rule is described as follows

$$\begin{aligned} &(X_1=x_{11} \vee X_1=x_{12} \vee X_1=x_{13} \vee \dots \vee X_1=x_{1m}) \\ &\neg (X_1=x_{11} \wedge X_{i1}=x_{i1} \wedge \dots), \\ &\neg (X_1=x_{12} \wedge X_{i2}=x_{i2} \wedge \dots), \\ &\dots \\ &\neg (X_1=x_{1m} \wedge X_{im}=x_{im} \wedge \dots) \end{aligned}$$

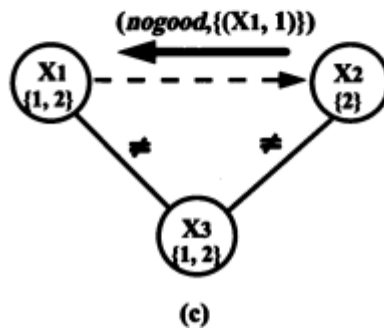
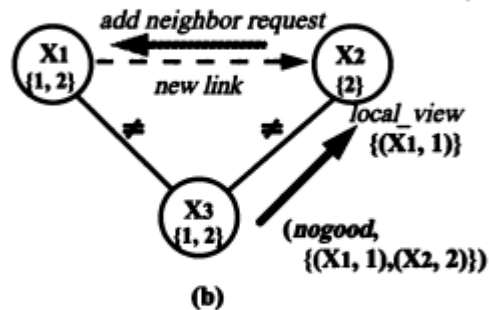
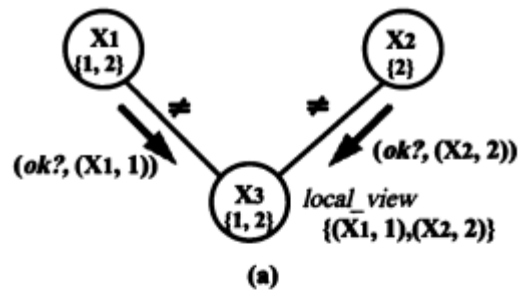
$$\bigwedge (X_{i1}=x_{i1} \wedge \dots \wedge X_{i2}=x_{i2} \wedge \dots \wedge X_{im}=x_{im} \wedge \dots)$$

- in the **HR based consistency algorithm**
 - each process represents its constraints as **nogoods**
 - the process generates **new nogoods** using the HR rule
 - combining the information about its domain and
 - existing nogoods
 - a **newly obtained nogood**
 - is communicated to related processes
 - if a new nogood is communicated, the process tries to generate further nogoods
 - using the communicated nogood)
 - if an empty set becomes a nogood
 - ⇒ the problem is **over-constrained**
 - a **superset of a nogood cannot be a solution**
- **disadvantage**
 - the HR rule can generate a very large number of nogoods
- if we restrict the application of the rules so that
 - only the nogoods whose lengths (# of variables) are less than k are produced
 - ⇒ the problem becomes **strongly k -consistent**
- the HR rules generation is used in the **asynchronous backtracking** algorithm

1.3 Asynchronous Backtracking (AB)

- is an asynchronous version of the classical BT algorithm
- in the AB
 - the priority order of the variables/processes is determined by the alphabetical order of the variables identifiers X_1, X_2, \dots, X_n
 - each process communicates its tentative value assignment neighboring processes
 - a process **changes** its assignment if its current value assignment is **not consistent** with the higher priority processes
 - if there is no value that is consistent with higher priority processes
 - ⇒
 - the process generates a new **nogood**
 - communicates the nogood to a higher priority process
 - ⇒
 - the higher priority process changes its value
 - the generation of a nogood is identical to the HR rule
 - **the AB algorithm generates only the nogoods that actually occur in the AB**
 - **each process**
 - maintains the current value assignment of other processes from its viewpoint (**local_view**)

- since the processes acts asynchronously and concurrently
- ⇒
 - the *local_view* may contain obsolete information
- if a process X_i **does not have a consistent value** with the higher priority processes
 - it generates a **nogood**
 - the receiver of the nogood must check whether the nogood is actually violated from its own *local_view*
- messages communicated between processes
 - *ok?* message
 - to communicate the current value
 - *nogood* message
 - to communicate a nogood
- the algorithm is described in [1], Section 4.2.4



[1]

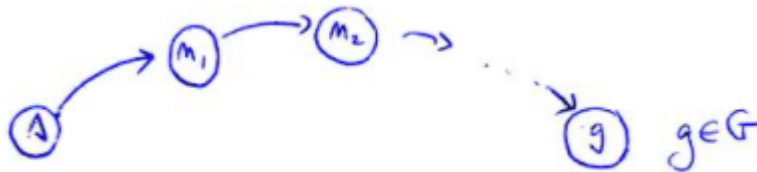
1.4 Other algorithms

- [Asynchronous Weak-Commitment Search](#)
 - the limitation of AB is that the process/variable ordering is statically determined
 - **AWCS** uses a value ordering heuristic
 - **min-conflict** heuristic
 - the value that minimizes the number of constraint violations with other variables is preferred
- [Distributed Forward Checking](#)
- [Distributed BackJumping](#)

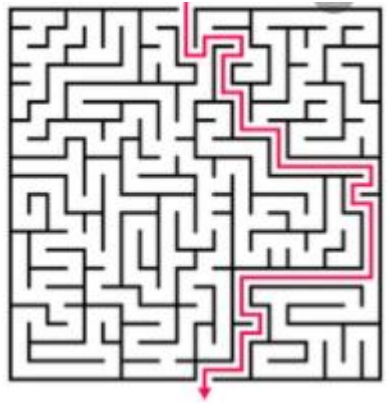
2. Path finding problems ([1], Section 4.3)

2.1 PFP – classical AI

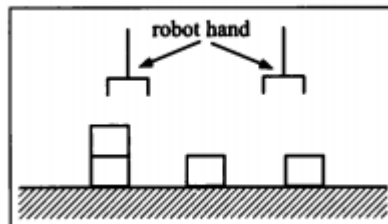
- **definition**
 - a set of nodes N , each representing a state;
 - a set of directed links L , each representing an operator available to a problem solving agent;
 - we assume that there exists a unique node s called the start node
 - representing the initial state
 - a set of nodes G - each node from G represents a goal state;
 - for each link, the *weight* of the link is defined
 - it represents the *cost* of applying the operator (is also called the *distance* between the nodes).
- we call the nodes that have directed links from a node i the *neighbors* of i .
- **goal of PFP**
 - finding a path from s to a node $g \in G$, following the links between the states
 - any path
 - optimal path



- **Examples**
 - **Toy problems:**
 - n -puzzle
 - searching a maze



- planning problems for (multiple) robot hands



- **Software Engineering**
 - Many SE problems are NP-complete optimization problems => metaheuristic techniques (GA, SA, Tabu search, HC), evolutionary algorithms, machine learning.
 - Requirements analysis, design, development, maintenance, testing.
 - CITO: Class Integration Test Ordering optimization
- **Bioinformatics**
 - DNA sequencing and reconstruction, DNA fragment assembly, gene finding and identification, gene expression profiling, protein structure prediction (secondary, tertiary), phylogenetic trees.
- **Medicine**
 - Radiation treatment planning for cancer patients, medical data classification, gene mutations in cancer, medical image segmentation, brain tumour tissue segmentation, chemotherapy treatments.
- **Other**
 - Weight optimization in Recurrent Neural Networks, Reinforcement learning, etc.

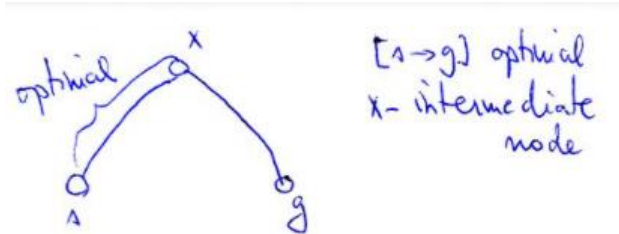
2.2 Distributed PFP (DPFP)

- *How can the PFP formalization be related to DAI?*
 - assume that multiple robots are exploring an unknown environment for finding a certain location (such a problem can be formalized as a DPFP)
- **algorithms for DPFP**
 1. **Asynchronous dynamic programming** (ADP)
 - the basis of other algorithms
 2. Learning Real time A* - LRTA* special cases of ADP
Real Time A* - RTA*

Moving Target Search
 Real Time Bidirectional Search
 Real Time Multiagent Search

2.3 Asynchronous Dynamic Programming (ADP)

- in a PFP, the *principle of optimality* holds (if a path is optimal, then every segment of it is optimal)



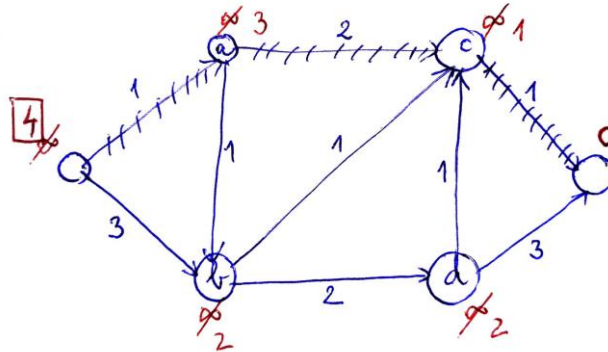
- let us denote by $h^*(i)$ - the shortest distance from node i to a goal node
- from the principle of optimality, the shortest distance via a neighbouring node j is given by
 - $f^*(i, j) = k(i, j) + h^*(j)$
 - where $k(i, j)$ represents the cost of the link from node i to node j
- if node i is not a goal node \Rightarrow the path from i to a goal node must visit one of the neighbouring nodes \Rightarrow
 - $h^*(i) = \min_{j \text{ neighbour of } i} f^*(i, j)$ holds
- if h^* is given for each node, the optimal path can be obtained by repeating the following procedure
 - for each neighbouring node j of the current node i , compute $f^*(i, j) = k(i, j) + h^*(j)$
 - then, move to the node j that gives $\min_{j \text{ neighbour of } i} f^*(i, j)$.
- ADP computes h^* by repeating the local computations for each node in the graph.

Let us assume the following situation

- for each node i , there exists a process/agent corresponding to i
- each process records $h(i)$ - the estimated value of $h^*(i)$
 - the initial value of $h(i)$ is arbitrary (e.g 0 or ∞) for all nodes excepting the goal nodes
 - for the goal nodes, the initial value for $h(i)$ is 0.
- each process can refer to the h values of its neighbour nodes (through shared memory/blackboard or message passing).
- the execution order of the processes is arbitrary
 - the processes are executed asynchronously and concurrently.

In this situation, each process i updates $h(i)$ by the following procedure.

- For each neighbouring node j , compute $f(i,j) = k(i,j) + h(j)$, where $h(j)$ is the current estimated distance from j to a goal node and $k(i,j)$ represents the cost of the link from node i to node j . Then, update $h(i)$ with $\min_{j \text{ neighbour of } i} f(i,j)$.



Theorem. If the costs of all links are positive, then $h(i)$ will eventually converge to the true value $h^*(i)$.

Remarks.

- In reality, ADP can not be used for a large PFP
 - if the number n of nodes is huge, we can not afford to have processes for all nodes.
- ADP can be considered a foundation for all the other algorithms (LRTA*, RTA*, etc).
 - in these algorithms instead of allocating processes for all nodes, some kind of control is introduced for enabling the execution by a reasonable number of processes/agents).
- More about DPFP may be found in [1], Section 4.3.

Bibliography

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