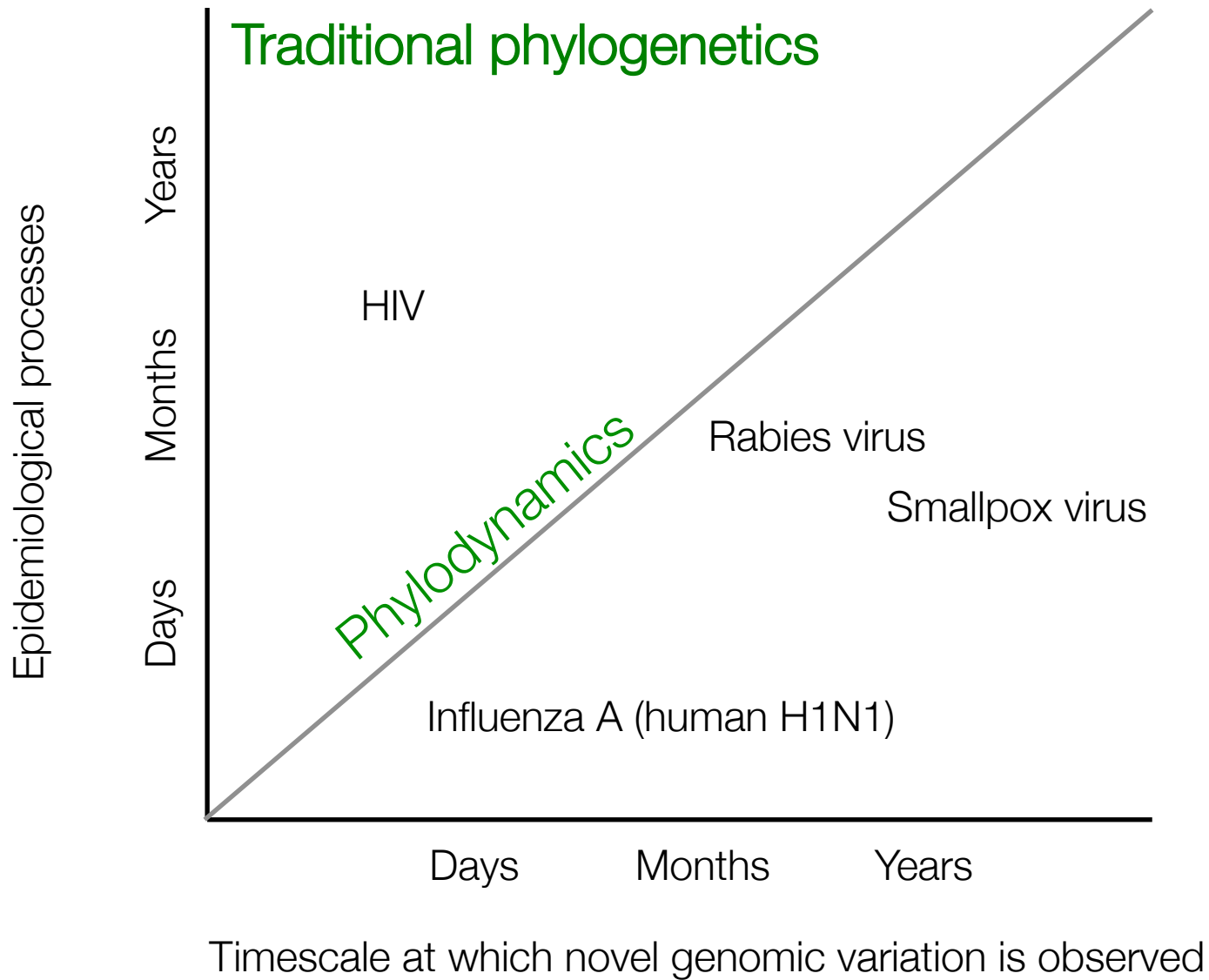


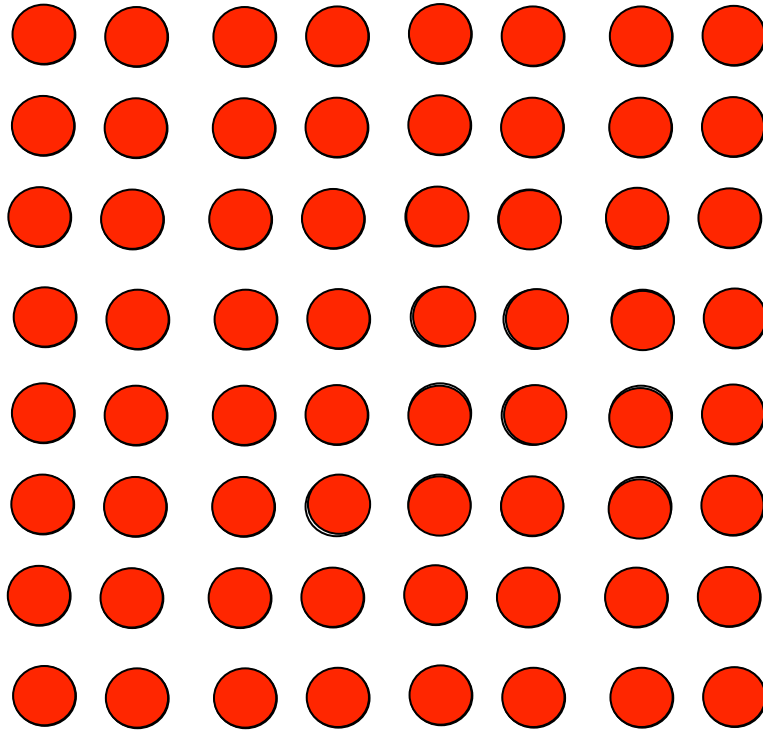
Lecture 2.4:

Infectious disease phylodynamics



The basic reproductive number

The basic reproductive number: R_0



$R_0 > 1$ Infection can spread

$R_0 < 1$ Infection will die out

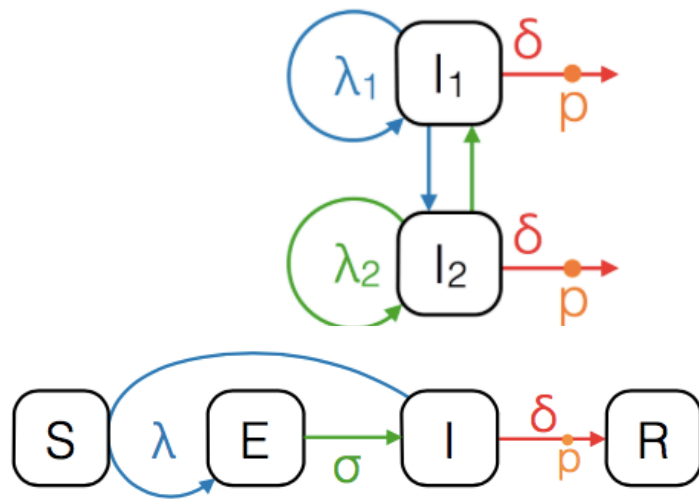
R_0 is the average number of secondary infections in a **fully susceptible** population

R_0 for some diseases

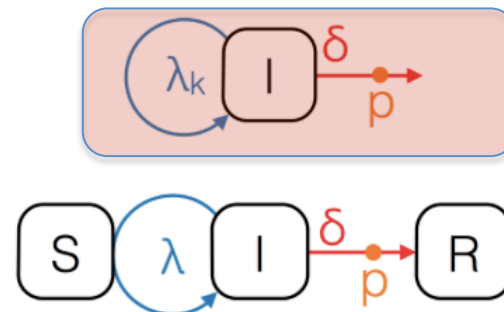
Measles	>12
HIV	2 – 5
Ebola	2.2 (Stadler et al. 2014)
TB	3.4 (Tanaka et al. 2006)

The basic reproductive number: R_0

- Can depend on many factors:
 - Duration of infection
 - Incubation period
 - Host immunity
 - Behavioral changes
- Some of these can be modeled using compartmental models:



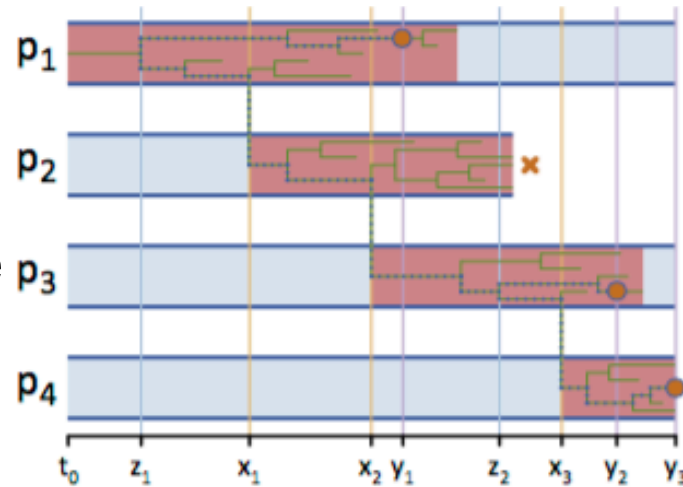
- λ — infection rate
- σ — incubation rate
- δ — becoming-noninfectious rate
- p — sampling probability



Phylogenetic epidemiology

Phylogenetics trees and infection

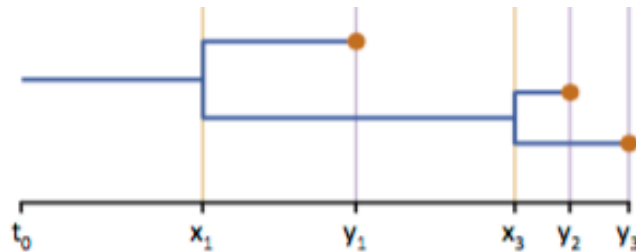
Complete transmission tree



Account for sampling fraction

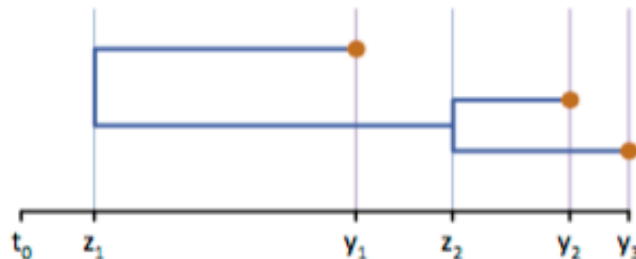
Assume that the sampled tree and reconstructed genealogy are equal

Sampled transmission tree



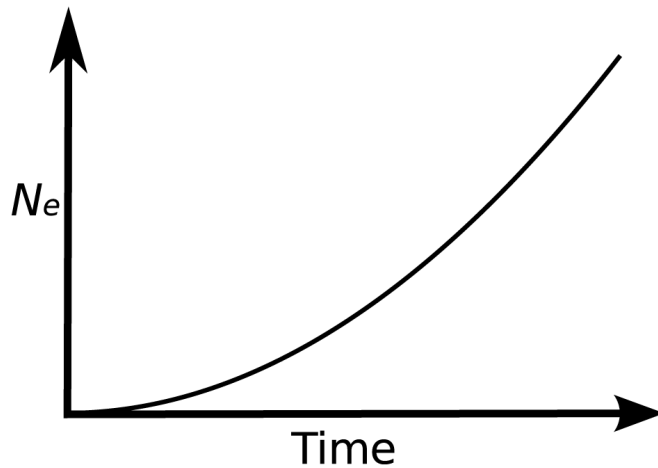
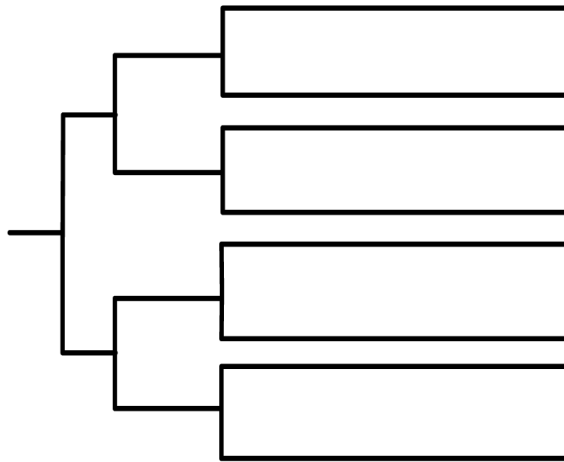
The genealogies have no information about who infected whom

Reconstructed genealogy

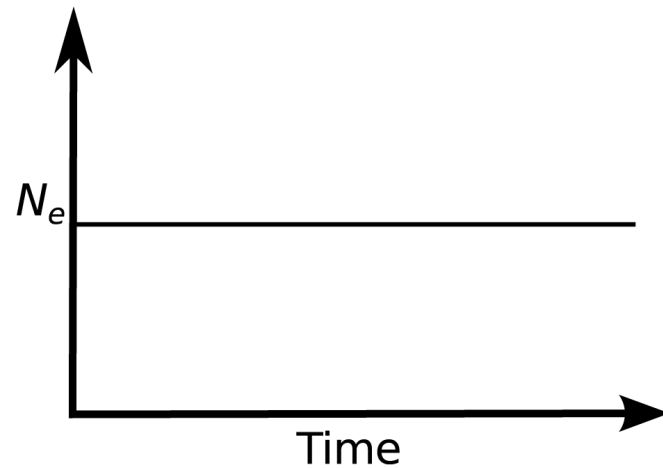
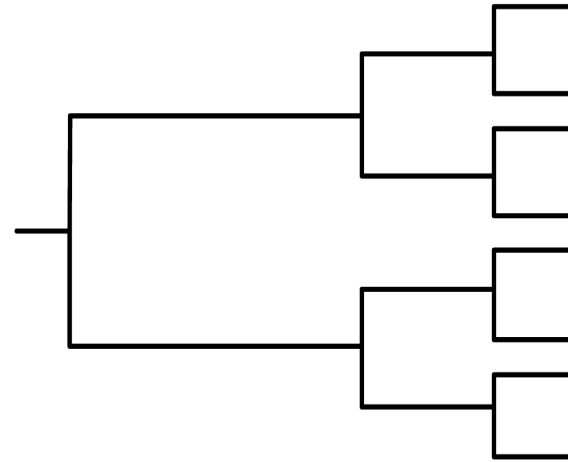


Estimating population size: the coalescent

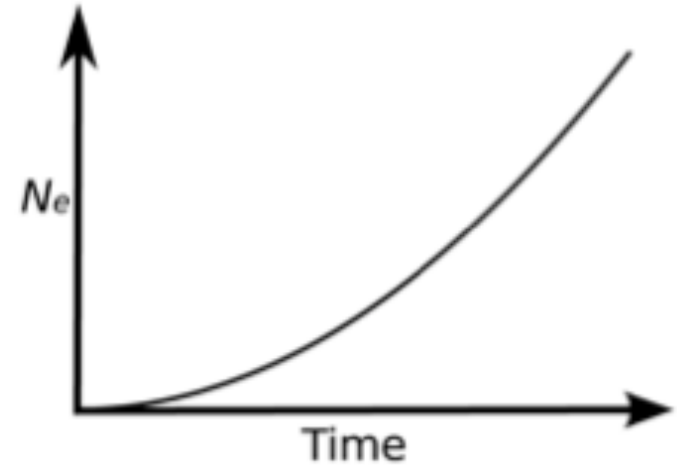
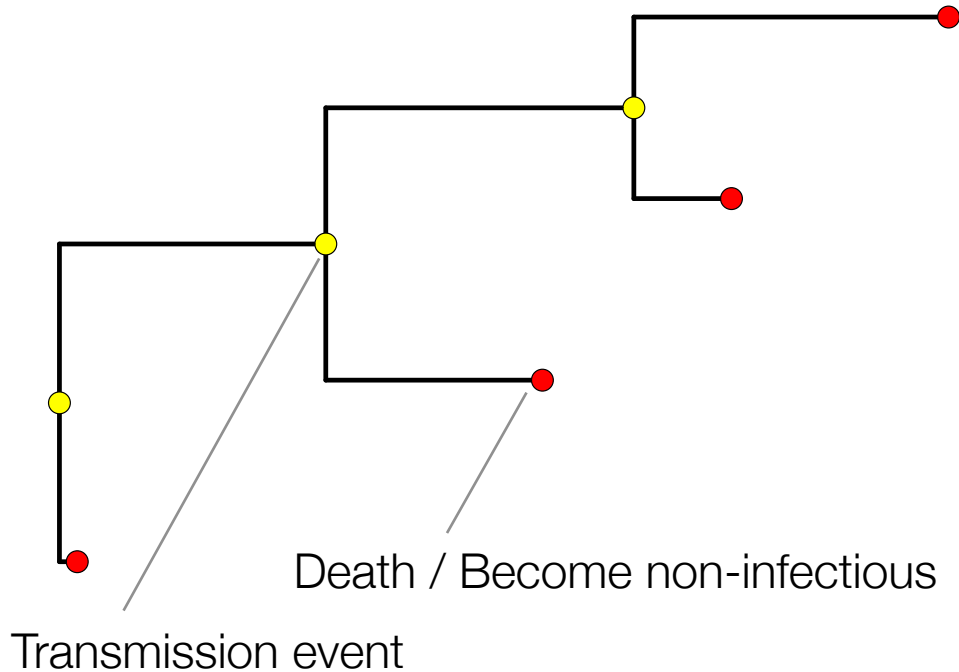
Exponential Growth



Constant Population Size



Estimating R_0 : coalescent phylodynamics



$$N(t) = N_0 e^{-rt}$$

$$r = (R_0 - 1) / D$$

r : exponential growth rate

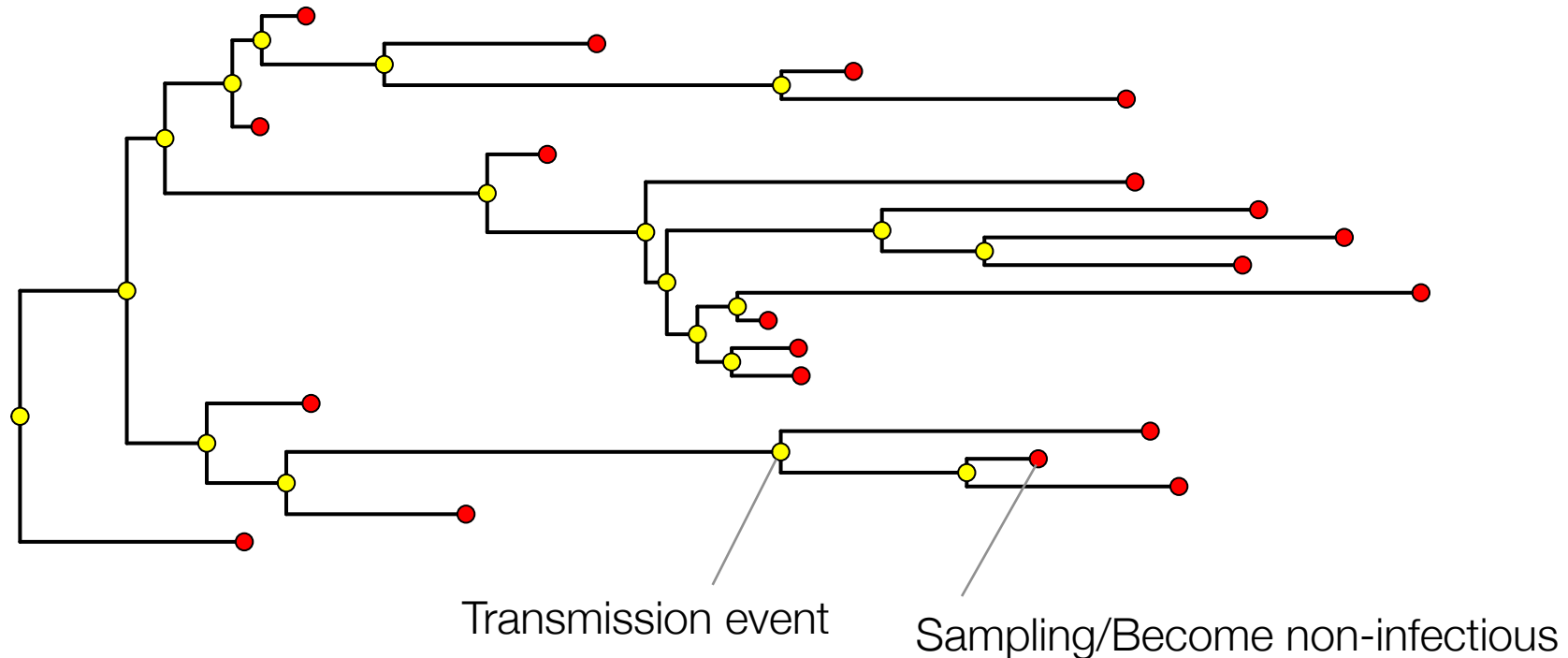
N_0 : initial population size

$N(t)$: population size at time t

R_0 : basic reproductive ratio

D : duration of infection

Estimating R_0 : Birth-Death models



λ : transmission rate (birth)

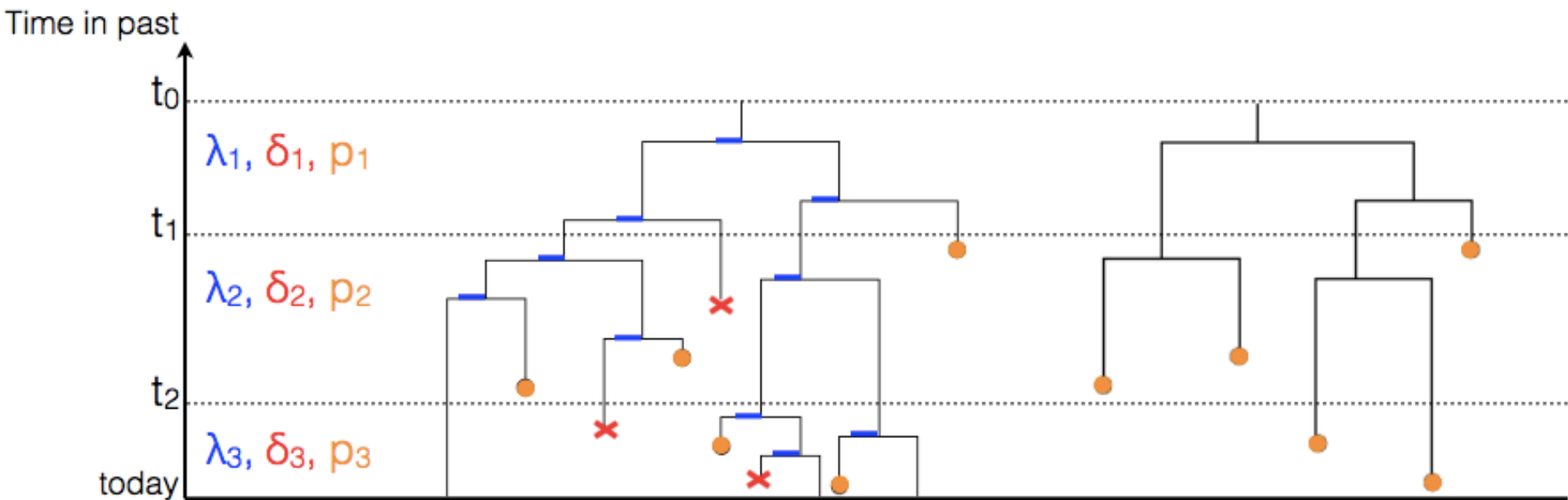
$$R_0 = \lambda / \delta$$

$\delta = \text{sampling} + \text{death/recovered}$

Skyline methods

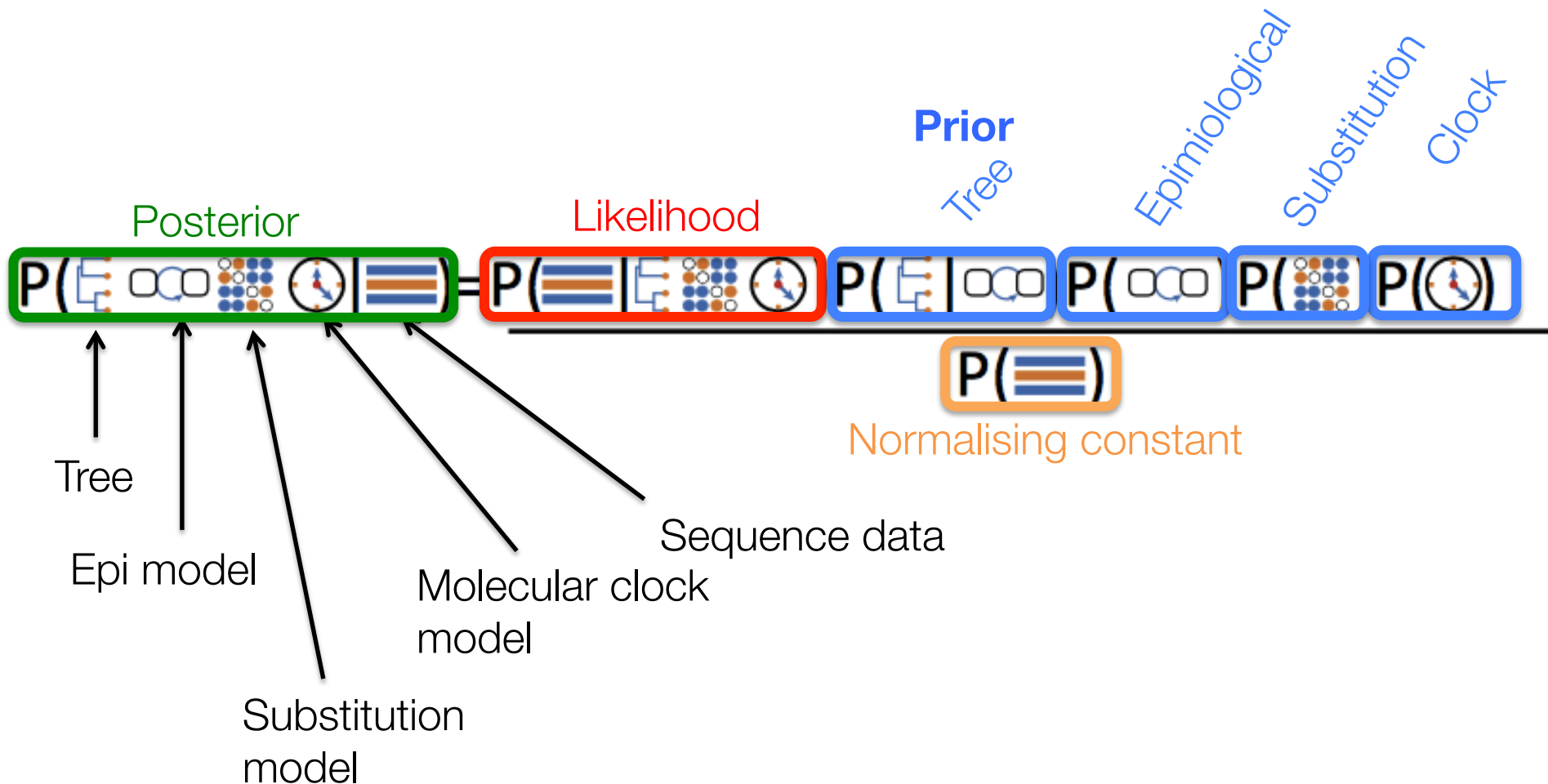
- Coalescent and Birth-Death methods assume constant parameters
- This assumption can be relaxed
 - Birth Death Skyline
 - Coalescent Skyline

$$R_e(t) \text{ is } R_0 \text{ at time } t, \\ R_e(0) = R_0$$



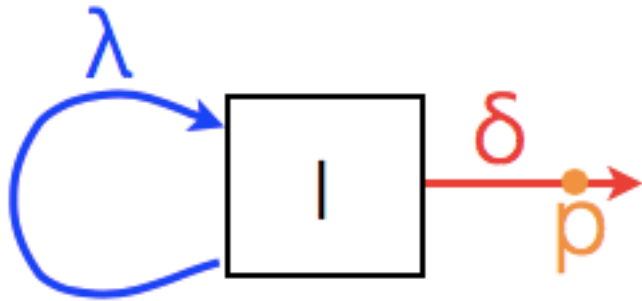
Modelling framework

Bayesian approach



Compartmental models

Birth-Death



$$R_0 = \lambda / (\delta)$$

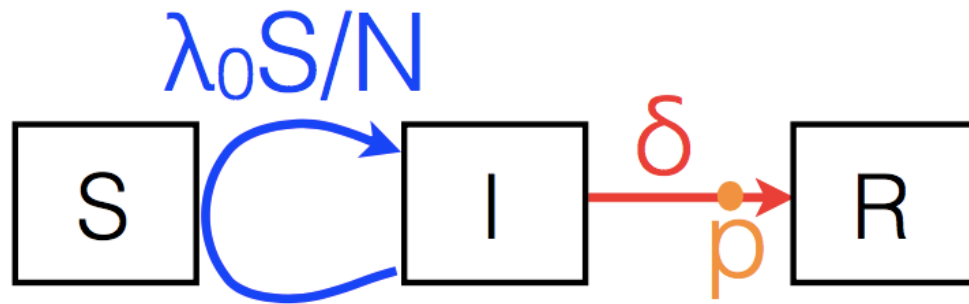
λ = transmission rate

δ = becoming non-infectious rate

ρ = sampling probability

Compartmental models

Birth-Death Susceptible-infected-recovered



$$R_0 = \lambda_0 / \delta$$

$$N = S + I + R$$

$$\lambda(S) = \lambda_0 S/N$$

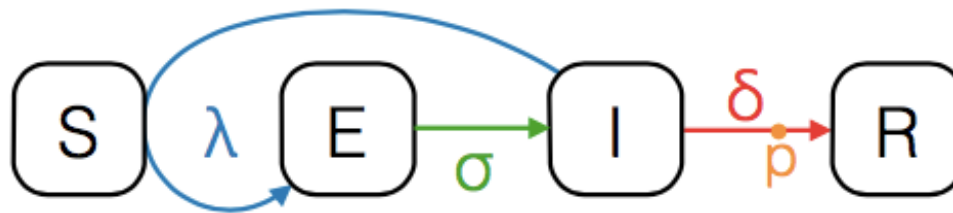
λ = transmission rate

δ = becoming non-infectious rate

ρ = sampling probability

Compartmental models

Birth-Death Exposed-infected-recovered



λ = transmission rate

δ = becoming non-infectious rate

ρ = sampling probability

σ = incubation rate

Compartmental models

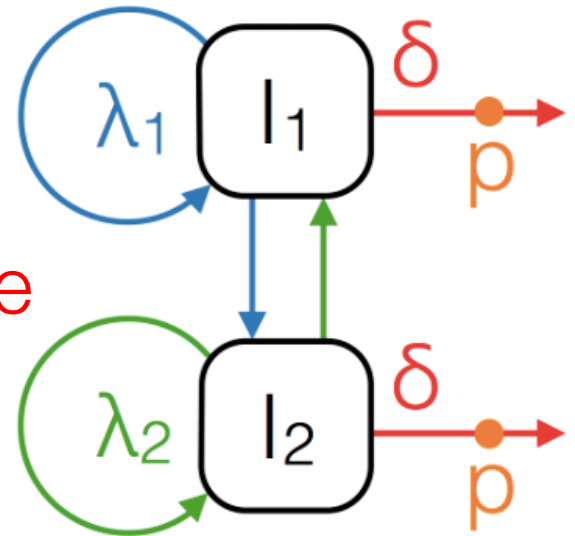
Birth-Death super-spreading

λ_1 = transmission rate 1

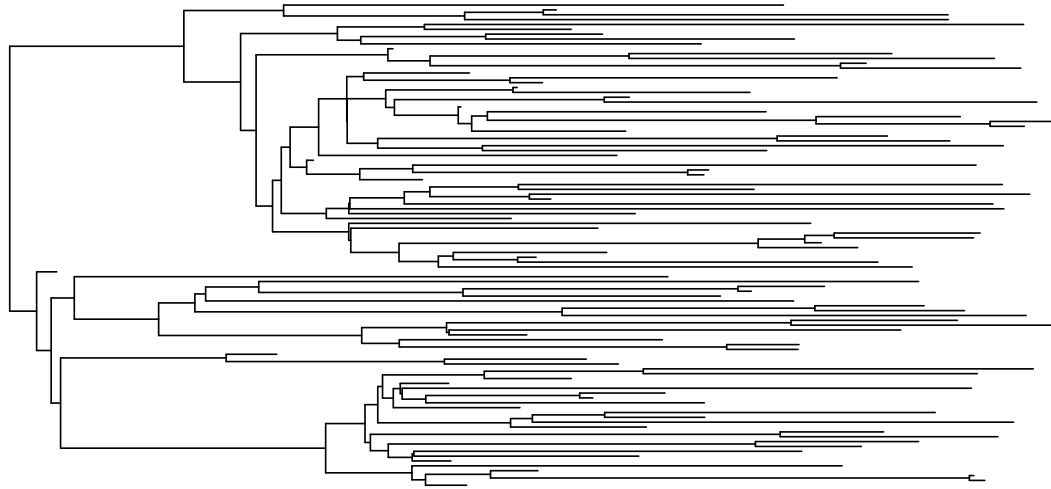
λ_2 = transmission rate 2

δ = becoming non-infectious rate

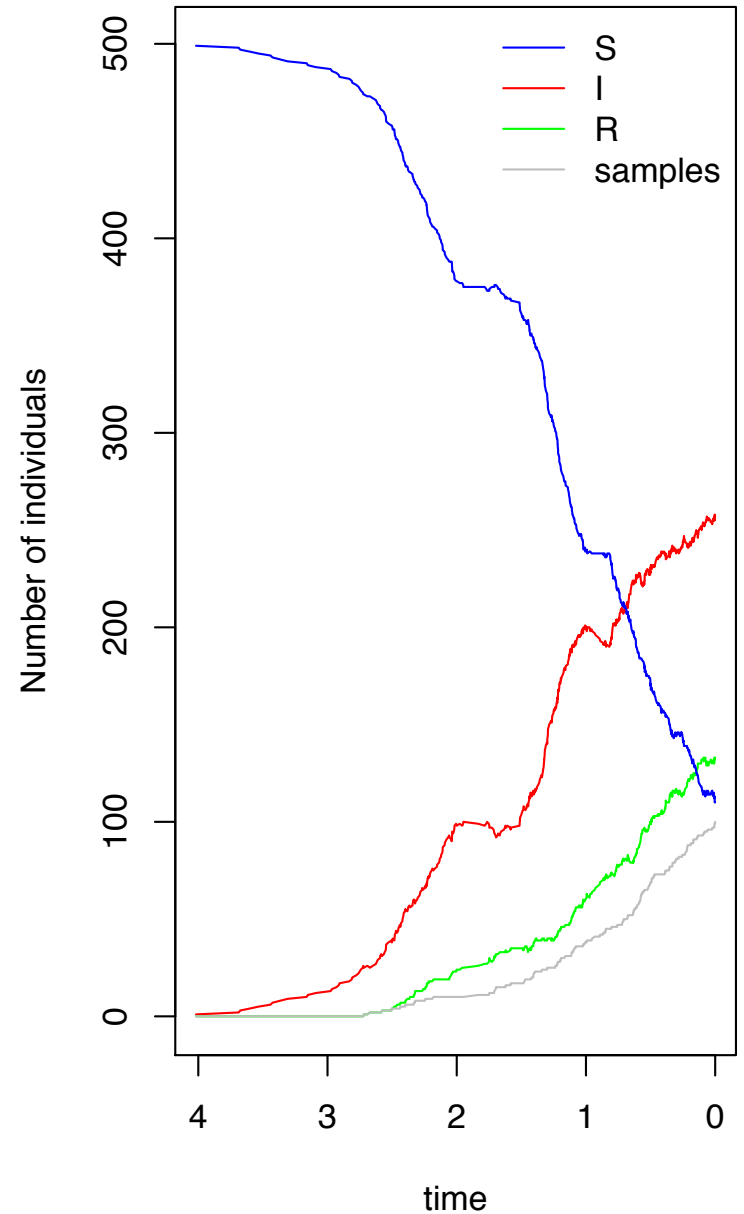
ρ = sampling probability



Simulating trajectories



MASTER (BEAST2)
(Vaughan and Drummond 2013)
TreeSim (Stadler 2011)



Useful references

Kühnert, Denise, et al. "Simultaneous reconstruction of evolutionary history and epidemiological dynamics from viral sequences with the birth–death SIR model." *Journal of the Royal Society Interface* 11.94 (2014): 20131106.

du Plessis, Louis, and Tanja Stadler. "Getting to the root of epidemic spread with phylodynamic analysis of genomic data." *Trends in microbiology* 23.7 (2015): 383-386.

Go to Practical 4: Phylogenetic
epidemiology in BEAST