Basic Algorithms Analysis in Javascript

Javascript as a Multiparadigm Language

Imperative

Procedural

Object-Oriented Event-Driven

Declarative

Functional

Prototypebased Dynamic typing

Imperative Programming vs. Declarative Programming

Imperative Programming

Declarative Programming

It's about how to do things

We use statements to say to the computer what to do

It's about manipulating the state of the system via its data structures

We rely on decision, branching and cycle statements

It's about what to do

We use expressions, that when evaluated tell the computer what we want

It's about not changing the state of immutable data structures within the system

We rely, typically on pure functions

Object-Oriented Programming (OOP) vs. Functional Programming (FP)

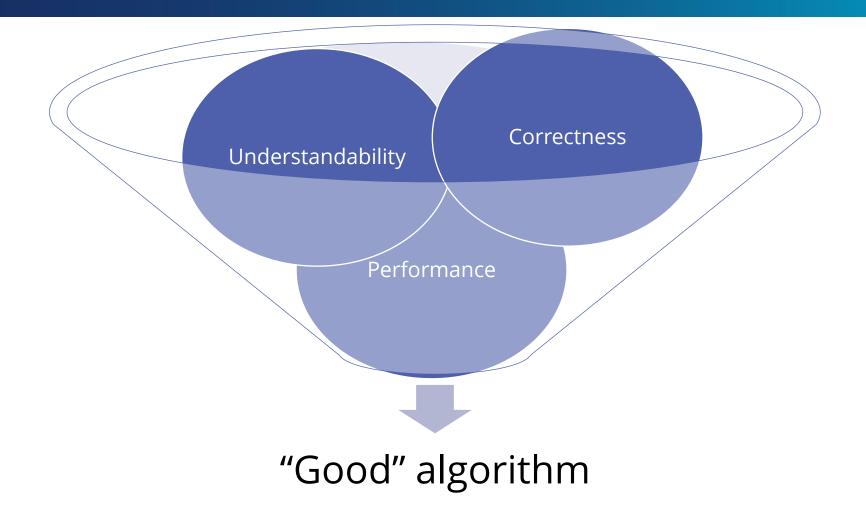
OOP

- Based on abstractions using objects
- Relies on mutable data
- It's an imperative approach
- Tightly related to iterations
- Structured using objects with operations
- Suitable for domains with many things with few operations
- Objects are more reusable than their operations

FP

- Based on evaluating functions
- Relies on immutable data
- It's a declarative approach
- Tightly related to recursion
- Structured using functions which process data structures
- Suitable for domains with few things with many operations
- Functions are highly reusable across the whole domain

Performance as a Key Algorithms Analysis Driver



How to Measure Algorithms Performance in Javascript?

- There are different ways to measure performance in WebUI environments (Chrome DevTools, for example).
- There are, also, different approaches to evaluate it (the RAIL model, for example).
- But the **simplest way** to measure a JS algorithm's performance is using performance.now().
- It's just about measuring how many milliseconds takes to execute the algorithm.
- However, it is not very reliable, because its results depend on many external factors.

Algorithms Complexity



Pure numbers

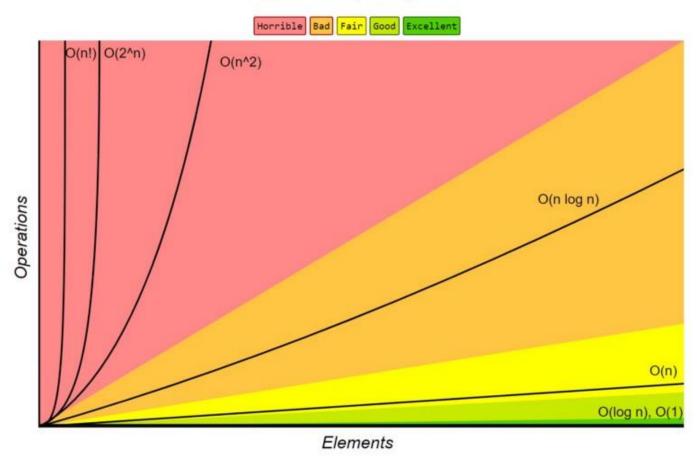
- Time
- Space

Expressing Time Complexity using Big-O Notation

- Big-O Notation is widely used to express the time complexity of an algorithm.
- It's a mathematical notation that describes the limiting behavior of a function when the argument tends towards a particular value or infinity.
- It's used to **classify** algorithms according to their complexity. The most usual of those classes are:
 - *O(1)*: Constant
 - *O(log n)*: Logarithmic
 - *O(n)*: Linear
 - *O(n log n)*: Loglinear
 - O(n²): Quadratic
 - *O(2")*: Exponential
 - *O(n!)*: Factorial

Expressing Time Complexity using Big-O Notation

Big-O Complexity Chart



See this with well-known algorithms: https://www.bigocheatsheet.com/

Big-o Notation via Asymptotic Analysis (1/4)

For determining the time complexity of an algorithm using asymptotic analysis, we shall first **determine the Time function** \mathbb{T} of the algorithm regarding the number n of input elements $\mathbb{T}(n)$. We'll follow the next steps:

- 1. We'll assume that executing every statement takes a **similar amount of time** (we could assume arbitrary **constants**).
- 2. The execution time of one code block is the **sum** of the times of each statement within it.
- 3. The execution time of an if...else statement is, at most, the time of the **longest alternative**.
- 4. The execution time of a loop is, at most, the sum of the times of each statement within it, multiplied for its **number of iterations**.
- 5. The execution time of a **nested loop** will result from multiplying the time that takes each of both loops.

Big-o Notation via Asymptotic Analysis (2/4)

Once we know the Time function T(n) of the algorithm, we may find it's Big-O time complexity, with the following steps:

1. Find the **fastest growing** term of the function.

2. Remove the coefficient of that term.

3. Put the result **within the parentheses** of the Big-O Notation expression.

Big-o Notation via Asymptotic Analysis (3/4)

```
function sum(n) {
    let sum = 0;
    for (let i = 1; i <= n; i++) {
        sum += i;
    }
    return sum;
}</pre>
```

1. Determined the Time function

```
T(n) = a + b*n + c
```

Found the fastest growing term
 b*n

Remove the coefficient of that term

1. Get the Big-O Notation expression O(n)

Big-o Notation via Asymptotic Analysis (4/4)

```
function printIdentityMatrix(n) {
    for (let i = 0; i < n; i++) {
        for (let j = 0; j < n; j++) {
            if(i==j) {
                document.write('1 ');
            }
        else {
                document.write('0 ');
        }
        document.write('<br>');
    }
}
```

1. Determined the Time function

$$T(n) = n*(a + b*n)$$

1. Found the fastest growing term

$$n*(a + b*n)$$

1. Remove the coefficient of that term

$$n*n \rightarrow n^2$$

1. Get the Big-O Notation expression $O(n^2)$

What About Doing these Analyses in Functional Programming?

 Finding the time complexity of a functional algorithm can be trickier.

• In functional programming, we don't see loops that often.

- Instead, we see **functions** (even pure or high-order ones) that often are **harder to analyze**:
 - Filter
 - Map
 - Reduce

References and Resources

- Imperative vs Declarative programming in JavaScript: https://medium.com/weekly-webtips/imperative-vs-declarative-programming-in-javascript-25511b90cdb7
- Functional Programming VS Object Oriented Programming (OOP) Which is better....? https://medium.com/@shaistha24/functional-programming-vs-object-oriented-programming-oop-which-is-better-82172e53a526
- performance.now(): https://developer.mozilla.org/es/docs/Web/API/Performance/now
- Big-O Cheatsheet: https://www.bigocheatsheet.com/
- Algorithms design with JavaScript: <u>https://www.youtube.com/watch?v=JgWm6sQwS_I</u>
- JavaScript Algorithms and Data Structures: https://www.freecodecamp.org/learn/javascript-algorithms-and-data-structures/
- Big-O Notation Calculator: https://shunnarski.github.io/BigO.html

