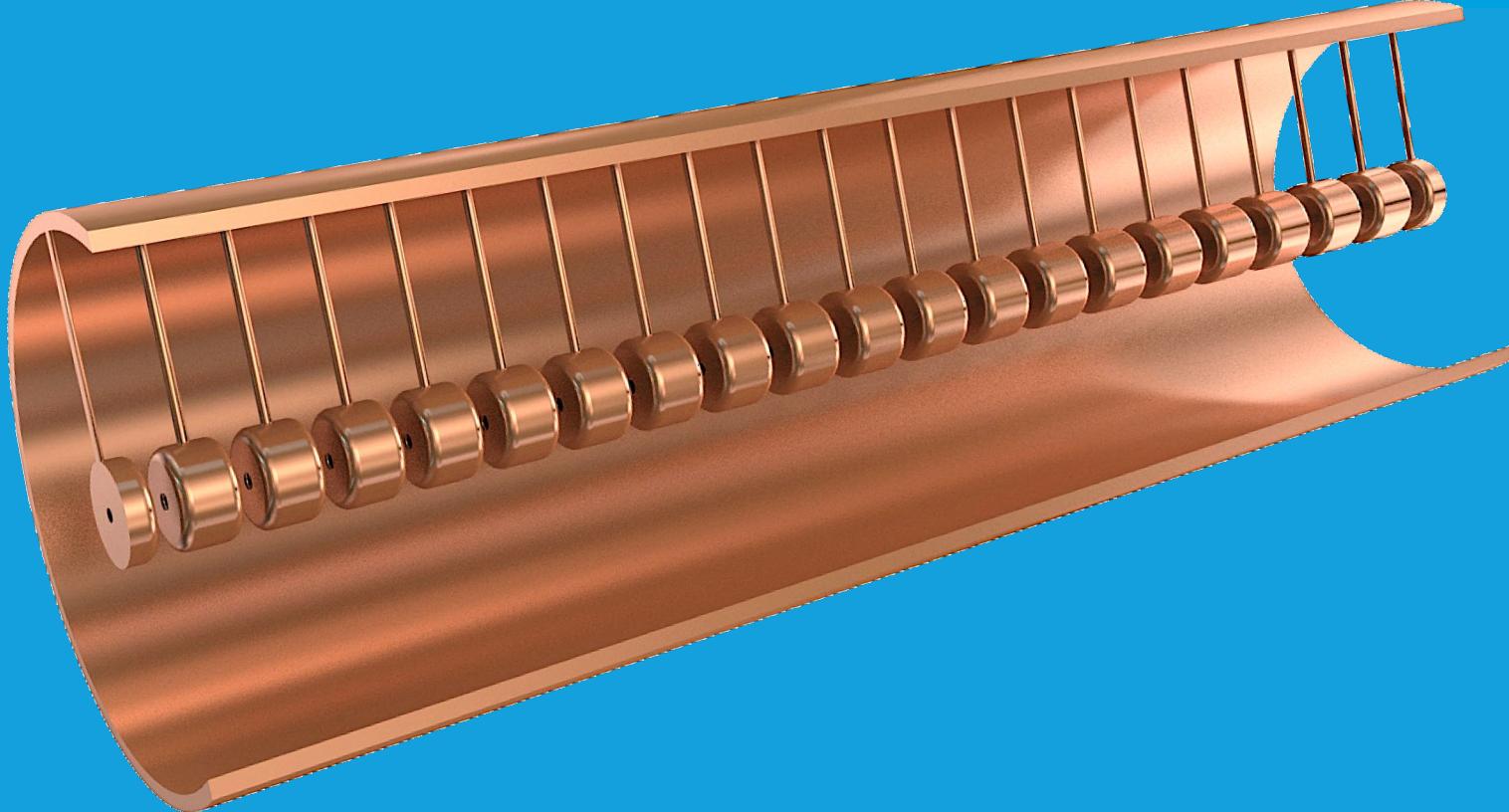


RF Cavity Design - an introduction -



EUROPEAN
SPALLATION
SOURCE



University of Oxford – John Adams Institute

17 November 2022

Ciprian Plostinar

Lecture Structure

- RF Cavity Design
 - Design Criteria
 - Figures of Merit
- Introduction to Superfish (2D)
- Examples:
 - Pill-box type cavity
 - DTL type cavity
 - Elliptical cavity
 - A ferrite loaded cavity
- Study of a simple cavity model
- Later in Hilary Term:
 - CST MicroWave Studio Demo (3D)
 - Open to all
 - Project work

RF Cavity Design

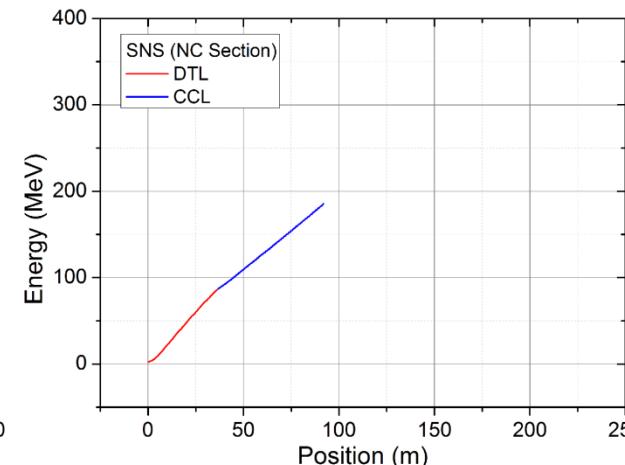
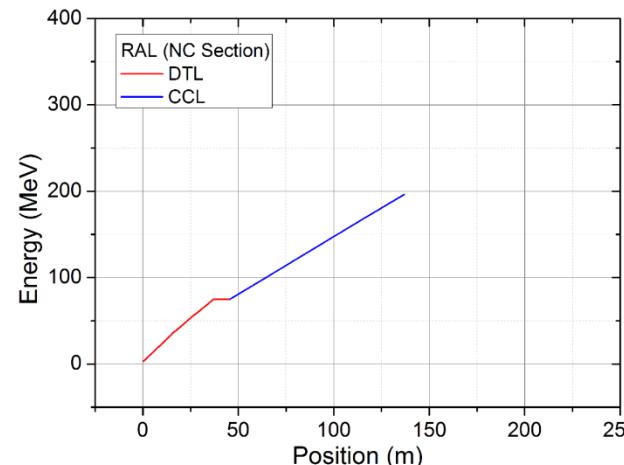
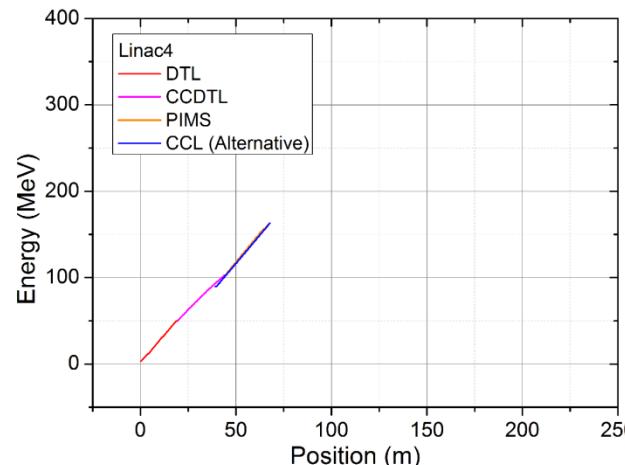
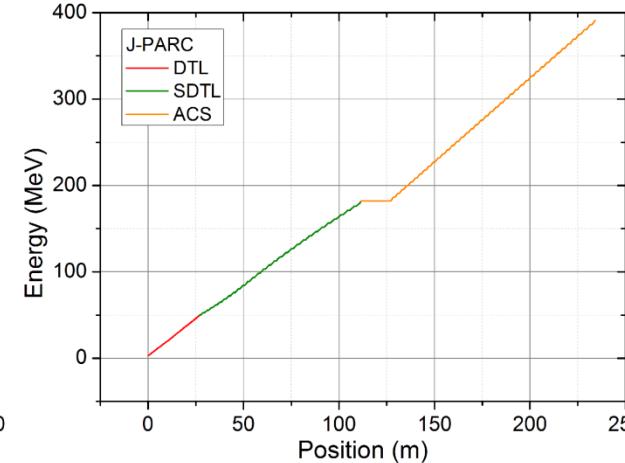
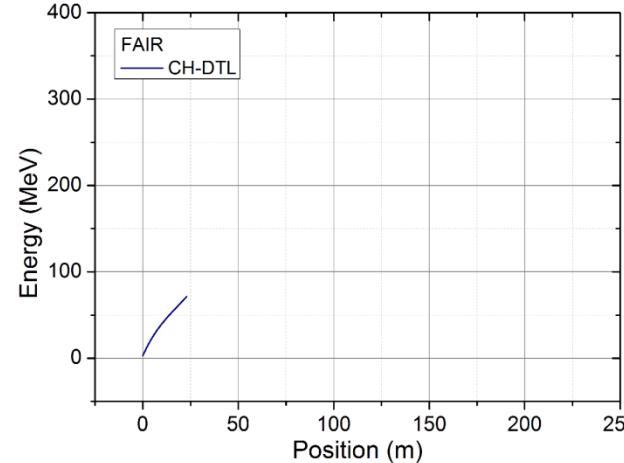
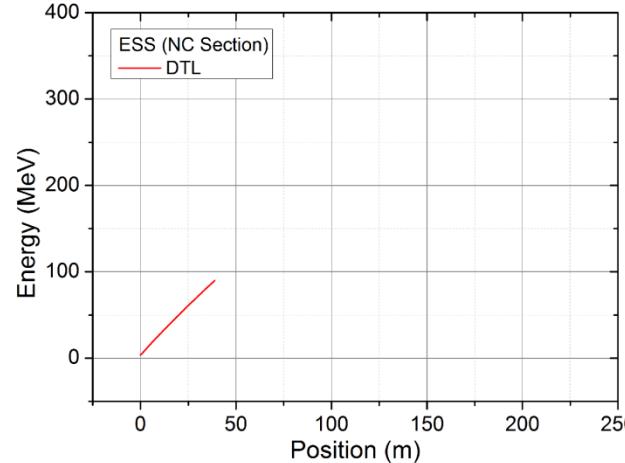
- the basics -



- In most particle accelerators, the energy is delivered to the particle by means of a large variety of devices, normally known as **cavity resonators**.
- The ideal cavity: volume of perfect dielectric limited by infinitely conducting walls.
- Hollow cylindrical resonator excited by a radio transmitter -> standing wave -> accelerating fields (the pillbox cavity).

Why Cavity Design Is Important?

Acceleration Profile in Several Linacs



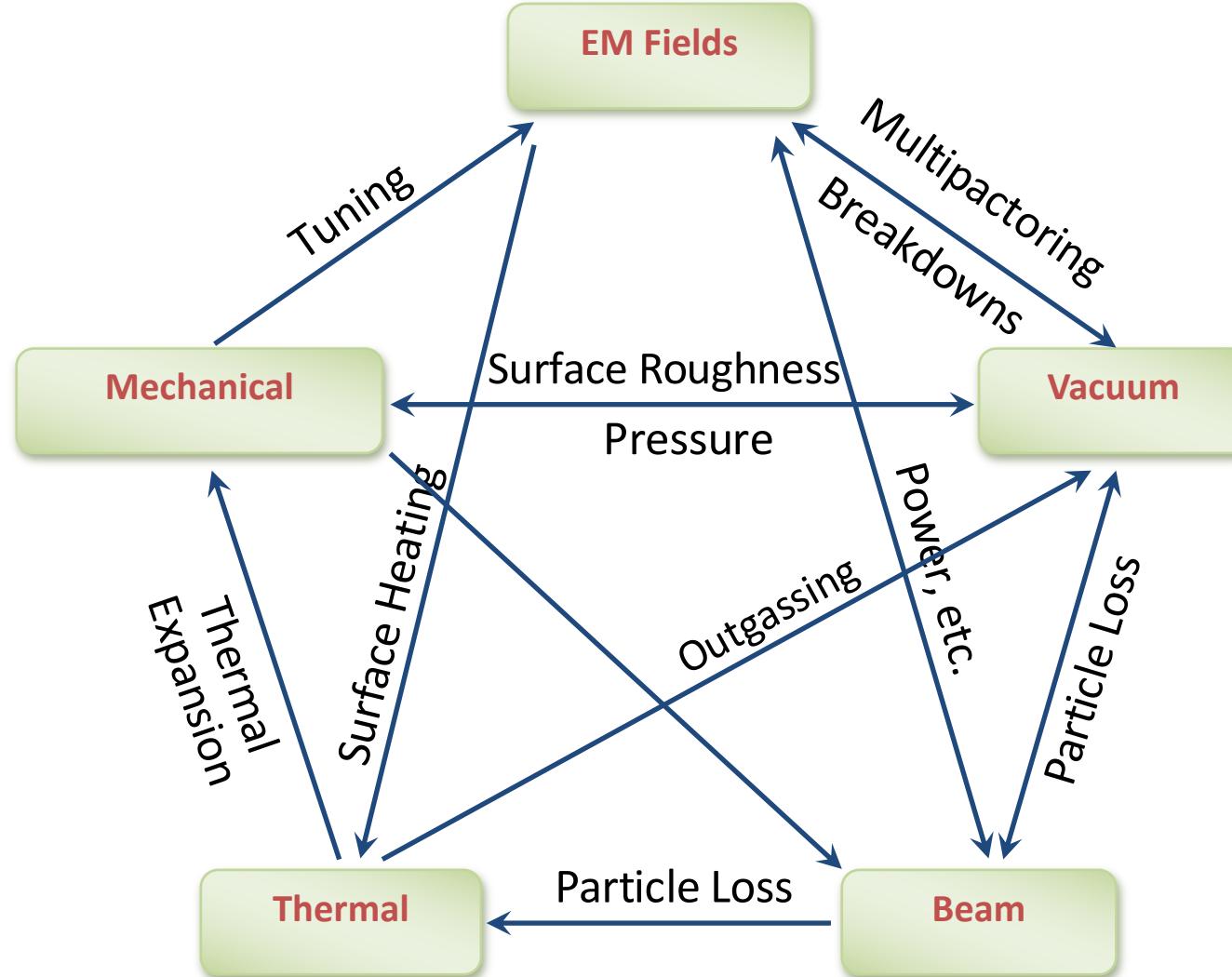
Design Process and Criteria



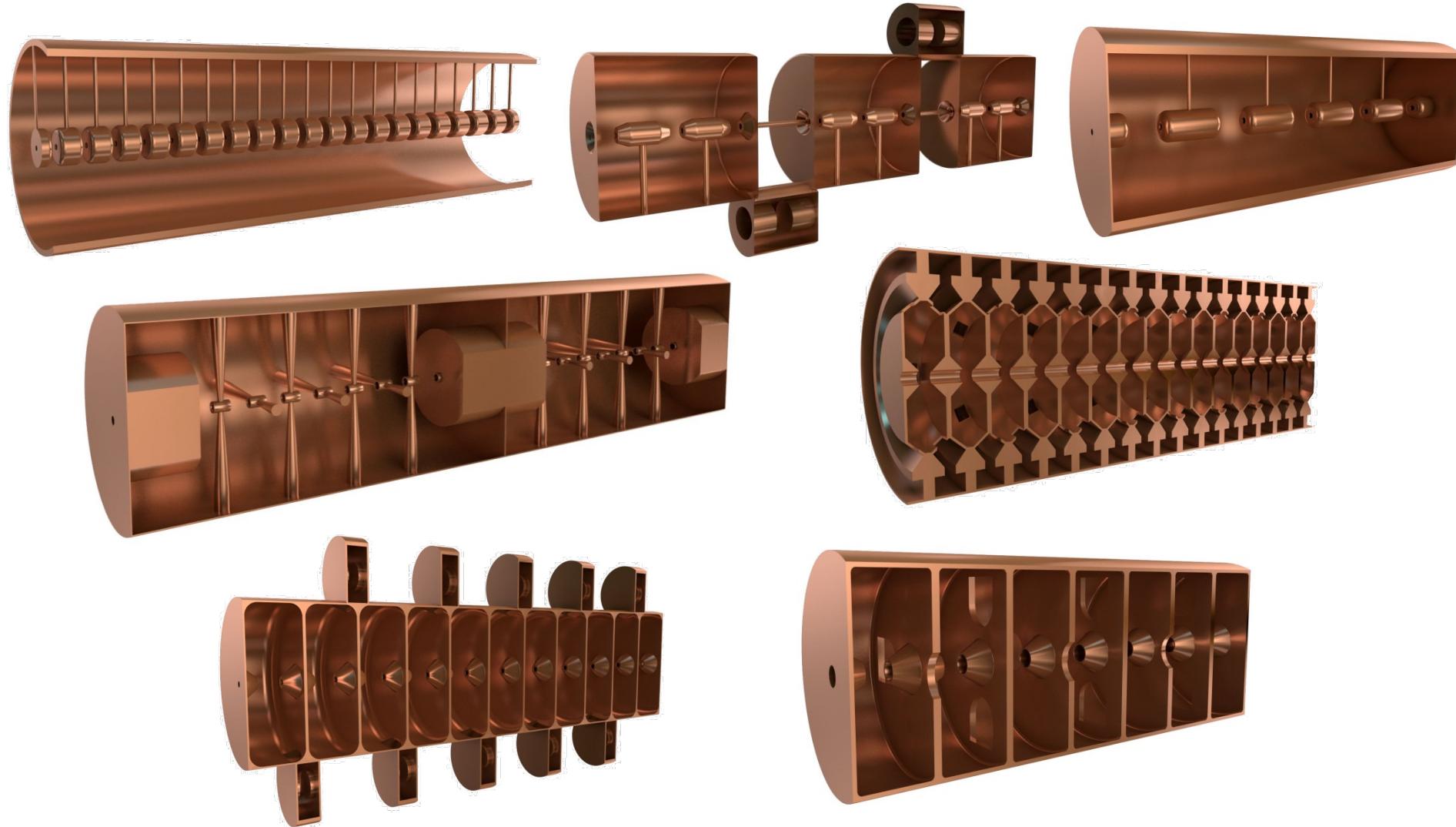
- Define the requirements:
 - Intended application
 - RF frequency
 - NC/SC
 - Voltage
 - Tuning
 - Etc.
- General design criteria:
 - Power Efficiency & RF Properties
 - Beam Dynamics considerations (control of loss and emittance growth, etc.) – especially true for linacs
 - Technologies and precisions involved
 - Tuning procedures (frequency, field profile, stability against perturbations)
 - Sensitivity to RF errors (phase and amplitude)
 - Etc.

The “Magic Pentagon” of Cavity Design

Interdependent Technologies



Cavity “Zoo”

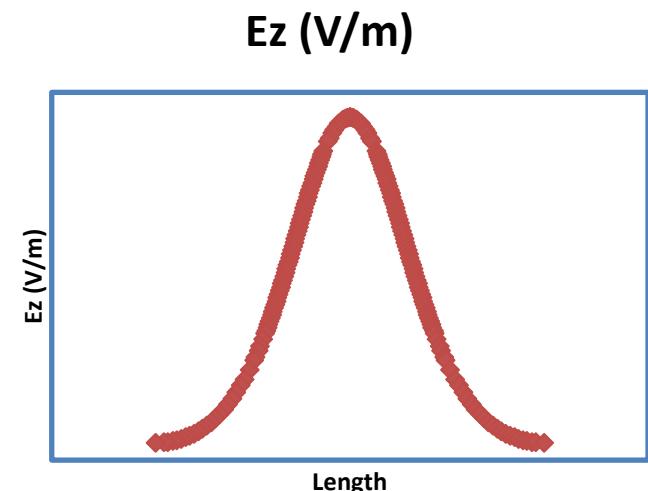
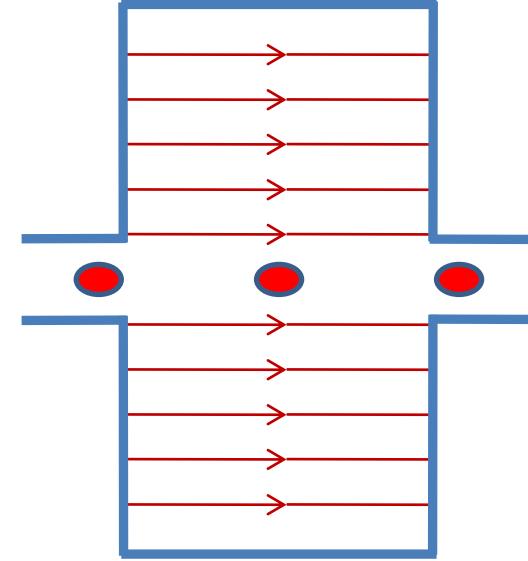


Figures of Merit

The Transit Time Factor, T

- While the particle crosses the cavity, the field is also varying
- The particle sees only a **fraction** of the peak voltage
- T is a measure of the reduction in energy gain cause by the sinusoidal time variation of the field in the cavity.

$$T = \frac{\int_{-L/2}^{L/2} E(0, z) \cdot \cos \frac{2\pi z}{\beta\lambda} dz}{\int_{-L/2}^{L/2} E(0, z) dz}$$



Figures of Merit

The Quality Factor, Q

- To first order, the Q-value will depend on the conductivity of the wall material only
- High Q -> narrower bandwidth -> higher amplitudes
- But, more difficult to tune, more sensitive to mechanical tolerances (even a slight temperature variation can shift the resonance)
- Q is dimensionless and gives only the ratios of energies, and not the real amount of power needed to maintain a certain resonant mode
- For resonant frequencies in the range 100 to 1000 MHz, typical values are 10,000 to 50,000 for normal conducting copper cavities; 10^8 to 10^{10} for superconducting cavities.

$$Q_0 = \frac{2\pi \cdot \text{stored energy}}{\text{energy consumed per period}} = \frac{2\pi W}{TP_0} = \omega \frac{U}{P_0}$$

Figures of Merit

Shunt Impedance

- A measure of the effectiveness of producing an axial voltage V_0 for a given power dissipated
- Typical values of ZT^2 for normal conducting linacs is 30 to 50 $M\Omega/m$. The shunt impedance is less relevant for superconducting cavities.

$$r_s = \frac{V_0^2}{P_0}$$

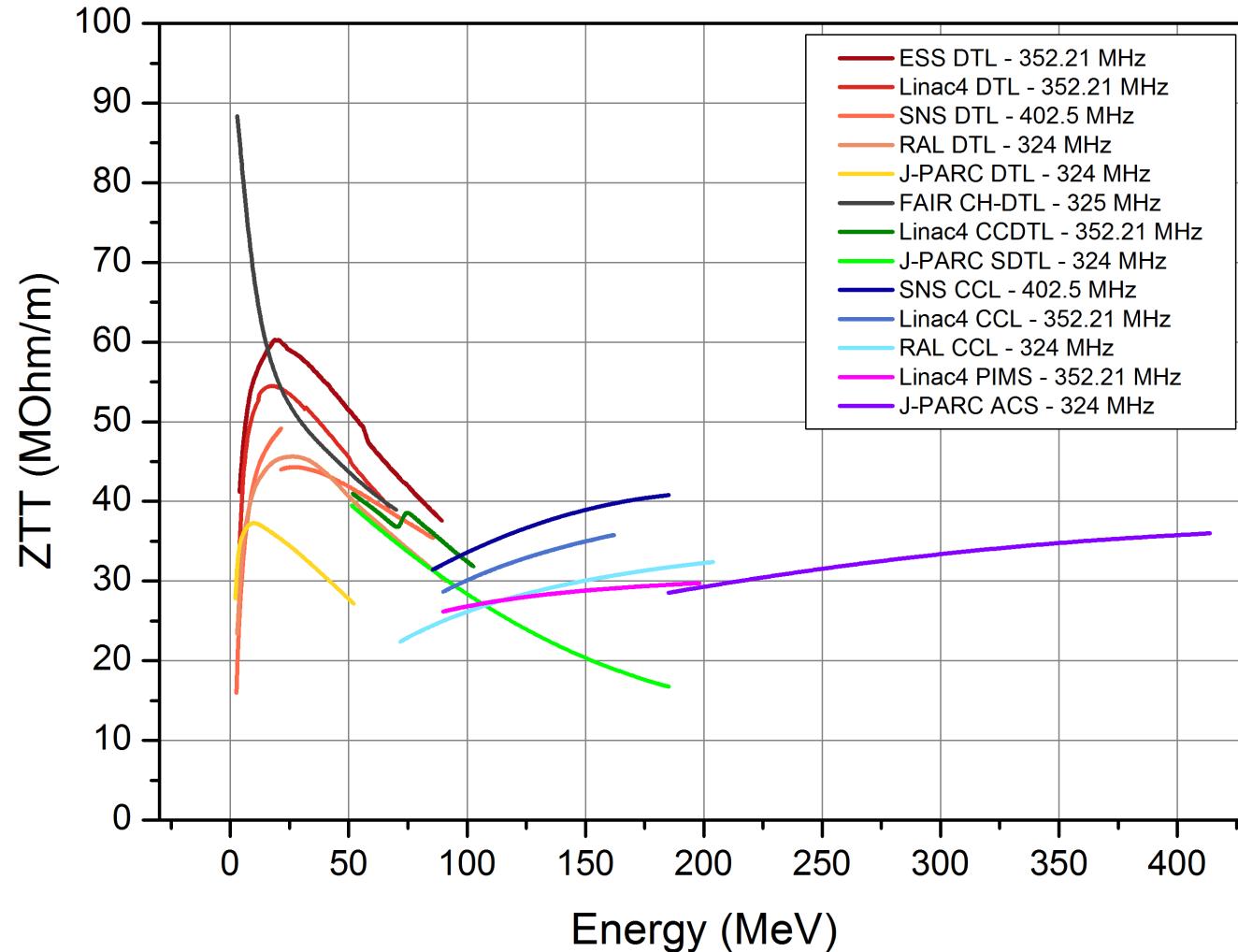
Shunt Impedance

$$ZT^2 = \frac{r}{L} = \frac{(E_0 T)^2}{P_0 / L}$$

Effective Shunt Impedance
per unit length

Figures of Merit

Shunt Impedance



Figures of Merit

r/Q



- Measures the efficiency of acceleration per unit of stored energy at a given frequency
- It is a function only of the cavity geometry and is independent of the surface properties that determine the power losses.

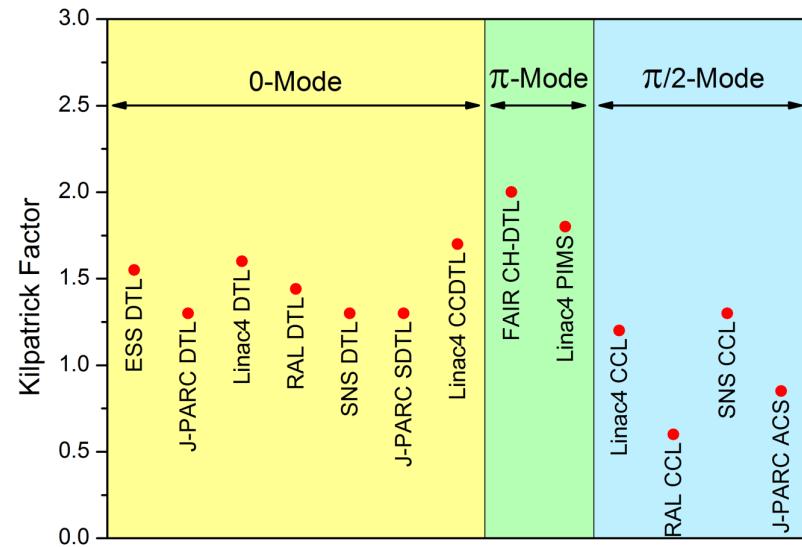
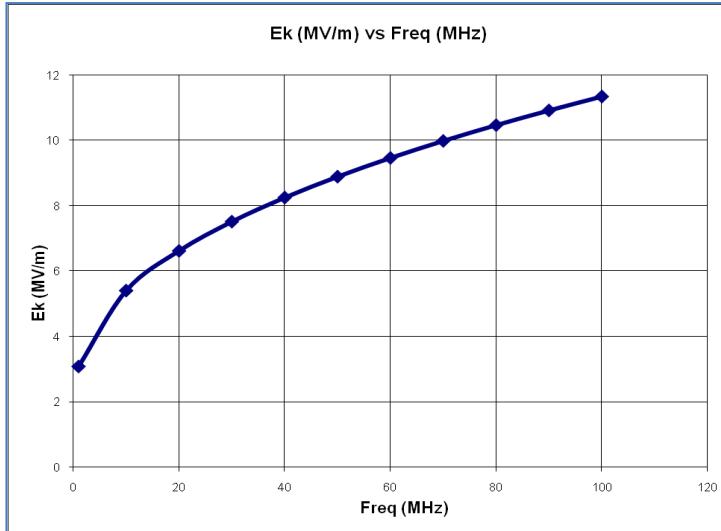
$$\frac{r}{Q} = \frac{(V_0 T)^2}{\omega U}$$

Figures of Merit

The Kilpatrick Factor

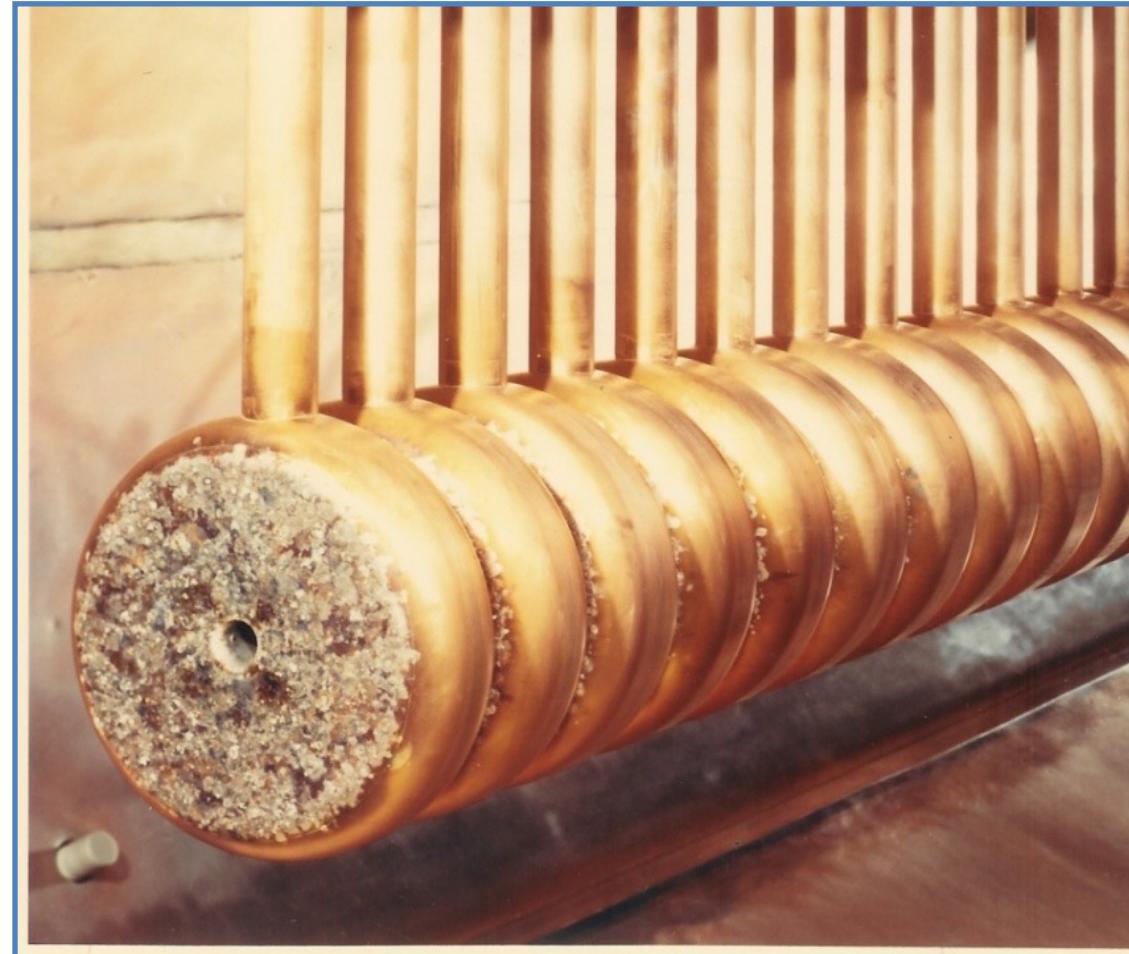
- High Field \rightarrow Electric breakdown
- Maximum achievable field is limited

$$f = 1.64 E_k^2 e^{-8.5/E_k}$$



Figures of Merit

The Kilpatrick Factor



SC Cavities

... some other factors to consider

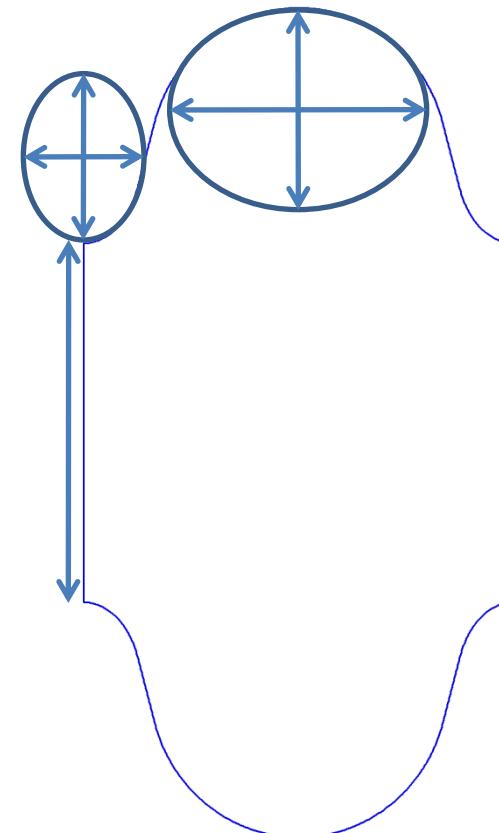


- E_{peak}/E_{acc} – field emissions limit (Eacc limit)
- B_{peak}/E_{acc} – quench limit (SC breakdown)
- G (Geometric Factor - the measure of energy loss in the metal wall for a given surface resistance)
- Higher Order Modes – manage and suppress HOM (e.g.: dipole modes can degrade the beam -> suppression scheme using HOM couplers)
- Multicell cavities: Field Flatness
- K_{cc} – Cell to cell coupling
- Etc.

SC Cavities

Basic design guidelines

- Optimise geometry to increase both r/Q and G resulting in less stored energy and less wall loss at a given gradient (low cryogenic losses)
- Optimise geometry to reduce E_{peak}/E_{acc} and B_{peak}/E_{acc}
- Find optimum K_{cc} . (e.g.: a small aperture increases r/Q and G (!), but reduces K_{cc} . A small K_{cc} increases the sensitivity of the field profile to cell frequency errors.)



Introduction to Poisson Superfish

Before you start



- You will need a laptop running Windows. If you have Linux/MacOS install VMWare/Wine.
- Please download and install Poisson Superfish. To do this go to the following address and follow the instructions:
 - http://laacg.lanl.gov/laacg/services/download_sf.phtml
- Please download the example files to your computer from the JAI website.
- An extensive documentation can be found in the Superfish home directory (usually C:/LANL).
 - Have a look at the SFCODES.DOC file. Table VI-4 explains how the object geometry is defined in Superfish (page 157).
 - For a list of Superfish variables, see SFINTRO.doc, Table III-3 (page 76)
- For any questions, email Ciprian (ciprian.plostinar@ess.eu) or Emmanuel (emmanuel.tsesmelis@cern.ch). Good luck!

Introduction to Poisson Superfish

The basics



- Poisson and Superfish are the main solver programs in a collection of programs from LANL for calculating static magnetic and electric fields and radio-frequency electromagnetic fields in either 2-D Cartesian coordinates or axially symmetric cylindrical coordinates.
- Finite Element Method

Introduction to Poisson Superfish Solvers

- **Automesh** – generates the mesh (always the first program to run)
- **Fish** – RF solver
- **Cfish** – version of Fish that uses complex variables for the rf fields, permittivity, and permeability.
- **Poisson** – magnetostatic and electrostatic field solver
- **Pandira** – another static field solver (can handle permanent magnets)
- **SFO, SF7** – postprocessing
- **Autofish** – combines Automesh, Fish and SFO
- **DTLfish, DTLCells, CCLfish, CCLcells, CDTfish, ELLfish, ELLCAV, MDTfish, RFQfish, SCCfish** – for tuning specific cavity types.
- **Kilpat, Force, WSFPlot**, etc.



A Pillbox Cavity

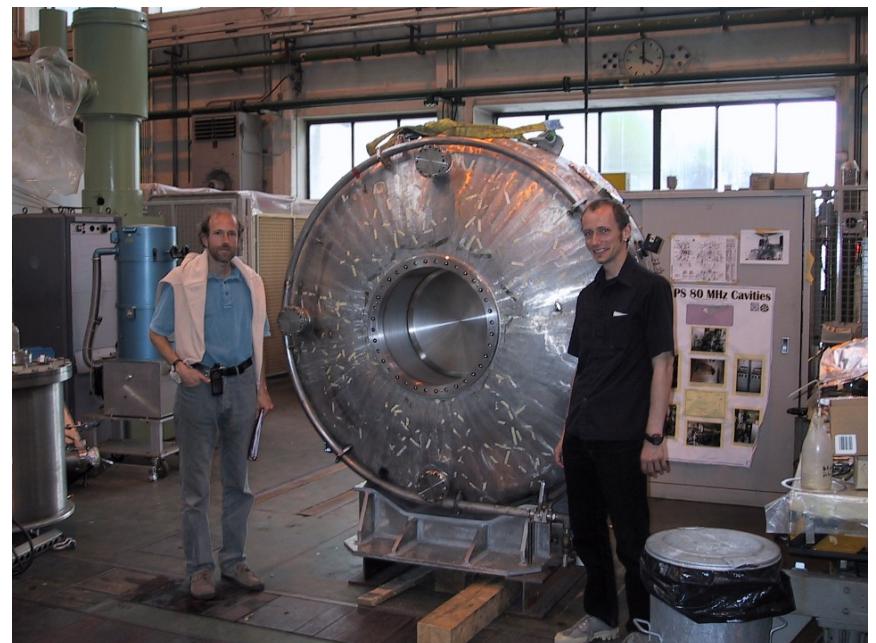
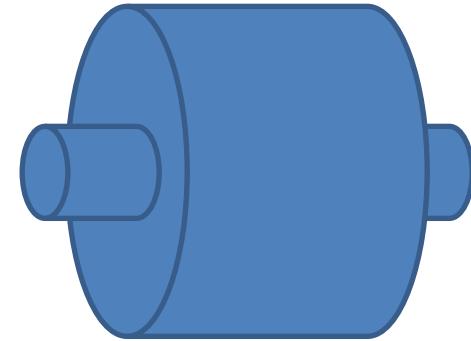
The simplest RF cavity

- For the accelerating mode (TM_{010}), the resonant wavelength is:
 - independent of the cell length
- Example: a 40 MHz pillbox type cavity would have a diameter of ~ 5.7 m
- In the picture, CERN 88 MHz

$$\lambda = \frac{\pi D}{x_1}$$

$$x_1 = 2.40483$$

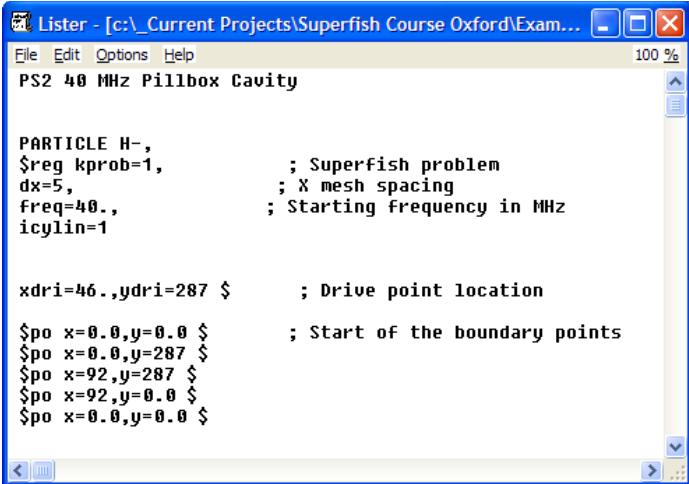
x_1 - first root of the zero-th order Bessel function $J_0(x)$



A Pillbox Cavity

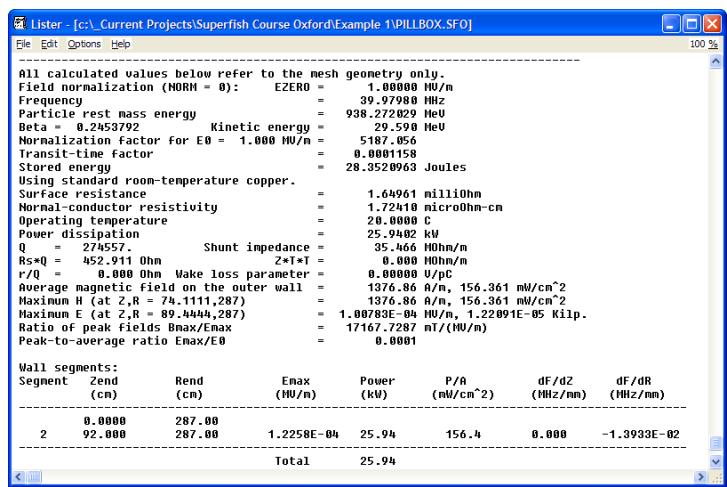
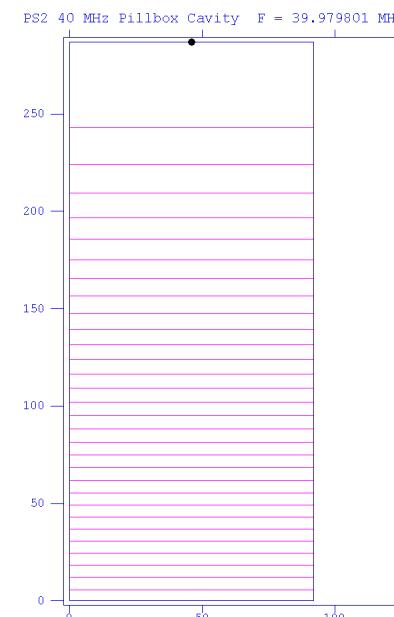
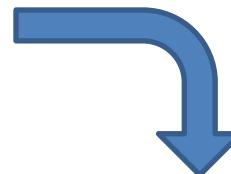
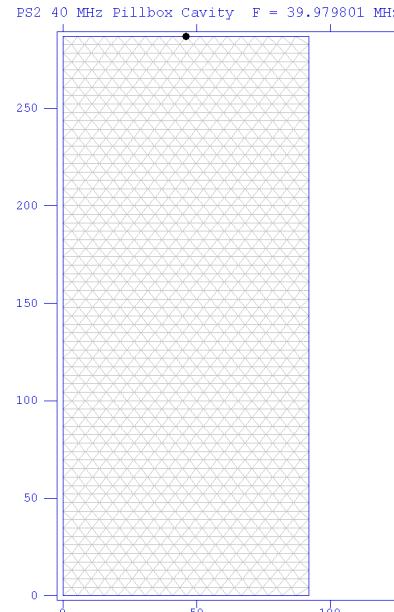
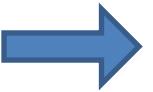
Superfish Implementation

Superfish input file



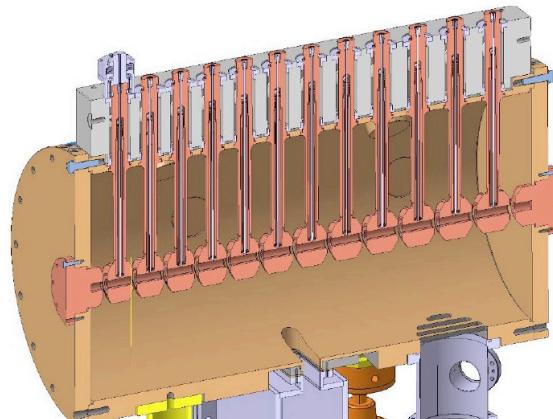
```
PARTICLE H-,
$reg kprob=1,           ; Superfish problem
dx=5,                  ; X mesh spacing
Freq=40.,              ; Starting frequency in MHz
icylin=1

xdri=46.,ydr=287 $    ; Drive point location
$po x=0.0,y=0.0 $      ; Start of the boundary points
$po x=0.0,y=287 $
$po x=92,y=287 $
$po x=92,y=0.0 $
$po x=0.0,y=0.0 $
```

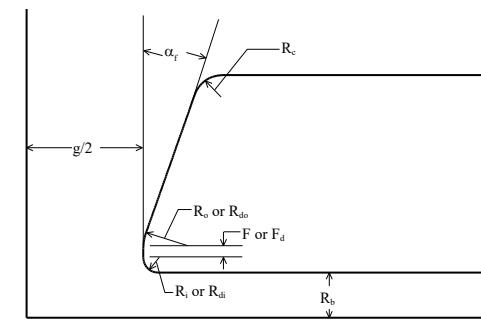
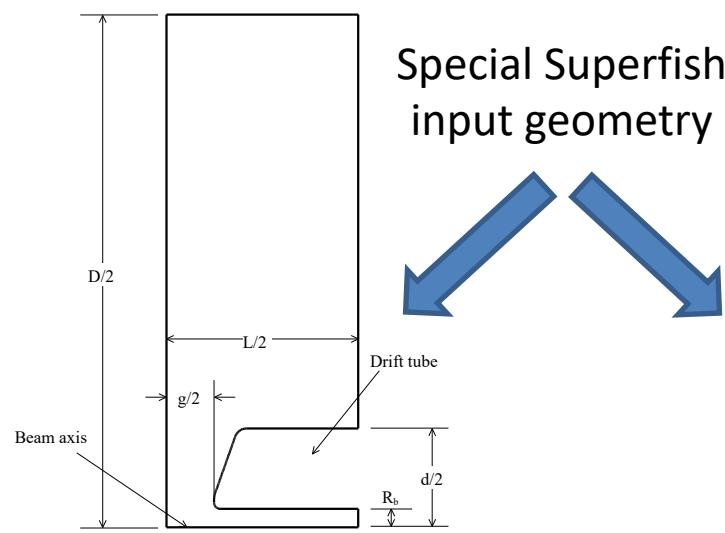
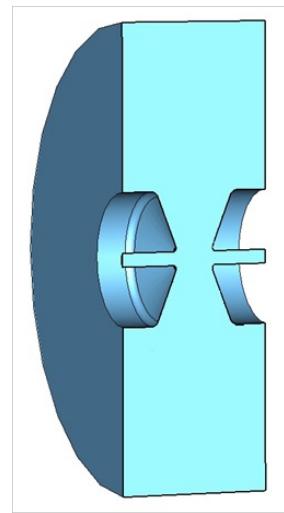
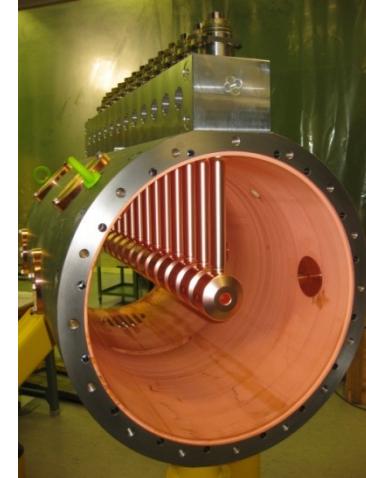


A Drift Tube Linac-type Cavity (DTL)

Basic Geometry



CERN Linac4 DTL
prototype



A Drift Tube Linac-type Cavity (DTL) Superfish Implementation

Superfish input file

```
File Edit Options Help
Title
DTL-type cavity
Resonant Frequency = 324 MHz
ENDTitle

PARTICLE H-
InitialEnergy 3 ; Energies used in program DTLCells

FILENAME_PREFIX DTL
SEQUENCE_NUMBER 1
FREQUENCY 324
BETA 0.079732
LENGTH 7.37748526582
DIAMETER 55.81982579555
G0_LENGTH_lambda 0.2
G0_Length 1.475497053164
E0_Normalization 2.5
E0T_Normalization 1.651388369868
CORNER_radius 0.5
INNER_nose_radius 0.15
OUTER_nose_radius 0.3
FLAT_length 0.2
FLAT_diameter 10
DRIFT_TUBE_Diameter 18
CAP_Change 0.0
STEM_Diameter 3
STEM_Count 1
BORE_radius 1.4
PHASE_length 180
DELTA_frequency 0.01
MESH_size 0.02
INCREMENT 2
START 4

; Start codes for DTLfish:
; 1 No tuning
; 2 Adjust tank diameter
; 3 Adjust drift tube diameter (not recommended)
; 4 Adjust gap
; 5 Adjust face angle

EndFile
```

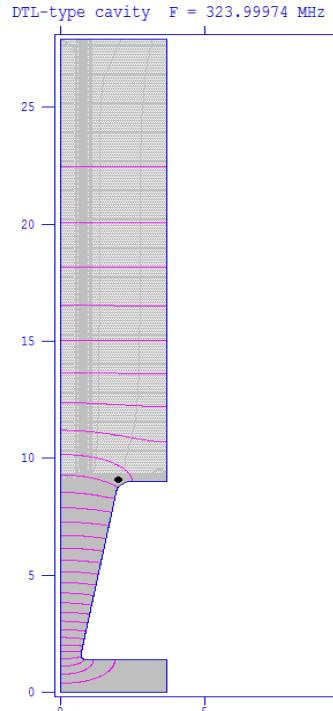
Geometry file

```
File Edit Options Help
DTL-type cavity
Resonant Frequency = 324 MHz
Adjusting gap, currently = 1.4754971, g/b1 = 0.2000000

IREG KPB08-1
M1=1
I0=324,0.9997439729
FRE=324
BETA=0.079732
KTHD=0-1
DPH1=180
DPH2=0
NBSLO=0,NBSRT=1,NBSLF=1
LINES=1
ICV1IN=1
NDRH=0
NDRW=0
NDRD=0
DTL=1
NMSS=-3
EPSD=1.E-6
EPSO=1.E-6
RHO=1.0
SDBI=1.998016697994
VDBI=1.09621635729
USL=1<->
; Allow convergence in 1 iteration
; X line-region physical locations:
XREG=0.557748526582,0.677748526582,0.947748526582,1.067748526582,
; X line-region logical locations:
LREG=1,8,11,25,28,
; Y line-region physical locations:
YREG=0.0282842712475,1.355753959129,3.098196086403,9.084852813742,
; Y line-region logical locations:
LREG=1,3,51,219,418,415,
LNMX=580 &
; Row number for Y = YMAX

; Start of boundary points
BPD X=0,Y=0,B=0 &
BPD X=0,Y=27.9091289778 &
BPD X=3.688748263291,Y=27.9091289778 &
BPD X=3.688748263291,Y=0 &
BPD X=2.431040968741,Y=0 &
BPD NI=2,XB=2.431040968741,YB=8.5, &
X=-0.492488765601,Y=-0.086824988835 &
BPD NI=2,XB=1.037748526582,YB=1.75, &
BPD NI=2,XB=1.037748526582,YB=1.75, &
X=-0.3,Y=0,B=0 &
BPD X=0.737748526582,Y=1.55, &
BPD X=0.737748526582,Y=0.086824988835 &
BPD X=0.8,Y=0.15 &
BPD X=3.688748263291,Y=1.4 &
BPD X=3.688748263291,Y=0,B=0 &
BPD X=0,B=0 &
```

Solution



An Elliptical-Type Cavity (think SC)

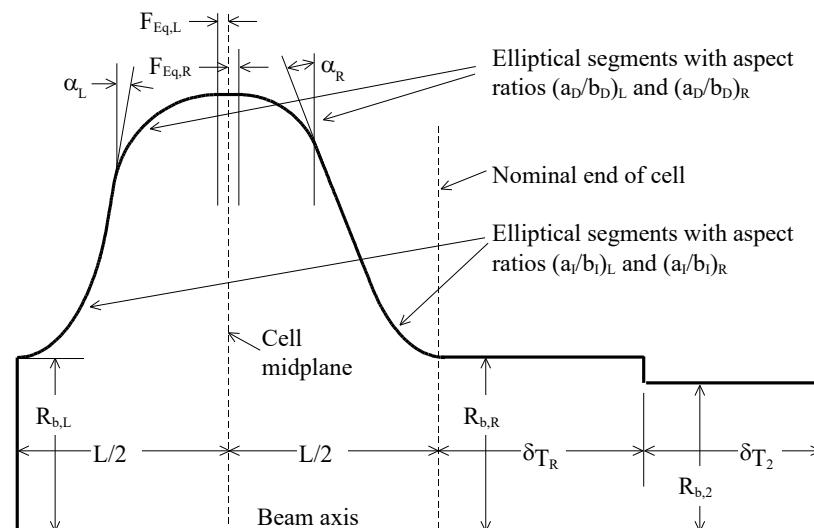
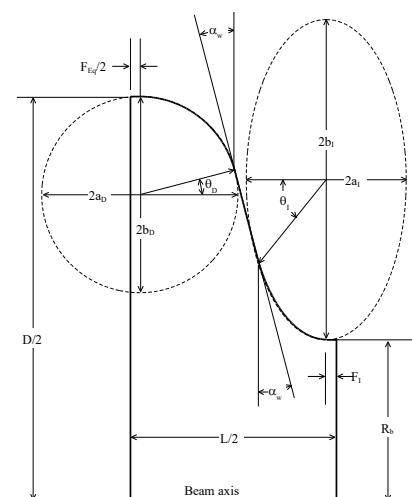
Basic Geometry



INFN & CEA 704 MHz
elliptical SC cavities



Special Superfish
input geometry



An Elliptical-Type Cavity (think SC)

Superfish Implementation

Superfish input file

```
Elliptical Cavity - Notepad
File Edit Format View Help
>Title
Tuning elliptical cavity NF muon linac
Design_diameter = 1
Resonant Frequency = 201.49 MHz, Bore radius = 23.00 cm
ENDtitle

REST_mass          105.658369
SUPERConductor    2 9.2 1.0E-08
NumberofCells      10 ; used by the ELLCAV code
FULL_cavity        0
FILE_name_prefix   elliptical
SEQUENCE_number    201.249
FREQUENCY          1
BETA               74.48796836258
LENGTH              74.48796836258
Diameter             137.094182998
E0_Normalization    14.8135743775
E0T_Normalization   10
Dome_A             20
LEFT_DOME_B         20
RIGHT_DOME_B        18.16662400282
DOME_A/B            1
LEFT_DOME_A/B       1
RIGHT_DOME_A/B      1
WALL_ANGLE          20
LEFT_WALL_angle     20
RIGHT_WALL_angle    20
EQUATOR_Flat        0.0
LEFT_Equator_Flat   0.0
RIGHT_Equator_Flat  0.0
IRIS_Flat            0.0
LEFT_Iris_Flat       0.0
RIGHT_Iris_Flat      0.0
RIGHT_BEAM_tube      60
IRIS_A/B             0.7
LEFT_IRIS_A/B        0.7
RIGHT_IRIS_A/B       0.7
BETASTART            0.0
BETATESTP            0.0
BETATABLE            0.0
BORE_diameter        23
LEFT_BORe_radius     23
RIGHT_BORe_radius    23
SECOND_TUBE_diameter 0.0
SECOND_TUBE_radius   0.0
DELTA_Frequency      0.01
MESH_size             1
INCREMENT            2
START                1

; Start codes for ELLfish:
; 1 No tuning
; 2 Set bore diameter
; 3 Adjust dome ellipse size
; 4 Adjust wall slope
; 5 Set wall slope with fixed iris ellipse size
; (Right side only in full cavities for 3, 4, and 5.)
Endfile
```

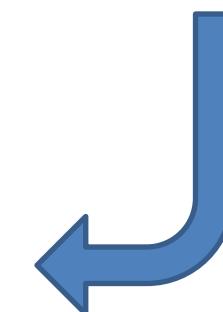
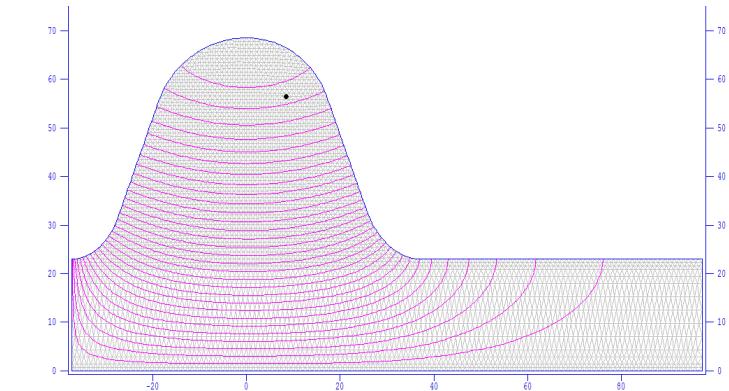
Geometry file

```
Lister - [c:\Current Projects\Superfish Course Oxford\Example 3\ELLIPTICAL.t]
File Edit Options Help
Title
Tuning elliptical cavity NF muon linac
Design_diameter = 1
Resonant Frequency = 201.49 MHz, Bore radius = 23.00 cm
No tuning on this cavity.

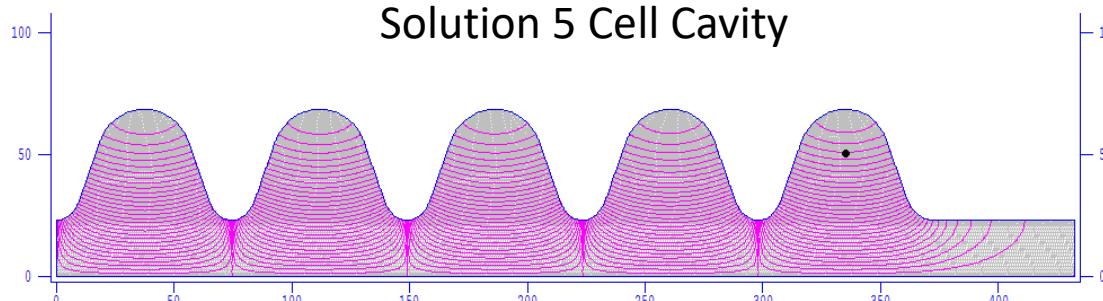
GRED_NPROB=1
NHT=1
FREQD=201.2491888163
FREQD=201.249
BETA=9.2
KHEI_HOB=1
DPH=180
NBSUP=1,NBSL0=0,NBSRT=0,NBSLF=0
; Superfish problem
; Material air or empty space
; Mode frequency, starting frequency is
; Design frequency, used (with DPH) to
; Periodic velocity, used (with DPH)
; SFO will use BET0 to compute wave number
; Phase length of the cavity, used (with DPH)
; Boundary conditions
; Fix intersections on line regions
; X>Z,V>R, cylindrical coordinates
; Normalize to EZERO
; Accelerating gradient times 1
; Superconducting elliptical cavity
; Rest mass value or indicator
; Mesh optimization convergence parameter
; Residual error, Superfish residual
; Superconducting temperature, degrees K
; Critical temperature, degrees K
; Residual BE-0B
; X0=0, Y0=0, Z0=0
; Drive point X coordinate
; Drive point Y coordinate
; Allow convergence in 1 iteration
; DX=1
; Line-region physical locations
; VRED=1.414213562373,4.24264867119,18.0502523169,20.8786795644,
; V line-region logical locations:
; LMAX=80 t ; Row number for V = VMAX

; Start of boundary points
BPO X=-37.24148418129,V=0.0 & ; 1
BPO X=-37.24148418129,V=0.0 & ; 2
BPO X=-37.24148418129,V=23.0 & ; 3
BPO X=-2,XB=-37.24148418129,VB=38.6695173324t, ; 4
X=0,Y=23.0 &
X=7.31750789735,V=7.22870935854 &
BPO X=-59.39385291572,V=55.38749436551 & ; 5
BPO X=-2,XB=0.0,V=48.547891499, ; 6
BPO X=0,Y=48.547891499 &
X=0,B,Y=28.0 &
BPO X=2,XB=0.0,V=50.38946749619, ; 7
X=18.16662400282,V=50.38946749619 &
X=25.633767923568,V=33.8679265119 & ; 8
BPO X=2,XB=37.24148418129,V=41.69808937394, ; 9
X=13.88625606,V=41.69808937394 &
X=13.88625606,V=41.69808937394 &
BPO X=97.24148418129,V=23.0 & ; 10
BPO X=97.24148418129,V=0.0 & ; 11
BPO X=0,Y=0.0 & ; 12
```

Solution 1 Cell



Solution 5 Cell Cavity

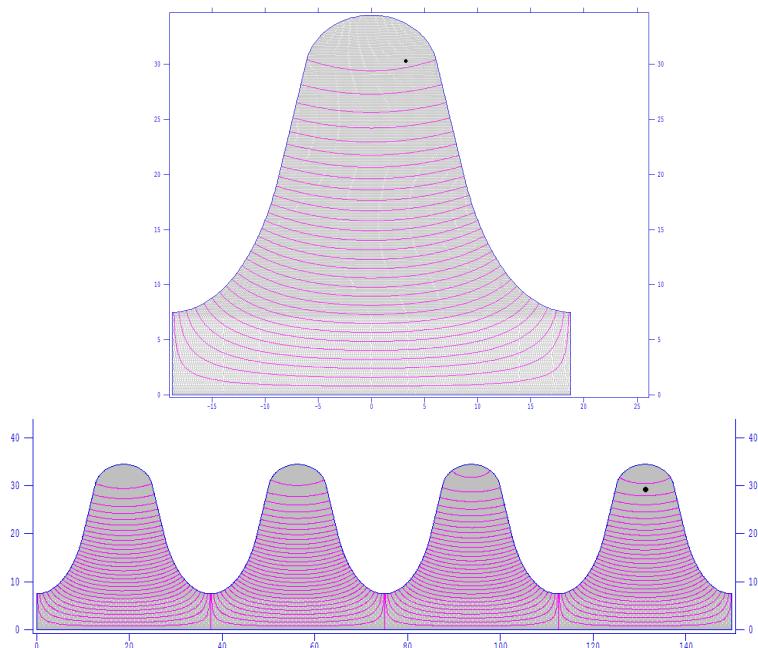


An Elliptical-Type Cavity (think SC)

Two Superfish Examples

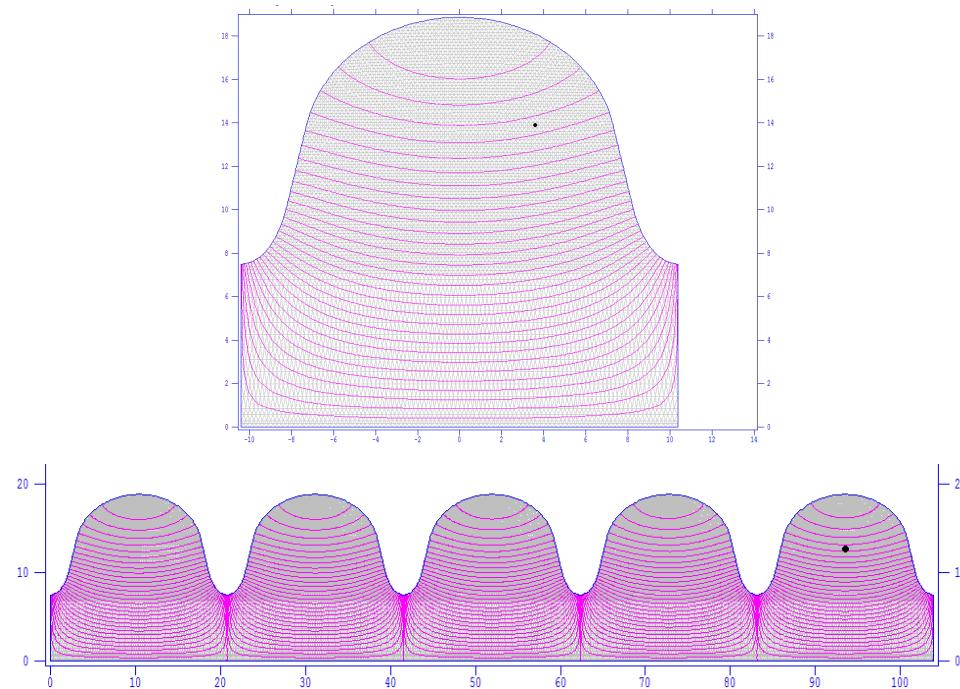
- Example 1: 400 MHz

- Like the LHC 400 MHz RF
- 4-cell cavity, 4 cavities/Cryomodule



- Example 2: 721.4 MHz

- SPL-like cavities
- 5-cell cavity



Ferrite Loaded Cavities

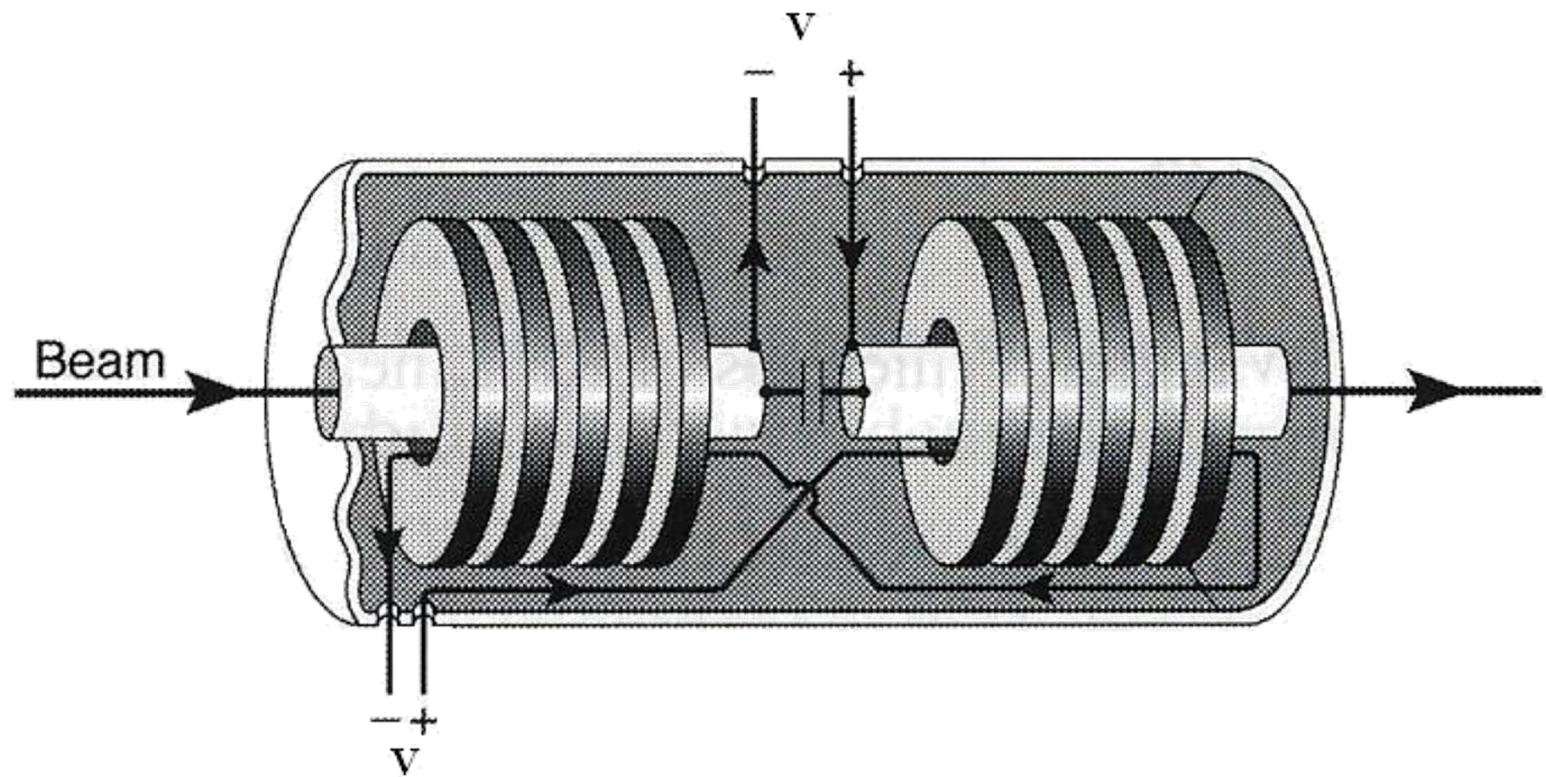
The Basics



- Bias current -> Variable magnetic field -> Variable magnetic permeability of the ferrite -> Frequency change
- The structure can be thought of as a resonant transformer in which the beam constitutes a one-turn secondary winding.
- Used when a variable resonant frequency is needed
- The torus of the ferrite encircles the beam path
- Ferrite properties are important (limit the cavity capabilities)
- Frequencies domain: 100 kHz and 60 MHz
- Typical gap voltage of up tens of kV
- Different requirements (large frequency ranges, rapid swings, space, etc) -> various designs.

Ferrite Loaded Cavities

The Basics



Ferrite Loaded Cavities

Superfish Implementation

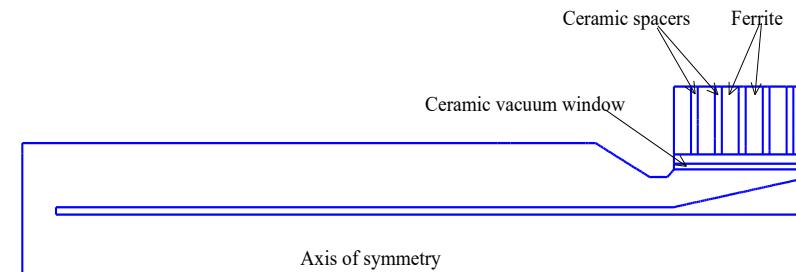
Six ferrite blocks: Epsilon = 14.5, Mu = 1.5

Five ceramic-spacers: Epsilon = 10.0, Mu = 1.0

Ceramic vacuum window: Epsilon = 9.0, Mu = 1.0

Cavity length: 116 cm

Number of gaps: 1

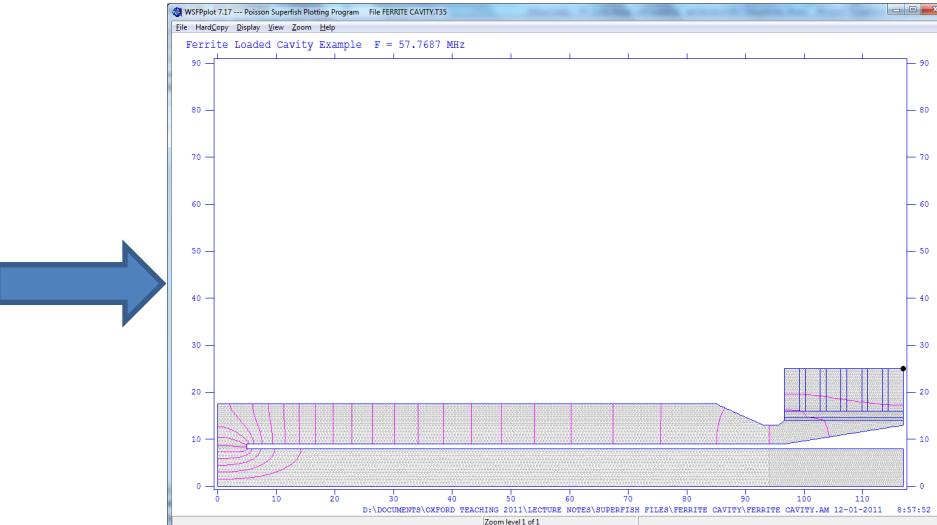


```
Lister - [D:\Documents\Oxford Teaching 2011\Lecture Notes\Superfish Files\Ferrite Cavity\Ferrite Cavity.am]
File Edit Options Encoding Help
Ferrite Loaded Cavity Example
Six ferrite blocks: Material 2, Epsilon = 14.5, Mu = 1.5
Five ceramic-spacers: Material 4, Epsilon = 10.0, Mu = 1.0
Ceramic vacuum window: Material 3, Epsilon = 9.0, Mu = 1.0
Initialize one large ferrite block, then superimpose ceramic spacers
[Originally appeared in 1987 Reference Manual C.12.2]

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&reg kprob=1,                                ! Superfish problem
icylin=1,                                     ! Cylindrical symmetry
freq=57.76775,                                ! Starting frequency
dslope=-1,                                     ! Allow convergence after one iteration
xreg1=94.0,                                    ! X line region
kreg1=188,                                     ! Logical coordinate for XREG1
yreg1=8,yreg2=9,                               ! Y line regions
yreg3=13,yreg4=17.5
lreg1=12,lreg2=15,
lreg3=21,lreg4=31,                            ! Logical coordinates FOR VREGs
kmax=260,lmax=43 &                            ! Maximum X and Y logical coordinates

&po x=0.0,y=0.0 &
&po x=116.88,y=0.0 &
&po x=116.88,y=8.0 &
&po x=5.0,y=8.0 &
&po x=5.0,y=9.0 &
&po x=96.64,y=9.0 &
&po x=116.88,y=13.0 &
&po x=116.88,y=13.0 &
&po x=96.64,y=25.0 &
&po x=96.64,y=14.0 &
&po x=95.64,y=13.0 &
&po x=93.0,y=13.0 &
&po x=85.0,y=17.5 &
&po x=0.0,y=17.5 &
&po x=0.0,y=0.0 &
```



And a lot more...



Now, use your imagination!