COM1029 Data Structures and Algorithms

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1 Algorithms

1.1 History of Algorithms

My boy Muhammad ibn Musa al-Khwarizmi was the first to write a book on the systematic solution of linear and quadratic equations. He was a Persian mathematician, astronomer, and geographer during the Abbasid Caliphate, a scholar in the House of Wisdom in Baghdad. He was the first to introduce the concept of algorithm to the Western world. The word algorithm comes from the Latin word algorithms, which is a Latinization of his name. He is also known for his work on algebra, which is derived from the Arabic word al-jabr.

1.2 Algorigthm analysis

1.2.1 Time complexity

Example (find the average of an array of n integers)

Quadratic example:

1.2.2 Dominant term

The dominant term is the one with highest power (degree) in a function Example: the cubic function f(N) = 10N3 + N2 + 40N + 80

- 10N3 is the dominant term (among 10N3, N2, 40N and 80)
- When we look at f(1000) = 10,001,00,080, we see that 10,000,000,000 is due to the 10N3 term
- If we use the approximation f(N) = 10N3, then we would only be 0.01% out

The value of f(N) is largely determined by the dominant term, for sufficiently large N

- The meaning of 'sufficiently large' varies according to the function

1.2.3 Big O notation

Compared to evaluating the dominant term, Big O notation is a more general way of expressing the time complexity of an algorithm. It is a way of expressing the upper bound of a function.

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Example: f(N) = 10N^3 + N^2 + 40N + 80 - f(N) is O(N3) - f(N) is O(N2) - f(N) is O(N) - f(N) is O(1)
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1.2.4 Upper bound (Pessimistic view)