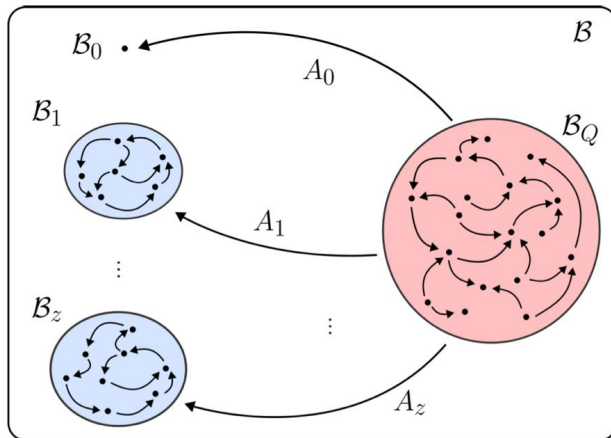


## 5 - Concentration in noisy PQC

Test the effect of non-unital noise for BP.

Change the absorption on from  $B_0$  to  $B_1$  with a customize ansatz (we will provide guidance and initial support). Measure the contribution to the variance with numerics or analytical solution



$$\mathbb{V}_{\rho,H}^{\infty} = \sum_z \frac{(\ell_{\rho})_z (\ell_H)_z}{d_z} + \frac{(\ell_{\rho})_z (A \ell_H)_z}{d_z}$$

- Reference:

<https://arxiv.org/pdf/2410.01893>

<https://pennylane.ai/blog/2021/05/how-to-simulate-noise-with-pennylane>

TO DO:

- Reproduce the numerics (see App E2, F)
- Expand the results using a different absorption

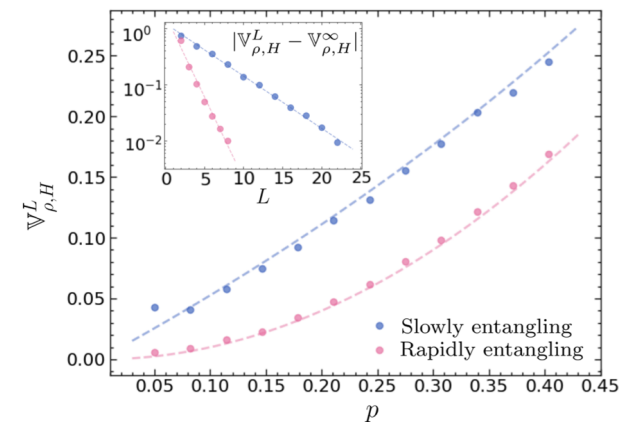


FIG. 3. Scaling of  $\mathbb{V}_{\rho,H}^L$  as a function of the noise strength and the entangling power of the intermediate channel. The main figure illustrates the scaling of  $\mathbb{V}_{\rho,H}^{\infty}$  with noise strength  $p$  for both rapidly entangling (pink) and slowly entangling (light blue) channels, using  $L = 8$  and  $L = 20$ , respectively. The dotted lines represent the theoretical predictions of Eq. (25) and Eq. (24). The inset verifies the exponential convergence of  $\mathbb{V}_{\rho,H}^L$  to  $\mathbb{V}_{\rho,H}^{\infty}$  at  $p = 0.1$ , justifying the chosen number of layers. The dotted lines represent an exponential fit to the numerical data. All plots are obtained using a  $n = 10$  qubit system.