

$$\min \sum_x \sum_m \sum_t c_{x,m,t}^{\text{gen}} \times q_{x,m,t} + \sum_{e'} \sum_t \bar{c}_{e'}^{\text{main}} \times \bar{q}_{e',t} + \sum_{e'} \sum_m \sum_t c_{e',m,t}^{\text{gen}} \times q_{e',m,t} + \sum_t c^{\text{stock}} \times q_t^{\text{stock,stored}}$$

s.t.:

$$d_{M1,t} - \left[ \sum_e q_{e,M1,t} \right] - q_t^{\text{stock,out}} + q_t^{\text{stock,in}} = 0 : \forall t \quad (\lambda_t^1)$$

$$d_{M2,t} - \sum_e q_{e,M2,t} = 0 : \forall t \quad (\lambda_t^2)$$

$$q_{e,M1,t} - \lambda_t^1 \cdot d_{M1,t} \leq 0 : \forall e, t \quad (\mu_{e,t}^1)$$

$$q_t^{\text{stock,stored}} - q_{t-1}^{\text{stock,stored}} + q_{t-1}^{\text{stock,out}} - q_{t-1}^{\text{stock,in}} = 0 : \underbrace{\forall t \setminus \{t_{\text{start}}\}}_{\forall t'} \quad (\lambda_{t'}^3)$$

$$\sum_m \sum_t q_{e,m,t} - Q_e \leq 0 : \forall e \quad (\mu_e^2)$$

$$\sum_m q_{e,m,t} - \bar{q}_{e,t} \leq 0 : \forall e, t \quad (\mu_{e,t}^3)$$

$$q_{t_{\text{start}}}^{\text{stock,stored}} = 0 \quad (\lambda^4)$$

$$\bar{q}_{e',t}^{\text{exp}} - \beta^{\text{add}} \times \sum_m q_{e',m,t} \leq 0 : \forall e', t \quad (\mu_{e',t}^4)$$

$$\bar{q}_{e',t}^{\text{retire}} - \beta^{\text{retire}} \times q_{e'}^{\text{init}} \leq 0 : \forall e', t \quad (\mu_{e',t}^5)$$

$$q_{t_{\text{start}}}^{\text{stock,out}} = 0 \quad (\lambda^{10})$$

$$\bar{q}_{e',t'} - \bar{q}_{e',t'-1} - \bar{q}_{e',t'-1}^{\text{exp}} + \bar{q}_{e',t'-1}^{\text{retire}} = 0 : \forall e', t' \quad (\lambda_{e',t'}^5)$$

$$\bar{q}_{e',t_{\text{start}}} - \bar{q}_{e'}^{\text{init}} = 0 : \forall e' \quad (\lambda_{e'}^6)$$

$$q_{t_{\text{end}}}^{\text{stock,out}} - q_{t_{\text{end}}}^{\text{stock,stored}} = 0 \quad (\lambda^7)$$

$$q_{t_{\text{end}}}^{\text{stock,in}} = 0 \quad (\lambda^8)$$

$$q_{\tilde{e},M1,\tilde{t}} = 0 : \forall \tilde{e}, \tilde{t} \quad (\lambda_{\tilde{e},\tilde{t}}^9)$$

$$-q_{e,m,t} \leq 0 : \forall e,m,t \left( \mu_{e,m,t}^6 \right)$$

$$-q_t^{\text{stock, stored}} \leq 0 : \forall t \left( \mu_t^7 \right)$$

$$-q_t^{\text{stock, out}} \leq 0 : \forall t \left( \mu_t^8 \right)$$

$$-q_t^{\text{stock, in}} \leq 0 : \forall t \left( \mu_t^9 \right)$$

$$-\bar{q}_{e',t} \leq 0 : \forall e',t \left( \mu_{e',t}^{10} \right)$$

$$-\bar{q}_{e',t}^{\text{exp}} \leq 0 : \forall e',t \left( \mu_{e',t}^{11} \right)$$

$$-\bar{q}_{e',t}^{\text{retire}} \leq 0 : \forall e',t \left( \mu_{e',t}^{12} \right)$$