

%attach /home/sebastien/Nutstore Files/SAGE/SimpleIntegralFusionRings.sage

*# Classification of all the non-pointed simple integral 1-Frobenius fusion rings, under the following bounds:
Rank<=r and FPdim<=d with (r,d) = (4, 10^12), (5, 10^7), (6, 10^6), (7, 10^5), (8, 20000), (9, 10000), (10, 5000), (11, 3000), (12,1000).*

*#r5d60t[[1, 1], [3, 2], [4, 1], [5, 1]]
#Finite simple group A5*

S60=[[
[1,0,0,0,0],[0,1,0,0,0],[0,0,1,0,0],[0,0,0,1,0],[0,0,0,0,1]],
[0,1,0,0,0],[1,1,0,0,1],[0,0,0,1,1],[0,0,1,1,1],[0,1,1,1,1]],
[0,0,1,0,0],[0,0,0,1,1],[1,0,1,0,1],[0,1,0,1,1],[0,1,1,1,1]],
[0,0,0,1,0],[0,0,1,1,1],[0,1,0,1,1],[1,1,1,1,1],[0,1,1,1,2]],
[0,0,0,0,1],[0,1,1,1,1],[0,1,1,1,1],[0,1,1,1,2],[1,1,1,2,2]]
]]

*#r6d168t[[1, 1], [3, 2], [6, 1], [7, 1], [8, 1]]
#Finite simple group PSL(2,7)*

S168=[[
[1,0,0,0,0,0],[0,1,0,0,0,0],[0,0,1,0,0,0],[0,0,0,1,0,0],[0,0,0,0,1,0],[0,0,0,0,0,1]],
[0,1,0,0,0,0],[0,0,1,1,0,0],[1,0,0,0,0,1],[0,0,1,0,1,1],[0,0,0,1,1,1],[0,1,0,1,1,1]],
[0,0,1,0,0,0],[1,1,0,0,0,1],[0,1,0,1,0,0],[0,1,0,0,1,1],[0,0,0,1,1,1],[0,0,1,1,1,1]],
[0,0,0,1,0,0],[0,0,1,0,1,1],[0,1,0,0,1,1],[1,0,0,2,1,2],[0,1,1,1,2,2],[0,1,1,2,2,2]],
[0,0,0,0,1,0],[0,0,0,1,1,1],[0,0,0,1,1,1],[0,1,1,1,2,2],[1,1,1,2,2,2],[0,1,1,2,2,3]],
[0,0,0,0,0,1],[0,1,0,1,1,1],[0,0,1,1,1,1],[0,1,1,2,2,2],[0,1,1,2,2,3],[1,1,1,2,3,3]]
]]

#r7d210t[[1, 1], [5, 3], [6, 1], [7, 2]]

S210=[[
[1,0,0,0,0,0,0],[0,1,0,0,0,0,0],[0,0,1,0,0,0,0],[0,0,0,1,0,0,0],[0,0,0,0,1,0,0],[0,0,0,0,0,1,0],[0,0,0,0,0,0,1]],
[0,1,0,0,0,0,0],[1,1,0,1,0,1,1],[0,0,1,0,1,1,1],[0,1,0,0,1,1,1],[0,0,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1]],
[0,0,1,0,0,0,0],[0,0,1,0,1,1,1],[1,1,1,0,0,1,1],[0,0,0,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1]],
[0,0,0,1,0,0,0],[0,1,0,0,1,1,1],[0,0,0,1,1,1,1],[1,0,1,1,0,1,1],[0,1,1,0,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1]],
[0,0,0,0,1,0,0],[0,0,1,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,0,1,1,1],[1,1,1,1,1,1,1],[0,1,1,1,2,1],[0,1,1,1,1,1,2]],
[0,0,0,0,0,1,0],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,2,1],[1,1,1,1,2,0,3],[0,1,1,1,1,3,1]],
[0,0,0,0,0,0,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,2],[0,1,1,1,1,3,1],[1,1,1,1,2,1,2]]
],
[
[1,0,0,0,0,0,0],[0,1,0,0,0,0,0],[0,0,1,0,0,0,0],[0,0,0,1,0,0,0],[0,0,0,0,1,0,0],[0,0,0,0,0,1,0],[0,0,0,0,0,0,1]],
[0,1,0,0,0,0,0],[1,1,0,1,0,1,1],[0,0,1,0,1,1,1],[0,1,0,0,1,1,1],[0,0,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1]],
[0,0,1,0,0,0,0],[0,0,1,0,0,1,1],[1,1,1,0,0,1,1],[0,0,0,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1]],
[0,0,1,0,0,0,0],[0,0,1,0,1,1,1],[1,1,1,0,0,1,1],[0,0,0,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1]],
[0,0,0,1,0,0,0],[0,1,0,0,1,1,1],[0,0,0,1,1,1,1],[1,0,1,1,0,1,1],[0,1,1,0,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1]],
[0,0,0,0,1,0,0],[0,0,1,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,0,1,1,1],[1,1,1,1,1,1,1],[0,1,1,1,2,1],[0,1,1,1,1,1,2]],
[0,0,0,0,0,1,0,0],[0,0,1,1,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,0,1,1,1],[1,1,1,1,1,1,1],[0,1,1,1,1,2,1],[0,1,1,1,1,1,2]],
[0,0,0,0,0,1,0],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,2,1],[1,1,1,1,2,1,2],[0,1,1,1,1,2,2]],
[0,0,0,0,0,0,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,2],[0,1,1,1,1,2,2],[1,1,1,1,2,2,1]]
]]

#r7d360t[[1,1],[5,2],[8,2],[9,1],[10,1]]

S360=[[
[1,0,0,0,0,0,0],[0,1,0,0,0,0,0],[0,0,1,0,0,0,0],[0,0,0,1,0,0,0],[0,0,0,0,1,0,0],[0,0,0,0,0,1,0],[0,0,0,0,0,0,1]],
[0,1,0,0,0,0,0],[1,1,0,0,0,1,1],[0,0,0,1,1,1,0],[0,0,1,1,1,1,1],[0,0,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,0,1,1,1,2]],
[0,0,1,0,0,0,0],[0,0,0,1,1,1,0],[1,0,1,0,0,1,1],[0,1,0,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,1,1,1,1],[0,0,1,1,1,1,2]],
[0,0,0,1,0,0,0],[0,0,1,1,1,1,1],[0,1,0,1,1,1,1],[1,1,1,1,2,1,2],[0,1,1,2,0,2,2],[0,1,1,2,2,2],[0,1,1,2,2,2,2]],
[0,0,0,0,1,0,0],[0,0,1,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,2,0,2,2],[1,1,1,0,3,1,2],[0,1,1,2,1,2,2],[0,1,1,2,2,2,2]],
[0,0,0,0,0,1,0],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,2,2,2],[0,1,1,2,1,2,2],[1,1,1,2,2,2,2],[0,1,1,2,2,2,3]],
[0,0,0,0,0,0,1],[0,1,0,1,1,1,2],[0,0,1,1,1,1,2],[0,1,1,2,2,2,2],[0,1,1,2,2,2,2],[0,1,1,2,2,2,3],[1,2,2,2,2,3,2]]
],
[

#Finite simple group A6

[1,0,0,0,0,0,0],[0,1,0,0,0,0,0],[0,0,1,0,0,0,0],[0,0,0,1,0,0,0],[0,0,0,0,1,0,0],[0,0,0,0,0,1,0],[0,0,0,0,0,0,1]],
[0,1,0,0,0,0,0],[1,1,0,0,0,1,1],[0,0,0,1,1,1,0],[0,0,1,1,1,1,1],[0,0,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,0,1,1,1,2]],
[0,0,1,0,0,0,0],[0,0,0,1,1,1,0],[1,0,1,0,0,1,1],[0,1,0,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,1,1,1,1],[0,0,1,1,1,1,2]],
[0,0,0,1,0,0,0],[0,0,1,1,1,1,1],[0,1,0,1,1,1,1],[1,1,1,1,1,1,2],[0,1,1,1,2,1,2],[0,1,1,1,2,2,2],[0,1,1,2,2,2,2]],
[0,0,0,0,1,0,0],[0,0,1,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,1,1,2,2],[1,1,1,1,2,1,2],[0,1,1,2,1,2,2],[0,1,1,2,2,2,2]],
[0,0,0,0,0,1,0],[0,0,1,1,1,1,1],[0,1,0,1,1,1,1],[0,1,1,1,1,2,2],[1,1,1,1,2,1,2],[0,1,1,2,1,2,2],[0,1,1,2,2,2,2]],
[0,0,0,0,0,0,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,1],[0,1,1,1,1,1,2],[0,1,1,1,1,2,2],[1,1,1,1,2,2,2],[0,1,1,2,2,2,3]],
[0,0,0,0,0,0,1],[0,1,0,1,1,1,2],[0,0,1,1,1,1,2],[0,1,1,2,2,2,2],[0,1,1,2,2,2,2],[0,1,1,2,2,2,3],[1,2,2,2,2,3,2]]
]]

#r7d7980t[[1, 1], [19, 1], [20, 1], [21, 1], [42, 2], [57, 1]]

S7980=[[
[1,0,0,0,0,0,0],[0,1,0,0,0,0,0],[0,0,1,0,0,0,0],[0,0,0,1,0,0,0],[0,0,0,0,1,0,0],[0,0,0,0,0,1,0],[0,0,0,0,0,0,1]],
[0,1,0,0,0,0,0],[1,0,0,1,2,2,3],[0,0,1,1,2,2,3],[0,1,1,1,2,2,3],[0,2,2,2,4,4,6],[0,2,2,2,4,4,6],[0,3,3,3,6,6,7]],
[0,0,1,0,0,0,0],[0,0,1,1,2,2,3],[1,1,1,1,2,2,3],[0,1,1,2,2,3],[0,2,2,2,5,4,6],[0,2,2,2,4,5,6],[0,3,3,3,6,6,8]],
[0,0,0,1,0,0,0],[0,1,1,1,2,2,3],[0,1,1,2,2,3],[1,1,2,2,0,4,3],[0,2,2,0,9,2,6],[0,2,2,4,2,7,6],[0,3,3,3,6,6,9]],
[0,0,0,0,1,0,0],[0,2,2,2,4,4,6],[0,2,2,2,5,4,6],[0,2,2,0,9,2,6],[1,4,5,9,2,15,12],[0,4,4,2,15,6,12],[0,6,6,6,12,12,18]],
[0,0,0,0,0,1,0],[0,2,2,2,4,4,6],[0,2,2,2,4,5,6],[0,2,2,4,2,7,6],[0,4,4,2,15,6,12],[1,4,5,7,6,12,12],[0,6,6,6,12,12,18]],
[0,0,0,0,0,0,1],[0,3,3,3,6,6,7],[0,3,3,3,6,6,8],[0,3,3,3,6,6,9],[0,6,6,6,12,12,18],[0,6,6,6,12,12,18],[1,7,8,9,18,18,22]]
],
[
[1,0,0,0,0,0,0],[0,1,0,0,0,0,0],[0,0,1,0,0,0,0],[0,0,0,1,0,0,0],[0,0,0,0,1,0,0],[0,0,0,0,0,1,0],[0,0,0,0,0,0,1]],
[0,1,0,0,0,0,0],[1,0,0,1,2,2,3],[0,0,1,1,2,2,3],[0,1,1,1,2,2,3],[0,2,2,2,4,4,6],[0,2,2,2,4,4,6],[0,3,3,3,6,6,7]],
[0,0,1,0,0,0,0],[0,0,1,1,2,2,3],[1,1,1,1,2,2,3],[0,1,1,2,2,3],[0,2,2,2,5,4,6],[0,2,2,2,4,5,6],[0,3,3,3,6,6,8]],
[0,0,0,1,0,0,0],[0,1,1,1,2,2,3],[0,1,1,2,2,3],[1,1,2,2,0,4,3],[0,2,2,0,7,4,6],[0,2,2,4,4,5,6],[0,3,3,3,6,6,9]],
[0,0,0,0,1,0,0],[0,2,2,2,4,4,6],[0,2,2,2,5,4,6],[0,2,2,0,7,4,6],[1,4,5,7,7,11,12],[0,4,4,4,11,9,12],[0,6,6,6,12,12,18]],
[0,0,0,0,0,1,0],[0,2,2,2,4,4,6],[0,2,2,2,4,5,6],[0,2,2,4,4,5,6],[0,4,4,4,11,9,12],[1,4,5,5,9,10,12],[0,6,6,6,12,12,18]],
[0,0,0,0,0,0,1],[0,3,3,3,6,6,7],[0,3,3,3,6,6,8],[0,3,3,3,6,6,9],[0,6,6,6,12,12,18],[0,6,6,6,12,12,18],[1,7,8,9,18,18,22]]
],
[
[1,0,0,0,0,0,0],[0,1,0,0,0,0,0],[0,0,1,0,0,0,0],[0,0,0,1,0,0,0],[0,0,0,0,1,0,0],[0,0,0,0,0,1,0],[0,0,0,0,0,0,1]],
[0,1,0,0,0,0,0],[1,0,0,1,2,2,3],[0,0,1,1,2,2,3],[0,1,1,1,2,2,3],[0,2,2,2,4,4,6],[0,2,2,2,4,4,6],[0,3,3,3,6,6,7]],
[0,0,1,0,0,0,0],[0,0,1,1,2,2,3],[1,1,1,1,2,2,3],[0,1,1,2,2,3],[0,2,2,2,5,4,6],[0,2,2,2,4,5,6],[0,3,3,3,6,6,8]],
[0,0,0,1,0,0,0],[0,1,1,1,2,2,3],[0,1,1,2,2,3],[1,1,2,2,0,4,3],[0,2,2,0,5,6,6],[0,2,2,4,6,3,6],[0,3,3,3,6,6,9]],
[0,0,0,0,1,0,0],[0,2,2,2,4,4,6],[0,2,2,2,5,4,6],[0,2,2,0,5,6,6],[1,4,5,5,8,11,12],[0,4,4,6,11,8,12],[0,6,6,6,12,12,18]],
[0,0,0,0,0,1,0],[0,2,2,2,4,4,6],[0,2,2,2,4,5,6],[0,2,2,4,6,3,6],[0,4,4,6,11,8,12],[1,4,5,3,8,12,12],[0,6,6,6,12,12,18]],
[0,0,0,0,0,0,1],[0,3,3,3,6,6,7],[0,3,3,3,6,6,8],[0,3,3,3,6,6,9],[0,6,6,6,12,12,18],[0,6,6,6,12,12,18],[1,7,8,9,18,18,22]]
],
[
[1,0,0,0,0,0,0],[0,1,0,0,0,0,0],[0,0,1,0,0,0,0],[0,0,0,1,0,0,0],[0,0,0,0,1,0,0],[0,0,0,0,0,1,0],[0,0,0,0,0,0,1]],
[0,1,0,0,0,0,0],[1,0,0,1,2,2,3],[0,0,1,1,2,2,3],[0,1,1,1,2,2,3],[0,2,2,2,4,4,6],[0,2,2,2,4,4,6],[0,3,3,3,6,6,7]],
[0,0,1,0,0,0,0],[0,0,1,1,2,2,3],[1,1,1,1,2,2,3],[0,1,1,2,2,3],[0,2,2,2,5,4,6],[0,2,2,2,4,5,6],[0,3,3,3,6,6,8]],
[0,0,0,1,0,0,0],[0,1,1,1,2,2,3],[0,1,1,2,2,3],[1,1,2,2,0,4,3],[0,2,2,0,3,8,6],[0,2,2,4,8,1,6],[0,3,3,3,6,6,9]],
[0,0,0,0,1,0,0],[0,2,2,2,4,4,6],[0,2,2,2,5,4,6],[0,2,2,0,3,8,6],[1,4,5,3,5,15,12],[0,4,4,8,15,3,12],[0,6,6,6,12,12,18]],
[0,0,0,0,0,1,0],[0,2,2,2,4,4,6],[0,2,2,2,4,5,6],[0,2,2,4,8,1,6],[0,4,4,8,15,3,12],[1,4,5,1,3,18,12],[0,6,6,6,12,12,18]],
[0,0,0,0,0,0,1],[0,3,3,3,6,6,7],[0,3,3,3,6,6,8],[0,3,3,3,6,6,9],[0,6,6,6,12,12,18],[0,6,6,6,12,12,18],[1,7,8,9,18,18,22]]
]]

#r8d660t[[1, 1], [5, 2], [10, 2], [11, 1], [12, 2]]

S660=[[

[illegible]

[illegible]

[illegible]

[1,0,0,0,0,0,0,0,1,0],[0,1,0,0,0,1,0,1,1,2],[0,0,1,1,1,1,1,1,2,3],[0,0,1,1,1,1,1,1,2,3],[0,1,1,1,3,1,2,2,4],[0,0,1,1,1,3,1,3,4],[0,1,1,1,1,2,1,2,5],[1,1,1,2,2,2,3,2,6],[0,2,3,3,4,4,5,6,10],
], [0,0,0,0,0,0,0,0,1],[0,0,1,1,1,1,1,2,3],[0,1,1,1,2,2,2,3,5],[0,1,1,1,2,2,2,3,5],[0,1,2,2,2,3,3,4,7],[0,1,2,2,3,2,3,4,7],[0,1,2,2,3,3,3,5,7],[0,2,3,3,4,4,5,6,10],[1,3,5,5,7,7,7,10,17]

[illegible]

[illegible]

```
#r9d3420t[[1, 1], [9, 2], [19, 1], [20, 4], [36, 1]]
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[illegible]

```
#r9d3960t[[1, 1], [8, 2], [9, 1], [10, 1], [15, 2], [40, 2]]
63960-[[
```

```

3960=[
[[1,0,0,0,0,0,0,0],[0,1,0,0,0,0,0,0],[0,0,1,0,0,0,0,0],[0,0,0,1,0,0,0,0],[0,0,0,0,1,0,0,0],[0,0,0,0,0,1,0,0],[0,0,0,0,0,0,1,0],[0,0,0,0,0,0,0,1],[0,0,0,0,0,0,0,0,1]],
[[0,1,0,0,0,0,0,0],[1,1,0,0,0,0,1,0],[0,0,0,1,0,0,1,0],[0,0,0,0,0,0,0,1],[0,0,0,0,0,0,0,2,1],[0,1,1,0,0,0,1,0,2],[0,0,0,0,1,2,0,4,3],[0,1,1,1,1,1,2,3,3]],
[[0,0,1,0,0,0,0,0],[0,0,0,1,0,0,1,0],[1,0,1,0,0,0,1,0,1],[0,0,0,0,0,0,0,1,1],[0,0,0,0,0,0,0,2,1],[0,1,1,1,0,0,1,0,2],[0,0,0,0,1,2,0,4,3],[0,1,1,1,1,1,2,3,3]],
[[0,0,0,1,0,0,0,0],[0,0,0,1,0,0,1,0],[0,1,0,1,0,0,1,0,1],[0,0,0,0,1,0,0,1,1],[0,0,0,0,0,1,0,2,1],[0,1,1,0,0,0,2,0,2],[0,0,0,0,1,2,0,5,3],[0,1,1,1,1,1,2,3,4]],
[[0,0,0,0,1,0,0,0],[0,0,0,0,0,0,1,1],[0,0,0,0,0,0,1,1],[0,0,0,0,1,0,0,1,1],[1,0,0,1,1,0,0,1,1,2],[0,0,0,0,0,1,1,2,1],[0,1,1,1,1,1,2,4,4],[0,1,1,1,1,2,1,4,4]],
[[0,0,0,0,1,0,0,0],[0,0,0,0,0,0,2,1],[0,0,0,0,0,0,2,1],[0,0,0,0,1,0,2,1],[0,0,0,0,0,1,1,2],[0,0,0,0,1,1,3,0,4],[0,2,2,2,1,0,4,7,5],[0,1,1,2,4,1,5,7]],
[[0,0,0,0,0,1,0,0],[0,1,1,0,0,1,0,2],[0,1,1,0,0,0,2,2],[0,0,0,0,1,0,2,1],[0,0,0,0,1,0,1,4,1],[1,1,1,2,1,1,3,0,3],[0,0,0,0,2,4,0,7,6],[0,2,2,2,1,1,3,6,6]],
[[0,0,0,0,0,0,1,0],[0,0,0,0,1,2,0,4,3],[0,0,0,0,1,2,0,5,3],[0,1,1,1,1,2,4,4],[0,2,2,2,1,0,4,7,5],[0,0,0,0,2,4,0,7,6],[1,4,4,5,4,7,7,13],[0,3,3,3,4,5,6,18]],
[[0,0,0,0,0,0,0,1],[0,1,1,1,1,1,2,3,3],[0,1,1,1,1,1,2,3,3],[0,1,1,1,1,1,2,3,4],[0,1,1,1,1,2,1,4,4],[0,1,1,1,2,3,2,6,6],[0,2,2,2,1,2,2,5,7],[0,3,3,3,4,6,5,17],[0,1,3,3,4,4,6,7,16]],
],
[[1,0,0,0,0,0,0,0],[0,1,0,0,0,0,0,0],[0,0,1,0,0,0,0,0],[0,0,0,1,0,0,0,0],[0,0,0,0,1,0,0,0],[0,0,0,0,0,1,0,0],[0,0,0,0,0,0,1,0],[0,0,0,0,0,0,0,1],[0,0,0,0,0,0,0,0,1]],
[[0,1,0,0,0,0,0,0],[1,1,0,0,0,0,1,0],[0,0,0,1,0,0,1,0],[0,0,0,1,0,0,1,0],[0,0,0,0,0,0,0,1],[0,0,0,0,0,0,0,2,1],[0,1,1,0,0,0,1,0,2],[0,0,0,0,1,2,0,4,3],[0,1,1,1,1,1,2,3,3]],
[[0,0,1,0,0,0,0,0],[0,0,0,1,0,0,1,0],[1,0,1,0,0,0,1,0,1],[0,0,0,0,0,0,0,1,1],[0,0,0,0,0,0,0,2,1],[0,1,1,0,0,0,1,0,2],[0,0,0,0,1,2,0,4,3],[0,1,1,1,1,1,2,3,3]],
[[0,0,0,1,0,0,0,0],[0,0,0,1,0,0,1,0],[0,1,0,1,0,0,1,0,1],[0,0,0,0,1,0,0,1,1],[0,0,0,0,0,1,0,2,1],[0,1,1,0,0,0,2,0,2],[0,0,0,0,1,2,0,5,3],[0,1,1,1,1,1,2,3,4]],
[[0,0,0,0,1,0,0,0],[0,0,0,0,0,0,1,1],[0,0,0,0,0,0,1,1],[0,0,0,0,1,0,0,1,1],[1,0,0,0,0,1,1,1,2],[0,0,0,0,0,1,1,2,1],[0,1,1,1,1,1,2,4,4],[0,1,1,1,1,2,1,4,4]],
[[0,0,0,0,0,1,0,0],[0,0,0,0,0,0,2,1],[0,0,0,0,0,0,2,1],[0,0,0,0,1,0,2,1],[0,0,0,0,0,1,1,2],[0,0,0,0,1,0,1,4,1],[0,2,2,2,1,0,4,7,5],[0,1,1,2,4,1,5,7]],
[[0,0,0,0,0,1,0,0],[0,1,1,0,0,1,0,2],[0,1,1,0,0,0,2,2],[0,0,0,0,1,0,2,1],[0,0,0,0,1,0,1,4,1],[1,1,1,2,1,1,3,0,3],[0,0,0,0,2,4,0,7,6],[0,2,2,2,1,1,3,6,6]],
[[0,0,0,0,0,0,1,0],[0,0,0,0,1,2,0,4,3],[0,0,0,0,1,2,0,4,3],[0,0,0,0,1,2,0,5,3],[0,1,1,1,1,2,4,4],[0,2,2,2,1,0,4,7,5],[0,0,0,0,2,4,0,7,6],[1,4,4,5,4,7,7,13],[0,3,3,3,4,5,6,18]],
[[0,0,0,0,0,0,0,1],[0,1,1,1,1,1,2,3,3],[0,1,1,1,1,1,2,3,3],[0,1,1,1,1,1,2,3,4],[0,1,1,1,1,2,1,4,4],[0,1,1,1,2,4,1,5,7],[0,2,2,2,1,1,3,6,6],[0,3,3,3,4,5,6,18],[0,1,3,3,4,4,6,7,15]],
],
[[1,0,0,0,0,0,0,0],[0,1,0,0,0,0,0,0],[0,0,1,0,0,0,0,0],[0,0,0,1,0,0,0,0],[0,0,0,0,1,0,0,0],[0,0,0,0,0,1,0,0],[0,0,0,0,0,0,1,0],[0,0,0,0,0,0,0,1],[0,0,0,0,0,0,0,0,1]],
[[0,1,0,0,0,0,0,0],[1,1,0,0,0,0,1,0],[0,0,0,1,0,0,1,0],[0,0,0,1,0,0,1,0],[0,0,0,0,0,0,0,1],[0,0,0,0,0,0,0,2,1],[0,1,1,0,0,0,1,0,2],[0,0,0,0,1,2,0,4,3],[0,1,1,1,1,1,2,3,3]],
[[0,0,1,0,0,0,0,0],[0,0,0,1,0,0,1,0],[1,0,1,0,0,0,1,0,1],[0,0,0,0,0,0,0,1,1],[0,0,0,0,0,0,0,2,1],[0,1,1,0,0,0,1,0,2],[0,0,0,0,1,2,0,4,3],[0,1,1,1,1,1,2,3,3]],
[[0,0,0,1,0,0,0,0],[0,0,0,1,0,0,1,1],[0,0,0,0,0,0,1,1],[0,0,0,0,1,0,0,1,1],[1,0,0,0,0,1,1,1,0],[0,0,0,0,1,2,2,1,1],[0,0,0,0,1,2,2,0,2],[0,1,1,1,1,1,2,4,4],[0,1,1,1,1,0,1,4,5]],
[[0,0,0,0,0,1,0,0],[0,0,0,0,0,0,2,1],[0,0,0,0,0,0,2,1],[0,0,0,0,1,0,2,1],[0,0,0,0,1,2,2,1,1],[1,0,0,0,1,2,4,1,0,3],[0,0,0,0,2,1,2,4,0],[0,2,2,2,1,0,4,7,5],[0,1,1,1,1,3,0,5,8]],
[[0,0,0,0,0,0,1,0],[0,1,1,0,0,1,0,2],[0,1,1,0,0,0,1,0,2],[0,0,0,0,1,2,2,0,2],[0,0,0,0,2,1,2,4,0],[0,1,1,2,2,2,4,0,2],[0,0,0,0,2,4,0,7,6],[0,2,2,2,0,0,2,6,7]],
[[0,0,0,0,0,0,0,1],[0,0,0,0,1,2,0,4,3],[0,0,0,0,1,2,0,4,3],[0,0,0,0,1,2,0,5,3],[0,1,1,1,1,2,4,4],[0,2,2,2,1,0,4,7,5],[0,0,0,0,2,4,0,7,6],[1,4,4,5,4,7,7,13],[0,3,3,3,4,5,6,18]],
[[0,0,0,0,0,0,0,0,1],[0,1,1,1,1,1,2,3,3],[0,1,1,1,1,1,2,3,3],[0,1,1,1,1,1,2,3,4],[0,1,1,1,0,1,0,4,5],[0,1,1,1,1,3,0,5,8],[0,2,2,2,0,0,2,6,7],[0,3,3,3,4,5,6,18],[0,1,3,3,4,5,8,7,15]],
]]

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```
#r9d7980t[[1,1],[19,2],[20,1],[21,1],[38,2],[42,2]]
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[illegible]

[illegible]


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A10d1638t[[1, 1], [6, 1], [7, 3], [13, 1], [14, 1], [18, 2], [21, 1]]
S1638=[[]
[[1,0,0,0,0,0,0,0,0],[0,1,0,0,0,0,0,0,0],[0,0,1,0,0,0,0,0,0],[0,0,0,1,0,0,0,0,0],[0,0,0,0,1,0,0,0,0],[0,0,0,0,0,1,0,0,0],[0,0,0,0,0,0,1,0,0],[0,0,0,0,0,0,0,1,0],[0,0,0,0,0,0,0,0,1],[0,0,0,0,0,0,0,0,0]]
[[1,0,0,0,0,0,0,0,0],[0,1,0,1,1,0,0,0,0],[0,1,0,0,0,0,0,1,0],[0,1,0,0,0,0,0,1,0],[0,1,0,0,0,0,0,1,0],[0,0,0,0,0,0,0,1,1,2],[0,1,0,0,0,0,0,1,1,2],[0,0,1,1,1,1,0,0,1,2],[0,0,1,1,1,1,1,0,0,2],[0,0,0,0,0,2,2,2,2,0]]
[[0,1,0,0,0,0,0,0,0],[0,1,0,0,0,0,0,1,1,0],[0,0,0,1,1,1,0,0,0,1],[0,0,1,1,0,0,1,0,0,1],[0,0,1,0,0,1,0,0,0,1],[0,0,1,0,0,1,1,1,1,1],[0,0,0,1,1,1,1,1,1,1],[0,1,0,0,0,1,1,2,2,1],[0,1,0,0,0,1,1,2,2,1],[0,0,1,1,1,1,1,1,1,3]]
[[0,0,0,1,0,0,0,0,0,0],[0,1,0,0,0,0,0,1,1,0],[0,0,1,1,0,0,0,1,0,0,1],[0,0,0,1,0,1,1,0,0,0,1],[0,0,0,1,0,1,1,1,1,1],[0,0,1,0,0,1,1,1,1,1],[0,0,1,0,0,1,1,1,1,1],[0,1,0,0,0,1,1,2,2,1],[0,1,0,0,0,1,1,2,2,1],[0,0,1,1,1,1,1,1,1,3]]
[[0,0,0,0,1,0,0,0,0,0],[0,1,0,0,0,0,0,1,1,0],[0,0,1,0,0,1,0,0,0,1],[0,0,0,1,0,1,0,0,0,1],[0,0,0,1,0,1,1,1,1,1],[0,0,0,1,0,1,1,1,1,1],[0,0,0,1,0,1,1,1,1,1],[0,0,0,1,0,1,1,1,1,1],[0,1,0,0,0,1,1,2,2,1],[0,1,0,0,0,1,1,2,2,1],[0,0,1,1,1,1,1,1,1,3]]
[[0,0,0,0,0,0,1,0,0,0],[0,0,0,0,0,0,0,1,1,2],[0,0,1,0,0,0,0,1,1,1,1],[0,0,0,1,0,0,0,1,1,1,1],[0,0,0,1,0,0,0,1,1,1,1],[0,0,0,1,1,1,2,2,2,1],[0,0,1,1,1,2,2,2,2,1],[0,1,1,1,2,2,2,2,3],[0,1,1,1,2,2,2,3,3],[0,2,1,1,1,1,2,3,5,3],[0,2,1,1,1,1,1,3,3,6]]
[[0,0,0,0,0,0,0,1,0,0],[0,0,1,1,1,1,0,0,1,2],[0,1,0,0,0,0,1,1,2,2,1],[0,1,0,0,0,0,1,1,2,2,1],[0,1,0,0,0,0,1,1,2,2,1],[0,1,1,1,2,2,2,3,3],[0,1,1,1,2,2,3,3,3],[0,1,2,2,2,3,1,5,5],[0,1,2,2,2,3,3,5,5],[0,2,1,1,1,3,3,5,5,4]]
[[0,0,0,0,0,0,0,0,1,0],[0,0,1,1,1,1,0,0,1,2],[0,1,0,0,0,0,1,1,2,2,1],[0,1,0,0,0,0,1,1,2,2,1],[0,1,0,0,0,0,1,1,2,2,1],[0,1,1,1,1,2,2,3,3],[0,1,1,1,1,2,2,3,3],[0,1,2,2,2,3,3,5,5],[0,1,2,2,2,3,3,5,5],[0,2,1,1,1,3,3,5,5,4]]

```


[illegible]

```
#r10d1680t[[1, 1], [7, 2], [14, 3], [15, 1], [16, 3]]
```

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

```
#r10d4620t[[1, 1], [11, 2], [20, 5], [21, 1], [44, 1]]
```

S4620=[[

#[0,1,2,3,4,5,6,7,8,9]

[1,0,0,0,0,0,0,0,0],[0,1,0,0,0,0,0,0,0],[0,0,1,0,0,0,0,0,0],[0,0,0,1,0,0,0,0,0],[0,0,0,0,1,0,0,0,0],[0,0,0,0,0,1,0,0,0],[0,0,0,0,0,0,1,0,0],[0,0,0,0,0,0,0,1,0],[0,0,0,0,0,0,0,0,1]
[0,1,0,0,0,0,0,0,0],[1,1,0,0,0,0,0,0,1,2],[0,0,0,1,1,1,1,1,0],[0,0,0,1,1,1,1,1,2],[0,0,1,1,1,1,1,1,2],[0,0,1,1,1,1,1,1,2],[0,0,1,1,1,1,1,1,2],[0,1,1,1,1,1,1,1,2],[0,2,0,2,2,2,2,2,5]
[0,0,1,0,0,0,0,0,0],[0,0,0,1,1,1,1,1,0],[1,0,1,0,0,0,0,0,1,2],[0,1,0,1,1,1,1,1,2],[0,1,0,1,1,1,1,1,2],[0,1,0,1,1,1,1,1,2],[0,1,0,1,1,1,1,1,2],[0,1,1,1,1,1,1,1,2],[0,1,1,1,1,1,1,1,2],[0,2,2,2,2,2,2,5]
[0,0,0,1,0,0,0,0,0],[0,0,1,1,1,1,1,1,2],[0,1,0,0,1,1,1,1,1,2],[0,1,1,2,2,2,2,1,4],[0,1,1,2,2,2,1,2,2,4],[0,1,1,2,1,2,2,2,2,4],[0,1,1,1,2,2,2,2,2,4],[0,2,2,4,4,4,4,4,8]
[0,0,0,0,1,0,0,0,0],[0,0,1,1,1,1,1,1,2],[0,1,0,1,1,1,1,1,2],[0,1,1,2,2,2,1,2,4],[0,1,1,2,2,1,2,2,4],[0,1,1,2,1,2,2,2,4],[0,1,1,2,1,2,2,2,4],[0,2,2,4,4,4,4,4,8]
[0,0,0,0,0,1,0,0,0],[0,0,1,1,1,1,1,1,2],[0,1,0,1,1,1,1,1,2],[0,1,1,2,2,1,2,2,4],[0,1,1,2,2,2,1,2,4],[0,1,1,2,2,2,1,2,4],[0,1,1,2,2,1,2,2,4],[0,1,1,2,2,1,2,2,4],[0,2,2,4,4,4,4,4,8]
[0,0,0,0,0,0,1,0,0],[0,0,1,1,1,1,1,1,2],[0,0,1,0,1,1,1,1,1,2],[0,1,1,2,1,2,2,2,4],[0,1,1,2,1,2,2,2,4],[0,1,1,2,2,2,1,2,4],[0,1,1,2,2,2,1,2,4],[0,1,1,2,2,2,1,2,4],[0,2,2,4,4,4,4,4,8]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

[illegible]

BL=[S60,S168,S210,S360,S7980,S660,S990,S1260,S1320,S504,S1092,S1320b,S1512,S2520,S2730,S3420,S3960,S7980b,S8736,S720,S1638,S1680,S1716,S2184,S2640,S3366,S4620,S720b,S990b,S2184b,S2448]

```
sage: for i in range(31):
.....:     for j in range(L[i]):
.....:         if not Burnside(BL[i][j]):
.....:             print([i,j])
.....:
[13, 2]
[13, 3]
[13, 7]
[13, 8]
```



```
[13, 8]
[16, 0]
[16, 1]
[16, 2]
[18, 0]
```

```
sage: %attach /home/sebastien/Nutstore Files/SAGE/AllCriteria.sage
```

```
sage: for i in range(31):
.....:     for j in range(L[i]):
.....:         M=BL[i][j]
.....:         [v,ro]=IntFormalCodegrees(M)
.....:         if v and IsIntDrinfeldInter(M,v,ro):
.....:             print([len(M),i,j])
.....:
[5, 0, 0]
[6, 1, 0]
[7, 2, 0]
[7, 2, 1]
[7, 3, 0]
[7, 3, 1]
[8, 5, 4]
[8, 5, 5]
[8, 5, 10]
[8, 5, 11]
[8, 5, 13]
[8, 5, 14]
[8, 8, 0]
[9, 9, 0]
[9, 9, 1]
[9, 10, 8]
[9, 10, 14]
[9, 10, 20]
[9, 10, 24]
[9, 10, 27]
[9, 10, 29]
[9, 11, 0]
[9, 13, 0]
[9, 13, 4]
[9, 15, 5]
[9, 15, 7]
[9, 15, 10]
[9, 15, 11]
[10, 21, 17]
[10, 21, 19]
[10, 21, 27]
[10, 21, 29]
[10, 21, 32]
[10, 21, 34]
[10, 21, 47]
[10, 21, 49]
[10, 21, 57]
[10, 21, 59]
[10, 21, 62]
[10, 21, 64]
[10, 21, 67]
[10, 21, 69]
[10, 21, 72]
[10, 21, 74]
[10, 26, 0]
[10, 26, 10]
[10, 26, 11]
[10, 26, 13]
[10, 26, 14]
[11, 28, 2]
[11, 28, 4]
[11, 30, 75]
[11, 30, 79]
[11, 30, 132]
[11, 30, 134]
[11, 30, 144]
[11, 30, 149]
[11, 30, 177]
[11, 30, 179]
```

```
% 59 among 505 are Drinfeld
```

```
sage: for i in range(31):
.....:     for j in range(L[i]):
.....:         M=BL[i][j]
.....:         [v,ro]=IntFormalCodegrees(M)
.....:         if v and IsIntDrinfeldInter(M,v,ro):
.....:             if SchurReformulated(M):
.....:                 print([len(M),i,j])
.....:
[5, 0, 0]
[6, 1, 0]
[7, 2, 1]
[7, 3, 1]
[8, 5, 5]
[8, 5, 11]
[9, 9, 0]
[9, 9, 1]
[9, 10, 14]
[9, 10, 29]
[9, 13, 4]
[9, 15, 10]
[9, 15, 11]
[10, 21, 49]
[10, 21, 74]
[10, 26, 0]
[11, 28, 2]
```

[11, 28, 4]
[11, 30, 75]
[11, 30, 79]
[11, 30, 132]
[11, 30, 134]
[11, 30, 144]
[11, 30, 149]
[11, 30, 177]
[11, 30, 179]

%among them, 26 are also 3-positive

% the four exotic ones of rank 9 are all open:
sage: SL=[BL[9][0],BL[9][1],BL[10][14],BL[10][29],BL[15][10],BL[15][11]]
sage: CheckingList(SL,60)
[0]
FPdim = 504.00000000000006
FPdims = [1.0, 7.000000000000001, 7.000000000000001, 7.000000000000001, 7.000000000000001, 7.999999999999999, 9.0, 9.0, 9.0]
simple
non-1/2-FrobType, so not modular cat
CC= [504, 9, 9, 9, 8, 7, 7, 7]
Non-pivotal Column= 1
Non-pivotal Column= 2
Non-pivotal Column= 3
Non-pivotal Column= 4
Non-pivotal Column= 5
Non-pivotal Column= 6
Non-pivotal Column= 7
Non-pivotal Column= 8
Isaacs list = [0, -1, -1, -1, -1, -1, -1, -1]
[1]
FPdim = 504.0
FPdims = [1.0, 7.000000000000001, 6.999999999999999, 6.999999999999999, 6.999999999999999, 7.999999999999999, 9.0, 9.0, 9.0]
simple
non-1/2-FrobType, so not modular cat
CC= [504, 9, 9, 9, 9, 8, 7, 7]
Non-pivotal Column= 1
Non-pivotal Column= 2
Non-pivotal Column= 3
Non-pivotal Column= 3
Non-pivotal Column= 4
Non-pivotal Column= 5
Non-pivotal Column= 6
Non-pivotal Column= 7
Non-pivotal Column= 8
Isaacs list = [0, -1, -1, -1, -1, -1, -1, -1]
[2]
FPdim = 1091.9999999999998
FPdims = [1.0, 7.000000000000001, 6.999999999999999, 11.999999999999998, 11.999999999999998, 11.999999999999998, 12.999999999999998, 14.0, 14.0]
simple
non-1/2-FrobType, so not modular cat
CC= [1092, 13, 13, 12, 7, 7, 6, 6]
Non-pivotal Column= 1
Non-pivotal Column= 2
Non-pivotal Column= 3
Non-pivotal Column= 4
Non-pivotal Column= 5
Non-pivotal Column= 6
Non-pivotal Column= 7
Non-pivotal Column= 8
Isaacs list = [0, -1, -1, -1, -1, -1, -1, -1]
[3]
FPdim = 1091.9999999999998
FPdims = [1.0, 7.000000000000001, 6.999999999999999, 11.999999999999998, 11.999999999999998, 11.999999999999998, 12.999999999999998, 14.0, 14.0]
simple
non-1/2-FrobType, so not modular cat
CC= [1092, 13, 13, 12, 12, 7, 7, 4]
Non-integral coeff [3, 3, 1] 13/2
Non-pivotal Column= 1
Non-pivotal Column= 2
Non-pivotal Column= 3
Non-pivotal Column= 3
Non-pivotal Column= 4
Non-pivotal Column= 5
Non-pivotal Column= 6
Non-pivotal Column= 7
Non-pivotal Column= 8
Isaacs list = [0, -1, -1, -1, -1, -1, -1, -1]
[4]
FPdim = 3420.0
FPdims = [1.0, 9.0, 9.0, 19.0, 20.0, 19.999999999999996, 20.0, 20.0, 36.0]
simple
non-1/2-FrobType, so not modular cat
CC= [3420, 19, 19, 9, 9, 9, 5, 4]
Non-pivotal Column= 1
Non-pivotal Column= 2
Non-pivotal Column= 3
Non-pivotal Column= 4
Non-pivotal Column= 5
Non-pivotal Column= 6
Non-pivotal Column= 7
Non-pivotal Column= 8
Isaacs list = [0, -1, -1, -1, -1, -1, -1, -1]
[5]
FPdim = 3419.9999999999995
FPdims = [1.0, 9.0, 9.0, 19.0, 19.999999999999996, 19.999999999999996, 19.999999999999996, 19.999999999999996, 36.0]
simple
non-1/2-FrobType, so not modular cat
CC= [3420, 19, 19, 9, 9, 9, 5, 4]
Non-pivotal Column= 1
Non-pivotal Column= 2
Non-pivotal Column= 3
Non-pivotal Column= 4
Non-pivotal Column= 5

```
Non-pivotal Column= 6
Non-pivotal Column= 7
Non-pivotal Column= 8
Isaacs list = [0, -1, -1, -1, -1, -1, -1, -1, -1]
```

```
# let us see those only 3-positive:
```

```
sage: c=0
....: for i in range(31):
....:     for j in range(L[i]):
....:         M=BL[i][j]
....:         if PositiveCo(M,3):
....:             c+=1; print([len(M),i,j])
....:
[5, 0, 0]
[6, 1, 0]
[7, 2, 1]
[7, 3, 1]
[8, 5, 5]
[8, 5, 11]
[9, 9, 0]
[9, 9, 1]
[9, 10, 14]
[9, 10, 29]
[9, 13, 4]
[9, 15, 8]
[9, 15, 9]
[9, 15, 10]
[9, 15, 11]
[10, 21, 49]
[10, 21, 74]
[10, 26, 0]
[11, 28, 2]
[11, 28, 4]
[11, 30, 75]
[11, 30, 79]
[11, 30, 132]
[11, 30, 134]
[11, 30, 144]
[11, 30, 149]
[11, 30, 177]
[11, 30, 179]
```

```
sage: c
28
```

```
...
```