

## Exercise Sheet 7 for Algorithms of Bioinformatics (Winter 2025/26)

**Hand In:** Until 2025-12-05 18:00, on ILIAS.

### Problem 1

10 points

Is it possible for 99 cities to be linked by roads, with each city being linked to exactly 17 other cities? Justify your answer, and generalize it.

### Problem 2

40 points

The  $t$ -addition  $k$ -mer problem is the following: Given a multiset  $\mathcal{R}[0..n)$  of  $k$ -mers, add at most  $t$  additional  $k$ -mers  $\mathcal{T}$  to the multiset, and create a string  $A$  of length  $n+t+k-1$ , so that every  $k$ -mer from  $\mathcal{R} \cup \mathcal{T}$  appears precisely once within  $A$  – or conclude that this is impossible.

Find an efficient algorithm for the  $t$ -addition  $k$ -mer problem. For full marks, the algorithm should run in  $O(f(t) \cdot (n+k))$  time for some function  $f$ .