

Exercise Sheet 7 for Algorithms of Bioinformatics (Winter 2025/26)

Hand In: Until 2025-12-05 18:00, on ILIAS.

Problem 1

10 points

Is it possible for 99 cities to be linked by roads, with each city being linked to exactly 17 other cities? Justify your answer, and generalize it.

Problem 2

40 points

The t -addition k -mer problem is the following: Given a multiset $\mathcal{R}[0..n]$ of k -mers, add at most t additional k -mers \mathcal{T} to the multiset, and create a string A of length $n+t+k-1$, so that every k -mer from $\mathcal{R} \cup \mathcal{T}$ appears precisely once within A – or conclude that this is impossible.

Find an efficient algorithm for the t -addition k -mer problem. For full marks, the algorithm should run in $O(f(t) \cdot (n + k))$ time for some function f .