

Fundamentos de lenguajes de programación

Inferencia de tipos: Ejemplos

carlos.andres.delgado@correounivalle.edu.co

Carlos Andrés Delgado S. Carlos Alberto Ramírez

Facultad de Ingeniería. Universidad del Valle

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Ejercicios inferencia de tipos

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Carlos Andrés
Delgado S.
Carlos Alberto
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Considere la siguiente expresión:

```
let
  j = proc(int x, ? y)
      +(x,y)
  t = proc(? k, int a, ? b)
      (k a b)
in (t j 2 3)
```

Indique su tipo

$t_1 \rightarrow (t_j \ 2 \ 3)$
 $t_j = \text{proc}(\dots) \dots$

$$t_t = \text{proc}(\dots)$$

$$t_x \rightarrow x$$

$$t_y \rightarrow y$$

$$t_k \rightarrow k$$

$$t_b \rightarrow b$$

$$t_q \rightarrow q$$

$$t_2 \rightarrow t(x, y)$$

$$t_3 \rightarrow (k, q, b)$$


$$c(t, j, z, 3)$$

$$j = \text{proc}(\dots)$$

$$t_t = (t_j * \text{int} * \text{int}) \rightarrow t_2$$

$$t_j = (\text{int} * t_y) \rightarrow t_2$$

$$f(x, y) \quad (t_x * t_y) \rightarrow t_z$$


 $(int * int) \rightarrow int$

$$\begin{aligned} t_y &= int \\ t_x &= int \\ t_z &= int \end{aligned}$$

$$t_e = (t_j * int * int) \rightarrow t_1$$

$$t_1 = t_3$$

$$t_e = (t_k * int * t_b) \rightarrow t_3$$

$$\begin{aligned} t_k &= t_j \\ t_b &= int \end{aligned}$$

$$t_k = (t_a * t_b) \rightarrow t_j$$

$$t_j = (int * t_y) \rightarrow \tilde{t}_2$$

$$t_a = int$$

$$t_g = t_b$$

$$t_3 = t_2$$

$$t_t = ((int * int \rightarrow int) * int * int) \rightarrow int$$

$$t_1 = int$$

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Respuesta:

- $y = \text{int}$
- $k = (\text{int} * \text{int} \rightarrow \text{int})$
- $b = \text{int}$
- La expresión es de tipo **int**

$f = \text{proc } (\text{int } a, \text{int } b) \rightarrow (a, b)$

$tf = (\text{int} * \text{int} \rightarrow t_2)$

$(f \times y)$

$tf = (tx * ty \rightarrow t_1)$

Recuerda: Relacionar llamado (app-exp) con la declaración (proc (....))

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Considere la siguiente expresión:

```
let
  j = proc(int x, ? y)
    if (y 2) then +(x,2) else -(x,3)
  t = proc(? k, int a, ? b, ? c)
    (k +(a,b) c)
  s = proc(? a) zero?(a)
in
  let
    p = proc(?m, ? n)
      (m n 5 14 s)
    in
      (p t j)
```

Handwritten notes: $t_m =$ (next to the inner let), $t_1 \rightarrow (p \ t \ j)$ (below the inner let), and $2) \text{ Variables}$ (to the right of the inner let).

Indique su tipo

$t_1 \rightarrow (p \ t \ j)$

$t_j \rightarrow \text{proc}(\dots)$	$t_x = \text{int}$	t_c
$t_t \rightarrow \text{proc}(\dots)$	t_y	t_m
$t_s \rightarrow \text{proc}(\dots)$	t_k	t_n
$t_p \rightarrow \text{proc}(\dots)$	$t_a = \text{int}$	
	t_b	
$t_2 = (y \ z)$		
$t_3 = t(x, z)$		
$t_4 = -(x \ z)$		
$t_5 = (k \ t_6 \ c)$	$t_8 = (m \ n \ t_5)$	
$t_6 = t(q, b)$		
$t_7 = \text{zero?}(q)$		

2) Propositional Equivalences

$$t_p = (\underbrace{t_i}_{\text{red}} * \underbrace{t_j}_{\text{red}}) \rightarrow \underbrace{t_1}_{\text{red}}$$

$$t_p = (\underbrace{t_m}_{\text{red}} * \underbrace{t_n}_{\text{red}}) \rightarrow \underbrace{t_0}_{\text{red}}$$

$$t_t = (\underbrace{t_k}_{\text{red}} * \text{int} * \underbrace{t_b}_{\text{red}} * \underbrace{t_c}_{\text{red}}) \rightarrow \underbrace{t_5}_{\text{red}}$$

$$t_j = (\text{int} * t_y) \rightarrow t_3$$

$$t_j = (\text{int} * t_y) \rightarrow t_4$$

$$t_m = (\underbrace{t_n}_{\text{red}} * \text{int} * \text{int} * \underbrace{t_s}_{\text{red}}) \rightarrow \underbrace{t_0}_{\text{red}}$$

$$t_t = (\underbrace{t_n}_{\text{red}} * \underbrace{\text{int}}_{\text{red}} * \underbrace{\text{int}}_{\text{red}} * \underbrace{t_s}_{\text{red}}) \rightarrow \underbrace{t_0}_{\text{red}}$$

$$t_y = (\text{int} \rightarrow t_2)$$

$$t_y = (\text{int} \rightarrow \text{bool})$$

$$[t_k = (t_6 * \underbrace{t_c}_{\text{red}}) \rightarrow \underbrace{t_5}_{\text{red}}]$$

$$t_q * t_b \rightarrow t_6$$

$$\text{int} * \text{int} \rightarrow \text{int}$$

$$t_x * \text{int} \rightarrow t_3$$

$$\text{int} * \text{int} \rightarrow \text{int}$$

$$t_x * \text{int} \rightarrow t_4$$

$t_8 = \text{int}$ $t_b = \text{int}$

$t_1 = t_8$ $t_e = \text{int}$

$t_1 = \text{int}$ $t_2 = \text{bool}$

$t_x = \text{int}$

$t_k = t_n$

$t_m = t_t$

$t_6 = \text{int}$

$t_y = (\text{int} \rightarrow \text{bool})$

$t_j = (\text{int} * (\text{int} \rightarrow \text{bool}) \rightarrow \text{int})$

$t_n = t_j$

$t_c = (\text{int} \rightarrow \text{bool})$

$t_5 = \text{int}$

$t_3 = \text{int}$

$t_4 = \text{int}$

$t_1 = t_8$

$t_5 = t_c$

$t_8 = t_5$

$t_t = ((\text{int} * (\text{int} \rightarrow \text{bool}) \rightarrow \text{int}) * \text{int} * \text{int} * (\text{int} \rightarrow \text{bool})) \rightarrow \text{int}$

$t_p = (t_x * t_j) \rightarrow \text{int}$

int

